

Chapter-17 : Current Electricity

1. (d) If E be electric field, then current density $j = \sigma E$

Also we know that current density $j = \frac{i}{A}$

Hence j is different for different area of cross-sections.
When j is different, then E is also different. Thus E is

not constant. The drift velocity v_d is given by $v_d = \frac{j}{ne}$
= different for different j values. Hence only current i will be constant.

2. (c) $v_d = \frac{I}{neA}$ Here, $I = 5.4A$, $n = 8.4 \times 10^{28}$, per m^3
 $A = 10^{-6}m^2$, $e = 1.6 \times 10^{-19}C$

$$\therefore v_d = \frac{5.4}{8.4 \times 10^{28} \times 1.6 \times 10^{-19} \times 10^{-6}} = 0.4 \text{ mm/s}$$

3. (a) By stretching, the volume of wire remains constant.

$$A \times \ell = A' \times \ell' \Rightarrow \pi r^2 \times \ell = \pi \frac{r'^2}{4} \times \ell'$$

$$\Rightarrow \ell' = 4\ell$$

$$\text{Now } R = \frac{\rho \ell}{A}, R' = \frac{\rho \ell'}{A'} = \frac{\rho 4\ell}{A/4} = 16 R.$$

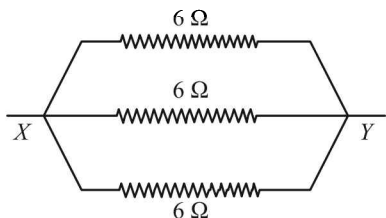
4. (c) Current, $I = \frac{\text{Charge}}{\text{Time}}$

$$\text{as charge } q = n \times 1.6 \times 10^{-19}$$

$$10^{-3} \text{ amp} = \frac{n \times 1.6 \times 10^{-19}}{1 \text{ sec}}$$

$$n = 6.25 \times 10^{15}.$$

5. (d) The equivalent circuit is given below :



The equivalent resistance is given by

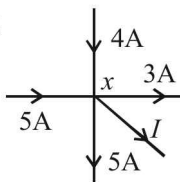
$$\frac{1}{R} = \frac{1}{6} + \frac{1}{6} + \frac{1}{6} = \frac{3}{6} = \frac{1}{2}$$

$$\Rightarrow R_{eq} = 2\Omega$$

6. (d) Equivalent resistance of parallel resistors is always less than any of the member of the resistance system.
7. (c) Short circuit current

$$i_{sc} = \frac{E}{r} \Rightarrow 3 = \frac{1.5}{r} \Rightarrow r = 0.5\Omega$$

8. (b) According to Kirchhoff's first law,
 $(+5A) + (+4A) + (-3A) + (-5A) + I = 0$
 $\Rightarrow I = -1A$
 -ve sign shows that current is flowing away from x



9. (a) $R_{20} = 20\Omega$, $R_{500} = 60$

$$R_t = R_0(1 + \alpha t)$$

$$\frac{R_{20}}{R_{500}} = \frac{R_0(1 + \alpha \times 20)}{R_0(1 + \alpha \times 500)}$$

$$\Rightarrow \frac{20}{60} = \frac{1 + 20\alpha}{1 + 500\alpha} \Rightarrow 1 + 500\alpha = 3 + 60\alpha$$

$$\Rightarrow 500\alpha - 60\alpha = 2 \Rightarrow \alpha = \frac{2}{440} = \frac{1}{220}$$

$$\frac{R_{20}}{R_t} = \frac{R_0 \left(1 + \frac{1}{220} \times 20 \right)}{R_0 \left(1 + \frac{1}{220} \times t \right)}$$

$$\frac{20}{25} = \frac{1 + \frac{1}{11}}{1 + \frac{t}{220}} \Rightarrow \frac{4}{5} = \frac{12/11}{1 + t/220} \Rightarrow 1 + \frac{t}{220} = \frac{15}{11}$$

$$\Rightarrow t = 80^\circ\text{C}.$$

10. (b) $I = \frac{E}{R + r}$

$$V = \frac{E}{R + r} R. \quad [\because V = IR]$$

$$\Rightarrow r = \frac{(E - V)}{V} R.$$

11. (d) ϕ (Potential gradient) $\downarrow \Rightarrow$ Sensitivity \uparrow

$$\phi = \frac{IR}{\ell}$$

12. (b) The resistance of metal decreases with decrease of temperature while for semiconductors, resistance increases when temperature decreases.

