CHAPTER – 3 PAIR OF LINEAR EQUATIONS IN TWO VARIABLES

ALGEBRAIC INTERPRETATION OF PAIR OF LINEAR EQUATIONS IN TWO VARIABLES

The pair of linear equations represented by these lines $a_1x + b_1y + c_1 = 0$ and $a_2x + b_2y + c_2 = 0$

- 1. If $\frac{a_1}{a_2} \neq \frac{b_1}{b_2}$ then the pair of linear equations has exactly one solution.
- 2. If $\frac{a_1}{a_2} = \frac{b_1}{b_2} = \frac{c_1}{c_2}$ then the pair of linear equations has infinitely many solutions.
- 3. If $\frac{a_1}{a_2} = \frac{b_1}{b_2} \neq \frac{c_1}{c_2}$ then the pair of linear equations has no solution.

S. No.	Pair of lines	Compare the ratios	Graphical representation	Algebraic interpretation
1	$ \begin{array}{c} a_1 x + b_1 y + c_1 = 0 \\ a_2 x + b_2 y + c_2 = 0 \end{array} $	$\frac{a_1}{a_2} \neq \frac{b_1}{b_2}$	Intersecting lines	Unique solution (Exactly one solution)
2	$ \begin{array}{c} a_1 x + b_1 y + c_1 = 0 \\ a_2 x + b_2 y + c_2 = 0 \end{array} $	$\frac{a_1}{a_2} = \frac{b_1}{b_2} = \frac{c_1}{c_2}$	Coincident lines	Infinitely many solutions
3	$ \begin{array}{c} a_1 x + b_1 y + c_1 = 0 \\ a_2 x + b_2 y + c_2 = 0 \end{array} $	$\frac{a_1}{a_2} = \frac{b_1}{b_2} \neq \frac{c_1}{c_2}$	Parallel lines	No solution

IMPORTANT QUESTIONS

1. On comparing the ratios $\frac{a_1}{a_2} = \frac{b_1}{b_2} = \frac{c_1}{c_2}$, find out whether the lines representing the following pairs

of linear equations intersect at a point, are parallel or coincident: (i) 5x - 4y + 8 = 0 and 7x + 6y - 9 = 0 (ii) 9x + 3y + 12 = 0 and 18x + 6y + 24 = 0(iii) 6x - 3y + 10 = 0 and 2x - y + 9 = 0.

- 2. On comparing the ratios $\frac{a_1}{a_2} = \frac{b_1}{b_2} = \frac{c_1}{c_2}$, find out whether the following pair of linear equations are
 - consistent, or inconsistent. (i) 3x + 2y = 5; 2x - 3y = 7 (ii) 2x - 3y = 8; 4x - 6y = 9(iii) 5x - 3y = 11; -10x + 6y = -22
- 3. Find the number of solutions of the following pair of linear equations: x + 2y - 8 = 02x + 4y = 16
- 4. Write whether the following pair of linear equations is consistent or not. x + y = 14, x - y = 4
- 5. Given the linear equation 3x + 4y 8 = 0, write another linear equation in two variables such that the geometrical representation of the pair so formed is parallel lines.
- 6. Find the value of k so that the following system of equations has no solution: 3x y 5 = 0, 6x 2y + k = 0
- 7. Find the value of k so that the following system of equation has infinite solutions: 3x - y - 5 = 0, 6x - 2y + k = 0
- 8. For which values of p, does the pair of equations given below has unique solution? 4x + py + 8 = 0 and 2x + 2y + 2 = 0

- 9. Determine k for which the system of equations has infinite solutions: 4x + y = 3 and 8x + 2y = 5k
- **10.** Find whether the lines representing the following pair of linear equations intersect at a point, are parallel or coincident:

2x - 3y + 6 = 0; 4x - 5y + 2 = 0

- 11. Find the value of k for which the system 3x + ky = 7, 2x 5y = 1 will have infinitely many solutions.
- 12. For what value of k, the system of equations 2x ky + 3 = 0, 4x + 6y 5 = 0 is consistent?
- **13.** For what value of k, the system of equations kx 3y + 6 = 0, 4x 6y + 15 = 0 represents parallel lines?
- 14. For what value of p, the pair of linear equations 5x + 7y = 10, 2x + 3y = p has a unique solution.
- 15. Find the value of m for which the pair of linear equations has infinitely many solutions.
- 2x + 3y 7 = 0 and (m 1)x + (m + 1)y = (3m 1)**16.** For what value of p will the following pair of linear equations have infinitely many solutions?
 - (p-3)x + 3y = p; px + py = 12
- 17. For what value of k will the system of linear equations has infinite number of solutions? kx + 4y = k 4, 16x + ky = k
- **18.** Find the values of a and b for which the following system of linear equations has infinite number of solutions:

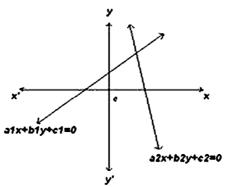
2x - 3y = 7, (a + b) x - (a + b - 3) y = 4a + b

- **19.** For what value of k will the equations x + 2y + 7 = 0, 2x + ky + 14 = 0 represent coincident lines?
- **20.** For what value of k, the following system of equations 2x + ky = 1, 3x 5y = 7 has (i) a unique solution (ii) no solution

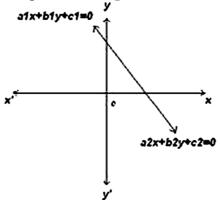
GRAPHICAL METHOD OF SOLUTION OF A PAIR OF LINEAR EQUATIONS

The graph of a pair of linear equations in two variables is represented by two lines.

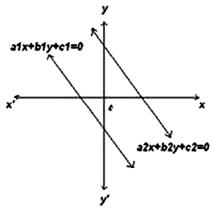
1. If the lines intersect at a point, then that point gives the unique solution of the two equations. In this case, the pair of equations is **consistent**.



2. If the lines coincide, then there are infinitely many solutions — each point on the line being a solution. In this case, the pair of equations is **dependent** (consistent).



3. If the lines are parallel, then the pair of equations has no solution. In this case, the pair of equations is **inconsistent**.



IMPORTANT QUESTIONS

Solve the equation graphically: x + 3y = 6 and 2x - 3y = 12. Solution: Given that

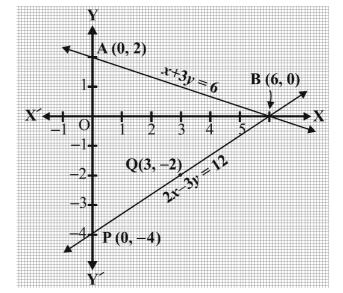
$$x+3y=6 \Rightarrow 3y=6-x \Rightarrow y=\frac{6-x}{3}$$

$$\boxed{\begin{array}{c|c} \mathbf{x} & 0 & 3 & 6\\ \hline \mathbf{y} & 2 & 1 & 0 \\ \end{array}}$$

and $2x-3y = 12 \Rightarrow 3y = 2x-12 \Rightarrow y = \frac{2x-12}{3}$

Х	0	3	6
У	-4	-2	0

Now plot the points and join the points to form the lines AB and PQ as shown in graph Since point B(6, 0) common to both the lines AB and PQ. Therefore, the solution of the pair of linear equations is x = 6 and y = 0



Questions for Practice

- 1. Determine by drawing graphs, whether the following pair of linear equations has a unique solution or not: 3x + 4y = 12; y = 2
- 2. Determine by drawing graphs, whether the following pair of linear equations has a unique solution or not: 2x 5 = 0, y + 4 = 0.
- 3. Draw the graphs of the equations 4x y 8 = 0 and 2x 3y + 6 = 0. Also, determine the vertices of the triangle formed by the lines and x-axis.
- 4. Solve the following system of linear equations graphically:3x 2y 1 = 0; 2x 3y + 6 = 0. Shade the region bounded by the lines and x-axis.
- **5.** Solve graphically: x + 4y = 10, y 2 = 0
- 6. Solve graphically: 2x 3y = 6, x 6 = 0
- 7. Solve the following system of equations graphically: 3x 5y + 1 = 0, 2x y + 3 = 0. Also find the points where the lines represented by the given equations intersect the x-axis.
- 8. Solve the following system of equations graphically: x 5y = 6, 2x 10y = 10Also find the points where the lines represented by the given equations intersect the x-axis.
- 9. Solve the following pair of linear equations graphically: x + 3y = 6; 2x 3y = 12Also find the area of the triangle formed by the lines representing the given equations with y-axis.

