

# JEE Main 2021

(February, March, July & August Attempt)

## Instructions

- This question paper contains of 30 Questions of Physics, divided into two Sections : **Section A** Objective Type Questions and **Section B** Numerical Type Questions.
- Section A contains 20 questions and all Questions are compulsory (**Marking Scheme** : Correct + 4, Incorrect -1) .
- Section B contains 10 questions out of which only 5 questions are to be attempted (**Marking Scheme** : Correct + 4, Incorrect 0) .

## 24 FEBRUARY SHIFT I

### Section A : Objective Type Questions

1. The work done by a gas molecule in an isolated system is given by,  $W = \alpha \beta^2 e^{-\frac{x^2}{\alpha kT}}$ , where  $x$  is the displacement,  $k$  is the Boltzmann constant and  $T$  is the temperature,  $\alpha$  and  $\beta$  are constants.

Then, the dimensions of  $\beta$  will be

- a.  $[M^2 L T^2]$                       b.  $[M^0 L T^0]$   
 c.  $[M L T^{-2}]$                       d.  $[M L^2 T^{-2}]$
2. Two stars of masses  $m$  and  $2m$  at a distance  $d$  rotate about their common centre of mass in free space. The period of revolution is
- a.  $\frac{1}{2\pi} \sqrt{\frac{3Gm}{d^3}}$                       b.  $2\pi \sqrt{\frac{d^3}{3Gm}}$   
 c.  $2\pi \sqrt{\frac{3Gm}{d^3}}$                       d.  $\frac{1}{2\pi} \sqrt{\frac{d^3}{3Gm}}$
3. Four identical particles of equal masses 1 kg made to move along the circumference of a circle of radius 1 m under the action of their own mutual gravitational attraction. The speed of each particle will be
- a.  $\sqrt{\frac{(1+2\sqrt{2})G}{2}}$                       b.  $\sqrt{\frac{G}{2}(1+2\sqrt{2})}$   
 c.  $\sqrt{G(1+2\sqrt{2})}$                       d.  $\sqrt{\frac{G}{2}(2\sqrt{2}-1)}$
4. Moment of inertia (MI) of four bodies, having same mass and radius, are reported as  
 $I_1$  = MI of thin circular ring about its diameter,  
 $I_2$  = MI of circular disk about an axis perpendicular to the disk and going through the centre,  
 $I_3$  = MI of solid cylinder about its axis  
 and  $I_4$  = MI of solid sphere about its diameter. Then,
- a.  $I_1 + I_2 = I_3 + \frac{5}{2}I_4$                       b.  $I_1 + I_3 < I_2 + I_4$   
 c.  $I_1 = I_2 = I_3 < I_4$                       d.  $I_1 = I_2 = I_3 > I_4$

5. Consider two satellites  $S_1$  and  $S_2$  with periods of revolution 1 h and 8 h respectively, revolving around a planet in circular orbits. The ratio of angular velocity of satellite  $S_1$  to the angular velocity of satellite  $S_2$  is

- a. 8 : 1                      b. 1 : 8  
 c. 2 : 1                      d. 1 : 4

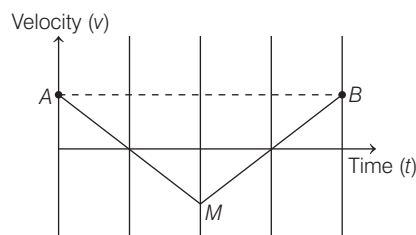
6. Each side of a box made of metal sheet in cubic shape is  $a$  at room temperature  $T$ , the coefficient of linear expansion of the metal sheet is  $\alpha$ . The metal sheet is heated uniformly, by a small temperature  $\Delta T$ , so that its new temperature is  $T + \Delta T$ . Calculate the increase in the volume of the metal box.

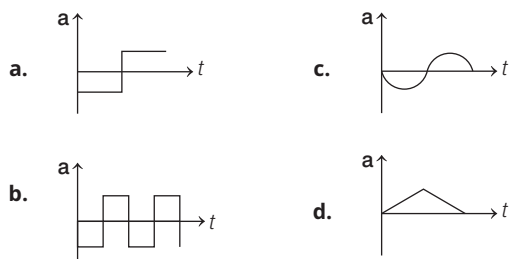
- a.  $4\pi a^3 \alpha \Delta T$                       b.  $4a^3 \alpha \Delta T$   
 c.  $\frac{4}{3}\pi a^3 \alpha \Delta T$                       d.  $3a^3 \alpha \Delta T$

7. If  $Y$ ,  $K$  and  $\eta$  are the values of Young's modulus, bulk modulus and modulus of rigidity of any material, respectively. Choose the correct relation for these parameters.

- a.  $Y = \frac{9K\eta}{2\eta + 3K}$  N/m<sup>2</sup>                      b.  $Y = \frac{9K\eta}{3K - \eta}$  N/m<sup>2</sup>  
 c.  $K = \frac{Y\eta}{9\eta - 3Y}$  N/m<sup>2</sup>                      d.  $\eta = \frac{3YK}{9K + Y}$  N/m<sup>2</sup>

8. If the velocity-time graph has the shape  $AMB$ , what would be the shape of the corresponding acceleration-time graph ?





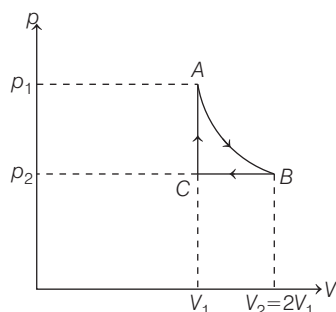
9.  $n$  mole of a perfect gas undergoes a cyclic process  $ABCA$  (see figure) consisting of the following processes.

$A \rightarrow B$  : Isothermal expansion at temperature  $T$ , so that the volume is doubled from  $V_1$  to  $V_2 = 2V_1$  and pressure changes from  $p_1$  to  $p_2$ .

$B \rightarrow C$  : Isobaric compression at pressure  $p_2$  to initial volume  $V_1$ .

$C \rightarrow A$  : Isochoric change leading to change of pressure from  $p_2$  to  $p_1$ .

Total work done in the complete cycle  $ABCA$  is



- a. 0  
b.  $nRT \ln 2$   
c.  $nRT \left( \ln 2 + \frac{1}{2} \right)$   
d.  $nRT \left( \ln 2 - \frac{1}{2} \right)$

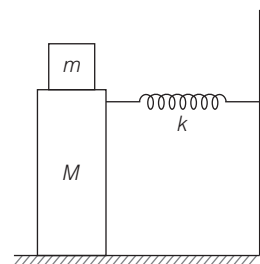
10. Match List-I with List-II.

List-I	List-II
A. Isothermal	1. Pressure constant
B. Isochoric	2. Temperature constant
C. Adiabatic	3. Volume constant
D. Isobaric	4. Heat content is constant

Choose the correct answer from the options given below.

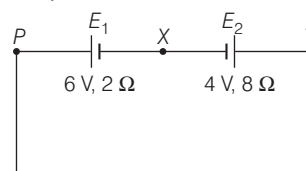
- |       |   |   |   |
|-------|---|---|---|
| A     | B | C | D |
| (a) 1 | 3 | 2 | 4 |
| (b) 3 | 2 | 1 | 4 |
| (c) 2 | 4 | 3 | 1 |
| (d) 2 | 3 | 4 | 1 |

11. In the given figure, a mass  $M$  is attached to a horizontal spring which is fixed on one side to a rigid support. The spring constant of the spring is  $k$ . The mass oscillates on a frictionless surface with time period  $T$  and amplitude  $A$ . When the mass is in equilibrium position as shown in the figure, another mass  $m$  is gently fixed upon it. The new amplitude of oscillation will be



- a.  $A \sqrt{\frac{M+m}{M}}$   
b.  $A \sqrt{\frac{M}{M+m}}$   
c.  $A \sqrt{\frac{M-m}{M}}$   
d.  $A \sqrt{\frac{M}{M-m}}$

12. A cell  $E_1$  of emf 6 V and internal resistance  $2\Omega$  is connected with another cell  $E_2$  of emf 4 V and internal resistance  $8\Omega$  (as shown in the figure). The potential difference across points  $X$  and  $Y$  is



- a. 2.0 V  
b. 3.6 V  
c. 5.6 V  
d. 10.0 V

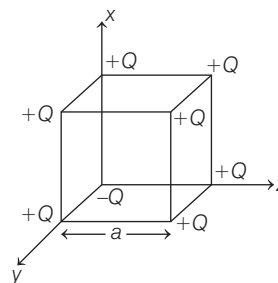
13. A current through a wire depends on time as  $i = \alpha_0 t + \beta t^2$ , where  $\alpha_0 = 20$  A/s and  $\beta = 8$  A s $^{-2}$ . Find the charge crossed through a section of the wire in 15 s.

- a. 260 C  
b. 2100 C  
c. 11250 C  
d. 2250 C

14. Two equal capacitors are first connected in series and then in parallel. The ratio of the equivalent capacities in the two cases will be

- a. 1 : 2  
b. 2 : 1  
c. 4 : 1  
d. 1 : 4

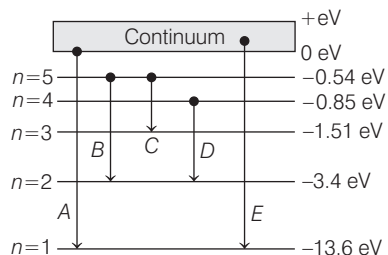
15. A cube of side  $a$  has point charges  $+Q$  located at each of its vertices except at the origin, where the charge is  $-Q$ . The electric field at the centre of cube is



- a.  $\frac{-Q}{3\sqrt{3}\pi\epsilon_0 a^2} (\hat{x} + \hat{y} + \hat{z})$   
b.  $\frac{Q}{3\sqrt{3}\pi\epsilon_0 a^2} (\hat{x} + \hat{y} + \hat{z})$   
c.  $\frac{-2Q}{3\sqrt{3}\pi\epsilon_0 a^2} (\hat{x} + \hat{y} + \hat{z})$   
d.  $\frac{2Q}{3\sqrt{3}\pi\epsilon_0 a^2} (\hat{x} + \hat{y} + \hat{z})$

16. If an emitter current is changed by 4 mA, the collector current changes by 3.5 mA. The value of  $\beta$  will be
- a. 7  
b. 0.875  
c. 0.5  
d. 3.5

17. In the given figure, the energy levels of hydrogen atom have been shown along with some transitions marked A, B, C, D and E. The transitions A, B and C respectively represent



- The first member of the Lyman series, third member of Balmer series and second member of Paschen series.
- The ionisation potential of hydrogen, second member of Balmer series and third member of Paschen series.
- The series limit of Lyman series, second member of Balmer series and second member of Paschen series.
- The series limit of Lyman series, third member of Balmer series and second member of Paschen series.

18. Given below are two statements :

**Statement I** Two photons having equal linear momenta have equal wavelengths.

**Statement II** If the wavelength of photon is decreased, then the momentum and energy of a photon will also decrease.

In the light of the above statements, choose the correct answer from the options given below.

- Both Statement I and Statement II are true.
  - Both Statement I and Statement II are false.
  - Statement I is true but Statement II is false.
  - Statement I is false but Statement II is true.
19. The focal length  $f$  is related to the radius of curvature  $r$  of the spherical convex mirror by
- $f = r$
  - $f = -r$
  - $f = -\frac{r}{2}$
  - $f = +\frac{r}{2}$

20. In a Young's double slit experiment, the width of the one of the slit is three times the other slit. The amplitude of the light coming from a slit is proportional to the slit-width. Find the ratio of the maximum to the minimum intensity in the interference pattern.
- 4 : 1
  - 2 : 1
  - 1 : 4
  - 3 : 1

## Section B : Numerical Type Questions

21. The coefficient of static friction between a wooden block of mass 0.5 kg and a vertical rough wall is 0.2. The magnitude of horizontal force that should be applied on the block to keep it adhere to the wall will be ..... N. [Take,  $g = 10 \text{ ms}^{-2}$ ]

22. An unpolarised light beam is incident on the polariser of a polarisation experiment and the intensity of light beam emerging from the analyser is measured as 100 lumens. Now, if the analyser is rotated around the horizontal axis (direction of light) by  $30^\circ$  in clockwise direction, the intensity of emerging light will be ..... lumens.

23. A ball with a speed of 9 m/s collides with another identical ball at rest. After the collision, the direction of each ball makes an angle of  $30^\circ$  with the original direction. The ratio of velocities of the balls after collision is  $x : y$ , where  $x$  is .....

24. A hydraulic press can lift 100 kg when a mass  $m$  is placed on the smaller piston. It can lift ..... kg when the diameter of the larger piston is increased by 4 times and that of the smaller piston is decreased by 4 times keeping the same mass  $m$  on the smaller piston.

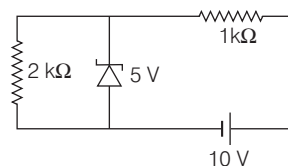
25. An inclined plane is bent in such a way that the vertical cross-section is given by  $y = \frac{x^2}{4}$  where,  $y$  is in vertical and  $x$  in horizontal direction. If the upper surface of this curved plane is rough with coefficient of friction  $\mu = 0.5$ , the maximum height in cm at which a stationary block will not slip downward is ..... cm.

26. A resonance circuit having inductance and resistance  $2 \times 10^{-4} \text{ H}$  and  $6.28 \Omega$  respectively oscillates at 10 MHz frequency. The value of quality factor of this resonator is .....

[Take,  $\pi = 3.14$ ]

27. An audio signal  $v_m = 20 \sin 2\pi(1500 t)$  amplitude modulates a carrier  $v_c = 80 \sin 2\pi(100000 t)$ . The value of per cent modulation is .....

28. In connection with the circuit drawn below, the value of current flowing through  $2 \text{ k}\Omega$  resistor is .....  $\times 10^{-4} \text{ A}$ .



29. An electromagnetic wave of frequency 5 GHz, is travelling in a medium whose relative electric permittivity and relative magnetic permeability both are 2. Its velocity in this medium is .....  $\times 10^7 \text{ m/s}$ .

30. A common transistor radio set requires 12 V (DC) for its operation. The DC source is constructed by using a transformer and a rectifier circuit, which are operated at 220 V (AC) on standard domestic AC supply. The number of turns of secondary coil are 24, then the number of turns of primary are .....

## Answers

- |          |          |         |             |          |            |          |          |          |           |
|----------|----------|---------|-------------|----------|------------|----------|----------|----------|-----------|
| 1. (c)   | 2. (b)   | 3. (*)  | 4. (d)      | 5. (a)   | 6. (d)     | 7. (c)   | 8. (a)   | 9. (d)   | 10. (d)   |
| 11. (b)  | 12. (c)  | 13. (c) | 14. (d)     | 15. (c)  | 16. (a)    | 17. (d)  | 18. (c)  | 19. (d)  | 20. (a)   |
| 21. (25) | 22. (75) | 23. (1) | 24. (25600) | 25. (25) | 26. (2000) | 27. (25) | 28. (25) | 29. (15) | 30. (440) |

**Note** (\*) None of the option is correct.

## 24 FEBRUARY SHIFT II

### Section A : Objective Type Questions

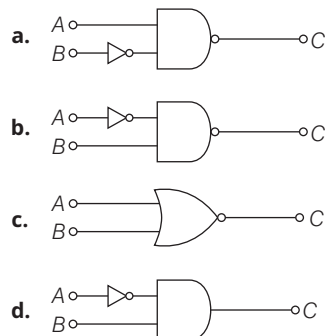
- When a particle executes SHM, the nature of graphical representation of velocity as a function of displacement is  
 a. circular                                      b. elliptical  
 c. parabolic                                      d. straight line
- Two electrons each are fixed at a distance  $2d$ . A third charge proton placed at the mid-point is displaced slightly by a distance  $x$  ( $x \ll d$ ) perpendicular to the line joining the two fixed charges. Proton will execute simple harmonic motion having angular frequency? ( $m$  = mass of charged particle)

- a.  $\left(\frac{2q^2}{\pi\epsilon_0 md^3}\right)^{\frac{1}{2}}$                                       b.  $\left(\frac{\pi\epsilon_0 md^3}{2q^2}\right)^{\frac{1}{2}}$
- c.  $\left(\frac{q^2}{2\pi\epsilon_0 md^3}\right)^{\frac{1}{2}}$                                       d.  $\left(\frac{2\pi\epsilon_0 md^3}{q^2}\right)^{\frac{1}{2}}$

- On the basis of kinetic theory of gases, the gas exerts pressure because its molecules  
 a. continuously lose their energy till it reaches wall  
 b. are attracted by the walls of container  
 c. continuously stick to the walls of container  
 d. suffer change in momentum when impinge on the walls of container
- A soft ferromagnetic material is placed in an external magnetic field. The magnetic domains  
 a. increase in size but no change in orientation  
 b. have no relation with external magnetic field  
 c. decrease in size and changes orientation  
 d. may increase or decrease in size and change its orientation



The logic circuit shown above is equivalent to



- The period of oscillation of a simple pendulum is  $T = 2\pi\sqrt{\frac{L}{g}}$ . Measured value of  $L$  is 1.0 m from metre scale having a minimum division of 1 mm and time of one complete oscillation is 1.95 s measured from stopwatch of 0.01 s resolution. The percentage error in the determination of  $g$  will be  
 a. 1.13%                                      b. 1.03%                                      c. 1.33%                                      d. 1.30%

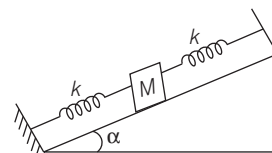
- Given below are two statements:

**Statement I**  $p$ - $n$  junction diodes can be used to function as transistor, simply by connecting two diodes, back to back, which acts as the base terminal.

**Statement II** In the study of transistor, the amplification factor  $\beta$  indicates ratio of the collector current to the base current.

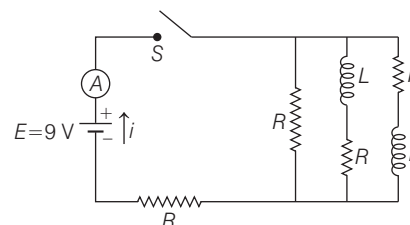
In the light of the above statements, choose the correct answer from the options given below.

- a. Statement I is false but Statement II is true.
  - b. Both Statement I and Statement II are true.
  - c. Both Statement I and Statement II are false.
  - d. Statement I is true but Statement II is false.
- In the given figure, a body of mass  $M$  is held between two massless springs, on a smooth inclined plane. The free ends of the springs are attached to firm supports. If each spring has spring constant  $k$ , then the frequency of oscillation of given body is



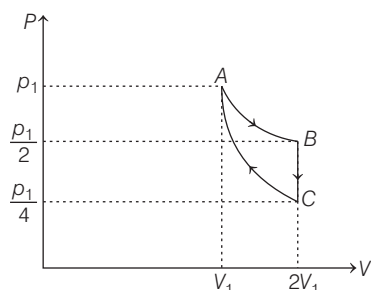
- a.  $\frac{1}{2\pi}\sqrt{\frac{k}{2M}}$                                       b.  $\frac{1}{2\pi}\sqrt{\frac{2k}{Mg\sin\alpha}}$
- c.  $\frac{1}{2\pi}\sqrt{\frac{2k}{M}}$                                       d.  $\frac{1}{2\pi}\sqrt{\frac{k}{Mg\sin\alpha}}$

- Figure shows a circuit that contains four identical resistors with resistance  $R = 2.0 \Omega$ , two identical inductors with inductance  $L = 2.0 \text{ mH}$  and an ideal battery with electromotive force  $E = 9 \text{ V}$ . The current  $i$  just after the switch  $S$  is closed will be



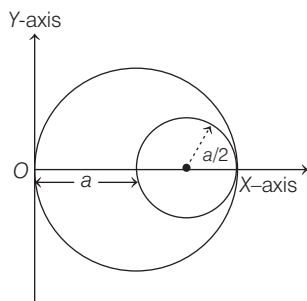
- a. 2.25 A                                      b. 3.0 A                                      c. 3.37 A                                      d. 9 A
- The de-Broglie wavelength of a proton and  $\alpha$ -particle are equal. The ratio of their velocities is  
 a. 4 : 3                                      b. 4 : 1                                      c. 4 : 2                                      d. 1 : 4
  - If one mole of an ideal gas at  $(p_1, V_1)$  is allowed to expand reversibly and isothermally (A to B), its pressure is reduced to one-half of the original pressure (see figure). This is followed by a constant volume cooling till its pressure is reduced to one-fourth of the initial value (B  $\rightarrow$  C). Then, it is restored to its initial

state by a reversible adiabatic compression (C to A). The net work done by the gas is equal to



- a.  $RT \left( \ln 2 - \frac{1}{2(\gamma-1)} \right)$       b.  $-\frac{RT}{2(\gamma-1)}$   
c. 0      d.  $RT \ln 2$

12. An X-ray tube is operated at 1.24 million volt. The shortest wavelength of the produced photon will be  
a.  $10^{-3}$  nm      b.  $10^{-1}$  nm  
c.  $10^{-2}$  nm      d.  $10^{-4}$  nm
13. Which of the following equations represents a travelling wave?  
a.  $y = A \sin(15x - 2t)$       b.  $y = Ae^{-x^2} (vt + \theta)$   
c.  $y = Ae^x \cos(\omega t - \theta)$       d.  $y = A \sin x \cos \omega t$
14. According to Bohr atom model, in which of the following transitions will the frequency be maximum?  
a.  $n = 4$  to  $n = 3$       b.  $n = 2$  to  $n = 1$   
c.  $n = 5$  to  $n = 4$       d.  $n = 3$  to  $n = 2$
15. If the source of light used in a Young's double slit experiment is changed from red to violet, then  
a. the consecutive fringe lines will come closer  
b. the central bright fringe will become a dark fringe  
c. the fringes will become brighter  
d. the intensity of minima will increase
16. A circular hole of radius  $\left(\frac{a}{2}\right)$  is cut out of a circular disc of radius  $a$  as shown in figure. The centroid of the remaining circular portion with respect to point O will be



- a.  $\frac{1}{6}a$       b.  $\frac{10}{11}a$       c.  $\frac{5}{6}a$       d.  $\frac{2}{3}a$

17. Zener breakdown occurs in a  $p$ - $n$  junction having  $p$  and  $n$  both  
a. lightly doped and have wide depletion layer  
b. heavily doped and have narrow depletion layer

- c. lightly doped and have narrow depletion layer  
d. heavily doped and have wide depletion layer

18. Match List-I with List-II.

List-I	List-II
A. Source of microwave frequency	1. Radioactive decay of nucleus
B. Source of infrared frequency	2. Magnetron
C. Source of gamma rays	3. Inner shell electrons
D. Source of X-rays	4. Vibration of atoms and molecules
	5. LASER
	6. R-C circuit

Choose the correct answer from the options given below.

- |      |   |   |   |      |   |   |   |
|------|---|---|---|------|---|---|---|
| A    | B | C | D | A    | B | C | D |
| a. 6 | 4 | 1 | 5 | b. 6 | 5 | 1 | 4 |
| c. 2 | 4 | 6 | 3 | d. 2 | 4 | 1 | 3 |

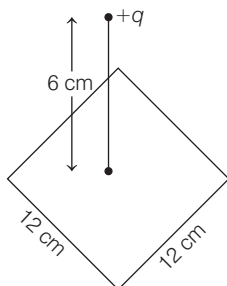
19. A particle is projected with velocity  $v_0$  along  $X$ -axis. A damping force is acting on the particle which is proportional to the square of the distance from the origin, i.e.  $ma = -\alpha x^2$ . The distance at which the particle stops is  
a.  $\left(\frac{3mv_0^2}{2\alpha}\right)^{\frac{1}{2}}$       b.  $\left(\frac{2mv_0}{3\alpha}\right)^{\frac{1}{3}}$   
c.  $\left(\frac{2mv_0^2}{3\alpha}\right)^{\frac{1}{2}}$       d.  $\left(\frac{3mv_0^2}{2\alpha}\right)^{\frac{1}{3}}$
20. A body weights 49 N on a spring balance at the North pole. What will be its weight recorded on the same weighing machine, if it is shifted to the equator?  
(Use,  $g = \frac{GM}{R^2} = 9.8 \text{ ms}^{-2}$  and radius of earth,  $R = 6400 \text{ km}$ )  
a. 49 N      b. 48.83 N  
c. 49.83 N      d. 49.17 N

## Section B : Numerical Type Questions

21. A uniform metallic wire is elongated by 0.04 m when subjected to a linear force  $F$ . The elongation, if its length and diameter is doubled and subjected to the same force will be ..... cm.
22. A cylindrical wire of radius 0.5 mm and conductivity  $5 \times 10^7 \text{ S/m}$  is subjected to an electric field of 10 mV/m. The expected value of current in the wire will be  $x^3 \pi \text{ mA}$ . The value of  $x$  is .....
23. A uniform thin bar of mass 6 kg and length 2.4 m is bent to make an equilateral hexagon. The moment of inertia about an axis passing through the centre of mass and perpendicular to the plane of hexagon is .....  $\times 10^{-1} \text{ kg-m}^2$ .
24. Two solids A and B of mass 1 kg and 2 kg respectively are moving with equal linear momentum. The ratio of their kinetic energies  $(KE)_A : (KE)_B$  will be  $\frac{A}{1}$ , so the value of A will be .....