13. (d) $P_1 = 100 \text{ W}$, $P_2 = 200 \text{ W}$

$$R_1 = \frac{V^2}{P_1} = \frac{220 \times 220}{100} = 22 \times 22\Omega$$

$$R_2 = \frac{220 \times 220}{200} = 22 \times 11\Omega$$

$$\therefore R_1 : R_2 = 2 : 1$$

14. (b) The resistance of bulb,

$$R = \frac{V^2}{P} = \frac{(220)^2}{100} = 484\Omega$$

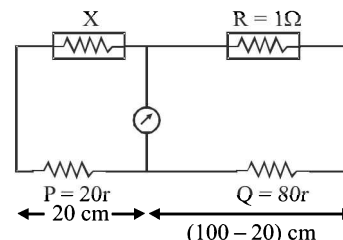
The current in bulb when on 110 V line

$$= \frac{V}{R} = \frac{110}{484} \text{ A}$$

Power consumed by bulb in 110 V line

$$= VI = \frac{110}{484} \times 110 = 25 \text{ W}.$$

15. (a) Let unknown resistance be X. Then condition of Wheatstone's bridge gives $\frac{X}{R} = \frac{20r}{80r}$, where r is resistance of wire per cm.



$$\therefore X = \frac{20}{80} \times R = \frac{1}{4} \times 1 = 0.25\Omega$$

16. (b) Given: $\frac{\ell_1}{\ell_2} = \frac{4}{3}$ and $\frac{r_1}{r_2} = \frac{2}{3}$

Since the two wires are connected in parallel, potential remains same. i.e.,

$$V = \text{constant.}$$

$$IR = \text{Constant}$$

$$\text{i.e., } I_1 R_1 = I_2 R_2 \Rightarrow \frac{I_1}{I_2} = \frac{R_2}{R_1} \quad \dots (i)$$

$$\text{But we know that, } R = \frac{\rho \ell}{A}$$

$$\begin{aligned} \therefore \frac{R_1}{R_2} &= \left(\frac{\ell_1}{A_1} \right) \left(\frac{A_2}{\ell_2} \right) = \left(\frac{\ell_1}{\ell_2} \right) \left(\frac{A_2}{A_1} \right) \\ &= \left(\frac{\ell_1}{\ell_2} \right) \left(\frac{r_2}{r_1} \right)^2 \quad (\text{since area, } A = \pi r^2) \\ &= \left(\frac{4}{3} \right) \left(\frac{3}{2} \right)^2 = 3 \end{aligned}$$

$$\text{Substitute this value in equation (i) we get, } \frac{I_1}{I_2} = \frac{1}{3}.$$

17. (a) For ohmic resistance $V \propto i \Rightarrow V = Ri$ (here R is constant)

18. (b) Given : Length of wire (ℓ) = 15m

$$\text{Area (A)} = 6 \times 10^{-7} \text{ m}^2$$

$$\text{Resistance (R)} = 5\Omega.$$

We know that resistance of the wire material

$$R = \rho \frac{\ell}{A} \Rightarrow 5 = \rho \times \frac{15}{6 \times 10^{-7}} = 2.5 \times 10^7 \rho$$

$$\Rightarrow \rho = \frac{5}{2.5 \times 10^7} = 2 \times 10^{-7} \Omega\text{-m}$$

[where ρ = coefficient of resistivity]

19. (c) All the lamps have been connected in parallel. Therefore, each operates at the same voltage of 220 V.

$$\therefore \text{Current drawn by each lamp} = \frac{220}{220} = 1 \text{ A}$$

$$\therefore \text{Total current drawn by lamps} = 5000 \text{ A.}$$

20. (b) $r = \frac{\ell_1 - \ell_2}{\ell_2} \times R\Omega$

$$\text{Here, } \ell_1 = 125 \text{ cm, } \ell_2 = 100 \text{ cm, } R = 2\Omega.$$

$$\therefore r = 0.5\Omega$$

21. (c) $H = P \times t = \frac{210 \times 5 \times 60}{4.2} = 15000 \text{ cal.}$

22. (a) Current through each bulb is same because these are connected in series.

