

RELATIONS AND FUNCTIONS

Multiple Choice Questions [MCQ]

1. Let $A = \{1, 2, 3\}$ and consider the relation $R = \{(1, 1), (2, 2), (3, 3), (1, 2), (2, 3), (2, 1)\}$. Then R is
 - (a) an equivalence relation
 - (b) reflexive and symmetric but not transitive
 - (c) reflexive and transitive but not symmetric
 - (d) reflexive but neither symmetric nor transitive
2. Let $A = \{1, 2, 3\}$ and consider the relation $R = \{(1, 1), (2, 2), (3, 3), (1, 2), (2, 3), (1, 3), (3, 1)\}$. Then R is
 - (a) an equivalence relation
 - (b) reflexive and symmetric but not transitive
 - (c) reflexive and transitive but not symmetric
 - (d) reflexive but neither symmetric nor transitive
3. Let $A = \{1, 2, 3\}$ and consider the relation $R = \{(1, 1), (2, 2), (3, 3), (1, 2), (2, 1)\}$. Then R is
 - (a) reflexive and symmetric but not transitive
 - (b) reflexive but neither symmetric nor transitive
 - (c) an equivalence relation
 - (d) reflexive and transitive but not symmetric
4. Let $A = \{1, 2, 3\}$ and consider the relation $R = \{(1, 1), (1, 2), (2, 1)\}$. Then R is
 - (a) reflexive and symmetric but not transitive
 - (b) symmetric but neither reflexive nor transitive
 - (c) reflexive but neither symmetric nor transitive
 - (d) reflexive and transitive but not symmetric
5. Let $A = \{1, 2, 3\}$ and consider the relation $R = \{(1, 3)\}$. Then R is
 - (a) transitive
 - (b) symmetric
 - (c) reflexive
 - (d) none of these
6. Let $A = \{1, 2, 3\}$ and consider the relation $R = \{(1, 1), (2, 2), (3, 3)\}$. Then R is
 - (a) reflexive and symmetric but not transitive
 - (b) reflexive but neither symmetric nor transitive
 - (c) reflexive and symmetric and transitive
 - (d) reflexive and transitive but not symmetric
7. Let $A = \{1, 2, 3\}$ and $R = \{(1, 1), (2, 3), (1, 2)\}$ be a relation on A , then the minimum number of ordered pairs to be added in R to make R reflexive and transitive.
 - (a) 4
 - (b) 2
 - (c) 3
 - (d) 1
8. The maximum number of equivalence relations on the set $\{1, 2, 3\}$ is
 - (a) 6
 - (b) 4
 - (c) 3
 - (d) 5
9. Let R be a relation on the set N be defined by $\{(x, y) : x, y \in N, 2x + y = 41\}$. Then, R is
 - (a) reflexive
 - (b) symmetric
 - (c) transitive
 - (d) none of these
10. Relation R in the set Z of all integers defined as $R = \{(x, y) : x - y \text{ is an even integer}\}$ is
 - (a) reflexive and transitive
 - (b) symmetric and Transitive
 - (c) reflexive and symmetric
 - (d) an equivalence relation
11. Let R be the relation on the set of all real numbers defined by $a R b$ iff $|a - b| \leq 1$. Then, R is
 - (a) reflexive and transitive
 - (b) symmetric and Transitive
 - (c) reflexive and symmetric
 - (d) an equivalence relation
12. Consider the non-empty set consisting of children in a family and a relation R defined as $a R b$ if a is sister of b . Then R is
 - (a) symmetric but not transitive
 - (b) transitive but not symmetric
 - (c) both symmetric and transitive
 - (d) neither symmetric nor transitive
13. Relation R in the set $A = \{1, 2, 3, 4, 5, 6, 7, 8\}$ as $R = \{(x, y) : x \text{ divides } y\}$ is
 - (a) reflexive and symmetric but not transitive
 - (b) reflexive and transitive but not symmetric
 - (c) reflexive but neither symmetric nor transitive
 - (d) symmetric but neither reflexive nor transitive