25. The root mean square speed of molecules of a given mass of a gas at  $27^\circ\text{C}$  and 1 atmosphere pressure is  $200\text{ ms}^{-1}$ . The root mean square speed of molecules of the gas at  $127^\circ\text{C}$  and 2 atmosphere pressure is  $\frac{x}{\sqrt{3}}\text{ ms}^{-1}$ . The value of  $x$  will be .....

26. A point charge of  $+12\text{ }\mu\text{C}$  is at a distance 6 cm vertically above the centre of a square of side 12 cm as shown in figure. The magnitude of the electric flux through the square will be .....  $\times 10^3\text{ N-m}^2/\text{C}$ .



27. A signal of 0.1 kW is transmitted in a cable. The attenuation of cable is  $-5\text{ dB per km}$  and cable length is 20 km. The power received at receiver is  $10^{-x}\text{ W}$ . The value of  $x$  is .....

$$[\text{Gain in dB} = 10 \log_{10} \left( \frac{P_0}{P_i} \right)]$$

28. A series  $L$ - $C$ - $R$  circuit is designed to resonate at an angular frequency  $\omega_0 = 10^5\text{ rad/s}$ . The circuit draws 16 W power from 120 V source at resonance. The value of resistance  $R$  in the circuit is .....  $\Omega$ .
29. Two cars are approaching each other at an equal speed of 7.2 km/h. When they see each other, both blow horns having frequency of 676 Hz. The beat frequency heard by each driver will be ..... Hz. [Velocity of sound in air is 340 m/s.]
30. An electromagnetic wave of frequency 3 GHz enters a dielectric medium of relative electric permittivity 2.25 from vacuum. The wavelength of this wave in that medium will be .....  $\times 10^{-2}\text{ cm}$ .

## Answers

- |         |         |         |         |           |           |         |           |         |           |
|---------|---------|---------|---------|-----------|-----------|---------|-----------|---------|-----------|
| 1. (b)  | 2. (c)  | 3. (d)  | 4. (d)  | 5. (d)    | 6. (a)    | 7. (a)  | 8. (c)    | 9. (a)  | 10. (b)   |
| 11. (a) | 12. (a) | 13. (a) | 14. (b) | 15. (a)   | 16. (c)   | 17. (b) | 18. (d)   | 19. (d) | 20. (b)   |
| 21. (2) | 22. (5) | 23. (8) | 24. (2) | 25. (400) | 26. (226) | 27. (8) | 28. (900) | 29. (8) | 30. (667) |

## 25 FEBRUARY SHIFT I

### Section A : Objective Type Questions

1. Given below are two statements: one is labelled as Assertion A and the other is labelled as Reason R.

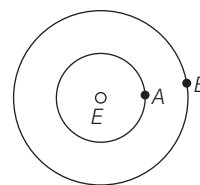
**Assertion (A)** When a rod lying freely is heated, no thermal stress is developed in it.

**Reason (R)** On heating, the length of the rod increases.

In the light of the above statements, choose the correct answer from the options given below

- Both A and R are true but R is not the correct explanation of A.
  - A is false but R is true.
  - A is true but R is false.
  - Both A and R are true and R is the correct explanation of A.
2. A student is performing the experiment of resonance column. The diameter of the column tube is 6 cm. The frequency of the tuning fork is 504 Hz. Speed of the sound at the given temperature is 336 m/s. The zero of the meter scale coincides with the top end of the resonance column tube. The reading of the water level in the column when the first resonance occurs is
- 13 cm
  - 16.6 cm
  - 18.4 cm
  - 14.8 cm
3. Two satellites A and B of masses 200 kg and 400 kg are revolving around the Earth at height of 600 km and 1600

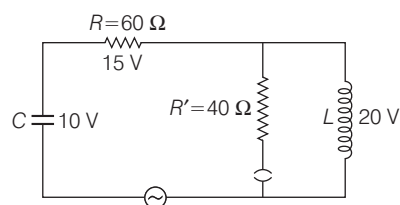
km, respectively. If  $T_A$  and  $T_B$  are the time periods of A and B respectively, then the value of  $T_B - T_A$  is



(Given, radius of Earth = 6400 km, mass of Earth =  $6 \times 10^{24}\text{ kg}$ )

- $1.33 \times 10^3\text{ s}$
- $3.33 \times 10^2\text{ s}$
- $4.24 \times 10^3\text{ s}$
- $4.24 \times 10^2\text{ s}$

4. The angular frequency of alternating current in an  $L$ - $C$ - $R$  circuit is 100 rad/s. The components connected are shown in the figure. Find the value of inductance of the coil and capacity of condenser.





- a. 0.8 H and  $150\mu\text{F}$       b. 0.8 H and  $250\mu\text{F}$   
 c. 1.33 H and  $250\mu\text{F}$       d. 1.33 H and  $150\mu\text{F}$

5. A proton, a deuteron and an  $\alpha$ -particle are moving with same momentum in a uniform magnetic field. The ratio of magnetic forces acting on them is ..... and their speed is ..... in the ratio.  
 a. 1 : 2 : 4 and 2 : 1 : 1      b. 2 : 1 : 1 and 4 : 2 : 1  
 c. 4 : 2 : 1 and 2 : 1 : 1      d. 1 : 2 : 4 and 1 : 1 : 2

6. Given, below are two statements

**Statement I** A speech signal of 2 kHz is used to modulate a carrier signal of 1 MHz. The bandwidth requirement for the signal is 4 kHz.

**Statement II** The side band frequencies are 1002 kHz and 998 kHz. In the light of the above statements, choose the correct answer from the options given below

- a. Statement I is true but Statement II is false.  
 b. Statement I is false but Statement II is true.  
 c. Both Statement I and Statement II are true.  
 d. Both Statement I and Statement II are false.

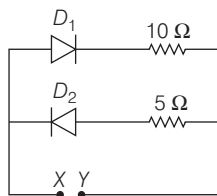
7. If the time period of a 2 m long simple pendulum is 2 s, the acceleration due to gravity at the place, where pendulum is executing SHM is

- a.  $\pi^2\text{ms}^{-2}$       b.  $9.8\text{ms}^{-2}$       c.  $2\pi^2\text{ms}^{-2}$       d.  $16\text{ms}^{-2}$

8. The pitch of the screw gauge is 1 mm and there are 100 divisions on the circular scale. When nothing is put in between the jaws, the zero of the circular scale lies 8 divisions below the reference line. When a wire is placed between the jaws, the first linear scale division is clearly visible while 72nd division on circular scale coincides with the reference line. The radius of the wire is

- a. 1.64 mm      b. 0.82 mm  
 c. 1.80 mm      d. 0.90 mm

9. A 5 V battery is connected across the points X and Y. Assume  $D_1$  and  $D_2$  to be normal silicon diodes. Find the current supplied by the battery, if the positive terminal of the battery is connected to point X.



- a.  $\sim 0.5\text{ A}$       b.  $\sim 1.5\text{ A}$   
 c.  $\sim 0.86\text{ A}$       d.  $\sim 0.43\text{ A}$

10. An  $\alpha$ -particle and a proton are accelerated from rest by a potential difference of 200 V. After this, their de-Broglie wavelengths are  $\lambda_\alpha$  and  $\lambda_p$ , respectively. The ratio  $\frac{\lambda_p}{\lambda_\alpha}$  is

- a. 3.8      b. 8      c. 7.8      d. 2.8

11. A diatomic gas having  $C_p = \frac{7}{2}R$  and  $C_v = \frac{5}{2}R$ , is heated at constant pressure. The ratio  $dU : dQ : dW$  is

- a. 5 : 7 : 3      b. 5 : 7 : 2      c. 3 : 7 : 2      d. 3 : 5 : 2

12. An engine of a train moving with uniform acceleration, passes the signal-post with velocity  $u$  and the last compartment with velocity  $v$ . The velocity with which middle point of the train passes the signal post is

- a.  $\sqrt{\frac{v^2 + u^2}{2}}$       b.  $\frac{v-u}{2}$       c.  $\frac{u+v}{2}$       d.  $\sqrt{\frac{v^2 - u^2}{2}}$

13. Match List-I with List-II

List-I	List-II
A. $h$ (Planck's constant)	1. $[\text{M L T}^{-1}]$
B. $E$ (kinetic energy)	2. $[\text{M L}^2\text{T}^{-1}]$
C. $V$ (electric potential)	3. $[\text{M L}^2\text{T}^{-2}]$
D. $P$ (linear momentum)	4. $[\text{M L}^2\text{T}^{-3}]$

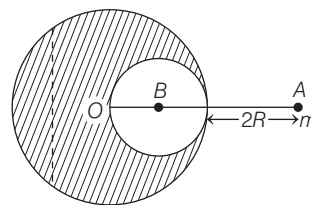
Choose the correct answer from the options given below.

- |    |   |   |   |   |
|----|---|---|---|---|
|    | A | B | C | D |
| a. | 3 | 4 | 2 | 1 |
| b. | 2 | 3 | 4 | 1 |
| c. | 1 | 2 | 4 | 3 |
| d. | 3 | 2 | 4 | 1 |

14. Magnetic fields at two points on the axis of a circular coil at a distance of 0.05 m and 0.2 m from the centre are in the ratio 8 : 1. The radius of coil is

- a. 0.2 m      b. 0.1 m  
 c. 0.15 m      d. 1.0 m

15. A solid sphere of radius  $R$  gravitationally attracts a particle placed at  $3R$  from its centre with a force  $F_1$ . Now, a spherical cavity of radius  $\left(\frac{R}{2}\right)$  is made in the sphere (as shown in figure) and the force becomes  $F_2$ . The value of  $F_1 : F_2$  is

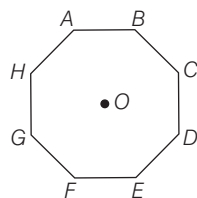


- a. 25 : 36      b. 36 : 25  
 c. 50 : 41      d. 41 : 50

16. Two radioactive substances X and Y originally have  $N_1$  and  $N_2$  nuclei, respectively. Half-life of X is half of the half-life of Y. After three half-lives of Y, number of nuclei of both are equal. The ratio  $\frac{N_1}{N_2}$  will be equal to

- a.  $\frac{1}{8}$       b.  $\frac{3}{1}$   
 c.  $\frac{8}{1}$       d.  $\frac{1}{3}$

17. In an octagon  $ABCDEFGH$  of equal side, what is the sum of  $\overline{AB} + \overline{AC} + \overline{AD} + \overline{AE} + \overline{AF} + \overline{AG} + \overline{AH}$  if,  $\overline{AO} = 2\hat{i} + 3\hat{j} - 4\hat{k}$ ?



- a.  $-16\hat{i} - 24\hat{j} + 32\hat{k}$       b.  $16\hat{i} + 24\hat{j} - 32\hat{k}$   
 c.  $16\hat{i} + 24\hat{j} + 32\hat{k}$       d.  $16\hat{i} - 24\hat{j} + 32\hat{k}$

18. Given below are two statements: one is labelled as Assertion A and the other is labelled as Reason R.

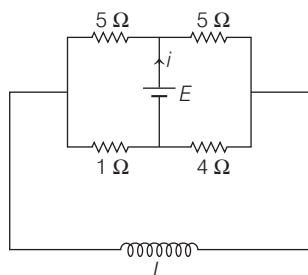
**Assertion A** The escape velocities of planet A and B are same. But A and B are of unequal mass.

**Reason R** The product of their mass and radius must be same,  $M_1 R_1 = M_2 R_2$

In the light of the above statements, choose the most appropriate answer from the options given below.

- (a) Both A and R are correct but R is not the correct explanation of A.  
 (b) A is correct but R is not correct.  
 (c) Both A and R are correct and R is the correct explanation of A.  
 (d) A is not correct but R is correct.

19. The current ( $i$ ) at time  $t = 0$  and  $t = \infty$  respectively for the given circuit is



- a.  $\frac{18E}{55}, \frac{5E}{18}$       b.  $\frac{10E}{33}, \frac{5E}{18}$       c.  $\frac{5E}{18}, \frac{18E}{55}$       d.  $\frac{5E}{18}, \frac{10E}{33}$

20. Two coherent light sources having intensity in the ratio  $2x$  produce an interference pattern. The ratio  $\frac{I_{\max} - I_{\min}}{I_{\max} + I_{\min}}$

will be

- a.  $\frac{2\sqrt{2x}}{x+1}$       b.  $\frac{\sqrt{2x}}{2x+1}$       c.  $\frac{\sqrt{2x}}{x+1}$       d.  $\frac{2\sqrt{2x}}{2x+1}$

## Section B : Numerical Type Questions

21. A transmitting station releases waves of wavelength 960 m. A capacitor of  $2.56 \mu\text{F}$  is used in the resonant circuit. The self-inductance of coil necessary for resonance is  $\dots \times 10^{-8} \text{ H}$ .

22. The electric field in a region is given

$$\mathbf{E} = \left( \frac{3}{5} E_0 \hat{i} + \frac{4}{5} E_0 \hat{j} \right) \frac{\text{N}}{\text{C}}$$

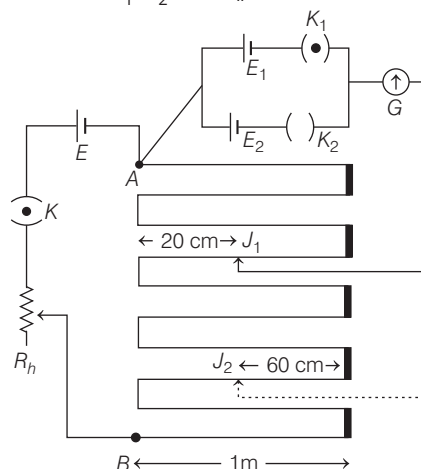
The ratio of flux of reported field through the rectangular surface of area  $0.2 \text{ m}^2$  (parallel to YZ-plane) to that of the surface of area  $0.3 \text{ m}^2$  (parallel to XZ-plane) is  $a : b$ , where  $a = \dots$ .

[Here  $\hat{i}$ ,  $\hat{j}$  and  $\hat{k}$  are unit vectors along X, Y and Z-axes, respectively]

23. In a certain thermodynamical process, the pressure of a gas depends on its volume as  $kV^3$ . The work done when the temperature changes from  $100^\circ\text{C}$  to  $300^\circ\text{C}$  will be  $\dots nR$ , where  $n$  denotes number of moles of a gas.

24. A small bob tied at one end of a thin string of length 1 m is describing a vertical circle, so that the maximum and minimum tension in the string are in the ratio 5 : 1. The velocity of the bob at the highest position is  $\dots \text{ m/s}$ . (Take,  $g = 10 \text{ m/s}^2$ )

25. In the given circuit of potentiometer, the potential difference  $E$  across  $AB$  (10 m length) is larger than  $E_1$  and  $E_2$  as well. For key  $K_1$  (closed), the jockey is adjusted to touch the wire at point  $J_1$ , so that there is no deflection in the galvanometer. Now, the first battery ( $E_1$ ) is replaced by second battery ( $E_2$ ) for working by making  $K_1$  open and  $K_2$  closed. The galvanometer gives then null deflection at  $J_2$ . The value of  $E_1/E_2$  is  $a/b$ , where  $a = \dots$ .



26. The same size images are formed by a convex lens when the object is placed at 20 cm or at 10 cm from the lens. The focal length of convex lens is  $\dots \text{ cm}$ .

27. 512 identical drops of mercury are charged to a potential of 2 V each. The drops are joined to form a single drop. The potential of this drop is  $\dots \text{ V}$ .

28. A coil of inductance 2 H having negligible resistance is connected to a source of supply whose voltage is given by  $V = 3t \text{ V}$  (where,  $t$  is in second). If the voltage is applied when  $t = 0$ , then the energy stored in the coil after 4 s is  $\dots \text{ J}$ .

29. A monoatomic gas of mass 4.0 u is kept in an insulated container. Container is moving with velocity 30 m/s. If container is suddenly stopped, then change in temperature of the gas ( $R = \text{gas constant}$ ) is  $\frac{x}{3R}$ . Value of  $x$  is  $\dots$ .

30. The potential energy ( $U$ ) of a diatomic molecule is a function dependent on  $r$  (interatomic distance) as  $U = \frac{\alpha}{r^{10}} - \frac{\beta}{r^5} - 3$

where,  $\alpha$  and  $\beta$  are positive constants. The equilibrium distance between two atoms will be  $\left( \frac{2\alpha}{\beta} \right)^{a/b}$ , where  $a = \dots$ .



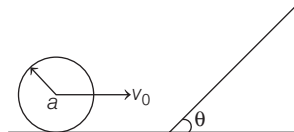
## Answers

- |          |         |          |         |         |          |           |           |            |         |
|----------|---------|----------|---------|---------|----------|-----------|-----------|------------|---------|
| 1. (a)   | 2. (d)  | 3. (a)   | 4. (b)  | 5. (b)  | 6. (c)   | 7. (c)    | 8. (b)    | 9. (d)     | 10. (d) |
| 11. (b)  | 12. (a) | 13. (b)  | 14. (b) | 15. (c) | 16. (c)  | 17. (b)   | 18. (b)   | 19. (d)    | 20. (d) |
| 21. (10) | 22. (1) | 23. (50) | 24. (5) | 25. (1) | 26. (15) | 27. (128) | 28. (144) | 29. (3600) | 30. (1) |

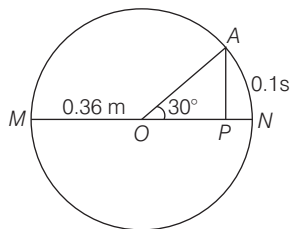
## 25 FEBRUARY SHIFT II

### Section A : Objective Type Questions

- If  $e$  is the electronic charge,  $c$  is the speed of light in free space and  $h$  is Planck's constant, the quantity  $\frac{1}{4\pi\epsilon_0} \frac{|e|^2}{hc}$  has dimensions of
  - $[MLT^0]$
  - $[MLT^{-1}]$
  - $[M^0L^0T^0]$
  - $[LC^{-1}]$
- A stone is dropped from the top of a building. When it crosses a point 5 m below the top, another stone starts to fall from a point 25 m below the top. Both stones reach the bottom of building simultaneously. The height of the building is
  - 45 m
  - 25 m
  - 35 m
  - 50 m
- A sphere of radius  $a$  and mass  $m$  rolls along a horizontal plane with constant speed  $v_0$ . It encounters an inclined plane at angle  $\theta$  and climbs upwards. Assuming that it rolls without slipping, how far up the sphere will travel?



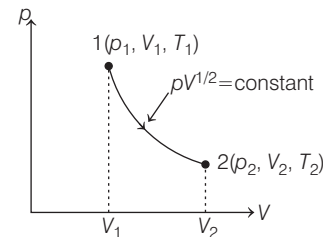
- $\frac{v_0^2}{2g \sin \theta}$
  - $\frac{v_0^2}{5g \sin \theta}$
  - $\frac{10v_0^2}{7g \sin \theta}$
  - $\frac{2}{5} \frac{v_0^2}{g \sin \theta}$
- The point A moves with a uniform speed along the circumference of a circle of radius 0.36 m and covers  $30^\circ$  in 0.1 s. The perpendicular projection P from A on the diameter MN represents the simple harmonic motion of P. The restoration force per unit mass when P touches M will be



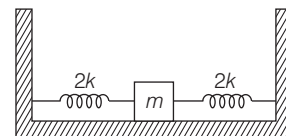
- 100 N
- 9.87 N
- 50 N
- 0.49 N

- Thermodynamic process is shown below on a  $p$ - $V$  diagram for one mole of an ideal gas.

If  $V_2 = 2V_1$ , then the ratio of temperature  $\frac{T_2}{T_1}$  is



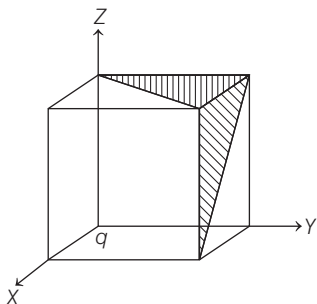
- $\frac{1}{\sqrt{2}}$
  - $\sqrt{2}$
  - $\frac{1}{2}$
  - 2
- Given below are two statements:  
**Statement I** In a diatomic molecule, the rotational energy at a given temperature obeys Maxwell's distribution.  
**Statement II** In a diatomic molecule, the rotational energy at a given temperature equals the translational kinetic energy for each molecule.  
 In the light of the above statements, choose the correct answer from the options given below.
    - Both Statement I and Statement II are true.
    - Both Statement I and Statement II are false.
    - Statement I is true but Statement II is false.
    - Statement I is false but Statement II is true.
  - Two identical springs of spring constant  $2k$  are attached to a block of mass  $m$  and to fixed support (see figure). When the mass is displaced from equilibrium position on either side, it executes simple harmonic motion. The time period of oscillations of this system is



- $2\pi\sqrt{\frac{m}{2k}}$
- $2\pi\sqrt{\frac{m}{k}}$
- $\pi\sqrt{\frac{m}{k}}$
- $\pi\sqrt{\frac{m}{2k}}$

8.  $Y = A \sin(\omega t + \phi_0)$  is the time-displacement equation of SHM. At  $t = 0$ , the displacement of the particle is  $Y = \frac{A}{2}$  and it is moving along negative  $x$ -direction. Then, the initial phase angle  $\phi_0$  will be
- a.  $\frac{\pi}{3}$       b.  $\frac{5\pi}{6}$       c.  $\frac{\pi}{6}$       d.  $\frac{2\pi}{3}$

9. A charge  $q$  is placed at one corner of a cube as shown in figure. The flux of electrostatic field  $\mathbf{E}$  through the shaded area is

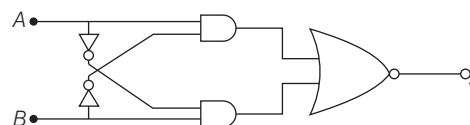


- a.  $\frac{q}{48\epsilon_0}$       b.  $\frac{q}{4\epsilon_0}$       c.  $\frac{q}{8\epsilon_0}$       d.  $\frac{q}{24\epsilon_0}$

10. An electron with kinetic energy  $K_1$  enters between parallel plates of a capacitor at an angle  $\alpha$  with the plates. It leaves the plates at angle  $\beta$  with kinetic energy  $K_2$ . Then, the ratio of kinetic energies  $K_1 : K_2$  will be
- a.  $\frac{\cos \beta}{\cos \alpha}$       b.  $\frac{\cos \beta}{\sin \alpha}$   
c.  $\frac{\sin^2 \beta}{\cos^2 \alpha}$       d.  $\frac{\cos^2 \beta}{\cos^2 \alpha}$
11. In a ferromagnetic material, below the Curie temperature, a domain is defined as
- a. a macroscopic region with zero magnetisation  
b. a macroscopic region with saturation magnetisation  
c. a macroscopic region with randomly oriented magnetic dipoles  
d. a macroscopic region with consecutive magnetic dipoles oriented in opposite direction
12. An  $L$ - $C$ - $R$  circuit contains resistance of  $110\Omega$  and a supply of  $220\text{ V}$  at  $300\text{ rad/s}$  angular frequency. If only capacitance is removed from the circuit, current lags behind the voltage by  $45^\circ$ . If on the other hand, only inductor is removed the current leads by  $45^\circ$  with the applied voltage. The rms current flowing in the circuit will be
- a.  $1\text{ A}$       b.  $1.5\text{ A}$       c.  $2\text{ A}$       d.  $2.5\text{ A}$
13. The stopping potential for electrons emitted from a photosensitive surface illuminated by light of wavelength  $491\text{ nm}$  is  $0.710\text{ V}$ . When the incident wavelength is changed to a new value, the stopping potential is  $1.43\text{ V}$ . The new wavelength is
- a.  $309\text{ nm}$       b.  $329\text{ nm}$   
c.  $382\text{ nm}$       d.  $400\text{ nm}$
14. Consider the diffraction pattern obtained from the sunlight incident on a pinhole of diameter  $0.1\mu\text{m}$ . If the

diameter of the pinhole is slightly increased, it will affect the diffraction pattern such that

- a. its size increases and intensity increases  
b. its size increases, but intensity decreases  
c. its size decreases, but intensity increases  
d. its size decreases and intensity decreases
15. An electron of mass  $m_e$  and a proton of mass  $m_p = 1836 m_e$  are moving with the same speed. The ratio of their de-Broglie wavelength  $\frac{\lambda_{\text{electron}}}{\lambda_{\text{proton}}}$  will be
- a. 1      b. 1836      c.  $\frac{1}{1836}$       d. 918
16. The wavelength of the photon emitted by a hydrogen atom when an electron makes a transition from  $n = 2$  to  $n = 1$  state is
- a.  $121.8\text{ nm}$       b.  $194.8\text{ nm}$   
c.  $490.7\text{ nm}$       d.  $913.3\text{ nm}$
17. If a message signal of frequency  $f_m$  is amplitude modulated with a carrier signal of frequency  $f_c$  and radiated through an antenna, the wavelength of the corresponding signal in air is
- a.  $\frac{c}{f_c - f_m}$       b.  $\frac{c}{f_c + f_m}$       c.  $\frac{c}{f_c}$       d.  $\frac{c}{f_m}$
18. For extrinsic semiconductors when doping level is increased,
- a. Fermi level of  $p$ -type semiconductor will go upward and Fermi level of  $n$ -type semiconductors will go downward  
b. Fermi level of  $p$ -type semiconductors will go downward and Fermi level of  $n$ -type semiconductor will go upward  
c. Fermi level of  $p$  and  $n$ -type semiconductors will not be affected  
d. Fermi level of both  $p$ -type and  $n$ -type semiconductors will go upward for  $T > T_F$  K and downward for  $T < T_F$  K, where  $T_F$  is Fermi temperature
19. Match List-I with List-II.
- | List-I         | List-II  |
|----------------|--|
| A. Rectifier   | 1. Used either for stepping up or stepping down the AC voltage                         |
| B. Stabiliser  | 2. Used to convert AC voltage into DC voltage  |
| C. Transformer | 3. Used to remove any ripple in the rectified output voltage                           |
| D. Filter      | 4. Used for constant output voltage even when the input voltage or load current change |
- Choose the correct answer from the options given below.
- |      |   |   |   |      |   |   |   |
|------|---|---|---|------|---|---|---|
| A    | B | C | D | A    | B | C | D |
| a. 2 | 1 | 3 | 4 | b. 2 | 4 | 1 | 3 |
| b. 2 | 1 | 4 | 3 | c. 3 | 4 | 1 | 2 |
20. The truth table for the following logic circuit is



a.