$$\text{since } \left(R = \frac{V^2}{P} \right), \text{ resistance of } 40 \text{ W bulb is more,}$$

hence greater heat is produced in the 40 W bulb, it glows brightest

$$H = I^2 R t$$

23. (b) $R_1 = R_0 [1 + \alpha \times 100] = 100 \quad \dots (i)$

$$R_2 = R_0 [1 + \alpha \times T] = 200 \quad \dots (ii)$$

On dividing we get

$$\frac{200}{100} = \frac{1 + \alpha T}{1 + 100\alpha} \Rightarrow 2 = \frac{1 + 0.005 T}{1 + 100 \times 0.005}$$

$$\Rightarrow T = 400^\circ\text{C}$$

24. (a) Here, the factor by which the length is changed is

$$n = \frac{\ell'}{\ell} = 3.$$

The new resistance R' is given by

$$R' = R (n^2) = 5(3)^2 = 45\Omega.$$

25. (c) If a heater boils m kg water in time t_1 and another heater boils the same water in t_2 , then both connected in series will boil the same water in time $t_s = t_1 + t_2$ and if in

$$\text{parallel } t_p = \frac{t_1 t_2}{t_1 + t_2} \quad [\text{Use time taken } \propto \text{Resistance}]$$

26. (b) $50 = 10[R + r]$

$$R + r = 5\Omega$$

$$50 = 40 \cdot R$$

$$r = 3.75 \Omega$$

$$\left[\because I = \frac{10}{.25} = 40 \text{ A} \right]$$

27. (d) Resistance of heater $R_h = \frac{V^2}{P} = \frac{100 \times 100}{1000} = 10\Omega$

$$\therefore \text{total resistance of circuit} = 10 + \frac{10 \times R}{10 + R}$$

$$= \frac{100 + 20R}{10 + R}$$

$$\text{Current in heater} = I \cdot \frac{R}{10 + R}$$

$$= \frac{100}{100 + 20R} \times \frac{R}{10 + R} = \frac{5 \times R}{5 + R}$$

$$\therefore \text{power } P = I^2 R_h$$

$$62.5 = \left(\frac{5R}{5 + R} \right)^2 \times 10$$

$$\therefore R = 5\Omega$$

28. (b) Given : $\frac{\ell_1}{\ell_2} = \frac{d_1}{d_2} = \frac{\rho_1}{\rho_2} = \frac{1}{2}$

Resistance of the wire,

$$R = \rho \frac{\ell}{A} = \rho \frac{\ell}{\pi (d/2)^2} = \frac{4\rho\ell}{\pi d^2} \quad \left[\because A = \pi r^2 = \pi \left(\frac{d}{2} \right)^2 \right]$$

$$\therefore \frac{R_1}{R_2} = \frac{\rho_1 \ell_1}{d_1^2} \times \frac{d_2^2}{\rho_2 \ell_2} = \left(\frac{\rho_1}{\rho_2} \right) \left(\frac{\ell_1}{\ell_2} \right) \left(\frac{d_2}{d_1} \right)^2$$

$$\text{i.e., } \frac{10}{R_2} = \left(\frac{1}{2} \right) \left(\frac{1}{2} \right) (2)^2$$

$$\frac{10}{R_2} = 1 \Rightarrow R_2 = 10\Omega$$

29. (c) $i = \frac{2 - 1.5}{20} = \frac{1}{40} \text{ A}$

$$E_A = 2 - ir = 2 - \frac{1}{40} \times 5 = 1.875 \text{ V}$$

$$E_B = 1.5 + ir = 1.625 \text{ V}$$

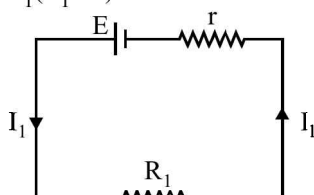
30. (d) $I = n e A v_d = 2 \times 10^{21} \times 1.6 \times 10^{-19} \times 10 \times 0.25 \times 10^{-3}$
 $= 2 \times 1.6 \times 0.25 = \frac{8}{10} = 0.8 \text{ A}$

31. (a) $r = \left(\frac{l_1}{l_2} - 1 \right) R = \left(\frac{125}{100} - 1 \right) 2 = 0.25 \times 2 = 0.5 \Omega$

32. (d) Let E and r be the emf and internal resistance of a battery respectively.
 In the first case