MCQ QUESTIONS (1 mark)

1.	The pair of equations $y = 0$ and $y = -7$ has (a) one solution (b) two solution			has (c) infinitely many solutions (d) no solution			
2.	The pair of equations x = a and y = b graphically represents the lines which are(a) parallel(b) intersecting at (a, b)(c) coincident(d) intersecting at (b, a)						
3.	is	for which the pa $(b) - 3$		ions cx – y	= 2 and 6x - 2y = 3 (d) no value	will have no solution	
4.	The pair of equations $5x - 15y = 8$ and $3x - 9y = 24/5$ has (a) infinite number of solutions (b) unique solution (c) no solution (d) one solution						
5.	The pair of equations $x + 2y + 5 = 0$ and $-3x - 6y + 1 = 0$ have (a) infinite number of solutions (b) unique solution (c) no solution (d) one solution						
6.	The sum of the get reversed. T (a) 36	he number is		er is 9. If 27 (d) 25	' is added to it, the d	igits of the numbers	
7.	The pair of equations $3x + 4y = 18$ and (a) infinite number of solutions (c) no solution		s (b)	5			
8.	If the pair of equations $2x + 3y = 7$ and $kx + \frac{9}{2}y = 12$ have no solution, then the value of k is:						
	(a) $\frac{2}{3}$	(b) – 3	(c)) 3	(d) $\frac{3}{2}$		
9.	If $bx + ay = a^2$ (a) $a - b$	$+ b^2$ and $ax - by$ (b) $b - a$		the value of $a^2 - b^2$	x - y equals: (d) $b^2 + a^2$.		
10.	If $2x + 3y = 0$ (a) 0	and $4x - 3y = 0$, (b) -1	then x + y (c)		(d) 2		
11.		$b-a$ and $\sqrt{b}x$ (b) $a-b$, then the vacation \sqrt{ab}	the of x, y is: (d) $-\sqrt{ab}$		
12.	If $31x + 43y = 117$ and $43 + 31y = 105$, then value of $x - y$ is:						
	(a) $\frac{1}{3}$	(b) – 3	(c)) 3	(d) $-\frac{1}{3}$		
13.	1	55 and 17x – 19	y = 53, the	n the value	of $x - y$ is:		
	(a) $\frac{1}{3}$	(b) – 3	(c)) 3	(d) 5		

- 14. If (6, k) is a solution of the equation 3x + y 22 = 0, then the value of k is: (a) 4 (b) -4 (c) 3 (d) -3
- 15. If 3x 5y = 1, $\frac{2x}{x y} = 4$, then the value of x + y is (a) $\frac{1}{3}$ (b) -3 (c) 3 (d) $-\frac{1}{3}$
- **16.** If 3x + 2y = 13 and 3x 2y = 5, then the value of x + y is: (a) 5 (b) 3 (c) 7 (d) none of these
- 17. If the pair of equations 2x + 3y = 5 and $5x + \frac{15}{2}y = k$ represent two coincident lines, then the

value of k is:

(a) -5 (b) $\frac{-25}{2}$ (c) $\frac{25}{2}$ (d) $\frac{-5}{2}$

18. If x = a, y = b is the solution of the equations x - y = 2 and x + y = 4, then the values of a and b are, respectively

(a) 3 and 5 (b) 5 and 3 (c) 3 and 1 (d) –1 and –3

- 19. Aruna has only Re 1 and Rs 2 coins with her. If the total number of coins that she has is 50 and the amount of money with her is Rs 75, then the number of Re 1 and Rs 2 coins are, respectively
 - (a) 35 and 15 (b) 35 and 20 (c) 15 and 35 (d) 25 and 25
- 20. The father's age is six times his son's age. Four years hence, the age of the father will be four times his son's age. The present ages, in years, of the son and the father are, respectively (a) 4 and 24 (b) 5 and 30 (c) 6 and 36 (d) 3 and 24