A	B	Y
0	0	0
0	1	1
1	0	1
1	1	0

b.

A	B	Y
0	0	1
0	1	0
1	0	0
1	1	1

c.

A	B	Y
0	0	1
0	1	0
1	0	1
1	1	0

d.

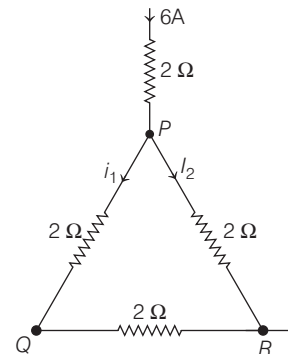
A	B	Y
0	0	0
0	1	1
1	0	0
1	1	1

### Section B : Numerical Type Questions

21. Two particles having masses 4 g and 16 g respectively are moving with equal kinetic energies. The ratio of the magnitudes of their linear momentum is  $n : 2$ . The value of  $n$  will be .....
22. The initial velocity  $v_i$  required to project a body vertically upward from the surface of the Earth to reach a height of  $10R$ , where  $R$  is the radius of the Earth, may be described in terms of escape velocity  $v_e$  such that  $v_i = \sqrt{\frac{x}{y}} \times v_e$ . The value of  $x$  will be .....
23. The percentage increase in the speed of transverse waves produced in a stretched string, if the tension is increased by 4%, will be ..... %.
24. If  $\mathbf{P} \times \mathbf{Q} = \mathbf{Q} \times \mathbf{P}$ , the angle between  $\mathbf{P}$  and  $\mathbf{Q}$  is  $\theta$  ( $0^\circ < \theta < 360^\circ$ ). The value of  $\theta$  will be .....°.
25. A reversible heat engine converts one-fourth of the heat input into work. When the temperature of the sink is

reduced by 52 K, its efficiency is doubled. The temperature in kelvin of the source will be .....

26. Two small spheres each of mass 10 mg are suspended from a point by threads 0.5 m long. They are equally charged and repel each other to a distance of 0.20 m. The charge on each of the sphere is  $\frac{a}{21} \times 10^{-8}$  C. The value of  $a$  will be .....
- [Given,  $g = 10 \text{ ms}^{-2}$ ]
27. Two identical conducting spheres with negligible volume have 2.1 nC and - 0.1 nC charges, respectively. They are brought into contact and then separated by a distance of 0.5 m. The electrostatic force acting between the spheres is .....  $\times 10^{-9}$  N.
- [Given,  $4\pi\epsilon_0 = \frac{1}{9 \times 10^9}$  SI unit]
28. The peak electric field produced by the radiation coming from the 8 W bulb at a distance of 10 m is  $\frac{x}{10} \sqrt{\frac{\mu_0 c}{\pi}} \frac{\text{V}}{\text{m}}$ . The efficiency of the bulb is 10% and it is a point source. The value of  $x$  is .....
29. A current of 6 A enters one corner  $P$  of an equilateral triangle  $PQR$  having three wires of resistance  $2 \Omega$  each and leaves by the corner  $R$ . The currents  $i_1$  in ampere is .....



30. The wavelength of an X-ray beam is  $10 \text{ \AA}$ . The mass of a fictitious particle having the same energy as that of the X-ray photons is  $\frac{x}{3} h$  kg. The value of  $x$  is ..... .
- ( $h$  = Planck's constant)

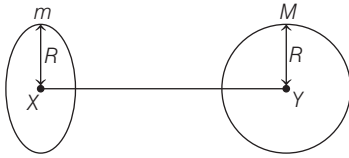
## Answers

- |         |          |         |           |           |           |            |         |         |          |
|---------|----------|---------|-----------|-----------|-----------|------------|---------|---------|----------|
| 1. (c)  | 2. (a)   | 3. (*)  | 4. (b)    | 5. (b)    | 6. (c)    | 7. (c)     | 8. (c)  | 9. (d)  | 10. (d)  |
| 11. (b) | 12. (c)  | 13. (c) | 14. (c)   | 15. (b)   | 16. (a)   | 17. (c)    | 18. (b) | 19. (b) | 20. (b)  |
| 21. (1) | 22. (10) | 23. (2) | 24. (180) | 25. (104) | 26. (630) | 27. (7.56) | 28. (2) | 29. (2) | 30. (10) |

## 26 FEBRUARY SHIFT I

### Objective Type Questions

1. Find the gravitational force of attraction between the ring and sphere as shown in the figure, where the plane of the ring is perpendicular to the line joining the centres. If  $\sqrt{8}R$  is the distance between the centres of a ring (of mass  $m$ ) and a sphere (of mass  $M$ ), where both have equal radius  $R$ .



- a.  $\frac{\sqrt{8}}{9} \cdot \frac{GmM}{R}$     b.  $\frac{2\sqrt{2}}{3} \cdot \frac{GmM}{R^2}$     c.  $\frac{1}{3\sqrt{8}} \cdot \frac{GmM}{R^2}$     d.  $\frac{\sqrt{8}}{27} \cdot \frac{GmM}{R^2}$
2. Consider the combination of two capacitors  $C_1$  and  $C_2$ , with  $C_2 > C_1$ , when connected in parallel, the equivalent capacitance is  $15/4$  time the equivalent capacitance of the same connected in series. Calculate the ratio of capacitors  $\frac{C_2}{C_1}$ .
- a.  $\frac{15}{11}$     b.  $\frac{111}{80}$     c.  $\frac{29}{15}$     d.  $\frac{15}{4}$
3. In a typical combustion engine, the work done by a gas molecule is given  $W = \alpha^2 \beta e^{\frac{-\beta x^2}{kT}}$ , where  $x$  is the displacement,  $k$  is the Boltzmann constant and  $T$  is the temperature. If  $\alpha$  and  $\beta$  are constants, dimensions of  $\alpha$  will be
- a.  $[MLT^{-2}]$     b.  $[M^0LT^0]$     c.  $[M^2LT^{-2}]$     d.  $[MLT^{-1}]$
4. If  $\lambda_1$  and  $\lambda_2$  are the wavelengths of the third member of Lyman and first member of the Paschen series respectively, then the value of  $\lambda_1 : \lambda_2$  is
- a. 1 : 9    b. 7 : 108    c. 7 : 135    d. 1 : 3
5. A short straight object of height 100 cm lies before the central axis of a spherical mirror, whose focal length has absolute value  $f = 40$  cm. The image of object produced by the mirror is of height 25 cm and has the same orientation of the object. One may conclude from the information.
- a. Image is real, same side of concave mirror  
b. Image is virtual, opposite side of concave mirror  
c. Image is real, same side of convex mirror  
d. Image is virtual, opposite side of convex mirror
6. Assume that a tunnel is dug along a chord of the earth, at a perpendicular distance  $\left(\frac{R}{2}\right)$  from the earth's centre, where  $R$  is the radius of the earth. The wall of the tunnel is frictionless. If a particle is released in this tunnel, it will execute a simple harmonic motion with a time period?

a.  $\frac{2\pi R}{g}$     b.  $\frac{g}{2\pi R}$     c.  $\frac{1}{2\pi} \sqrt{\frac{g}{R}}$     d.  $2\pi \sqrt{\frac{R}{g}}$

7. An alternating current is given by the equation  $i = i_1 \sin \omega t + i_2 \cos \omega t$ . The rms current will be
- a.  $\frac{1}{\sqrt{2}} (i_1^2 + i_2^2)^{1/2}$     b.  $\frac{1}{\sqrt{2}} (i_1 + i_2)^2$   
c.  $\frac{1}{2} (i_1^2 + i_2^2)^{1/2}$     d.  $\frac{1}{\sqrt{2}} (i_1 + i_2)$
8. The normal density of a material is  $\rho$  and its bulk modulus of elasticity is  $K$ . The magnitude of increase in density of material, when a pressure  $p$  is applied uniformly on all sides, will be
- a.  $\frac{\rho K}{p}$     b.  $\frac{\rho p}{K}$     c.  $\frac{K}{\rho p}$     d.  $\frac{\rho K}{p}$
9. A particle is moving with uniform speed along the circumference of a circle of radius  $R$  under the action of a central fictitious force  $F$  which is inversely proportional to  $R^3$ . Its time period of revolution will be given by
- a.  $T \propto R^2$     b.  $T \propto R^{3/2}$   
c.  $T \propto R^{5/2}$     d.  $T \propto R^{4/3}$
10. A planet revolving in elliptical orbit has
- a constant velocity of revolution
  - has the least velocity when it is nearest to the Sun
  - its areal velocity is directly proportional to its velocity
  - areal velocity is inversely proportional to its velocity.
  - to follow a trajectory such that the areal velocity is constant.
- Choose the correct answer from the options given below.
- a. Only I    b. Only IV  
c. Only III    d. Only V
11. Given below are two statements : one is labelled as Assertion A and the other is labelled as Reason R.
- Assertion A** Body  $P$  having mass  $M$  moving with speed  $u$  has head-on collision elastically with another body  $Q$  having mass  $m$  initially at rest. If  $m \ll M$ , body  $Q$  will have a maximum speed equal to  $2u$  after collision.
- Reason R** During elastic collision, the momentum and kinetic energy are both conserved.
- In the light of the above statements, choose the most appropriate answer from the options given below.
- a. A is not correct but R is correct.  
b. Both A and R are correct but R is not the correct explanation of A.  
c. Both A and R are correct and R is the correct explanation of A.  
d. A is correct but R is not correct.
12. Four identical solid spheres each of mass  $m$  and radius  $a$  are placed with their centres on the four corners of a square of side  $b$ . The moment of inertia of the system

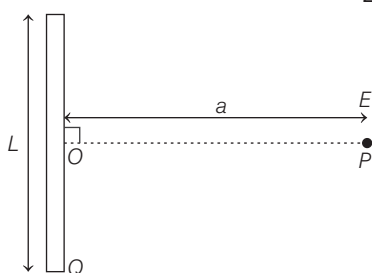
about one side of square, where the axis of rotation is parallel to the plane of the square is

- a.  $\frac{4}{5} ma^2 + 2mb^2$       b.  $\frac{8}{5} ma^2 + mb^2$   
c.  $\frac{8}{5} ma^2 + 2mb^2$       d.  $\frac{4}{5} ma^2$

13. In a Young's double slit experiment, two slits are separated by 2 mm and the screen is placed one metre away. When a light of wavelength 500 nm is used, the fringe separation will be

- a. 0.25 mm      b. 0.50 mm  
c. 0.75 mm      d. 1 mm

14. Find the electric field at point  $P$  (as shown in figure) on the perpendicular bisector of a uniformly charged thin wire of length  $L$  carrying a charge  $Q$ . The distance of the point  $P$  from the centre of the rod is  $a = \frac{\sqrt{3}}{2} L$ .

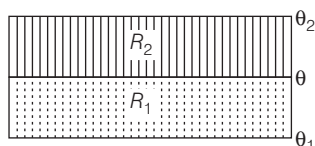


- a.  $\frac{\sqrt{3}Q}{4\pi\epsilon_0 L^2}$       b.  $\frac{Q}{3\pi\epsilon_0 L^2}$   
c.  $\frac{Q}{2\sqrt{3}\pi\epsilon_0 L^2}$       d.  $\frac{Q}{4\pi\epsilon_0 L^2}$

15. If two similar springs each of spring constant  $K_1$  are joined in series, the new spring constant and time period would be changed by a factor

- a.  $\frac{1}{2}, \sqrt{2}$       b.  $\frac{1}{4}, \sqrt{2}$   
c.  $\frac{1}{4}, 2\sqrt{2}$       d.  $\frac{1}{2}, 2\sqrt{2}$

16. The temperature  $\theta$  at the junction of two insulating sheets, having thermal resistances  $R_1$  and  $R_2$  as well as top and bottom temperatures  $\theta_1$  and  $\theta_2$  (as shown in figure) is given by



- a.  $\frac{\theta_2 R_2 - \theta_1 R_1}{R_2 - R_1}$       b.  $\frac{\theta_1 R_2 - \theta_2 R_1}{R_2 - R_1}$       c.  $\frac{\theta_1 R_2 + \theta_2 R_1}{R_1 + R_2}$       d.  $\frac{\theta_1 R_1 + \theta_2 R_2}{R_1 + R_2}$

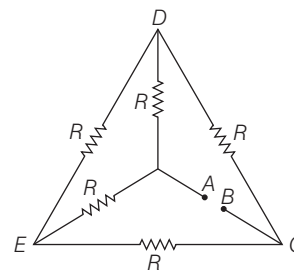
17. Given below are two statements: One is labelled as Assertion A and the other is labelled as Reason R.

**Assertion A** An electron microscope can achieve better resolving power than an optical microscope.

**Reason R** The de-Broglie's wavelength of the electrons emitted from an electron gun is much less than wavelength of visible light.

In the light of the above statements, choose the correct answer from the options given below.

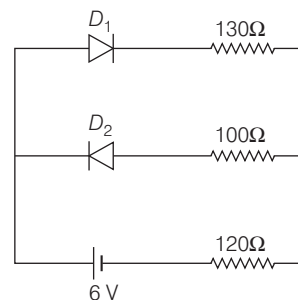
- a. A is true but R is false.  
b. Both A and R are true and R is the correct explanation of A.  
c. Both A and R are true but R is not the correct explanation of A.  
d. A is false but R is true.
18. LED is constructed from GaAsP semiconducting material. The energy gap of this LED is 1.9 eV. Calculate the wavelength of light emitted and its colour. [ $h = 6.63 \times 10^{-34}$  Js and  $c = 3 \times 10^8$  ms $^{-1}$ ]  
a. 1046 nm and red colour      b. 654 nm and orange colour  
c. 1046 nm and blue colour      d. 654 nm and red colour
19. A large number of water drops, each of radius  $r$ , combine to have a drop of radius  $R$ . If the surface tension is  $T$  and mechanical equivalent of heat is  $J$ , the rise in heat energy per unit volume will be  
a.  $\frac{2T}{J} \left( \frac{1}{r} - \frac{1}{R} \right)$       b.  $\frac{2T}{rJ}$       c.  $\frac{3T}{rJ}$       d.  $\frac{3T}{J} \left( \frac{1}{r} - \frac{1}{R} \right)$
20. Five equal resistances are connected in a network as shown in figure. The net resistance between the points A and B is



- a.  $2R$       b.  $\frac{R}{2}$       c.  $\frac{3R}{2}$       d.  $R$

## Section B : Numerical Type Questions

21. A person standing on a spring balance inside a stationary lift measures 60 kg. The weight of that person, if the lift descends with uniform downward acceleration of 1.8 m/s $^2$  will be ..... N. [ $g = 10$  m/s $^2$ ]
22. In an electrical circuit, a battery is connected to pass 20 C of charge through it in a certain given time. The potential difference between two plates of the battery is maintained at 15 V. The work done by the battery is ..... J.
23. The circuit contains two diodes each with a forward resistance of 50  $\Omega$  and with infinite reverse resistance. If the battery voltage is 6V, the current through the 120  $\Omega$  resistance is ..... mA.



24. A radiation is emitted by 1000 W bulb and it generates an electric field and magnetic field at  $P$ , placed at a distance of 2 m. The efficiency of the bulb is 1.25%. The value of peak electric field at  $P$  is  $x \times 10^{-1}$  V/m. Value of  $x$  is .....

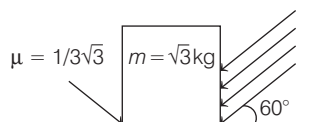
(Rounded-off to the nearest integer)

[Take,  $\epsilon_0 = 8.85 \times 10^{-12} \text{ C}^2\text{N}^{-1}\text{m}^{-2}$ ,  $c = 3 \times 10^8 \text{ ms}^{-1}$ ]

25. A boy pushes a box of mass 2 kg with a force  $\mathbf{F} = (20\mathbf{i} + 10\mathbf{j})$  N on a frictionless surface. If the box was initially at rest, then ..... m is displacement along the  $X$ -axis after 10 s.

26. As shown in the figure, a block of mass  $\sqrt{3}$  kg is kept on a horizontal rough surface of coefficient of friction  $1/3\sqrt{3}$ . The critical force to be applied on the vertical surface as shown at an angle  $60^\circ$  with horizontal such that it does not move, will be  $3x$ . The value of  $x$  will be .....

$[g = 10 \text{ ms}^{-2}; \sin 60^\circ = \frac{\sqrt{3}}{2}; \cos 60^\circ = \frac{1}{2}]$



27. A container is divided into two chambers by a partition. The volume of first chamber is 4.5 L and second chamber is 5.5 L. The first chamber contain 3.0 mol of gas at pressure 2.0 atm and second chamber contain 4.0 mol of gas at pressure 3.0 atm. After the partition is removed and the mixture attains equilibrium, then the common equilibrium pressure existing in the mixture is  $x \times 10^{-1}$  atm. Value of  $x$  is .....

28. The mass per unit length of a uniform wire is 0.135 g/cm. A transverse wave of the form  $y = -0.21 \sin(x + 30t)$  is produced in it, where  $x$  is in metre and  $t$  is in second. Then, the expected value of tension in the wire is  $x \times 10^{-2}$  N. Value of  $x$  is ..... (Round-off to the nearest integer)

29. In a series  $L$ - $C$ - $R$  resonant circuit, the quality factor is measured as 100. If the inductance is increased by two fold and resistance is decreased by two fold, then the quality factor after this change will be .....

30. The maximum and minimum amplitude of an amplitude modulated wave is 16 V and 8 V, respectively. The modulation index for this amplitude modulated wave is  $x \times 10^{-2}$ . The value of  $x$  is .....

## Answers

- |           |           |          |           |           |            |            |            |           |             |
|-----------|-----------|----------|-----------|-----------|------------|------------|------------|-----------|-------------|
| 1. (d)    | 2. (*)    | 3. (b)   | 4. (c)    | 5. (d)    | 6. (d)     | 7. (a)     | 8. (b)     | 9. (a)    | 10. (d)     |
| 11. (c)   | 12. (c)   | 13. (a)  | 14. (c)   | 15. (a)   | 16. (c)    | 17. (b)    | 18. (d)    | 19. (d)   | 20. (d)     |
| 21. (492) | 22. (300) | 23. (20) | 24. (137) | 25. (500) | 26. (3.33) | 27. (25.5) | 28. (1215) | 29. (400) | 30. (33.33) |

Note (\*) None of the option is correct.

## 26 FEBRUARY SHIFT II

### Objective Type Questions

1. If  $C$  and  $V$  represent capacity and voltage respectively, then what are the dimensions of  $\lambda$ , where  $\frac{C}{V} = \lambda$ ?

- a.  $[M^{-2}L^{-3}T^6]$       b.  $[M^{-3}L^{-4}T^7]$   
c.  $[M^{-1}L^{-3}T^{-7}]$       d.  $[M^{-2}L^{-4}T^7]$

2. The length of metallic wire is  $l_1$  when tension in it is  $T_1$ . It is  $l_2$  when the tension is  $T_2$ . The original length of the wire will be

- a.  $\frac{l_1 + l_2}{2}$       b.  $\frac{T_2 l_1 + T_1 l_2}{T_1 + T_2}$       c.  $\frac{T_2 l_1 - T_1 l_2}{T_2 - T_1}$       d.  $\frac{T_1 l_1 - T_2 l_2}{T_2 - T_1}$

3. An aeroplane with its wings spread 10 m, is flying at a speed of 180 km/h in a horizontal direction. The total intensity of Earth's field at that part is  $2.5 \times 10^{-4} \text{ Wb/m}^2$  and the angle of dip is  $60^\circ$ . The emf induced between the tips of the plane wings will be

- a. 108.25 mV      b. 54.125 mV  
c. 88.37 mV      d. 62.50 mV

4. A tuning fork A of unknown frequency produces 5 beats/s with a fork of known frequency 340 Hz. When fork A is filled, the beat frequency decreases to 2 beats/s. What is the frequency of fork A?

- a. 342 Hz      b. 345 Hz      c. 335 Hz      d. 338 Hz

5. A particle executes SHM, the graph of velocity as a function of displacement is

- a. a circle      b. a parabola  
c. an ellipse      d. a helix

6. The trajectory of a projectile in a vertical plane is  $y = \alpha x - \beta x^2$ , where  $\alpha$  and  $\beta$  are constants and  $x$  and  $y$  are respectively the horizontal and vertical distances of the projectile from the point of projection. The angle of projection  $\theta$  and the maximum height attained  $H$  are respectively given by

- a.  $\tan^{-1} \alpha, \frac{\alpha^2}{4\beta}$       b.  $\tan^{-1} \beta, \frac{\alpha^2}{2\beta}$   
c.  $\tan^{-1} \alpha, \frac{4\alpha^2}{\beta}$       d.  $\tan^{-1} \left( \frac{\beta}{\alpha} \right), \frac{\alpha^2}{\beta}$



7. A cord is wound round the circumference of wheel of radius  $r$ . The axis of the wheel is horizontal and the moment of inertia about it is  $I$ . A weight  $mg$  is attached to the cord at the end. The weight falls from rest. After falling through a distance  $h$ , the square of angular velocity of wheel will be

a.  $\frac{2mgh}{I + 2mr^2}$     b.  $\frac{2mgh}{I + mr^2}$     c.  $2gh$     d.  $\frac{2gh}{I + mr^2}$

8. The internal energy ( $U$ ), pressure ( $p$ ) and volume ( $V$ ) of an ideal gas are related as  $U = 3pV + 4$ . The gas is  
a. diatomic only    b. polyatomic only  
c. Either monoatomic or diatomic    d. monoatomic only

9. Given below are two statements: one is labelled as Assertion (A) and the other is labelled as Reason (R).

**Assertion (A)** For a simple microscope, the angular size of the object equals the angular size of the image.

**Reason (R)** Magnification is achieved as the small object can be kept much closer to the eye than 25 cm and hence, it subtends a large angle.

In the light of the above statements, choose the most appropriate answer from the options given below.