Current flowing in the circuit $I_1 = \frac{E}{R_1 + r}$

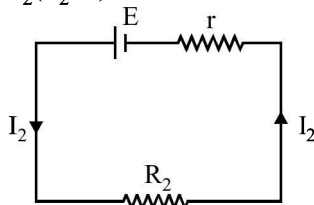
or $E = I_1(R_1 + r)$



In the second case

Current flowing in the circuit $I_2 = \frac{E}{R_2 + r}$

or $E = I_2(R_2 + r)$



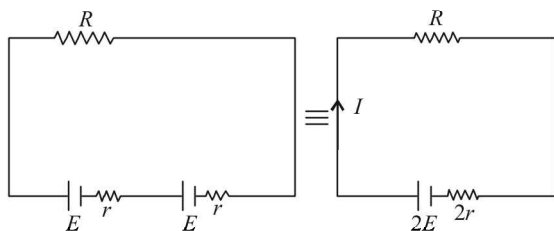
Equating equations (i) and (ii), we get

$$I_1(R_1 + r) = I_2(R_2 + r) \Rightarrow I_1 R_1 + I_1 r = I_2 R_2 + I_2 r$$

$$I_1 R_1 - I_2 R_2 = (I_2 - I_1)r \Rightarrow (I_2 - I_1)r = I_1 R_1 - I_2 R_2$$

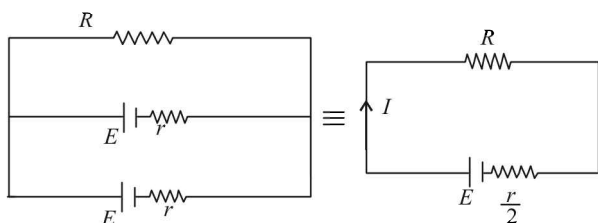
$$r = \frac{I_1 R_1 - I_2 R_2}{I_2 - I_1}$$

33. (a) Cells connected in series



$$J_1 = I^2 R = \left(\frac{2E}{2r + R} \right)^2 \cdot R \quad \dots(1)$$

Cells connected in parallel



$$J_2 = I^2 R = \left(\frac{E}{R + \frac{r}{2}} \right)^2 \times R \quad \dots(2)$$

Given $J_1 = 2.25 J_2$

$$\frac{(2E)^2}{(2r + R)^2} \cdot R = 2.25 \frac{E^2}{\left(R + \frac{r}{2}\right)^2} \cdot R$$

$$\therefore \frac{4}{(2r + R)^2} = \frac{2.25}{\left(R + \frac{r}{2}\right)^2}$$

$$\therefore 4[R + 0.5]^2 = 2.25[2 + R]^2 \quad [\because r = 1\Omega]$$

$$\therefore 2(R + 0.5) = 1.5(2 + R)$$

$$\therefore R = 4\Omega$$

34. (c) ABD, ACD are in series. They are connected in parallel

$$\text{i.e., } \frac{1}{6} + \frac{1}{6} = \frac{1}{3} \text{ i.e., } R = 3\Omega$$

35. (c) $i = n e A v_d$

$$\Rightarrow v_d = \frac{i}{n e A} = \frac{100}{10^{28} \times 1.6 \times 10^{-19} \times 3.14 \times 10^{-4}}$$

$$= \frac{100 \times 10^{-5}}{1.6 \times 3.14} = 0.2 \times 10^{-3} = 2 \times 10^{-4} \text{ m/s}$$

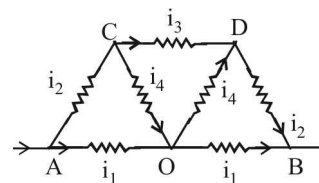
36. (d) At A current is distributed and at B currents are collected. Between A and B, the distribution is symmetrical. It has been shown in the figure. It appears that current in AO and OB remains same. At O, current i_4 returns back without any change. If we detach O from AB there will not be any change in distribution. Now, CO & OD will be in series hence its total resistance $= 2\Omega$

It is in parallel with CD, so, equivalent resistance

$$= \frac{2 \times 1}{2 + 1} = \frac{2}{3} \Omega$$

This equivalent resistance is in series with AC & DB, so, total resistance

$$= \frac{2}{3} + 1 + 1 = \frac{8}{3} \Omega$$



Now $\frac{8}{3} \Omega$ is parallel to AB, that is, 2Ω , so total resistance

$$= \frac{8/3 \times 2}{8/3 + 2} = \frac{16/3}{14/3} = \frac{16}{14} = \frac{8}{7} \Omega$$

37. (a) The potential difference across 4Ω resistance is given by

$$V = 4 \times i_1 = 4 \times 1.2 = 4.8 \text{ volt}$$

So, the potential across 8Ω resistance is also 4.8 volt.

$$\text{Current } i_2 = \frac{V}{8} = \frac{4.8}{8} = 0.6 \text{ amp}$$

Current in 2Ω resistance $i = i_1 + i_2$

$$\therefore i = 1.2 + 0.6 = 1.8 \text{ amp}$$

Potential difference across 2Ω resistance

$$V_{BC} = 1.8 \times 2 = 3.6 \text{ volts}$$

38. (c) $P = I^2 R$. Hence $\frac{dP}{P} = \frac{2dI}{I}$. Since $\frac{dI}{I} = 1\%$.

