

Friction in Solids

Types of Friction

Static Friction: Friction acting on an object so as to keep it static.

Kinetic Friction: Friction acting on a moving object so as to reduce its velocity. The direction of Kinetic Frictional Force is in opposite direction to its motion.

Rolling Friction: Friction acting on Rolling objects.

Law of Static Friction

$$F_s \leq \mu_s N$$

Law of kinetic Friction

$$F_k \leq \mu_k N$$

Law of Rolling Friction

$$F_R \leq \mu_R N$$

Angle of Friction:-

The angle made by the resultant reaction force with the vertical (normal reaction) is known as the angle of the friction.

Now, in the triangle OAB

$$AB/OB = \cot\theta$$

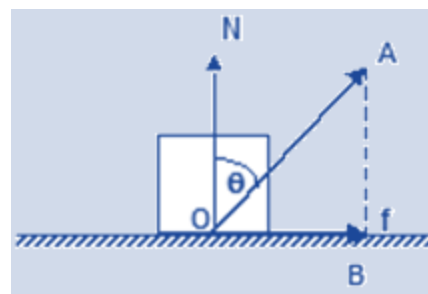
$$\text{So, } OB = AB / \cot\theta$$

$$= AB \tan\theta$$

$$\text{Or, } \tan\theta = OB/AB$$

$$= f / N$$

$$\text{So, } \tan\theta = f / N = \mu_s$$



Angle of Repose:

It is the angle which an inclined plane makes with the horizontal so that a body placed over it just begins to slide of its own accord.

Consider a body of mass m resting on an inclined plane of inclination θ . The forces acting on the body are shown – F_f being the force of friction. If friction is large enough, the body will not slide down.

$$\text{along } x: mg \sin \theta - f = 0 \quad \dots(1)$$

$$\text{Along } y: N - mg \cos \theta = 0 \quad \dots(2)$$

$$\text{i.e. } N = mg \cos \theta \text{ and } f = mg \sin \theta$$

$$\text{Thus, } f \leq \mu_s N \text{ gives,}$$

$$mg \sin \theta \leq \mu_s mg \cos \theta$$

So, $\tan \theta \leq \mu_s$. This signifies, the coefficient of static friction between the two surfaces, in order that the body doesn't slide down.

When θ is increased, then $\tan \theta > \mu$. Thus sliding begins, and the angle $\theta_r = \tan^{-1} \mu$. This angle is known as the angle of repose.