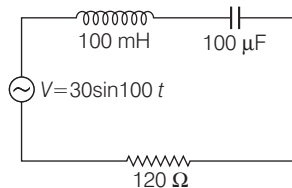
- a. A is true but R is false.  
b. Both A and R are true but R is not the correct explanation of A.  
c. Both A and R are true and R is the correct explanation of A.  
d. A is false but R is true.
10. Given below are two statements:

**Statement I** An electric dipole is placed at the centre of a hollow sphere. The flux of electric field through the sphere is zero but the electric field is not zero anywhere in the sphere.

**Statement II** If  $R$  is the radius of a solid metallic sphere and  $Q$  be the total charge on it. The electric field at any point on the spherical surface of radius  $r$  ( $r < R$ ) is zero but the electric flux passing through this closed spherical surface of radius  $r$  is not zero.

In the light of the above statements, choose the correct answer from the options given below.

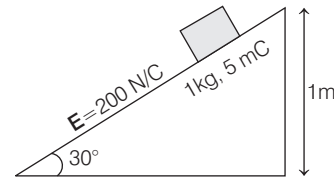
- a. Both Statement I and Statement II are true.  
b. Statement I is true but Statement II is false.  
c. Both Statement I and Statement II are false.  
d. Statement I is false but Statement II is true.
11. The recoil speed of a hydrogen atom after it emits a photon in going from  $n = 5$  state to  $n = 1$  state will be  
a. 4.17 m/s    b. 2.19 m/s    c. 3.25 m/s    d. 4.34 m/s
12. Find the peak current and resonant frequency of the following circuit (as shown in figure).



- a. 0.2 A and 50 Hz    b. 0.2 A and 100 Hz  
c. 2 A and 100 Hz    d. 2 A and 50 Hz
13. An inclined plane making an angle of  $30^\circ$  with the horizontal is placed in a uniform horizontal electric field 200 N/C as shown in the figure. A body of mass 1 kg and

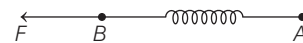
charge 5 mC is allowed to slide down from rest at a height of 1 m. If the coefficient of friction is 0.2, find the time taken by the body to reach the bottom.

[Take,  $g = 9.8 \text{ m/s}^2$ ,  $\sin 30^\circ = \frac{1}{2}$ ,  $\cos 30^\circ = \frac{\sqrt{3}}{2}$ ]



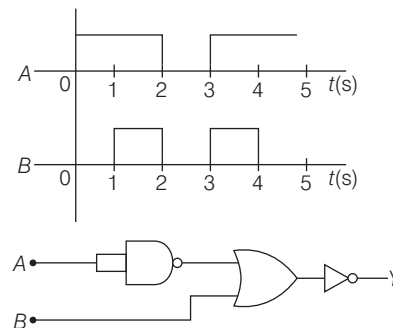
- a. 0.92 s    b. 0.46 s    c. 2.3 s    d. 1.3 s

14. Two masses A and B, each of mass  $M$  are fixed together by a massless spring. A force acts on the mass B as shown in figure. If the mass A starts moving away from mass B with acceleration  $a$ , then the acceleration of mass B will be



- a.  $\frac{Ma - F}{M}$     b.  $\frac{MF}{F + Ma}$   
c.  $\frac{F + Ma}{M}$     d.  $\frac{F - Ma}{M}$

15. Draw the output signal  $Y$  in the given combination of gates



- a.
- b.
- c.
- d.

16. A radioactive sample is undergoing  $\alpha$ -decay. At any time  $t_1$ , its activity is  $A$  and another time  $t_2$ , the activity is  $\frac{A}{5}$ .

What is the average life time for the sample?

- a.  $\frac{\ln 5}{t_2 - t_1}$     b.  $\frac{t_1 - t_2}{\ln 5}$     c.  $\frac{t_2 - t_1}{\ln 5}$     d.  $\frac{\ln(t_2 + t_1)}{2}$

17. A scooter accelerates from rest for time  $t_1$  at constant rate  $a_1$  and then retards at constant rate  $a_2$  for time  $t_2$  and comes to rest. The correct value of  $t_1/t_2$  will be

- a.  $\frac{a_1 + a_2}{a_2}$     b.  $\frac{a_2}{a_1}$     c.  $\frac{a_1}{a_2}$     d.  $\frac{a_1 + a_2}{a_1}$

18. Given below are two statements:

**Statement I** A second's pendulum has a time period of 1 s.

**Statement II** It takes precisely one second to move between the two extreme positions.

In the light of the above statements, choose the correct answer from the options given below.

- a. Both Statement I and Statement II are false.  
b. Statement I is false but Statement II is true.  
c. Statement I is true but Statement II is false.  
d. Both Statement I and Statement II are true.

19. A wire of  $1\Omega$  has a length of 1m. It is stretched till its length increases by 25%. The percentage change in resistance to the nearest integer is

- a. 56%    b. 25%    c. 12.5%    d. 76%

20. The incident ray, reflected ray and the outward drawn normal are denoted by the unit vectors  $\mathbf{a}$ ,  $\mathbf{b}$  and  $\mathbf{c}$ , respectively. Then, choose the correct relation for these vectors.

- a.  $\mathbf{b} = \mathbf{a} + 2\mathbf{c}$     b.  $\mathbf{b} = 2\mathbf{a} + \mathbf{c}$     c.  $\mathbf{b} = \mathbf{a} - 2(\mathbf{a} \cdot \mathbf{c})\mathbf{c}$     d.  $\mathbf{b} = \mathbf{a} - \mathbf{c}$

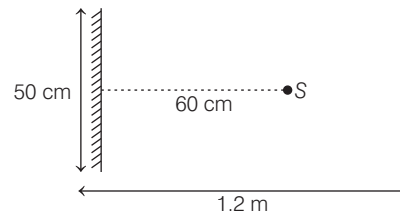
## Numerical Type Questions

21. The volume  $V$  of a given mass of monoatomic gas changes with temperature  $T$  according to the relation  $V = kT^{2/3}$ . The work done when temperature changes by 90 K will be  $xR$ . The value of  $x$  is.....  
[ $R$  = universal gas constant]

22. If the highest frequency modulating a carrier is 5 kHz, then the number of AM broadcast stations accommodated in a 90 kHz bandwidth are .....

23. Two stream of photons, possessing energies equal to twice and ten times the work function of metal are incident on the metal surface successively. The value of ratio of maximum velocities of the photoelectrons emitted in the two respective cases is  $x : y$ . The value of  $x$  is .....

24. A point source of light  $S$ , placed at a distance 60 cm in front of the centre of a plane mirror of width 50 cm, hangs vertically on a wall. A man walks in front of the mirror along a line parallel to the mirror at a distance 1.2 m from it (see in the figure). The distance between the extreme points, where he can see the image of the light source in the mirror is ..... cm.

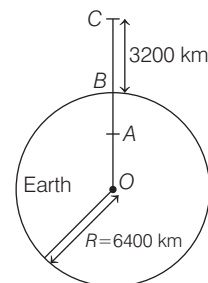


25. A particle executes SHM with amplitude  $a$  and time period  $T$ . The displacement of the particle when its speed is half of maximum speed is  $\sqrt{x}a/2$ . The value of  $x$  is .....

26. 27 similar drops of mercury are maintained at 10 V each. All these spherical drops combine into a single big drop. The potential energy of the bigger drop is ..... times that of a smaller drop.

27. Time period of a simple pendulum is  $T$ . The time taken to complete  $5/8$  oscillations starting from mean position is  $\frac{\alpha}{\beta} T$ . The value of  $\alpha$  is .....

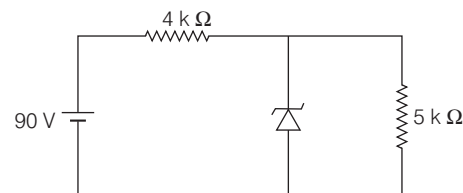
28. In the reported figure of Earth, the value of acceleration due to gravity is same at point A and C but it is smaller than that of its value at point B (surface of the Earth). The value of  $OA : AB$  will be  $x : y$ . The value of  $x$  is .....



29. 1 mole of rigid diatomic gas performs a work of  $Q/5$  when heat  $Q$  is supplied to it. The molar heat capacity of the gas during this transformation is  $\frac{xR}{8}$ . The value of  $x$  is .....

[ $R$  = universal gas constant]

30. The Zener diode has a  $V_z = 30$  V. The current passing through the diode for the following circuit is ..... mA.



## Answers

- |          |         |         |           |         |           |         |         |          |         |
|----------|---------|---------|-----------|---------|-----------|---------|---------|----------|---------|
| 1. (d)   | 2. (c)  | 3. (a)  | 4. (c)    | 5. (c)  | 6. (a)    | 7. (b)  | 8. (b)  | 9. (c)   | 10. (b) |
| 11. (a)  | 12. (a) | 13. (d) | 14. (d)   | 15. (d) | 16. (c)   | 17. (b) | 18. (b) | 19. (a)  | 20. (c) |
| 21. (60) | 22. (9) | 23. (1) | 24. (150) | 25. (3) | 26. (243) | 27. (7) | 28. (4) | 29. (25) | 30. (9) |

## 16 MARCH SHIFT I

### Section A : Objective Type Questions

1. One main scale division of a vernier callipers is  $a$  cm and  $n$ th division of the vernier scale coincide with  $(n - 1)$ th division of the main scale. The least count of the callipers (in mm) is

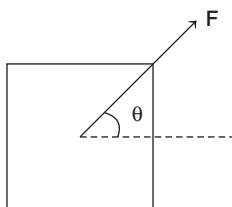
a.  $\frac{10na}{(n-1)}$       b.  $\frac{10a}{(n-1)}$       c.  $\left(\frac{n-1}{10n}\right)a$       d.  $\frac{10a}{n}$

2. For changing the capacitance of a given parallel plate capacitor, a dielectric material of dielectric constant  $K$  is used, which has the same area as the plates of the capacitor. The thickness of the dielectric slab is  $\frac{3}{4}d$ ,

where  $d$  is the separation between the plates of parallel plate capacitor. The new capacitance ( $C'$ ) in terms of original capacitance ( $C_0$ ) is given by the following relation

a.  $C' = \frac{3+K}{4K}C_0$       b.  $C' = \frac{4+K}{3}C_0$   
c.  $C' = \frac{4K}{K+3}C_0$       d.  $C' = \frac{4}{3+K}C_0$

3. A block of mass  $m$  slides along a floor, while a force of magnitude  $F$  is applied to it at an angle  $\theta$  as shown in figure. The coefficient of kinetic friction is  $\mu_k$ . Then, the block's acceleration  $a$  is given by ( $g$  is acceleration due to gravity)

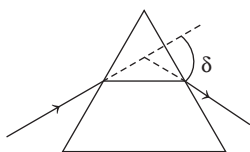


a.  $-\frac{F}{m}\cos\theta - \mu_k\left(g - \frac{F}{m}\sin\theta\right)$       b.  $\frac{F}{m}\cos\theta - \mu_k\left(g - \frac{F}{m}\sin\theta\right)$   
c.  $\frac{F}{m}\cos\theta - \mu_k\left(g + \frac{F}{m}\sin\theta\right)$       d.  $\frac{F}{m}\cos\theta + \mu_k\left(g - \frac{F}{m}\sin\theta\right)$

4. The pressure acting on a submarine is  $3 \times 10^5$  Pa at a certain depth. If the depth is doubled, the percentage increase in the pressure acting on the submarine would be (Assume that atmospheric pressure is  $1 \times 10^5$  Pa, density of water is  $10^3 \text{ kg m}^{-3}$ ,  $g = 10 \text{ ms}^{-2}$ )

a.  $\frac{200}{3}\%$       b.  $\frac{200}{5}\%$       c.  $\frac{5}{200}\%$       d.  $\frac{3}{200}\%$

5. The angle of deviation through a prism is minimum when



- A. incident ray and emergent ray are symmetric to the prism  
B. the refracted ray inside the prism becomes parallel to its base

- C. angle of incidence is equal to that of the angle of emergence

- D. angle of emergence is double the angle of incidence

Choose the correct answer from the options given below.

- a. Statements (A), (B) and (C) are true.  
b. Only statement (D) is true.  
c. Only statements (A) and (B) are true.  
d. Statements (B) and (C) are true.

6. A plane electromagnetic wave of frequency 500 MHz is travelling in vacuum along  $y$ -direction. At a particular point in space and time,  $\mathbf{B} = 8.0 \times 10^{-8} \hat{\mathbf{z}}$  T. The value of electric field at this point is (speed of light =  $3 \times 10^8 \text{ ms}^{-1}$ ;

$\hat{\mathbf{x}}$ ,  $\hat{\mathbf{y}}$ ,  $\hat{\mathbf{z}}$  are unit vectors along  $x$ ,  $y$  and  $z$ -direction).

a.  $-24\hat{\mathbf{x}}$  V/m      b.  $2.6\hat{\mathbf{x}}$  V/m      c.  $24\hat{\mathbf{x}}$  V/m      d.  $-2.6\hat{\mathbf{x}}$  V/m

7. The maximum and minimum distance of a comet from the Sun are  $1.6 \times 10^{12}$  m and  $8.0 \times 10^{10}$  m, respectively. If the speed of the comet at the nearest point is  $6 \times 10^4 \text{ ms}^{-1}$ , then the speed at the farthest point is

a.  $15 \times 10^3$  m/s      b.  $60 \times 10^3$  m/s  
c.  $30 \times 10^3$  m/s      d.  $4.5 \times 10^3$  m/s

8. A bar magnet of length 14 cm is placed in the magnetic meridian with its North pole pointing towards the geographic North pole. A neutral point is obtained at a distance of 18 cm from the centre of the magnet. If  $B_H = 0.4$  G, then the magnetic moment of the magnet is ( $1 \text{ G} = 10^{-4} \text{ T}$ )

a.  $2.88 \times 10^3 \text{ J T}^{-1}$       b.  $2.88 \times 10^2 \text{ J T}^{-1}$   
c.  $2.88 \text{ J T}^{-1}$       d.  $28.8 \text{ J T}^{-1}$

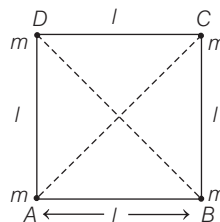
9. The volume  $V$  of an enclosure contains a mixture of three gases, 16 g of oxygen, 28 g of nitrogen and 44 g of carbon dioxide at absolute temperature  $T$ . Consider  $R$  as universal gas constant. The pressure of the mixture of gases is

a.  $\frac{88RT}{V}$       b.  $\frac{3RT}{V}$       c.  $\frac{5RT}{2V}$       d.  $\frac{4RT}{V}$

10. In thermodynamics, heat and work are

- a. path functions  
b. intensive thermodynamic state variables  
c. extensive thermodynamic state variables  
d. point functions

11. Four equal masses,  $m$  each are placed at the corners of a square of length ( $l$ ) as shown in the figure. The moment of inertia of the system about an axis passing through  $A$  and parallel to  $DB$  would be



a.  $1ml^2$       b.  $2ml^2$       c.  $3ml^2$       d.  $\sqrt{3}ml^2$

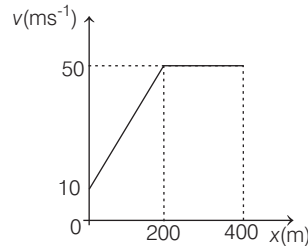
- 12.** A conducting wire of length  $l$ , area of cross-section  $A$  and electric resistivity  $\rho$  is connected between the terminals of a battery. A potential difference  $V$  is developed between its ends, causing an electric current. If the length of the wire of the same material is doubled and the area of cross-section is halved, the resultant current would be

a.  $\frac{1}{4} \frac{VA}{\rho l}$       b.  $\frac{3}{4} \frac{VA}{\rho l}$       c.  $\frac{1}{4} \frac{\rho l}{VA}$       d.  $4 \frac{VA}{\rho l}$

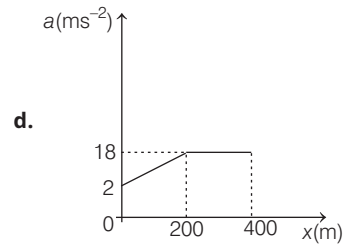
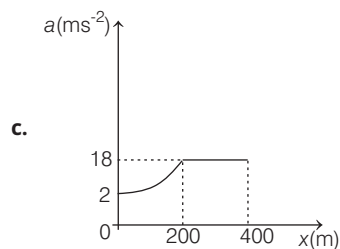
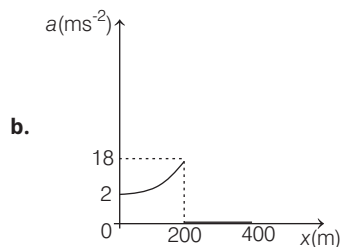
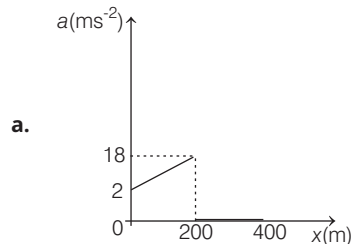
- 13.** Time period of a simple pendulum is  $T$  inside a lift, when the lift is stationary. If the lift moves upwards with an acceleration  $g/2$ , then the time period of pendulum will be

a.  $\sqrt{3}T$       b.  $\frac{T}{\sqrt{3}}$   
c.  $\sqrt{\frac{3}{2}}T$       d.  $\sqrt{\frac{2}{3}}T$

- 14.** The velocity-displacement graph describing the motion of a bicycle is shown in the following figure.



The acceleration-displacement graph of the bicycle's motion is best described by

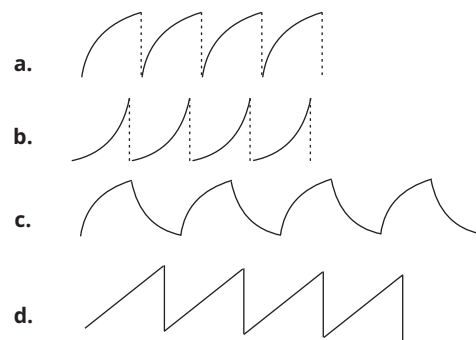
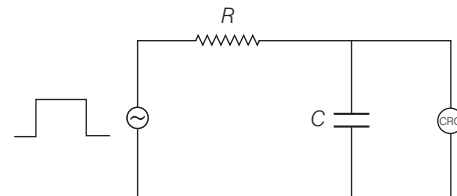


- 15.** A 25 m long antenna is mounted on an antenna tower. The height of the antenna tower is 75 m. The wavelength (in m) of the signal transmitted by this antenna would be  
a. 300      b. 400      c. 200      d. 100

- 16.** For an electromagnetic wave travelling in free space, the relation between average energy densities due to electric ( $U_e$ ) and magnetic ( $U_m$ ) fields is

a.  $U_e = U_m$       b.  $U_e > U_m$   
c.  $U_e < U_m$       d.  $U_e \neq U_m$

- 17.** An  $R$ - $C$  circuit as shown in the figure is driven by an AC source generating a square wave. The output wave pattern monitored by CRO would look close to



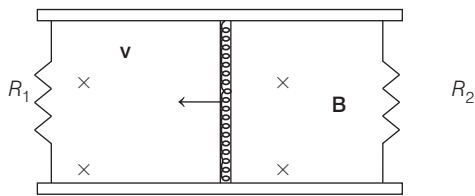
- 18.** The stopping potential in the context of photoelectric effect depends on the following property of incident electromagnetic radiation

a. phase      b. intensity  
c. amplitude      d. frequency

- 19.** A block of 200 g mass moves with a uniform speed in a horizontal circular groove, with vertical side walls of radius 20 cm. If the block takes 40 s to complete one round, the normal force by the side walls of the groove is

a. 0.0314 N      b.  $9.859 \times 10^{-2}$  N  
c.  $6.28 \times 10^{-3}$  N      d.  $9.859 \times 10^{-4}$  N

- 20.** A conducting bar of length  $L$  is free to slide on two parallel conducting rails as shown in the figure



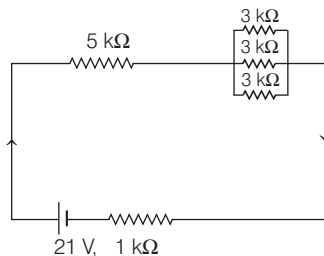
Two resistors  $R_1$  and  $R_2$  are connected across the ends of the rails. There is a uniform magnetic field  $\mathbf{B}$  pointing into the page. An external agent pulls the bar to the left at a constant speed  $v$ .

The correct statement about the directions of induced currents  $I_1$  and  $I_2$  flowing through  $R_1$  and  $R_2$  respectively is

- both  $I_1$  and  $I_2$  are in anti-clockwise direction.
- both  $I_1$  and  $I_2$  are in clockwise direction.
- $I_1$  is in clockwise direction and  $I_2$  is in anti-clockwise direction.
- $I_1$  is in anticlockwise direction and  $I_2$  is in clockwise direction.

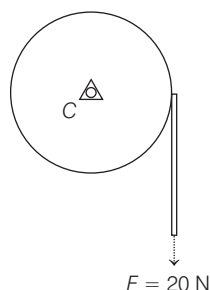
### Section B : Numerical Type Questions

21. In the figure given, the electric current flowing through the  $5\text{ k}\Omega$  resistor is  $x\text{ mA}$ .



The value of  $x$  to the nearest Integer is ...3...

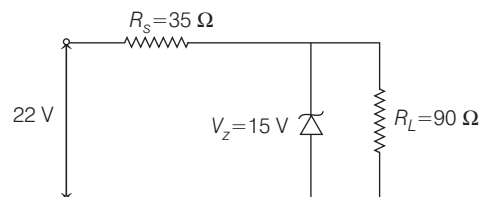
22. A fringe width of  $6\text{ mm}$  was produced for two slits separated by  $1\text{ mm}$  apart. The screen is placed  $10\text{ m}$  away. The wavelength of light used is  $x\text{ nm}$ . The value of  $x$  to the nearest integer is .....
23. Consider a  $20\text{ kg}$  uniform circular disc of radius  $0.2\text{ m}$ . It is pin supported at its centre and is at rest initially. The disc is acted upon by a constant force  $F = 20\text{ N}$  through a massless string wrapped around its periphery as shown in the figure.



Suppose the disc makes  $n$  number of revolutions to attain an angular speed of  $50\text{ rad s}^{-1}$ . The value of  $n$  to the nearest integer, is .....

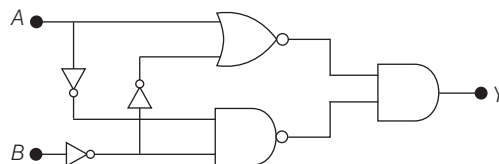
(Given, in one complete revolution, the disc rotates by  $6.28\text{ rad}$ .)

24. The first three spectral lines of H-atom in the Balmer series are given  $\lambda_1, \lambda_2, \lambda_3$  considering the Bohr atomic model, the wavelengths of first and third spectral lines ( $\lambda_1 / \lambda_3$ ) are related by a factor of approximately  $x \times 10^{-1}$ . The value of  $x$  to the nearest integer, is .....
25. The value of power dissipated across the Zener diode ( $V_z = 15\text{ V}$ ) connected in the circuit as shown in the figure is  $x \times 10^{-1}\text{ W}$ .

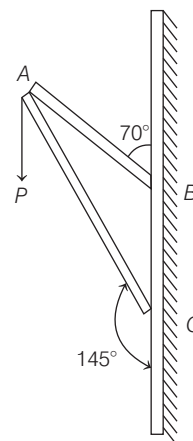


The value of  $x$ , to the nearest integer, is .....

26. A sinusoidal voltage of peak value  $250\text{ V}$  is applied to a series  $L$ - $C$ - $R$  circuit, in which  $R = 8\text{ }\Omega$ ,  $L = 24\text{ mH}$  and  $C = 60\text{ }\mu\text{F}$ . The value of power dissipated at resonant condition is  $x\text{ kW}$ . The value of  $x$  to the nearest integer is .....
27. In the logic circuit shown in the figure, if input  $A$  and  $B$  are 0 to 1 respectively, the output at  $Y$  would be  $x$ . The value of  $x$  is .....



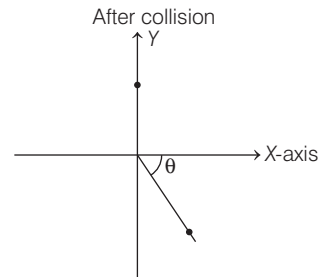
28. The resistance  $R = V/I$ , where  $V = (50 \pm 2)\text{ V}$  and  $I = (20 \pm 0.2)\text{ A}$ . The percentage error in  $R$  is  $x\%$ . The value of  $x$  to the nearest integer is.....
29. Consider a frame that is made up of two thin massless rods  $AB$  and  $AC$  as shown in the figure. A vertical force  $\mathbf{P}$  of magnitude  $100\text{ N}$  is applied at point  $A$  of the frame.