Hence $\frac{dP}{P} = 2\%$.

39. (c) $P = V^2 / R$

$$\Rightarrow R = V^2 / P = 4 \times 10^4 / 100 = 400 \Omega.$$

$$S = 10^4 / 200 = 0.5 \times 10^2 = 50 \Omega.$$

$$R / S = 8$$

40. (a) As voltage of appliance remains constant, the amount of heat produced is given by,

$$H = \frac{V^2}{R} t \quad \dots (i)$$

when resistance is reduced by 20%, new resistance is $R' = R - 0.2 R = 0.8 R$

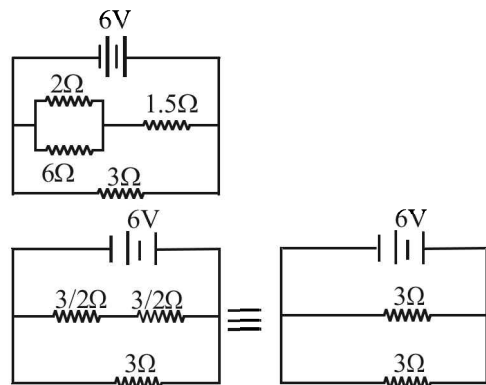
$$H' = \frac{V^2}{0.8R} t' \quad \dots (ii)$$

Equating Eqs. (i) and (ii), we get

$$\frac{V^2}{R} t = \frac{V^2}{0.8R} t'$$

$$\Rightarrow t' = 0.8t = 0.8 \times 12 = 9.6 \text{ min}$$

41. (a)



hence $R_{eq} = 3/2$; $\therefore I = \frac{6}{3/2} = 4A$

42. (b) According to the condition of balancing

$$\frac{55}{20} = \frac{R}{80} \Rightarrow R = 220\Omega$$

43. (c) $L \propto l$

$$\frac{L_1}{L_2} = \frac{l_1}{l_2}$$

$$\frac{10}{11} = \frac{2.5}{l_2}$$

$$10l_2 = 2.5 \times 11$$

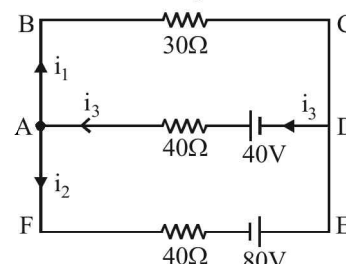
$$l_2 = \frac{2.5 \times 11}{10} = 2.75 \text{ m}$$

44. (a) In series circuit it is always preferable to use formula $I^2 R$, because I throughout is same.

$$I = \frac{120}{6+9} = 8$$

$$\therefore P = I^2 R = 64 \times 6 = 384$$

45. (b) The circuit can be simplified as follows :



Applying KCL at junction A

$$i_3 = i_1 + i_2 \quad \dots (i)$$

Applying Kirchhoff's voltage law for the loop ABCDA

$$-30i_1 - 40i_3 + 40 = 0$$

$$\Rightarrow -30i_1 - 40(i_1 + i_2) + 40 = 0$$

$$\Rightarrow 7i_1 + 4i_2 = 4 \quad \dots (ii)$$

Applying Kirchhoff's voltage law for the loop ADEFA

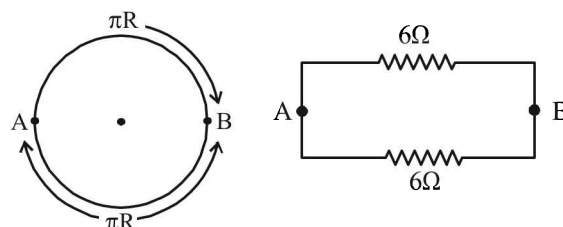
$$-40i_2 + 40i_3 + 80 + 40 = 0$$

$$\Rightarrow -40i_2 - 40(i_1 + i_2) = -120$$

$$\Rightarrow i_1 + 2i_2 = 3 \quad \dots (iii)$$

On solving eq. (ii) and (iii) $i_1 = -0.4 A$

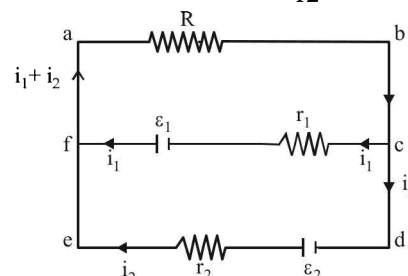
46. (a)