- 14.** Let L denote the set of all straight lines in a plane. Let a relation R be defined by $l_1 R l_2$ if and only if l_1 is perpendicular to l_2 , $\forall l_1, l_2 \in L$. Then R is
- (a) symmetric (b) reflexive
(c) transitive (d) reflexive and symmetric
- 15.** If $A = \{a, b, c\}$ then number of relations containing (a, b) and (a, c) which are reflexive and symmetric but not transitive is
- (a) 4 (b) 3
(c) 2 (d) 1
- 16.** The relation R in the set $\{1, 2, 3, \dots, 13, 14\}$ defined by $R = \{(x, y) : 3x - y = 0\}$ is
- (a) symmetric (b) reflexive
(c) transitive (d) none of these
- 17.** The relation R in the set of natural numbers N defined by $R = \{(x, y) : x > y\}$ is
- (a) reflexive and symmetric but not transitive (b) transitive but neither reflexive nor symmetric
(c) reflexive but neither symmetric nor transitive (d) symmetric but neither reflexive nor transitive
- 18.** A function $f : X \rightarrow Y$ is one-one (or injective), then which of the following is true?
- (a) $\forall x_1, x_2 \in X, f(x_1) = f(x_2) \Rightarrow x_1 = x_2$. (b) $x_1 \neq x_2 \Rightarrow f(x_1) \neq f(x_2)$.
(c) both (a) and (b) are true (d) none of these
- 19.** A function $f : X \rightarrow Y$ is said to be onto (or surjective), then which of the following is true?
- (a) if $\forall y \in Y, \exists$ some $x \in X$ such that $y = f(x)$ (b) range of $f = Y$
(c) both (a) and (b) are true (d) none of these
- 20.** A function $f : X \rightarrow Y$ is said to be bijective, if f is
- (a) one-one only (b) onto only
(c) one-one but not onto (d) one-one and onto
- 21.** If a set A contains m elements and the set B contains n elements with $n > m$, then number of bijective functions from A to B will be:
- (a) $m \times n$ (b) m^n
(c) n^m (d) 0
- 22.** Which of the following functions from I (Set of Integers) to itself is a bijection?
- (a) $f(x) = x^3$ (b) $f(x) = x + 2$
(c) $f(x) = 2x + 1$ (d) $f(x) = x^2 + x$
- 23.** Let $X = \{-1, 0, 1\}$, $Y = \{0, 2\}$ and a function $f : X \rightarrow Y$ defined by $y = 2x^4$, is
- (a) one-one onto (b) one-one into
(c) many-one onto (d) many-one into
- 24.** Let $f(x) = x^2 - 4x - 5$, then
- (a) f is one-one on R (b) f is not one-one on R
(c) f is bijective on R (d) None of these
- 25.** The function $f : R \rightarrow R$ given by $f(x) = x^2$, $x \in R$ when R is the set of real numbers, is
- (a) one-one and onto (b) onto but not one-one
(c) neither one-one nor onto (d) one-one but not onto
- 26.** The signum function, $f : R \rightarrow R$ is given by $f(x) = \begin{cases} 1, & \text{if } x > 0 \\ 0, & \text{if } x = 0 \\ -1, & \text{if } x < 0 \end{cases}$
- (a) one-one (b) many-one
(c) onto (d) none of these

27. Let $f: \mathbb{R} \rightarrow \mathbb{R}$ be defined by $f(x) = \begin{cases} 3x, & \text{if } x \leq 1 \\ x^2, & \text{if } 1 < x \leq 3 \\ 2x, & \text{if } x > 3 \end{cases}$, then $f(-1) + f(2) + f(4)$ is

- (a) 9 (b) 3
(c) 4 (d) 8

28. The greatest integer function $f: \mathbb{R} \rightarrow \mathbb{R}$ be defined by $f(x) = [x]$ is

- (a) one-one and onto (b) onto but not one-one
(c) one-one but not onto (d) neither one-one nor onto

29. The function $f: \mathbb{N} \rightarrow \mathbb{N}$, where \mathbb{N} is the set of natural numbers is defined by

$$f(x) = \begin{cases} n^2, & \text{if } n \text{ is odd} \\ n^2 + 1, & \text{if } n \text{ is even} \end{cases}$$

- (a) one-one and onto (b) neither one-one nor onto
(c) one-one but not onto (d) onto but not one-one

30. The total number of injective mappings from a set with m elements to a set with n elements, $m \leq n$, is

- (a) n^m (b) m^n
(c) mn (d) $\frac{n!}{(n-m)!}$

ANSWERS

Q. No.	1	2	3	4	5	6	7	8	9	10
Answer	(d)	(c)	(c)	(b)	(a)	(c)	(c)	(d)	(d)	(d)
Q. No.	11	12	13	14	15	16	17	18	19	20
Answer	(c)	(b)	(b)	(a)	(d)	(d)	(b)	(c)	(c)	(d)
Q. No.	21	22	23	24	25	26	27	28	29	30
Answer	(d)	(b)	(c)	(b)	(c)	(b)	(a)	(d)	(c)	(d)