Suppose the force is  $\mathbf{P}$  resolved parallel to the arms  $AB$  and  $AC$  of the frame. The magnitude of the resolved component along the arm  $AC$  is  $x\text{ N}$ . The value of  $x$ , to the nearest integer, is .....

[Given,  $\sin(35^\circ) = 0.573$ ,  $\cos(35^\circ) = 0.819$ ,  $\sin(110^\circ) = 0.939$ ,  $\cos(110^\circ) = -0.342$ ]

30. A ball of mass 10 kg moving with a velocity  $10\sqrt{3}\text{ ms}^{-1}$  along X-axis, hits another ball of mass 20 kg, which is at rest. After collision, the first ball comes to rest and the second one disintegrates into two equal pieces. One of the pieces starts moving along Y-axis at a speed of 10 m/s. The second piece starts moving at a speed of 20 m/s at an angle  $\theta$  (degree) with respect to the X-axis. The configuration of pieces after collision is shown in the figure. The value of  $\theta$  to the nearest integer is .....



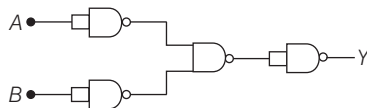
## Answers

- |         |           |          |          |         |         |         |         |          |          |
|---------|-----------|----------|----------|---------|---------|---------|---------|----------|----------|
| 1. (d)  | 2. (c)    | 3. (b)   | 4. (a)   | 5. (a)  | 6. (a)  | 7. (c)  | 8. (c)  | 9. (c)   | 10. (a)  |
| 11. (c) | 12. (a)   | 13. (d)  | 14. (a)  | 15. (d) | 16. (a) | 17. (c) | 18. (d) | 19. (d)  | 20. (c)  |
| 21. (3) | 22. (600) | 23. (20) | 24. (15) | 25. (5) | 26. (4) | 27. (0) | 28. (5) | 29. (82) | 30. (30) |

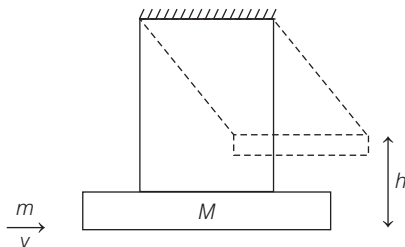
## 16 MARCH SHIFT II

### Section A : Objective Type Questions

1. The following logic gate is equivalent to



- a. NOR Gate  
b. OR Gate  
c. AND Gate  
d. NAND Gate
2. A large block of wood of mass  $M = 5.99\text{ kg}$  is hanging from two long massless cords. A bullet of mass  $m = 10\text{ g}$  is fired into the block and gets embedded in it. The system (block + bullet) then swing upwards, their centre of mass rising a vertical distance  $h = 9.8\text{ cm}$  before the (block + bullet) pendulum comes momentarily to rest at the end of its arc. The speed of the bullet just before collision is (Take  $g = 9.8\text{ ms}^{-2}$ )

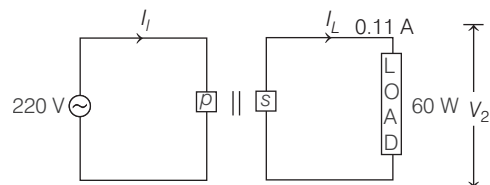


- a. 841.4 m/s  
b. 811.4 m/s  
c. 831.4 m/s  
d. 821.4 m/s
3. A charge  $Q$  is moving  $dl$  distance in the magnetic field  $\mathbf{B}$ . Find the value of work done by  $\mathbf{B}$ .
- a. 1  
b. Infinite  
c. Zero  
d. -1
4. What will be the nature of flow of water from a circular tap, when its flow rate increased from 0.18 L/min to 0.48

L/min ? The radius of the tap and viscosity of water are 0.5 cm and  $10^{-3}\text{ Pa-s}$ , respectively.

(Density of water =  $10^3\text{ kg/m}^3$ )

- a. Unsteady to steady flow  
b. Remains steady flow  
c. Remains turbulent flow  
d. Steady flow to unsteady flow
5. A mosquito is moving with a velocity  $\mathbf{v} = (0.5t^2\hat{i} + 3t\hat{j} + 9\hat{k})$  m/s and accelerating in uniform conditions. What will be the direction of mosquito after 2s?
- a.  $\tan^{-1}\left(\frac{2}{3}\right)$  from X-axis  
b.  $\tan^{-1}\left(\frac{2}{3}\right)$  from Y-axis  
c.  $\tan^{-1}\left(\frac{5}{2}\right)$  from Y-axis  
d.  $\tan^{-1}\left(\frac{5}{2}\right)$  from X-axis
6. Find out the surface charge density at the intersection of point  $X = 3\text{ m}$  plane and X-axis, in the region of uniform line charge of 8 nC/m lying along the Z-axis in free space.
- a.  $0.424\text{ nC m}^{-2}$   
b.  $47.88\text{ nC m}^{-2}$   
c.  $0.07\text{ nC m}^{-2}$   
d.  $4.0\text{ nC m}^{-2}$
7. The de-Broglie wavelength associated with an electron and a proton were calculated by accelerating them through same potential of 100 V. What should nearly be the ratio of their wavelengths? ( $m_p = 1.00727u$ ,  $m_e = 0.00055u$ )
- a. 1860 : 1  
b.  $(1860)^2 : 1$   
c. 41.4 : 1  
d. 43 : 1
8. For the given circuit, comment on the type of transformer used.



- a. Auxilliary transformer  
b. Auto transformer  
c. Step-up transformer  
d. Step down transformer



9. The half-life of  $\text{Au}^{198}$  is 2.7 days. The activity of 1.50 mg of  $\text{Au}^{198}$  if its atomic weight is  $198 \text{ g mol}^{-1}$  is ( $N_A = 6 \times 10^{23} / \text{mol}$ )

a. 240 Ci      b. 357 Ci      c. 535 Ci      d. 252 Ci

10. Calculate the value of mean free path ( $\lambda$ ) for oxygen molecules at temperature  $27^\circ\text{C}$  and pressure  $101 \times 10^5 \text{ Pa}$ . Assume the molecular diameter  $0.3 \text{ nm}$  and the gas is ideal.

( $k = 1.38 \times 10^{-23} \text{ J K}^{-1}$ )

a. 58 nm      b. 32 nm      c. 86 nm      d. 102 nm

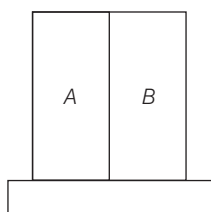
11. The refractive index of a converging lens is 1.4. What will be the focal length of this lens if it is placed in a medium of same refractive index? (Assume the radii of curvature of the faces of lens are  $R_1$  and  $R_2$  respectively)

a. 1      b. Infinite      c.  $\frac{R_1 R_2}{R_1 - R_2}$       d. Zero

12. In order to determine the Young's modulus of a wire of radius  $0.2 \text{ cm}$  (measured using a scale of least count =  $0.001 \text{ cm}$ ) and length  $1 \text{ m}$  (measured using a scale of least count =  $1 \text{ mm}$ ), a weight of mass  $1 \text{ kg}$  (measured using a scale of least count =  $1 \text{ g}$ ) was hanged to get the elongation of  $0.5 \text{ cm}$  (measured using a scale of least count  $0.001 \text{ cm}$ ). What will be the fractional error in the value of Young's modulus determined by this experiment?

a. 0.14%      b. 0.9%      c. 9%      d. 1.4%

13. A bimetallic strip consists of metals  $A$  and  $B$ . It is mounted rigidly as shown. The metal  $A$  has higher coefficient of expansion compared to that of metal  $B$ . When the bimetallic strip is placed in a cold bath, it will



a. bend towards the right      b. not bend but shrink  
c. Neither bend nor shrink      d. bend towards the left

14. A resistor develops  $500 \text{ J}$  of thermal energy in  $20 \text{ s}$ , when a current of  $1.5 \text{ A}$  is passed through it. If the current is increased from  $1.5 \text{ A}$  to  $3 \text{ A}$ , what will be the energy developed in  $20 \text{ s}$ ?

a.  $1500 \text{ J}$       b.  $1000 \text{ J}$       c.  $500 \text{ J}$       d.  $2000 \text{ J}$

15. **Statement I** A cyclist is moving on an unbanked road with a speed of  $7 \text{ kmh}^{-1}$  and takes a sharp circular turn along a path of radius of  $2 \text{ m}$  without reducing the speed. The static friction coefficient is  $0.2$ . The cyclist will not slip and pass the curve ( $g = 9.8 \text{ m/s}^2$ )

**Statement II** If the road is banked at an angle of  $45^\circ$ , cyclist can cross the curve of  $2 \text{ m}$  radius with the speed of  $18.5 \text{ kmh}^{-1}$  without slipping.

In the light of the above statements, choose the correct answer from the options given below.

a. Statement I is false and statement II is true.  
b. Statement I is true and statement II is false.  
c. Both statement I and statement II are false.  
d. Both statement I and statement II are true.

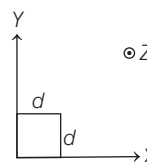
16. Two identical antennas mounted on identical towers are separated from each other by a distance of  $45 \text{ km}$ . What should nearly be the minimum height of receiving antenna to receive the signals in line of sight?

(Assume, radius of earth is  $6400 \text{ km}$ .)

a.  $19.77 \text{ m}$       b.  $39.55 \text{ m}$       c.  $79.1 \text{ m}$       d.  $158.2 \text{ m}$

17. The magnetic field in a region is given by  $\mathbf{B} = B_0 \left( \frac{x}{a} \right) \hat{k}$ . A

square loop of side  $d$  is placed with its edges along the  $X$  and  $Y$ -axes. The loop is moved with a constant velocity  $\mathbf{v} = v_0 \hat{i}$ . The emf induced in the loop is



a.  $\frac{B_0 v_0 d}{2a}$       b.  $\frac{B_0 v_0 d}{2a}$       c.  $\frac{B_0 v_0 d^2}{a}$       d.  $\frac{B_0 v_0 d^2}{2a}$

18. Amplitude of a mass-spring system, which is executing simple harmonic motion decreases with time. If mass =  $500 \text{ g}$ , decay constant =  $20 \text{ g/s}$ , then how much time is required for the amplitude of the system to drop to half of its initial value? ( $\ln 2 = 0.693$ )

a.  $34.65 \text{ s}$       b.  $17.32 \text{ s}$       c.  $0.034 \text{ s}$       d.  $15.01 \text{ s}$

19. Calculate the time interval between 33% decay and 67% decay if half-life of a substance is  $20 \text{ min}$ .

a.  $60 \text{ min}$       b.  $20 \text{ min}$       c.  $40 \text{ min}$       d.  $13 \text{ min}$

20. Red light differs from blue light as they have

a. different frequencies and different wavelengths  
b. different frequencies and same wavelengths  
c. same frequencies and same wavelengths  
d. same frequencies and different wavelengths

## Section B : Numerical Type Questions

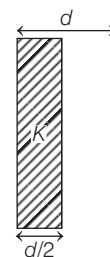
21. The energy dissipated by a resistor is  $10 \text{ mJ}$  in  $1 \text{ s}$  when an electric current of  $2 \text{ mA}$  flows through it. The resistance is .....  $\Omega$ .

(Round off to the nearest integer)

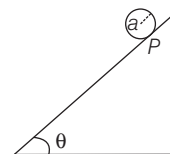
22. In a parallel plate capacitor set up, the plate area of capacitor is  $2 \text{ m}^2$  and the plates are separated by  $1 \text{ m}$ . If the space between the plates are filled with a dielectric material of thickness  $0.5 \text{ m}$  and area  $2 \text{ m}^2$  (see figure) the capacitance of the set-up will be .....  $\epsilon_0$ .

(Dielectric constant of the material =  $3.2$ )

(Round off to the nearest integer)



23. A force  $\mathbf{F} = 4\hat{i} + 3\hat{j} + 4\hat{k}$  is applied on an intersection point of  $x = 2$  plane and  $X$ -axis. The magnitude of torque of this force about a point (2, 3, 4) is .....  
(Round off to the nearest integer)
24. If one wants to remove all the mass of the earth to infinity in order to break it up completely. The amount of energy that needs to be supplied will be  $\frac{x}{5} \frac{GM^2}{R}$ , where  $x$  is .....  
(Round off to the nearest integer)  
( $M$  is the mass of earth,  $R$  is the radius of earth and  $G$  is the gravitational constant.)
25. A deviation of  $2^\circ$  is produced in the yellow ray when prism of crown and flint glass are achromatically combined. Taking dispersive powers of crown and flint glass are 0.02 and 0.03 respectively and refractive index for yellow light for these glasses are 1.5 and 1.6, respectively. The refracting angles for crown glass prism will be .....° (in degree).  
(Round off to the nearest integer)
26. A body of mass 2 kg moves under a force of  $(2\hat{i} + 3\hat{j} + 5\hat{k})\text{N}$ . It starts from rest and was at the origin initially. After 4 s, its new coordinates are (8,  $b$ , 20). The value of  $b$  is .....  
(Round off to the nearest integer)
27. A swimmer can swim with velocity of 12 km/h in still water. Water flowing in a river has velocity 6 km/h. The direction with respect to the direction of flow of river water he should swim in order to reach the point on the other bank just opposite to his starting point is .....° (in degree).  
(Round off to the nearest integer)
28. A closed organ pipe of length  $L$  and an open organ pipe contain gases of densities  $\rho_1$  and  $\rho_2$  respectively. The compressibility of gases are equal in both the pipes. Both the pipes are vibrating in their first overtone with same frequency. The length of the open pipe is  $\frac{x}{3} L \sqrt{\frac{\rho_1}{\rho_2}}$  where  $x$  is .....  
(Round off to the nearest integer)
29. A solid disc of radius  $a$  and mass  $m$  rolls down without slipping on an inclined plane making an angle  $\theta$  with the horizontal. The acceleration of the disc will be  $\frac{2}{b} g \sin \theta$ , where  $b$  is .....  
(Round off to the nearest integer)  
( $g$  = acceleration due to gravity)  
( $\theta$  = angle as shown in figure)



30. For an ideal heat engine, the temperature of the source is  $127^\circ\text{C}$ . In order to have 60% efficiency the temperature of the sink should be .....  $^\circ\text{C}$ .  
(Round off to the nearest integer)

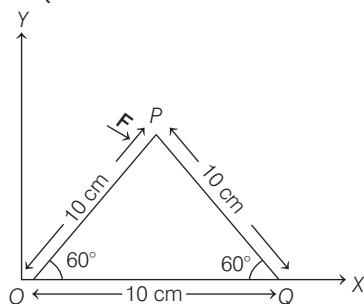
## Answers

- |            |         |          |         |          |          |           |         |         |           |
|------------|---------|----------|---------|----------|----------|-----------|---------|---------|-----------|
| 1. (a)     | 2. (c)  | 3. (c)   | 4. (d)  | 5. (*)   | 6. (a)   | 7. (d)    | 8. (c)  | 9. (b)  | 10. (d)   |
| 11. (b)    | 12. (d) | 13. (d)  | 14. (d) | 15. (d)  | 16. (b)  | 17. (c)   | 18. (a) | 19. (b) | 20. (a)   |
| 21. (2500) | 22. (3) | 23. (20) | 24. (3) | 25. (12) | 26. (12) | 27. (120) | 28. (4) | 29. (3) | 30. (113) |

## 17 MARCH SHIFT I

### Section A : Objective Type Questions

1. A triangular plate is shown below. A force  $\mathbf{F} = 4\hat{i} - 3\hat{j}$  is applied at point  $P$ . The torque at point  $P$  with respect to point  $O$  and  $Q$  are



- a.  $-15 - 20\sqrt{3}$ ,  $15 - 20\sqrt{3}$   
b.  $15 + 20\sqrt{3}$ ,  $15 - 20\sqrt{3}$   
c.  $15 - 20\sqrt{3}$ ,  $15 + 20\sqrt{3}$   
d.  $-15 + 20\sqrt{3}$ ,  $15 + 20\sqrt{3}$
2. When two soap bubbles of radii  $a$  and  $b$  ( $b > a$ ) coalesce, the radius of curvature of common surface is  
a.  $\frac{ab}{b-a}$       b.  $\frac{a+b}{ab}$       c.  $\frac{b-a}{ab}$       d.  $\frac{ab}{a+b}$
3. A polyatomic ideal gas has 24 vibrational modes. What is the value of  $\gamma$ ?  
a. 1.03      b. 1.30  
c. 1.37      d. 10.3
4. If an electron is moving in the  $n$ th orbit of the hydrogen atom, then its velocity  $v_n$  for the  $n$ th orbit is given as  
a.  $v_n \propto n$       b.  $v_n \propto \frac{1}{n}$       c.  $v_n \propto n^2$       d.  $v_n \propto \frac{1}{n^2}$

5. An electron of mass  $m$  and a photon have same energy  $E$ . The ratio of wavelength of electron to that of photon is ( $c$  being the velocity of light)

a.  $\frac{1}{c} \left( \frac{2m}{E} \right)^{1/2}$       b.  $\frac{1}{c} \left( \frac{E}{2m} \right)^{1/2}$   
c.  $\left( \frac{E}{2m} \right)^{1/2}$       d.  $c(2mE)^{1/2}$

6. Two identical metal wires of thermal conductivities  $K_1$  and  $K_2$  respectively are connected in series. The effective thermal conductivity of the combination is

a.  $\frac{2K_1K_2}{K_1 + K_2}$       b.  $\frac{K_1 + K_2}{2K_1K_2}$   
c.  $\frac{K_1 + K_2}{K_1K_2}$       d.  $\frac{K_1K_2}{K_1 + K_2}$

7. The vernier scale used for measurement has a positive zero error of 0.2 mm. If while taking a measurement, it was noted that '0' on the vernier scale lies between 8.5 cm and 8.6 cm, vernier coincidence is 6, then the correct value of measurement is ..... cm.

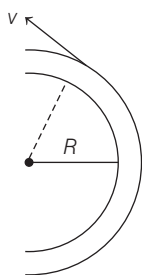
a. 8.36      b. 8.54  
c. 8.58      d. 8.56

8. An AC current is given by  $I = I_1 \sin \omega t + I_2 \cos \omega t$ . A hot wire ammeter will give a reading

a.  $\sqrt{\frac{I_1^2 - I_2^2}{2}}$       b.  $\sqrt{\frac{I_1^2 + I_2^2}{2}}$   
c.  $\frac{I_1 + I_2}{\sqrt{2}}$       d.  $\frac{I_1 + I_2}{2\sqrt{2}}$

9. A modern grand-prix racing car of mass  $m$  is travelling on a flat track in a circular arc of radius  $R$  with a speed  $v$ . If the coefficient of static friction between the tyres and the track is  $\mu_s$ , then the magnitude of negative lift  $f_L$  acting downwards on the car is

(Assume forces on the four tyres are identical and  $g$  = acceleration due to gravity)



a.  $m \left( \frac{v^2}{\mu_s R} + g \right)$       b.  $m \left( \frac{v^2}{\mu_s R} - g \right)$   
c.  $m \left( g - \frac{v^2}{\mu_s R} \right)$       d.  $-m \left( g + \frac{v^2}{\mu_s R} \right)$

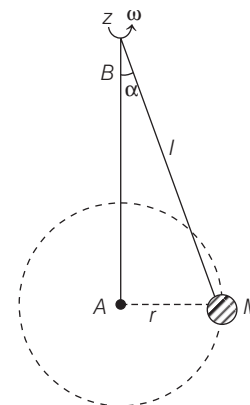
10. A car accelerates from rest at a constant rate  $\alpha$  for some time after which it decelerates at a constant rate  $\beta$  to come to rest. If the total time elapsed is  $t$  seconds, the total distance travelled is

a.  $\frac{4\alpha\beta}{(\alpha + \beta)} t^2$       b.  $\frac{2\alpha\beta}{(\alpha + \beta)} t^2$       c.  $\frac{\alpha\beta}{2(\alpha + \beta)} t^2$       d.  $\frac{\alpha\beta}{4(\alpha + \beta)} t^2$

11. A solenoid of 1000 turns per metre has a core with relative permeability 500. Insulated windings of the solenoid carry an electric current of 5 A. The magnetic flux density produced by the solenoid is (Permeability of free space =  $4\pi \times 10^{-7}$  H/m)

a.  $\pi T$       b.  $2 \times 10^{-3} \pi T$       c.  $\frac{\pi}{5} T$       d.  $10^{-4} \pi T$

12. A mass  $M$  hangs on a massless rod of length  $l$  which rotates at a constant angular frequency. The mass  $M$  moves with steady speed in a circular path of constant radius. Assume that the system is in steady circular motion with constant angular velocity  $\omega$ . The angular momentum of  $M$  about point  $A$  is  $L_A$  which lies in the positive  $z$ -direction and the angular momentum of  $M$  about  $B$  is  $L_B$ . The correct statement for this system is



- a.  $L_A$  and  $L_B$  are both constant in magnitude and direction  
b.  $L_B$  is constant in direction with varying magnitude  
c.  $L_B$  is constant, both in magnitude and direction  
d.  $L_A$  is constant, both in magnitude and direction

13. For what value of displacement the kinetic energy and potential energy of a simple harmonic oscillation become equal?

a.  $x = 0$       b.  $x = \pm A$       c.  $x = \pm \frac{A}{\sqrt{2}}$       d.  $x = \frac{A}{2}$

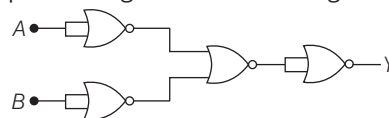
14. A Carnot's engine working between 400 K and 800 K has a work output of 1200 J per cycle. The amount of heat energy supplied to the engine from the source in each cycle is

a. 3200 J      b. 1800 J      c. 1600 J      d. 2400 J

15. The thickness at the centre of a plano convex lens is 3 mm and the diameter is 6 cm. If the speed of light in the material of the lens is  $2 \times 10^8 \text{ ms}^{-1}$ , then the focal length of the lens is

a. 0.30 cm      b. 15 cm      c. 1.5 cm      d. 30 cm

16. The output of the given combination gates represents



- a. XOR gate      b. NAND gate  
c. AND gate      d. NOR gate

17. A boy is rolling a 0.5 kg ball on the frictionless floor with the speed of  $20 \text{ ms}^{-1}$ . The ball gets deflected by an obstacle on the way. After deflection it moves with 5% of its initial kinetic energy. What is the speed of the ball now?

a.  $19.0 \text{ ms}^{-1}$       b.  $4.47 \text{ ms}^{-1}$       c.  $14.41 \text{ ms}^{-1}$       d.  $1.00 \text{ ms}^{-1}$

18. Which level of the single ionized carbon has the same energy as the ground state energy of hydrogen atom?

a. 1      b. 6      c. 4      d. 8

19. Two ideal polyatomic gases at temperatures  $T_1$  and  $T_2$  are mixed so that there is no loss of energy. If  $f_1$  and  $f_2$ ,  $m_1$  and  $m_2$ ,  $n_1$  and  $n_2$  be the degrees of freedom, masses, number of molecules of the first and second gas respectively, the temperature of mixture of these two gases is

a.  $\frac{n_1 T_1 + n_2 T_2}{n_1 + n_2}$       b.  $\frac{n_1 f_1 T_1 + n_2 f_2 T_2}{n_1 f_1 + n_2 f_2}$   
 c.  $\frac{n_1 f_1 T_1 + n_2 f_2 T_2}{f_1 + f_2}$       d.  $\frac{n_1 f_1 T_1 + n_2 f_2 T_2}{n_1 + n_2}$

20. A current of 10 A exists in a wire of cross sectional area of  $5 \text{ mm}^2$  with a drift velocity of  $2 \times 10^{-3} \text{ ms}^{-1}$ . The number of free electrons in each cubic metre of the wire is  
 a.  $2 \times 10^6$       b.  $625 \times 10^{25}$       c.  $2 \times 10^{25}$       d.  $1 \times 10^{23}$

## Section B : Numerical Type Questions

21. For VHF signal broadcasting, .....  $\text{km}^2$  of maximum service area will be covered by an antenna tower of height 30 m, if the receiving antenna is placed at ground. Let radius of the Earth be 6400 km. (Round off to the nearest integer). (Take  $\pi$  as 3.14)

22. The angular speed of truck wheel is increased from 900 rpm to 2460 rpm in 26 s. The number of revolutions by the truck engine during this time is .....