The resistance of length $2\pi R$ is 12Ω . Hence the resistance of length πR is 6Ω . Thus two resistances of 6Ω can be represented as shown in fig. 2.

$$\therefore \text{Equivalent resistance } R = \frac{6 \times 6}{12} = 3\Omega$$

47. (d)



Applying Kirchhoff's rule in loop abcfa

$$\varepsilon_1 - (i_1 + i_2) R - i_1 r_1 = 0.$$

48. (c) Total power consumed by electrical appliances in the building, $P_{\text{total}} = 2500 \text{ W}$

$$\text{Watt} = \text{Volt} \times \text{ampere}$$

$$\Rightarrow 2500 = V \times I \Rightarrow 2500 = 220 I \Rightarrow I \approx 12 A$$

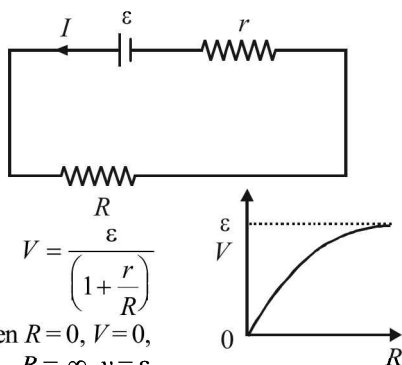
(Minimum capacity of main fuse)

49. (c) The current through the resistance R

$$I = \left(\frac{\varepsilon}{R+r} \right)$$

The potential difference across R

$$V = IR = \left(\frac{\varepsilon}{R+r} \right) R$$



when $R=0$, $V=0$,

$R=\infty$, $V=\varepsilon$

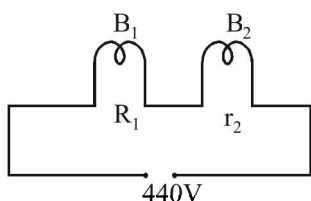
Thus V increases as R increases upto certain limit, but it does not increase further.

50. (c) The current upto which bulb of marked 25W-220V, will

not fuse $I_1 = \frac{W_1}{V_1} = \frac{25}{220}$ Amp

Similarly, $I_2 = \frac{W_2}{V_2} = \frac{100}{220}$ Amp

The current flowing through the circuit



$$I = \frac{440}{R_{\text{eff}}}$$

$$R_{\text{eff}} = R_1 + R_2$$

$$R_1 = \frac{V_1^2}{P_1} = \frac{(220)^2}{25}; \quad R_2 = \frac{V_2^2}{P} = \frac{(220)^2}{100}$$

$$I = \frac{440}{\frac{(220)^2}{25} + \frac{(220)^2}{100}} = \frac{440}{(220)^2 \left[\frac{1}{25} + \frac{1}{100} \right]}$$

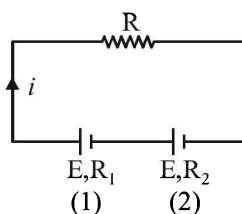
$$I = \frac{40}{220} \text{ Amp}$$

$$\therefore I_1 \left(= \frac{25}{220} \text{ A} \right) < I \left(= \frac{40}{220} \text{ A} \right) < I_2 \left(= \frac{100}{220} \text{ A} \right)$$

Thus the bulb marked 25W-220 will fuse.

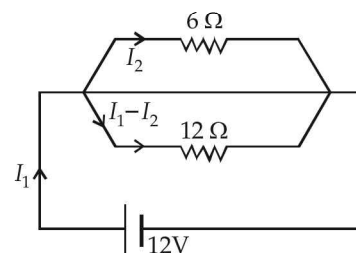
51. (d) $i = \frac{2E}{R+R_1+R_2}$

From cell (2) $E = V + iR_2 = 0 + iR_2$



$$\Rightarrow E = \frac{2E}{R+R_1+R_2} \times R_2 \Rightarrow R = R_2 - R_1$$

52. (d) The given circuit is an extension of wheatstone bridge, therefore points P and Q are at the same potential and point S and T are also at the same potential. Therefore no current passes through PQ and ST and the circuit reduces to as shown



$$I_1 = \frac{12}{4} \quad \left[\because R_{\text{eq}} = \frac{6 \times 12}{6+12} \right]$$

$$= 3 \text{ A}$$

$$\therefore I_2 = 3 \left[\frac{12}{6+12} \right] = 2 \text{ A}$$

As P and Q are equipotential and potential at S is less than the potential at P (potential drops across a resistance as current passes through it), therefore $V_S < V_Q$.

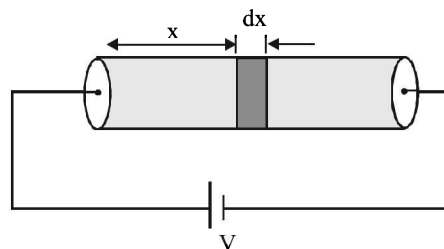
53. (d) A balanced Wheatstone' bridge exists between A & B.

$$R_{\text{eq}} = R$$

current through circuit is V/R

current through AFCEB = $V/2R$

54. (a) Consider an elemental part of solid at a distance x from left end of width dx .



Resistance of this elemental part is,

$$dR = \frac{\rho dx}{\pi a^2} = \frac{\rho_0 x dx}{\pi a^2}$$

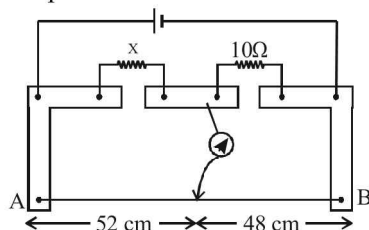
$$R = \int dR = \int_0^L \frac{\rho_0 x dx}{\pi a^2} = \frac{\rho_0 L^2}{2\pi a^2}$$

$$\text{Current through cylinder is, } I = \frac{V}{R} = \frac{V \times 2\pi a^2}{\rho_0 L^2}$$

Potential drop across element is, $dV = I dR = \frac{2V}{L^2} x dx$

$$E(x) = \frac{dV}{dx} = \frac{2V}{L^2} x$$

55. (b) At Null point



$$\frac{X}{\ell_1} = \frac{10}{\ell_2}$$

Here $\ell_1 = 52 + \text{End correction} = 52 + 1 = 53 \text{ cm}$

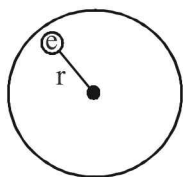
$\ell_2 = 48 + \text{End correction} = 48 + 2 = 50 \text{ cm}$

$$\therefore \frac{X}{53} = \frac{10}{50} \quad \therefore X = \frac{53}{5} = 10.6 \Omega$$

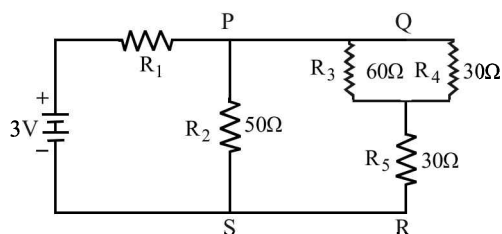
56. (a) $eE = m_e \omega^2 r$

$$\Rightarrow V = \int E dr = \frac{m_e \omega^2}{e} \int_0^R r dr$$

$$\Rightarrow V = \frac{m_e \omega^2 R^2}{2e} \Rightarrow A = 2$$



57. (a)



Net resistance between Q & R =

$$R' = \frac{60 \times 30}{60 + 30} + 30 = 50 \Omega$$

So, equivalent resistance

$$R_{eq} = \frac{50 \times 50}{50 + 50} + 50 = 75 \Omega$$

$$\text{Current in the circuit is } I = \frac{3}{75} = \frac{1}{25} \text{ A}$$

$$\text{Potential drop across } R_1 = 50 \times \frac{1}{25} = 2 \text{ V}$$

\therefore Potential difference across PS or QR is same and given by $3 - 2 = 1 \text{ volt}$

$$\text{Current across QR} = \frac{1}{50} \text{ A}$$

Potential drop across R_5 is given by

$$\frac{1}{50} \times 30 = 0.6 \text{ V}$$

Hence, potential drop across R_4 is $= 1 - 0.6 = 0.4 \text{ V}$

58. (d) $R_1 = R_0 [1 + \alpha_1 \Delta t]; \quad R_2 = R_0 [1 + \alpha_2 \Delta t]$