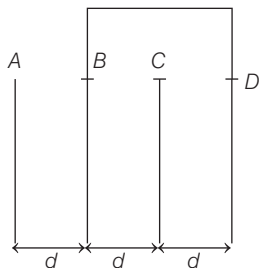
(Assuming the acceleration to be uniform).

23. The equivalent resistance of series combination of two resistors is  $s$ . When they are connected in parallel, the equivalent resistance is  $p$ . If  $s = np$ , then the minimum value for  $n$  is .....

(Round off to the nearest integer)

24. Four identical rectangular plates with length,  $l = 2 \text{ cm}$  and breadth,  $b = 3/2 \text{ cm}$  are arranged as shown in figure. The equivalent capacitance between A and C is  $\frac{x\epsilon_0}{d}$ . The value of  $x$  is .....

(Round off to the nearest integer)



25. The radius in kilometre to which the present radius of Earth ( $R = 6400 \text{ km}$ ) to be compressed so that the escape velocity is increased 10 times is .....

26. Consider two identical springs each of spring constant  $k$  and negligible mass compared to the mass  $M$  as shown. Fig.1 shows one of them and Fig.2 shows their series combination. The ratios of time period of oscillation of the two SHM is  $\frac{T_b}{T_a} = \sqrt{x}$ , where value of  $x$  is .....

(Round off to the nearest integer)

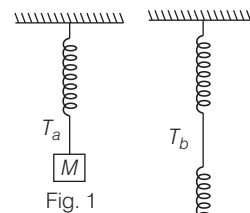


Fig. 1

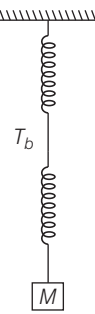


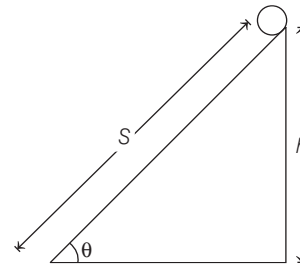
Fig. 2

27. The following bodies,

1. a ring      2. a disc  
 3. a solid cylinder      4. a solid sphere

of same mass  $m$  and radius  $R$  are allowed to roll down without slipping simultaneously from the top of the inclined plane. The body which will reach first at the bottom of the inclined plane is .....

(Mark the body as per their respective numbering given in the question)

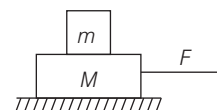


28. A parallel plate capacitor whose capacitance  $C$  is  $14 \text{ pF}$  is charged by a battery to a potential difference  $V = 12 \text{ V}$  between its plates. The charging battery is now disconnected and a porcelain plate with  $K = 7$  is inserted between the plates, then the plate would oscillate back and forth between the plates with a constant mechanical energy of .....  $\text{pJ}$ .

(Assume no friction)

29. Two blocks ( $m = 0.5 \text{ kg}$  and  $M = 4.5 \text{ kg}$ ) are arranged on a horizontal frictionless table as shown in figure. The coefficient of static friction between the two blocks is  $3/7$ . Then, the maximum horizontal force that can be applied on the larger block so that the blocks move together is ..... N.

(Round off to the nearest integer. Take,  $g = 9.8 \text{ ms}^{-2}$ )



30. If  $2.5 \times 10^{-6} \text{ N}$  average force is exerted by a light wave on a non-reflecting surface of  $30 \text{ cm}^2$  area during 40 min of time span, the energy flux of light just before it falls on the surface is .....  $\text{W / cm}^2$ .

(Round off to the nearest integer. Assume complete absorption and normal incidence conditions are there.)

## Answers

- |            |           |         |         |          |         |         |           |          |          |
|------------|-----------|---------|---------|----------|---------|---------|-----------|----------|----------|
| 1. (b)     | 2. (a)    | 3. (a)  | 4. (b)  | 5. (b)   | 6. (a)  | 7. (b)  | 8. (b)    | 9. (b)   | 10. (c)  |
| 11. (a)    | 12. (d)   | 13. (c) | 14. (d) | 15. (d)  | 16. (b) | 17. (b) | 18. (b)   | 19. (b)  | 20. (b)  |
| 21. (1206) | 22. (728) | 23. (4) | 24. (2) | 25. (64) | 26. (2) | 27. (4) | 28. (864) | 29. (21) | 30. (25) |

## 17 MARCH SHIFT II

### Section A : Objective Type Questions

1. A rubber ball is released from a height of 5 m above the floor. It bounces back repeatedly, always rising to 81/100 of the height through which it falls. Find the average speed of the ball.  
(Take,  $g = 10 \text{ ms}^{-2}$ )

a.  $3.0 \text{ ms}^{-1}$     b.  $3.5 \text{ ms}^{-1}$     c.  $2.0 \text{ ms}^{-1}$     d.  $2.5 \text{ ms}^{-1}$

2. If one mole of the polyatomic gas is having two vibrational modes and  $\beta$  is the ratio of molar specific heats for polyatomic gas  $\left(\beta = \frac{C_p}{C_v}\right)$ , then the value of  $\beta$  is

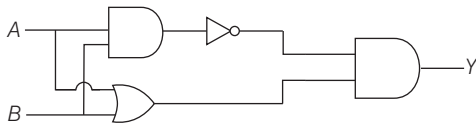
a. 1.02    b. 1.2    c. 1.25    d. 1.35

3. A block of mass 1 kg attached to a spring is made to oscillate with an initial amplitude of 12 cm. After 2 min, the amplitude decreases to 6 cm. Determine the value of the damping constant for this motion.

(Take,  $\ln 2 = 0.693$ )

a.  $0.69 \times 10^2 \text{ kg/s}$     b.  $3.3 \times 10^2 \text{ kg/s}$   
c.  $1.16 \times 10^{-2} \text{ kg/s}$     d.  $5.7 \times 10^{-3} \text{ kg/s}$

4. Which one of the following will be the output of the given circuit ?



a. NOR Gate    b. NAND Gate    c. AND Gate    d. XOR Gate

5. An object is located at 2 km beneath the surface of the water. If the fractional compression  $\Delta V / V$  is 1.36% , the ratio of hydraulic stress to the corresponding hydraulic strain will be .....

(Take, density of water is  $1000 \text{ kg m}^{-3}$  and  $g = 981 \text{ ms}^{-2}$ )

a.  $1.96 \times 10^7 \text{ Nm}^{-2}$     b.  $1.44 \times 10^7 \text{ Nm}^{-2}$   
c.  $2.26 \times 10^9 \text{ Nm}^{-2}$     d.  $1.44 \times 10^9 \text{ Nm}^{-2}$

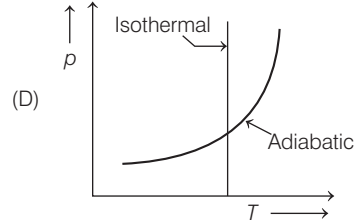
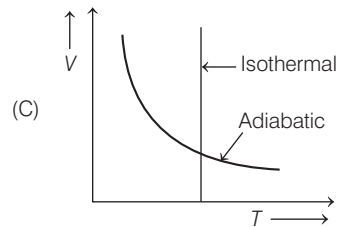
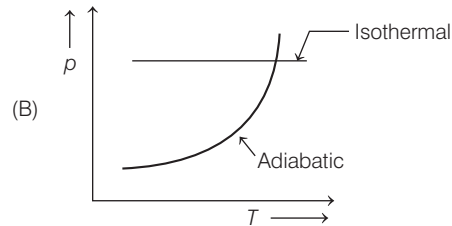
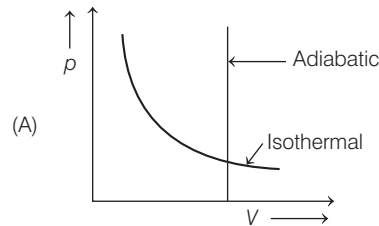
6. A geostationary satellite is orbiting around an arbitrary planet  $P$  at a height of  $11R$  above the surface of  $P$ ,  $R$  being the radius of  $P$ . The time period of another satellite in hours at a height of  $2R$  from the surface of  $P$  is .....  
 $P$  has the time period of 24 h.

a.  $6\sqrt{2}$     b.  $6/\sqrt{2}$     c. 3    d. 5

7. A sound wave of frequency 245 Hz travels with the speed of  $300 \text{ ms}^{-1}$  along the positive X-axis. Each point of the wave moves to and fro through a total distance of 6 cm. What will be the mathematical expression of this travelling wave ?

- a.  $y(x, t) = 0.03[\sin 5.1x - (0.2 \times 10^3)t]$   
b.  $y(x, t) = 0.06[\sin 5.1x - (1.5 \times 10^3)t]$   
c.  $y(x, t) = 0.06[\sin 0.8x - (0.5 \times 10^3)t]$   
d.  $y(x, t) = 0.03[\sin 5.1x - (1.5 \times 10^3)t]$

8. Which one is the correct option for the two different thermodynamic processes?



- a. C and A    b. C and D  
c. Only A    d. B and C

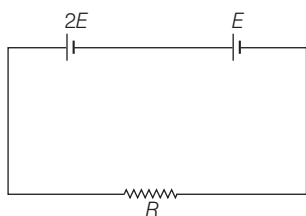
9. The velocity of a particle is  $v = v_0 + gt + Ft^2$ . Its position is  $x = 0$  at  $t = 0$ , then its displacement after time ( $t = 1$ ) is

a.  $v_0 + g + F$     b.  $v_0 + \frac{g}{2} + \frac{F}{3}$   
c.  $v_0 + \frac{g}{2} + F$     d.  $v_0 + 2g + 3F$

10. A carrier signal  $C(t) = 25\sin(2.512 \times 10^{10}t)$  is amplitude modulated by a message signal  $m(t) = 5\sin(1.57 \times 10^8 t)$  and transmitted through an antenna. What will be the bandwidth of the modulated signal?

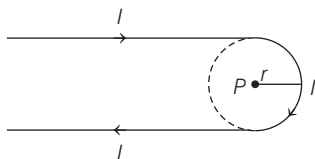
a. 8 GHz                      b. 2.01 GHz  
c. 1987.5 MHz              d. 50 MHz

11. Two cells of emf  $2E$  and  $E$  with internal resistance  $r_1$  and  $r_2$  respectively are connected in series to an external resistor  $R$  (see figure). The value of  $R$ , at which the potential difference across the terminals of the first cell becomes zero is



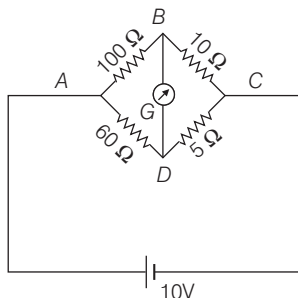
a.  $r_1 + r_2$                   b.  $\frac{r_1}{2} - r_2$                   c.  $\frac{r_1}{2} + r_2$                   d.  $r_1 - r_2$

12. A hairpin like shape as shown in figure is made by bending a long current carrying wire. What is the magnitude of a magnetic field at point  $P$  which lies on the centre of the semicircle?



a.  $\frac{\mu_0 I}{4\pi r} (2 - \pi)$     b.  $\frac{\mu_0 I}{4\pi r} (2 + \pi)$     c.  $\frac{\mu_0 I}{2\pi r} (2 + \pi)$     d.  $\frac{\mu_0 I}{2\pi r} (2 - \pi)$

13. The four arms of a Wheatstone bridge have resistances as shown in the figure. A galvanometer of  $15 \Omega$  resistance is connected across  $BD$ . Calculate the current through the galvanometer when a potential difference of  $10 \text{ V}$  is maintained across  $AC$ .



a.  $2.44 \mu\text{A}$                       b.  $2.44 \text{ mA}$   
c.  $4.87 \text{ mA}$                       d.  $4.87 \mu\text{A}$

14. Two particles  $A$  and  $B$  of equal masses are suspended from two massless springs of spring constants  $k_1$  and  $k_2$ , respectively. If the maximum velocities during oscillations are equal, the ratio of the amplitude of  $A$  and  $B$  is

a.  $\frac{k_2}{k_1}$                       b.  $\frac{k_1}{k_2}$                       c.  $\sqrt{\frac{k_1}{k_2}}$                       d.  $\sqrt{\frac{k_2}{k_1}}$

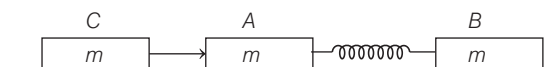
15. Match List-I with List-II

List-I	List-II
A. Phase difference between current and voltage in a purely resistive AC circuit	1. $\frac{\pi}{2}$ ; current leads voltage
B. Phase difference between current and voltage in a pure inductive AC circuit	2. zero
C. Phase difference between current and voltage in a pure capacitive AC circuit	3. $\frac{\pi}{2}$ ; current lags voltage
D. Phase difference between current and voltage in an $L$ - $C$ - $R$ series circuit	4. $\tan^{-1}\left(\frac{X_C - X_L}{R}\right)$

Choose the most appropriate answer from the options given below.

	A	B	C	D
a.	1	3	4	2
b.	2	4	3	1
c.	2	3	4	1
d.	2	3	1	4

16. Two identical blocks  $A$  and  $B$  each of mass  $m$  resting on the smooth horizontal floor are connected by a light spring of natural length  $L$  and spring constant  $k$ . A third block  $C$  of mass  $m$  moving with a speed  $v$  along the line joining  $A$  and  $B$  collides with  $A$ . The maximum compression in the spring is



a.  $v\sqrt{\frac{m}{2k}}$                       b.  $\sqrt{\frac{mv}{2k}}$   
c.  $\sqrt{\frac{mv}{k}}$                       d.  $\sqrt{\frac{m}{2k}}$

17. The atomic hydrogen emits a line spectrum consisting of various series. Which series of hydrogen atomic spectra is lying in the visible region?

a. Brackett series                      b. Paschen series  
c. Lyman series                      d. Balmer series

18. Two identical photocathodes receive the light of frequencies  $f_1$  and  $f_2$ , respectively. If the velocities of the photoelectrons coming out are  $v_1$  and  $v_2$  respectively, then

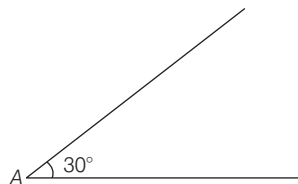
a.  $v_1^2 - v_2^2 = \frac{2h}{m} [f_1 - f_2]$                       b.  $v_1^2 + v_2^2 = \frac{2h}{m} [f_1 + f_2]$   
c.  $v_1 - v_2 = \left[ \frac{2h}{m} (f_1 + f_2) \right]^{\frac{1}{2}}$                       d.  $v_1 - v_2 = \left[ \frac{2h}{m} (f_1 - f_2) \right]^{\frac{1}{2}}$

19. What happens to the inductive reactance and the current in a purely inductive circuit, if the frequency is halved?

a. Both inductive reactance and current will be halved.  
b. Inductive reactance will be halved and current will be doubled.  
c. Inductive reactance will be doubled and current will be halved.  
d. Both inductive reactance and current will be doubled.



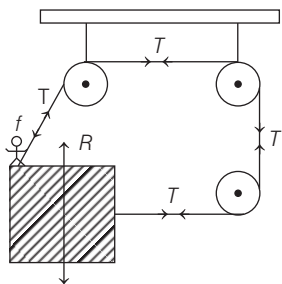
20. A sphere of mass 2 kg and radius 0.5 m is rolling with an initial speed of  $1 \text{ ms}^{-1}$  goes up an inclined plane which makes an angle of  $30^\circ$  with the horizontal plane, without slipping. How long will the sphere take to return to the starting point A ?



- a. 0.60 s      b. 0.52 s      c. 0.57 s      d. 0.80 s

### Section B : Numerical Type Questions

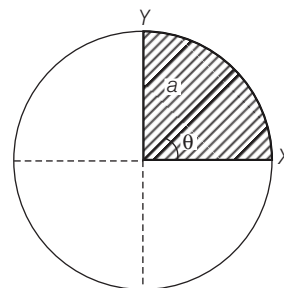
21. The electric field intensity produced by the radiation coming from a 100 W bulb at a distance of 3 m is  $E$ . The electric field intensity produced by the radiation coming from 60 W at the same distance is  $\sqrt{\frac{x}{5}} E$ , where the value of  $x$  is .....
22. A body of mass 1 kg rests on a horizontal floor with which it has a coefficient of static friction  $\frac{1}{\sqrt{3}}$ . It is desired to make the body move by applying the minimum possible force  $F$  newton. The value of  $F$  will be .....  
(Round off to the nearest integer)  
(Take,  $g = 10 \text{ ms}^{-2}$ )
23. A boy of mass 4 kg is standing on a piece of wood having mass 5 kg. If the coefficient of friction between the wood and the floor is 0.5, the maximum force that the boy can exert on the rope, so that the piece of wood does not move from its place is ..... N. (Round off to the nearest integer) (Take,  $g = 10 \text{ ms}^{-2}$ )



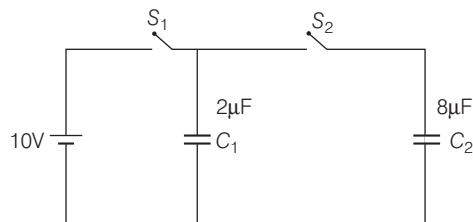
24. Suppose you have taken a dilute solution of oleic acid in such a way that its concentration becomes  $0.01 \text{ cm}^3$  of oleic acid per  $\text{cm}^3$  of the solution. Then, you make a thin film of this solution (monomolecular thickness) of area  $4 \text{ cm}^2$  by considering 100 spherical drops of radius  $\left(\frac{3}{40\pi}\right)^{\frac{1}{3}} \times 10^{-3} \text{ cm}$ . Then, the thickness of oleic acid layer will be  $x \times 10^{-14} \text{ m}$ , where  $x$  is .....
25. A particle of mass  $m$  moves in a circular orbit in a central potential field  $U(r) = U_0 r^4$ . If Bohr's quantisation conditions are applied, radii of possible orbitals  $r_n$  vary with  $n^{1/\alpha}$ , where  $\alpha$  is .....

26. The electric field in a region is given by  $\mathbf{E} = \frac{2}{5}E_0 \hat{i} + \frac{3}{5}E_0 \hat{j}$  with  $E_0 = 4.0 \times 10^3 \text{ N/C}$ . The flux of this field through a rectangular surface area  $0.4 \text{ m}^2$  parallel to the  $yz$ -plane is .....  $\text{N-m}^2 \text{ C}^{-1}$ .

27. The disc of mass  $M$  with uniform surface mass density  $\sigma$  is shown in the figure. The centre of mass of the quarter disc (the shaded area) is at the position  $\frac{x a}{3\pi}, \frac{x a}{3\pi}$ , where  $x$  is .....  
(Round off to the nearest integer)  
( $a$  is an area as shown in the figure)



28. The image of an object placed in air formed by a convex refracting surface is at a distance of 10 m behind the surface. The image is real and is at  $2/3$  of the distance of the object from the surface. The wavelength of light inside the surface is  $2/3$  times the wavelength in air. The radius of the curved surface is  $\frac{x}{13} \text{ m}$ . The value of  $x$  is .....  
(Round off to the nearest integer)
29. A  $2 \mu\text{F}$  capacitor  $C_1$  is first charged to a potential difference of 10 V using a battery. Then, the battery is removed and the capacitor is connected to an uncharged capacitor  $C_2$  of  $8 \mu\text{F}$ . The charge in  $C_2$  on equilibrium condition is .....  $\mu\text{C}$ .  
(Round off to the nearest integer)



30. Seawater at a frequency  $f = 9 \times 10^2 \text{ Hz}$ , has permittivity  $\epsilon = 80\epsilon_0$  and resistivity  $r = 0.25 \Omega\text{-m}$ . Imagine a parallel plate capacitor is immersed in seawater and is driven by an alternating voltage source  $V(t) = V_0 \sin(2\pi ft)$ . Then, the conduction current density becomes  $10^x$  times the displacement current density after time  $t = \frac{1}{800} \text{ s}$ . The value of  $x$  is .....  
(Take,  $\frac{1}{4\pi\epsilon_0} = 9 \times 10^9 \text{ N-m}^2 \text{ C}^{-2}$ )

## Answers

1. (d)	2. (b)	3. (c)	4. (d)	5. (d)	6. (c)	7. (d)	8. (b)	9. (b)	10. (d)
11. (b)	12. (b)	13. (c)	14. (d)	15. (d)	16. (a)	17. (d)	18. (a)	19. (b)	20. (c)
21. (3)	22. (5)	23. (30)	24. (25)	25. (3)	26. (640)	27. (4)	28. (30)	29. (16)	30. (6)

## 18 MARCH SHIFT I

### Section A : Objective Type Questions

1. An oil drop of radius 2 mm with a density  $3 \text{ g cm}^{-3}$  is held stationary under a constant electric field  $3.55 \times 10^5 \text{ Vm}^{-1}$  in the Millikan's oil drop experiment. What is the number of excess electrons that the oil drop will possess? (Take,  $g = 9.81 \text{ m/s}^2$ )  
 a.  $48.8 \times 10^{11}$     b.  $1.73 \times 10^{10}$     c.  $17.3 \times 10^{10}$     d.  $1.73 \times 10^{12}$

2. Match List-I with List-II.

	List-I		List-II
A.	10 km height over Earth's surface	(i)	Thermosphere
B.	70 km height over Earth's surface	(ii)	Mesosphere
C.	180 km height over Earth's surface	(iii)	Stratosphere
D.	270 km height over Earth's surface	(iv)	Troposphere

	A	B	C	D				
a.	(iv)	(iii)	(ii)	(i)	b.	(i)	(iv)	(iii)
c.	(iii)	(ii)	(i)	(iv)	d.	(ii)	(i)	(iv)

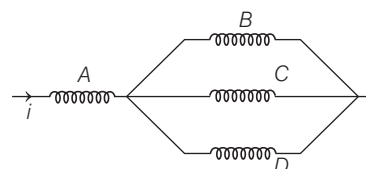
3. Imagine that the electron in a hydrogen atom is replaced by a muon ( $\mu$ ). The mass of muon particle is 207 times that of an electron and charge is equal to the charge of an electron. The ionisation potential of this hydrogen atom will be  
 a. 13.6 eV    b. 2815.2 eV    c. 331.2 eV    d. 27.2 eV

4. A plane electromagnetic wave of frequency 100 MHz is travelling in vacuum along the x-direction. At a particular point in space and time,  $\mathbf{B} = 2.0 \times 10^{-8} \hat{\mathbf{k}} \text{ T}$  (where,  $\hat{\mathbf{k}}$  is unit vector along z-direction). What is  $\mathbf{E}$  at this point?  
 a.  $0.6 \hat{\mathbf{j}} \text{ V/m}$     b.  $6.0 \hat{\mathbf{k}} \text{ V/m}$     c.  $6.0 \hat{\mathbf{j}} \text{ V/m}$     d.  $0.6 \hat{\mathbf{k}} \text{ V/m}$

5. A thin circular ring of mass  $M$  and radius  $r$  is rotating about its axis with an angular speed  $\omega$ . Two particles having mass  $m$  each are now attached at diametrically opposite points. The angular speed of the ring will become

a.  $\omega \frac{M}{M+m}$     b.  $\omega \frac{M+2m}{M}$     c.  $\omega \frac{M}{M+2m}$     d.  $\omega \frac{M-2m}{M+2m}$

6. Four identical long solenoids A, B, C and D are connected to each other as shown in the figure. If the magnetic field at the centre of A is 3T, the field at the centre of C would be (Assume that, the magnetic field is confined with in the volume of respective solenoid)



- a. 12T    b. 6T    c. 9T    d. 1T

7. The time period of a simple pendulum is given by  $T = 2\pi\sqrt{l/g}$ . The measured value of the length of pendulum is 10 cm known to a 1mm accuracy. The time for 200 oscillations of the pendulum is found to be 100 s using a clock of 1s resolution. The percentage accuracy in the determination of  $g$  using this pendulum is x. The value of x to the nearest integer is

- a. 2%    b. 3%    c. 5%    d. 4%

8. A constant power delivering machine has towed a box, which was initially at rest, along a horizontal straight line. The distance moved by the box in time  $t$  is proportional to

- a.  $t^{2/3}$     b.  $t^{3/2}$     c.  $t$     d.  $t^{1/2}$

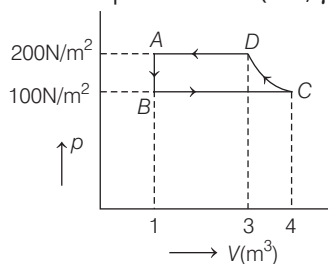
9. What will be the average value of energy along one degree of freedom for an ideal gas in thermal equilibrium at a temperature  $T$ ? ( $k_B$  is Boltzmann constant)