In Series, $R = R_1 + R_2$

$$= R_0 [2 + (\alpha_1 + \alpha_2) \Delta t] = 2R_0 \left[1 + \left(\frac{\alpha_1 + \alpha_2}{2} \right) \Delta t \right]$$

$$\therefore \alpha_{eq} = \frac{\alpha_1 + \alpha_2}{2}$$

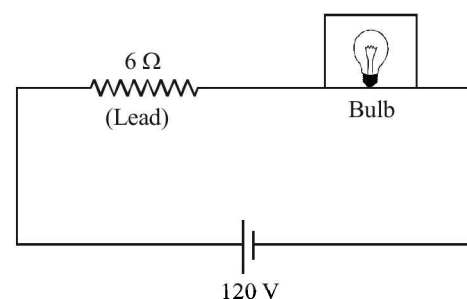
$$\text{In Parallel, } \frac{1}{R} = \frac{1}{R_1} + \frac{1}{R_2} = \frac{1}{R_0 [1 + \alpha_1 \Delta t]} + \frac{1}{R_0 [1 + \alpha_2 \Delta t]}$$

$$\Rightarrow \frac{1}{\frac{R_0}{2} (1 + \alpha_{eq} \Delta t)} = \frac{1}{R_0 (1 + \alpha_1 \Delta t)} + \frac{1}{R_0 (1 + \alpha_2 \Delta t)}$$

$$2(1 - \alpha_{eq} \Delta t) = (1 - \alpha_1 \Delta t)(1 - \alpha_2 \Delta t)$$

$$\therefore \alpha_{eq} = \frac{\alpha_1 + \alpha_2}{2}$$

59. (d)



Power of bulb = 60 W (given)

$$\text{Resistance of bulb} = \frac{120 \times 120}{60} = 240 \Omega \quad \left[\because P = \frac{V^2}{R} \right]$$

Power of heater = 240W (given)

$$\text{Resistance of heater} = \frac{120 \times 120}{240} = 60 \Omega$$

Voltage across bulb before heater is switched on,

$$V_1 = \frac{240}{246} \times 120 = 117.73 \text{ volt}$$

Voltage across bulb after heater is switched on,

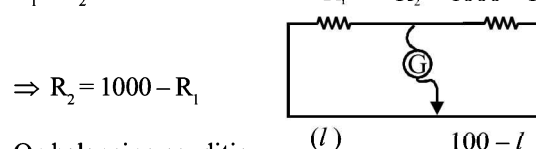
$$V_2 = \frac{48}{54} \times 120 = 106.66 \text{ volt}$$

Hence decrease in voltage

$$V_1 - V_2 = 117.073 - 106.66 = 10.04 \text{ Volt (approximately)}$$

60. (c) $R_1 + R_2 = 1000$

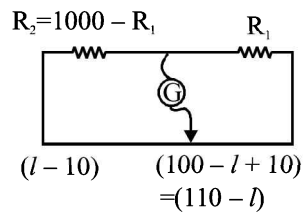
$$R_1 \quad R_2 = 1000 - R_1$$



On balancing condition

$$R_1(100 - l) = (1000 - R_1)l \quad \dots(i)$$

On Interchanging resistance balance point shifts left by 10 cm



On balancing condition

$$(1000 - R_1)(110 - l) = R_1(l - 10)$$

$$\text{or, } R_1(l - 10) = (1000 - R_1)(110 - l) \quad \dots(\text{ii})$$

Dividing eqn (i) by (ii)

$$\frac{100 - l}{l - 10} = \frac{l}{110 - l}$$

$$\Rightarrow (100 - l)(110 - l) = l(l - 10)$$

$$\Rightarrow 11000 - 100l - 110l + l^2 = l^2 - 10l$$

$$\Rightarrow 11000 = 200l$$

$$\text{or, } l = 55$$

Putting the value of ' l ' in eqn (i)

$$R_1(100 - 55) = (1000 - R_1)55$$

$$\Rightarrow R_1(45) = (1000 - R_1)55$$

$$\Rightarrow R_1(9) = (1000 - R_1)11$$

$$\Rightarrow 20 R_1 = 11000$$

$$\therefore R_1 = 550 \text{ K}\Omega$$