- a.  $\frac{1}{2} k_B T$     b.  $\frac{2}{3} k_B T$     c.  $\frac{3}{2} k_B T$     d.  $k_B T$

10. A radioactive sample disintegrates via two independent decay processes having half-lives  $T_{1/2}^{(1)}$  and  $T_{1/2}^{(2)}$ , respectively. The effective half-life  $T_{1/2}$  of the nuclei is

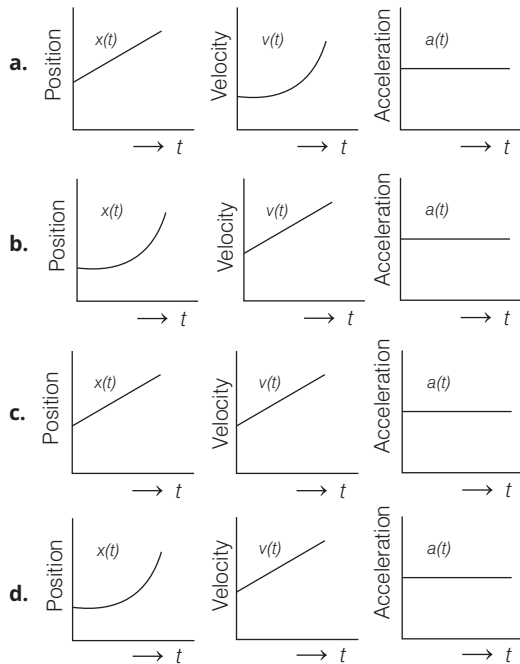
- a.  $T_{1/2} = \frac{T_{1/2}^{(1)} + T_{1/2}^{(2)}}{T_{1/2}^{(1)} - T_{1/2}^{(2)}}$     b.  $T_{1/2} = T_{1/2}^{(1)} + T_{1/2}^{(2)}$   
 c.  $T_{1/2} = \frac{T_{1/2}^{(1)} T_{1/2}^{(2)}}{T_{1/2}^{(1)} + T_{1/2}^{(2)}}$     d. None of these

11. The  $p$ - $V$  diagram of a diatomic ideal gas system going under cyclic process as shown in figure. The work done during an adiabatic process CD is (use,  $\gamma = 1.4$ )



- a. -500J    b. -400J    c. 400J    d. 200J

12. In Young's double slit arrangement, slits are separated by a gap of 0.5 mm, and the screen is placed at a distance of 0.5 m from them. The distance between the first and the third bright fringe formed when the slits are illuminated by a monochromatic light of  $5890 \text{ \AA}$  is  
 a.  $1178 \times 10^{-9} \text{ m}$                       b.  $1178 \times 10^{-6} \text{ m}$   
 c.  $1178 \times 10^{-12} \text{ m}$                       d.  $5890 \times 10^{-7} \text{ m}$
13. A particle is travelling 4 times as fast as an electron. Assuming the ratio of de-Broglie wavelength of a particle to that of electron is 2 : 1, the mass of the particle is  
 a.  $\frac{1}{16}$  times the mass of electron  
 b. 8 times the mass of electron  
 c. 16 times the mass of electron  
 d.  $\frac{1}{8}$  times the mass of electron
14. The position, velocity and acceleration of a particle moving with a constant acceleration can be represented by

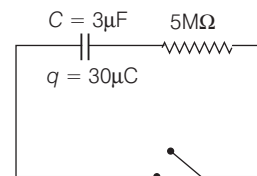


15. In the experiment of Ohm's law, a potential difference of 5.0 V is applied across the end of a conductor of length 10.0 cm and diameter of 5.00 mm. The measured current in the conductor is 2.00 A. The maximum permissible percentage error in the resistivity of the conductor is  
 a. 3.9                      b. 8.4                      c. 7.5                      d. 3.0
16. In a series  $L$ - $C$ - $R$  resonance circuit, if we change the resistance only, from a lower to higher value,  
 a. the bandwidth of resonance circuit will increase  
 b. the resonance frequency will increase  
 c. the quality factor will increase  
 d. the quality factor and the resonance frequency will remain constant
17. An AC source rated 220 V, 50 Hz is connected to a resistor. The time taken by the current to change from its maximum to the rms value is  
 a. 2.5 ms                      b. 25 ms                      c. 2.5 s                      d. 0.25 ms

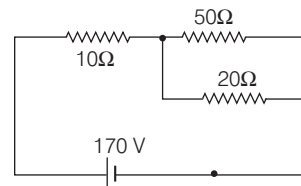
18. Your friend is having eye sight problem. She is not able to see clearly a distant uniform window mesh and it appears to her as non-uniform and distorted. The doctor diagnosed the problem as  
 a. astigmatism  
 b. myopia with astigmatism  
 c. presbyopia with astigmatism  
 d. myopia and hypermetropia
19. A loop of flexible wire of irregular shape carrying current is placed in an external magnetic field. Identify the effect of the field on the wire.  
 a. Loop assumes circular shape with its plane normal to the field.  
 b. Loop assumes circular shape with its plane parallel to the field.  
 c. Wire gets stretched to become straight.  
 d. Shape of the loop remains unchanged.
20. The time period of a satellite in a circular orbit of radius  $R$  is  $T$ . The period of another satellite in a circular orbit of radius  $9R$  is  
 a.  $9 T$                       b.  $27 T$   
 c.  $12 T$                       d.  $3 T$

## Section B : Numerical Type Questions

21. A particle performs simple harmonic motion with a period of 2 s. The time taken by the particle to cover a displacement equal to half of its amplitude from the mean position is  $1/a$  s. The value of  $a$  to the nearest integer is .....
22. The circuit shown in the figure consists of a charged capacitor of capacity  $3 \mu\text{F}$  and a charge of  $30 \mu\text{C}$ . At time  $t = 0$ , when the key is closed, the value of current flowing through the  $5 \text{ M}\Omega$  resistor is  $x \mu\text{A}$ . The value of  $x$  to the nearest integer is .....



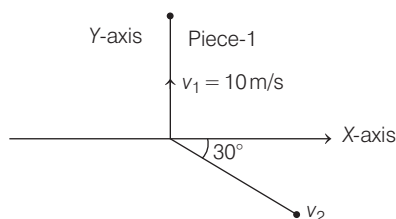
23. The voltage across the  $10 \Omega$  resistor in the given circuit is  $x$  volt.



The value of  $x$  to the nearest integer is .....

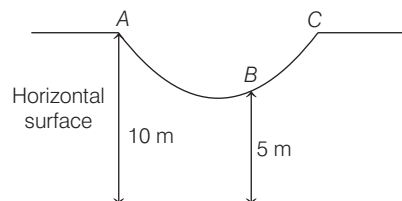
24. Two separate wires  $A$  and  $B$  are stretched by 2 mm and 4 mm respectively, when they are subjected to a force of 2 N. Assume that both the wires are made up of same material and the radius of wire  $B$  is 4 times that of the radius of wire  $A$ . The length of the wires  $A$  and  $B$  are in the ratio of  $a : b$ . Then,  $a/b$  can be expressed as  $1/x$ , where  $x$  is .....

25. A person is swimming with a speed of 10 m/s at an angle of  $120^\circ$  with the flow and reaches to a point directly opposite on the other side of the river. The speed of the flow is  $x$  m/s. The value of  $x$  to the nearest integer is .....
26. A parallel plate capacitor has plate area  $100 \text{ m}^2$  and plate separation of 10 m. The space between the plates is filled upto a thickness 5 m with a material of dielectric constant of 10. The resultant capacitance of the system is  $x$  pF. The value of  $\epsilon_0 = 8.85 \times 10^{-12} \text{ fm}^{-1}$ . The value of  $x$  to the nearest integer is .....
27. A ball of mass 10 kg moving with a velocity  $10\sqrt{3} \text{ m/s}$  along the X-axis, hits another ball of mass 20 kg which is at rest. After the collision, first ball comes to rest while the second ball disintegrates into two equal pieces. One piece starts moving along Y-axis with a speed of 10 m/s. The second piece starts moving at an angle of  $30^\circ$  with respect to the X-axis. The velocity of the ball moving at  $30^\circ$  with X-axis is  $x$  m/s. The configuration of pieces after collision is shown in the figure below. The value of  $x$  to the nearest integer is .....



28. As shown in the figure, a particle of mass 10 kg is placed at a point A. When the particle is slightly displaced to its right, it starts moving and reaches the point B. The speed of the particle at B is  $x$  m/s. (Take,  $g = 10 \text{ m/s}^2$ )

The value of  $x$  to the nearest integer is .....



29. An  $n$ - $p$ - $n$  transistor operates as a common emitter amplifier with a power gain of  $10^6$ . The input circuit resistance is  $100\Omega$  and the output load resistance is  $10 \text{ k}\Omega$ . The common emitter current gain  $\beta$  will be ..... (Round off to the nearest integer)
30. A bullet of mass 0.1 kg is fired on a wooden block to pierce through it, but it stops after moving a distance of 50 cm into it. If the velocity of bullet before hitting the wood is 10 m/s and it slows down with uniform deceleration, then the magnitude of effective retarding force on the bullet is  $x$  N. The value of  $x$  to the nearest integer is .....

## Answers

- |         |         |          |          |         |           |          |          |           |          |
|---------|---------|----------|----------|---------|-----------|----------|----------|-----------|----------|
| 1. (b)  | 2. (a)  | 3. (b)   | 4. (c)   | 5. (c)  | 6. (d)    | 7. (b)   | 8. (b)   | 9. (a)    | 10. (c)  |
| 11. (a) | 12. (b) | 13. (d)  | 14. (b)  | 15. (a) | 16. (a)   | 17. (a)  | 18. (b)  | 19. (a)   | 20. (b)  |
| 21. (6) | 22. (2) | 23. (70) | 24. (32) | 25. (5) | 26. (161) | 27. (20) | 28. (10) | 29. (100) | 30. (10) |

## 18 MARCH SHIFT II

### Section A : Objective Type Questions

1. Which of the following statements are correct?
- Electric monopoles do not exist, whereas magnetic monopoles exist.
  - Magnetic field lines due to a solenoid at its ends and outside cannot be completely straight and confined.
  - Magnetic field lines are completely confined within a toroid.
  - Magnetic field lines inside a bar magnet are not parallel.
  - $\chi = -1$  is the condition for a perfect diamagnetic material, where  $\chi$  is its magnetic susceptibility.

Choose the correct answer from the options given below.

- |            |            |
|------------|------------|
| a. C and E | b. B and D |
| c. A and B | d. B and C |

2. An object of mass  $m_1$  collides with another object of mass  $m_2$ , which is at rest. After the collision, the objects move with equal speeds in opposite direction. The ratio of the masses  $m_2 : m_1$  is
- |          |          |          |          |
|----------|----------|----------|----------|
| a. 3 : 1 | b. 2 : 1 | c. 1 : 2 | d. 1 : 1 |
|----------|----------|----------|----------|
3. For an adiabatic expansion of an ideal gas, the fractional change in its pressure is equal to (where,  $\gamma$  is the ratio of specific heats)
- |                           |                           |                                     |                   |
|---------------------------|---------------------------|-------------------------------------|-------------------|
| a. $-\gamma \frac{dV}{V}$ | b. $-\gamma \frac{V}{dV}$ | c. $-\frac{1}{\gamma} \frac{dV}{V}$ | d. $\frac{dV}{V}$ |
|---------------------------|---------------------------|-------------------------------------|-------------------|
4. A proton and an  $\alpha$ -particle, having kinetic energies  $K_p$  and  $K_\alpha$ , respectively, enter into a magnetic field at right angles. The ratio of the radii of trajectory of proton to that of  $\alpha$ -particle is 2 : 1. The ratio of  $K_p : K_\alpha$  is
- |          |          |          |          |
|----------|----------|----------|----------|
| a. 1 : 8 | b. 8 : 1 | c. 1 : 4 | d. 4 : 1 |
|----------|----------|----------|----------|

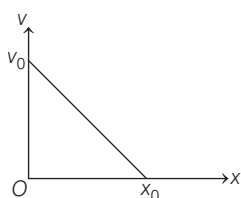
5. A plane electromagnetic wave propagating along  $y$ -direction can have the following pair of electric field (**E**) and magnetic field (**B**) components.

a.  $E_y, B_y$  or  $E_z, B_z$       b.  $E_y, B_x$  or  $E_x, B_y$   
 c.  $E_x, B_z$  or  $E_z, B_x$       d.  $E_x, B_y$  or  $E_y, B_x$

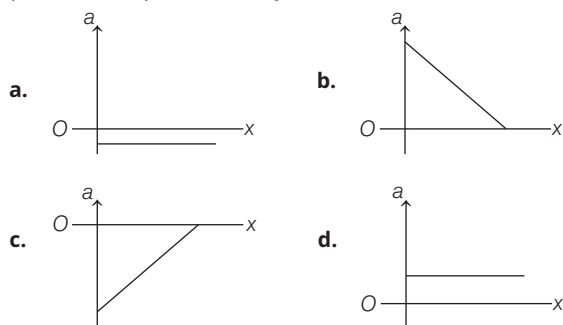
6. Consider a uniform wire of mass  $M$  and length  $L$ . It is bent into a semicircle. Its moment of inertia about a line perpendicular to the plane of the wire passing through the centre is

a.  $\frac{1}{4} \frac{ML^2}{\pi^2}$       b.  $\frac{2}{5} \frac{ML^2}{\pi^2}$       c.  $\frac{ML^2}{\pi^2}$       d.  $\frac{1}{2} \frac{ML^2}{\pi^2}$

7. The velocity-displacement graph of a particle is shown in the figure.



The acceleration-displacement graph of the same particle is represented by



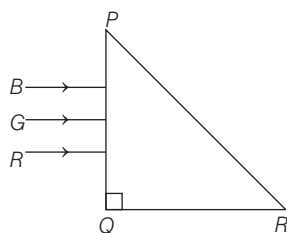
8. The correct relation between  $\alpha$  (ratio of collector current to emitter current) and  $\beta$  (ratio of collector current to base current) of a transistor is

a.  $\beta = \frac{\alpha}{1+\alpha}$       b.  $\alpha = \frac{\beta}{1-\alpha}$       c.  $\beta = \frac{1}{1-\alpha}$       d.  $\alpha = \frac{\beta}{1+\beta}$

9. Three rays of light, namely red (R), green (G) and blue (B) are incident on the face PQ of a right angled prism PQR as shown in figure

The refractive indices of the material of the prism for red, green and blue wavelength are 1.27, 1.42 and 1.49, respectively. The colour of the ray(s) emerging out of the face PR is

a. green      b. red      c. blue and green      d. blue



10. If the angular velocity of Earth's spin is increased such that the bodies at the equator start floating, the duration of the day would be approximately

(Take  $2g = 10 \text{ ms}^{-2}$ , the radius of Earth,  $R = 6400 \times 10^3 \text{ m}$ , take  $\pi = 3.14$ )

a. 60 min      b. does not change  
 c. 1200 min      d. 84 min

11. The decay of a proton to neutron is

a. not possible as proton mass is less than the neutron mass  
 b. possible only inside the nucleus  
 c. not possible but neutron to proton conversion is possible  
 d. always possible as it is associated only with  $\beta^+$  decay

12. In a series  $L$ - $C$ - $R$  circuit, the inductive reactance ( $X_L$ ) is  $10 \Omega$  and the capacitive reactance ( $X_C$ ) is  $4 \Omega$ . The resistance ( $R$ ) in the circuit is  $6 \Omega$ . The power factor of the circuit is

a.  $\frac{1}{2}$       b.  $\frac{1}{2\sqrt{2}}$       c.  $\frac{1}{\sqrt{2}}$       d.  $\frac{\sqrt{3}}{2}$

13. The angular momentum of a planet of mass  $M$  moving around the Sun in an elliptical orbit is  $L$ . The magnitude of the areal velocity of the planet is

a.  $\frac{4L}{M}$       b.  $\frac{L}{M}$       c.  $\frac{2L}{M}$       d.  $\frac{L}{2M}$

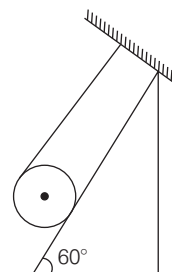
14. The function of time representing a simple harmonic motion with a period of  $\frac{\pi}{\omega}$  is

a.  $\sin(\omega t) = \cos(\omega t)$       b.  $\cos(\omega t) + \cos(2\omega t) + \cos(3\omega t)$   
 c.  $\sin^2(\omega t)$       d.  $3\cos\left(\frac{\pi}{4} - 2\omega t\right)$

15. A solid cylinder of mass  $m$  is wrapped with an inextensible light string and, is placed on a rough inclined plane as shown in the figure. The frictional force acting between the cylinder and the inclined plane is

(The coefficient of static friction,  $\mu_s$ , is 0.4)

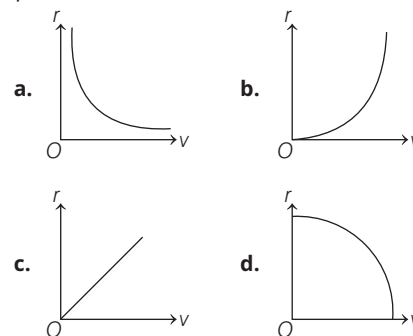
a.  $\frac{7}{2} mg$       b.  $5 mg$   
 c.  $\frac{mg}{5}$       d. 0



16. The time taken for the magnetic energy to reach 25% of its maximum value, when a solenoid of resistance  $R$ , inductance  $L$  is connected to a battery, is

a.  $\frac{L}{R} \ln 5$       b. infinite      c.  $\frac{L}{R} \ln 2$       d.  $\frac{L}{R} \ln 10$

17. A particle of mass  $m$  moves in a circular orbit under the central potential field,  $U(r) = -C/r$ , where  $C$  is a positive constant. The correct radius-velocity graph of the particle's motion is



18. An ideal gas in a cylinder is separated by a piston in such a way that the entropy of one part is  $S_1$  and that of the other part is  $S_2$ . Given that  $S_1 > S_2$ . If the piston is removed, then the total entropy of the system will be

a.  $S_1 \times S_2$       b.  $S_1 - S_2$       c.  $\frac{S_1}{S_2}$       d.  $S_1 + S_2$

19. Consider a sample of oxygen behaving like an ideal gas. At 300 K, the ratio of root mean square (rms) velocity to the average velocity of gas molecule would be (Molecular weight of oxygen is 32 g/mol;  $R = 8.3 \text{ J K}^{-1} \text{ mol}^{-1}$ )

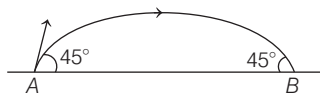
a.  $\sqrt{\frac{3}{3}}$       b.  $\sqrt{\frac{8}{3}}$       c.  $\sqrt{\frac{3\pi}{8}}$       d.  $\sqrt{\frac{8\pi}{3}}$

20. The speed of electrons in a scanning electron microscope is  $1 \times 10^7 \text{ ms}^{-1}$ . If the protons having the same speed are used instead of electrons, then the resolving power of scanning proton microscope will be changed by a factor of

a. 1837      b.  $\frac{1}{1837}$       c.  $\sqrt{1837}$       d.  $\frac{1}{\sqrt{1837}}$

## Section B : Numerical Type Questions

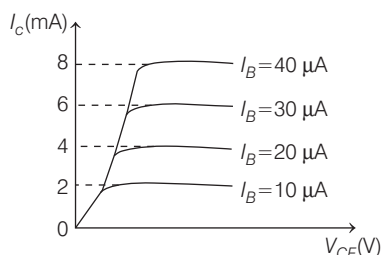
21. The projectile motion of a particle of mass 5 g is shown in the figure.



The initial velocity of the particle is  $5\sqrt{2} \text{ ms}^{-1}$  and the air resistance is assumed to be negligible. The magnitude of the change in momentum between the points A and B is  $x \times 10^{-2} \text{ kg-ms}^{-1}$ . The value of  $x$  to the nearest integer, is .....

22. A ball of mass 4 kg, moving with a velocity of  $10 \text{ ms}^{-1}$ , collides with a spring of length 8 m and force constant  $100 \text{ Nm}^{-1}$ . The length of the compressed spring is  $x$  m. The value of  $x$  to the nearest integer, is .....

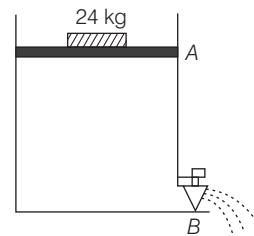
23. The typical output characteristics curve for a transistor working in the common-emitter configuration is shown in the figure.



The estimated current gain from the figure is .....

24. Consider a water tank as shown in the figure. It's cross-sectional area is  $0.4 \text{ m}^2$ . The tank has an opening B near the bottom whose cross-section area is  $1 \text{ cm}^2$ . A load of 24 kg is applied on the water at the top when the height of the water level is 40 cm above the bottom, the velocity of water coming out the opening B is  $v \text{ ms}^{-1}$ . The value of  $v$ , to the nearest integer, is .....

(Take value of  $g$  to be  $10 \text{ ms}^{-2}$ )



25. A TV transmission tower antenna is at a height of 20 m. Suppose that the receiving antenna is at

(i) ground level

(ii) a height of 5 m.

The increase in antenna range in case (ii) relative to case (i) is  $n\%$ .

The value of  $n$ , to the nearest integer, is .....

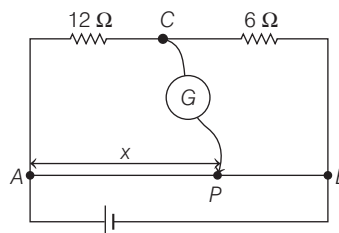
26. The radius of a sphere is measured to be  $(7.50 \pm 0.85) \text{ cm}$ .

Suppose the percentage error in its volume is  $x$ . The value of  $x$  to the nearest  $x$ , is .....

27. An infinite number of point charges, each carrying  $1 \mu\text{C}$  charge, are placed along the  $Y$ -axis at  $y = 1\text{m}, 2\text{m}, 4\text{m}, 8\text{m}$ . The total force on a  $1 \text{ C}$  point charge, placed at the origin, is  $x \times 10^3 \text{ N}$ . The value of  $x$  to the nearest integer, is .....

(Take,  $\frac{1}{4\pi\epsilon_0} = 9 \times 10^9 \text{ N-m}^2/\text{C}^2$ )

28. Consider a 72 cm long wire AB as shown in the figure. The galvanometer jockey is placed at P on AB at a distance  $x$  cm from A. The galvanometer shows zero deflection.



The value of  $x$ , to the nearest integer, is .....

29. Two wires of same length and thickness having specific resistances  $6 \Omega\text{-cm}$  and  $3 \Omega\text{-cm}$  respectively are connected in parallel. The effective resistivity is  $\rho \Omega\text{-cm}$ . The value of  $\rho$  to the nearest integer, is .....

30. A galaxy is moving away from the Earth at a speed of  $286 \text{ kms}^{-1}$ . The shift in the wavelength of a red line at  $630 \text{ nm}$  is  $x \times 10^{-10} \text{ m}$ . The value of  $x$  to the nearest integer, is .....

(Take the value of speed of light  $c$ , as  $3 \times 10^8 \text{ ms}^{-1}$ )

## Answers

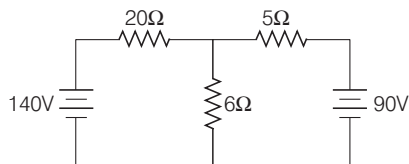
- |         |         |           |         |          |          |          |          |         |         |
|---------|---------|-----------|---------|----------|----------|----------|----------|---------|---------|
| 1. (a)  | 2. (a)  | 3. (a)    | 4. (d)  | 5. (c)   | 6. (c)   | 7. (c)   | 8. (d)   | 9. (b)  | 10. (d) |
| 11. (b) | 12. (c) | 13. (d)   | 14. (d) | 15. (c)  | 16. (c)  | 17. (a)  | 18. (d)  | 19. (c) | 20. (a) |
| 21. (5) | 22. (6) | 23. (200) | 24. (3) | 25. (50) | 26. (34) | 27. (12) | 28. (48) | 29. (4) | 30. (6) |



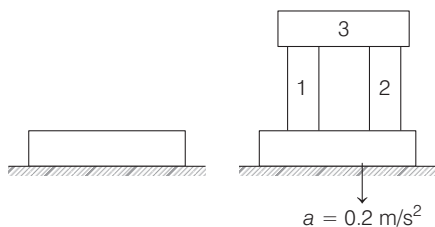
## 20 JULY SHIFT I

### Section A : Objective Type Questions

1. The value of current in the  $6\Omega$  resistance is

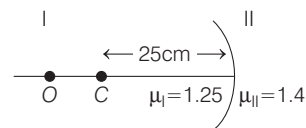


- a. 4 A  
b. 8 A  
c. 10 A  
d. 6 A
2. The normal reaction  $N$  for a vehicle of 800 kg mass, negotiating a turn on a  $30^\circ$  banked road at maximum possible speed without skidding is  $\dots \times 10^3$  kg-m/s<sup>2</sup>. [Take,  $\mu_s = 0.2$ ]
- a. 10.2  
b. 7.2  
c. 12.4  
d. 6.96
3. A radioactive material decays by simultaneous emission of two particles with half-lives of 1400 yr and 700 yr, respectively. What will be the time after the which one-third of the material remains? [Take,  $\ln 3 = 1.1$ ]
- a. 1110 yr  
b. 700 yr  
c. 340 yr  
d. 740 yr
4. A steel block of 10 kg rests on a horizontal floor as shown. When three iron cylinders are placed on it as shown, the block and cylinders go down with an acceleration  $0.2 \text{ m/s}^2$ . The normal reaction  $R$  by the floor, if mass of the iron cylinders are equal and of 20 kg each, is  $\dots$  N. [Take,  $g = 10 \text{ m/s}^2$  and  $\mu_s = 0.2$ ]

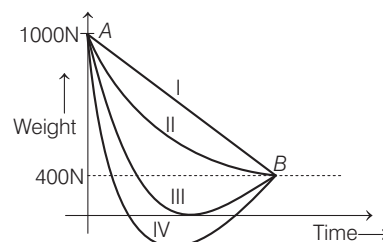


- a. 716  
b. 686  
c. 714  
d. 684
5. AC voltage  $V(t) = 20 \sin \omega t$  volt of frequency 50 Hz is applied to a parallel plate capacitor. The separation between the plates is 2 mm and the area is  $1 \text{ m}^2$ . The amplitude of the oscillating displacement current for the applied AC voltage is  $\dots$ . [Take,  $\epsilon_0 = 8.85 \times 10^{-12} \text{ F/m}$ ]
- a.  $21.14 \mu\text{A}$   
b.  $83.37 \mu\text{A}$   
c.  $27.79 \mu\text{A}$   
d.  $55.58 \mu\text{A}$

6. Region I and II are separated by a spherical surface of radius 25 cm. An object is kept in region I at a distance of 40 cm from the surface. The distance of the image from the surface is



- a. 55.44 cm  
b. 9.52 cm  
c. 18.23 cm  
d. 37.58 cm
7. A person whose mass is 100 kg travels from Earth to Mars in a spaceship. Neglect all other objects in sky and take acceleration due to gravity on the surface of the Earth and Mars as  $10 \text{ m/s}^2$  and  $4 \text{ m/s}^2$ , respectively. Identify from the below figures, the curve that fits best for the weight of the passenger as a function of time.



- a. III  
b. I  
c. IV  
d. II
8. The amount of heat needed to raise the temperature of 4 moles of a rigid diatomic gas from  $0^\circ\text{C}$  to  $50^\circ\text{C}$  when no work is done is  $\dots$ . ( $R$  is the universal gas constant)
- a.  $250 R$   
b.  $750 R$   
c.  $175 R$   
d.  $500 R$
9. If  $\mathbf{A}$  and  $\mathbf{B}$  are two vectors satisfying the relation  $\mathbf{A} \cdot \mathbf{B} = |\mathbf{A} \times \mathbf{B}|$ . Then, the value of  $|\mathbf{A} - \mathbf{B}|$  will be
- a.  $\sqrt{A^2 + B^2}$   
b.  $\sqrt{A^2 + B^2 + \sqrt{2}AB}$   
c.  $\sqrt{A^2 + B^2 + 2AB}$   
d.  $\sqrt{A^2 + B^2 - \sqrt{2}AB}$
10. A deuteron and an  $\alpha$ -particle having equal kinetic energy enter perpendicular into a magnetic field. Let  $r_d$  and  $r_\alpha$  be their respective radii of circular path. The value of  $r_d/r_\alpha$  is equal to
- a.  $1/\sqrt{2}$   
b.  $\sqrt{2}$   
c. 1  
d. 2
11. A nucleus of mass  $M$  emits  $\gamma$ -ray photon of frequency  $\nu$ . The loss of internal energy by the nucleus is [Take,  $c$  is the speed of electromagnetic wave.]
- a.  $h\nu$   
b. zero  
c.  $h\nu \left[ 1 - \frac{h\nu}{2Mc^2} \right]$   
d.  $h\nu \left[ 1 + \frac{h\nu}{2Mc^2} \right]$

12. A certain charge  $Q$  is divided into two parts  $q$  and  $(Q - q)$ .

How should the charges  $Q$  and  $q$  be divided, so that  $q$  and  $(Q - q)$  placed at a certain distance apart experience maximum electrostatic repulsion ?

- a.  $Q = \frac{q}{2}$                                       b.  $Q = 2q$   
c.  $Q = 4q$                                       d.  $Q = 3q$

13. A current of 5 A is passing through a non-linear magnesium wire of cross-section  $0.04 \text{ m}^2$ . At every point, the direction of current density is at an angle of  $60^\circ$  with the unit vector of area of cross-section. The magnitude of electric field at every point of the conductor is

(Take, resistivity of magnesium,  $\rho = 44 \times 10^{-8} \Omega\text{-m}$ )

- a.  $11 \times 10^{-2} \text{ V/m}$                                       b.  $11 \times 10^{-7} \text{ V/m}$   
c.  $11 \times 10^{-5} \text{ V/m}$                                       d.  $11 \times 10^{-3} \text{ V/m}$

14. Consider a mixture of gas molecule of types  $A$ ,  $B$  and  $C$  having masses  $m_A < m_B < m_C$ . The ratio of their root mean square speeds at normal temperature and pressure is

- a.  $v_A = v_B = v_C = 0$                                       b.  $\frac{1}{v_A} > \frac{1}{v_B} > \frac{1}{v_C}$   
c.  $v_A = v_B \neq v_C$                                       d.  $\frac{1}{v_A} < \frac{1}{v_B} < \frac{1}{v_C}$

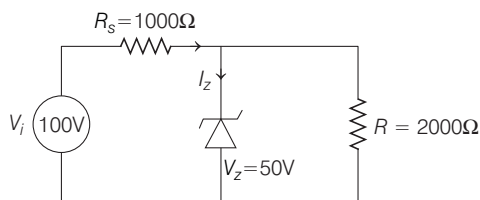
15. A butterfly is flying with a velocity  $4\sqrt{2} \text{ m/s}$  in North-East direction. Wind is slowly blowing at  $1 \text{ m/s}$  from North to South. The resultant displacement of the butterfly in 3 s is

- a. 3 m                                      b. 20 m                                      c.  $12\sqrt{2} \text{ m}$                                       d. 15 m

16. The value of tension in a long thin metal wire has been changed from  $T_1$  to  $T_2$ . The lengths of the metal wire at two different values of tension  $T_1$  and  $T_2$  are  $l_1$  and  $l_2$ , respectively. The actual length of the metal wire is

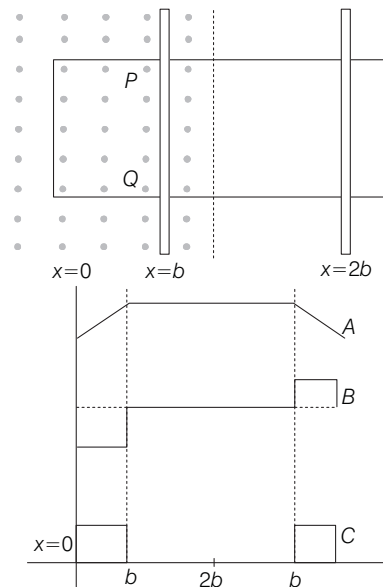
- a.  $\frac{T_1 l_2 - T_2 l_1}{T_1 - T_2}$                                       b.  $\frac{T_1 l_1 - T_2 l_2}{T_1 - T_2}$   
c.  $\frac{l_1 + l_2}{2}$                                       d.  $\sqrt{T_1 T_2 l_1 l_2}$

17. For the circuit shown below, calculate the value of  $I_z$ .



- a. 25 mA                                      b. 0.15 A  
c. 0.1 A                                      d. 0.05 A

18. The arm  $PQ$  of a rectangular conductor is moving from  $x = 0$  to  $x = 2b$  outwards and then inwards from  $x = 2b$  to  $x = 0$  as shown in the figure. A uniform magnetic field perpendicular to the plane is acting from  $x = 0$  to  $x = b$ . Identify the graph showing the variation of different quantities with distance.



- a.  $A$  - flux,  $B$  - power dissipated,  $C$  - emf  
b.  $A$  - power dissipated,  $B$  - flux,  $C$  - emf  
c.  $A$  - flux,  $B$  - emf,  $C$  - power dissipated  
d.  $A$  - emf,  $B$  - power dissipated,  $C$  - flux

19. The entropy of any system is given by

$$S = \alpha^2 \beta \ln \left[ \frac{\mu k R}{J \beta^2} + 3 \right]$$

where,  $\alpha$  and  $\beta$  are the constants;  $\mu$ ,  $J$ ,  $k$  and  $R$  are number of moles, mechanical equivalent of heat, Boltzmann constant and gas constant, respectively.

[ Take,  $S = \frac{dQ}{T}$  ]

Choose the incorrect option.

- a.  $\alpha$  and  $J$  have the same dimensions.  
b.  $S$ ,  $\beta$ ,  $k$  and  $\mu R$  have the same dimensions.  
c.  $S$  and  $\alpha$  have different dimensions.  
d.  $\alpha$  and  $k$  have the same dimensions.

20. The radiation corresponding to  $3 \rightarrow 2$  transition of a hydrogen atom falls on a gold surface to generate photoelectrons. These electrons are passed through a magnetic field of  $5 \times 10^{-4} \text{ T}$ . Assume that the radius of the largest circular path followed by these electrons is 7 mm, the work-function of the metal is (Take, mass of electron  $= 9.1 \times 10^{-31} \text{ kg}$ )

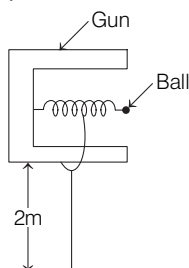
- a. 1.36 eV                                      b. 1.88 eV  
c. 0.16 eV                                      d. 0.82 eV

## Section B : Numerical Type Questions

21. In a spring gun having spring constant  $100 \text{ N/m}$  a small ball  $B$  of mass  $100 \text{ g}$  is put in its barrel (as shown in figure) by compressing the spring through  $0.05 \text{ m}$ . There should be a box placed at a distance  $d$  on the ground, so that the ball falls in it. If the ball leaves the

gun horizontally at a height of 2 m above the ground. The value of  $d$  is ..... m.

(Take,  $g=10\text{ m/s}^2$ )



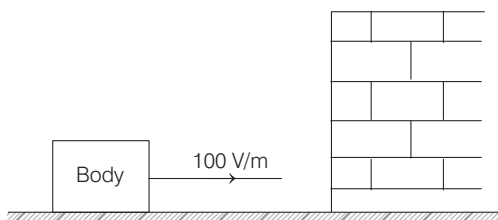
- 22.** In an  $L$ - $C$ - $R$  series circuit, an inductor 30 mH and a resistor  $1\Omega$  are connected to an AC source of angular frequency 300 rad/s. The value of capacitance for which, the current leads the voltage by  $45^\circ$  is  $\frac{1}{x} \times 10^{-3}$  F. Then, the value of  $x$  is .....

- 23.** The amplitude of wave disturbance propagating in the positive  $x$ -direction is given by  $y = \frac{1}{(1+x)^2}$  at time  $t = 0$

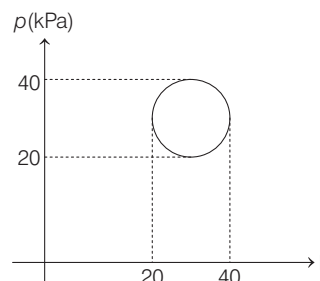
and  $y = \frac{1}{1+(x-2)^2}$  at  $t = 1\text{ s}$ , where  $x$  and  $y$  are in metre.

The shape of wave does not change during the propagation. The velocity of the wave will be ..... m/s.

- 24.** A body having specific charge  $8\mu\text{C/g}$  is resting on a frictionless plane at a distance 10 cm from the wall (as shown in the figure). It starts moving towards the wall when a uniform electric field of 100 V/m is applied horizontally towards the wall. If the collision of the body with the wall is perfectly elastic, then the time period of the motion will be ..... s.



- 25.** In the reported figure, heat energy absorbed by a system in going through a cyclic process is .....  $\pi\text{J}$ .



- 26.** A circular disc reaches from top to bottom of an inclined plane of length  $L$ . When it slips down the plane, it takes time  $t_1$ . When it rolls down the plane, it takes time  $t_2$ . The value of  $\frac{t_2}{t_1}$  is  $\sqrt{\frac{3}{x}}$ . The value of  $x$  will be .....

- 27.** A rod of mass  $M$  and length  $L$  is lying on a horizontal frictionless surface. A particle of mass  $m$  travelling along the surface hits at one end of the rod with a velocity  $u$  in a direction perpendicular to the rod. The collision is completely elastic. After collision, particle comes to rest. The ratio of masses  $\left(\frac{m}{M}\right)$  is  $\frac{1}{x}$ . The value of  $x$  will be .....

- 28.** An object viewed from a near point distance of 25 cm, using a microscopic lens with magnification 6, gives an unresolved image. A resolved image is observed at infinite distance with a total magnification double the earlier using an eyepiece along with the given lens and a tube of length 0.6 m, if the focal length of the eyepiece is equal to ..... cm.

- 29.** The frequency of a car horn encountered a change from 400 Hz to 500 Hz, when the car approaches a vertical wall. If the speed of sound is 330 m/s, then the speed of car is ..... km/h.

- 30.** A carrier wave  $V_c(t) = 160\sin(2\pi \times 10^6 t)$  V is made to vary between  $V_{\max} = 200$  V and  $V_{\min} = 120$  V by a message signal  $V_m(t) = A_m \sin(2\pi \times 10^3 t)$  V. The peak voltage  $A_m$  of the modulating signal is .....

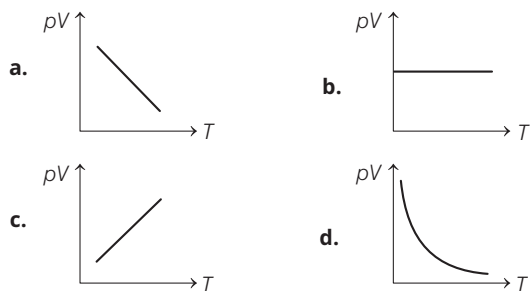
## Answers

- |             |         |         |         |           |         |         |          |           |          |
|-------------|---------|---------|---------|-----------|---------|---------|----------|-----------|----------|
| 1. (c)      | 2. (a)  | 3. (d)  | 4. (b)  | 5. (c)    | 6. (d)  | 7. (a)  | 8. (d)   | 9. (d)    | 10. (b)  |
| 11. (d)     | 12. (b) | 13. (c) | 14. (d) | 15. (d)   | 16. (a) | 17. (a) | 18. (c)  | 19. (d)   | 20. (d)  |
| 21. (0.003) | 22. (3) | 23. (2) | 24. (1) | 25. (100) | 26. (2) | 27. (4) | 28. (25) | 29. (132) | 30. (40) |

## 20 JULY SHIFT II

### Section A : Objective Type Questions

- If the kinetic energy of a moving body becomes four times of its initial kinetic energy, then the percentage change in its momentum will be  
a. 100%      b. 200%      c. 300%      d. 400%
- A boy reaches the airport and finds that the escalator is not working. He walks up the stationary escalator in time  $t_1$ . If he remains stationary on a moving escalator, then the escalator takes him up in time  $t_2$ . The time taken by him to walk up on the moving escalator will be  
a.  $\frac{t_1 t_2}{t_2 - t_1}$       b.  $\frac{t_1 + t_2}{2}$       c.  $\frac{t_1 t_2}{t_2 + t_1}$       d.  $t_2 - t_1$
- A satellite is launched into a circular orbit of radius  $R$  around Earth, while a second satellite is launched into a circular orbit of radius  $1.02 R$ . The percentage difference in the time periods of the two satellites is  
a. 1.5      b. 2.0      c. 0.7      d. 3.0
- With what speed should a galaxy move outward with respect to Earth, so that the sodium-D line at wavelength  $5890 \text{ \AA}$  is observed at  $5896 \text{ \AA}$  ?  
a. 306 km/s      b. 322 km/s      c. 296 km/s      d. 336 km/s
- The length of a metal wire is  $l_1$ , when the tension in it is  $T_1$  and is  $l_2$  when the tension is  $T_2$ . The natural length of the wire is  
a.  $\sqrt{l_1 l_2}$       b.  $\frac{l_1 T_2 - l_2 T_1}{T_2 - T_1}$       c.  $\frac{l_1 T_2 + l_2 T_1}{T_2 + T_1}$       d.  $\frac{l_1 + l_2}{2}$
- In an electromagnetic wave, the electric field vector and magnetic field vector are given as  $\mathbf{E} = E_0 \hat{i}$  and  $\mathbf{B} = B_0 \hat{k}$ , respectively. The direction of propagation of electromagnetic wave is along  
a.  $\hat{k}$       b.  $\hat{j}$       c.  $(-\hat{k})$       d.  $(-\hat{j})$
- For a series  $L$ - $C$ - $R$  circuit with  $R = 100 \Omega$ ,  $L = 0.5 \text{ mH}$  and  $C = 0.1 \text{ pF}$  connected across 220 V-50 Hz AC supply, the phase angle between current and supplied voltage and the nature of the circuit is  
a.  $0^\circ$ , resistive circuit  
b.  $\approx 90^\circ$ , predominantly inductive circuit  
c.  $0^\circ$  resonance circuit  
d.  $\approx 90^\circ$ , predominantly capacitive circuit
- Which of the following graphs represent the behaviour of an ideal gas ? (Symbols have their usual meanings.)



- A particle is making simple harmonic motion along the X-axis. If at distances  $x_1$  and  $x_2$  from the mean position, the velocities of the particle are  $v_1$  and  $v_2$  respectively, then the time period of its oscillation is given as

a.  $T = 2\pi \sqrt{\frac{x_2^2 + x_1^2}{v_1^2 - v_2^2}}$       b.  $T = 2\pi \sqrt{\frac{x_2^2 + x_1^2}{v_1^2 + v_2^2}}$   
c.  $T = 2\pi \sqrt{\frac{x_2^2 - x_1^2}{v_1^2 + v_2^2}}$       d.  $T = 2\pi \sqrt{\frac{x_2^2 - x_1^2}{v_1^2 - v_2^2}}$

- An electron having de-Broglie wavelength  $\lambda$  is incident on a target in a X-ray tube. Cut-off wavelength of emitted X-ray is

a. Zero      b.  $\frac{2m^2 c^2 \lambda^2}{h^2}$       c.  $\frac{2mc \lambda^2}{h}$       d.  $\frac{hc}{mc}$

- A body rolls down an inclined plane without slipping. The kinetic energy of rotation is 50% of its translational kinetic energy. The body is

- a. solid sphere      b. solid cylinder  
c. hollow cylinder      d. ring

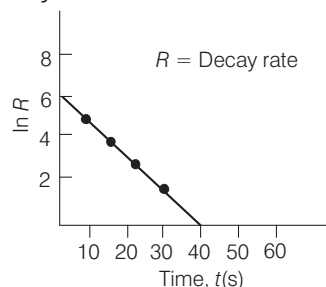
- If time ( $t$ ), velocity ( $v$ ) and angular momentum ( $l$ ) are taken as the fundamental units, then the dimension of mass ( $m$ ) in terms of  $t, v$  and  $l$  is

a.  $[t^{-1} v^1 l^{-2}]$       b.  $[t^1 v^2 l^{-1}]$   
c.  $[t^{-2} v^{-1} l^1]$       d.  $[t^{-1} v^{-2} l^1]$

- The correct relation between the degrees of freedom  $f$  and the ratio of specific heat  $\gamma$  is

a.  $f = \frac{2}{\gamma - 1}$       b.  $f = \frac{2}{\gamma + 1}$       c.  $f = \frac{\gamma + 1}{2}$       d.  $f = \frac{1}{\gamma + 1}$

- For a certain radioactive process, the graph between  $\ln R$  and  $t$  (sec) is obtained as shown in the figure. Then, the value of half-life for the unknown radioactive material is approximately



- a. 9.15 s      b. 6.93 s      c. 2.62 s      d. 4.62 s

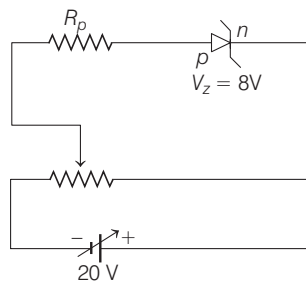
- Consider a binary star system of star A and star B with masses  $m_A$  and  $m_B$  revolving in a circular orbit of radii  $r_A$  and  $r_B$ , respectively. If  $T_A$  and  $T_B$  are the time period of star A and star B respectively, then

a.  $\frac{T_A}{T_B} = \left(\frac{r_A}{r_B}\right)^{\frac{3}{2}}$       b.  $T_A = T_B$   
c.  $T_A > T_B$  (if  $m_A > m_B$ )      d.  $T_A > T_B$  (if  $r_A > r_B$ )

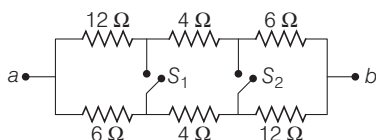
16. At an angle of  $30^\circ$  to the magnetic meridian, the apparent dip is  $45^\circ$ . Find the true dip.  
 a.  $\tan^{-1}(\sqrt{3})$     b.  $\tan^{-1}\left(\frac{1}{\sqrt{3}}\right)$     c.  $\tan^{-1}\left(\frac{2}{\sqrt{3}}\right)$     d.  $\tan^{-1}\left(\frac{\sqrt{3}}{2}\right)$
17. A body at rest is moved along a horizontal straight line by a machine delivering a constant power. The distance moved by the body in time  $t$  is proportional to  
 a.  $t^{\frac{3}{2}}$     b.  $t^{\frac{1}{2}}$     c.  $t^{\frac{1}{4}}$     d.  $t^{\frac{3}{4}}$
18. Two vectors  $\mathbf{P}$  and  $\mathbf{Q}$  have equal magnitudes. If the magnitude of  $\mathbf{P} + \mathbf{Q}$  is  $n$  times the magnitude of  $\mathbf{P} - \mathbf{Q}$ , then angle between  $\mathbf{P}$  and  $\mathbf{Q}$  is  
 a.  $\sin^{-1}\left(\frac{n-1}{n+1}\right)$     b.  $\cos^{-1}\left(\frac{n-1}{n+1}\right)$   
 c.  $\sin^{-1}\left(\frac{n^2-1}{n^2+1}\right)$     d.  $\cos^{-1}\left(\frac{n^2-1}{n^2+1}\right)$
19. Two small drops of mercury each of radius  $R$  coalesce to form a single large drop. The ratio of total surface energy before and after the change is  
 a.  $2^{1/3} : 1$     b.  $1 : 2^{1/3}$     c.  $2 : 1$     d.  $1 : 2$
20. The magnetic susceptibility of a material of a rod is 499. Permeability in vacuum is  $4\pi \times 10^{-7}$  H/m. Absolute permeability of the material of the rod is  
 a.  $4\pi \times 10^{-4}$  H/m    b.  $2\pi \times 10^{-4}$  H/m  
 c.  $3\pi \times 10^{-4}$  H/m    d.  $\pi \times 10^{-4}$  H/m

### Numerical Type Questions

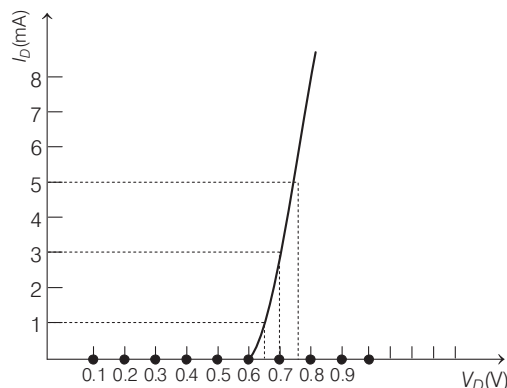
21. A Zener diode having Zener voltage 8 V and power dissipation rating of 0.5 W is connected across a potential divider arranged with maximum potential drop across Zener diode is as shown in the diagram. The value of protective resistance  $R_p$  is .....  $\Omega$ .



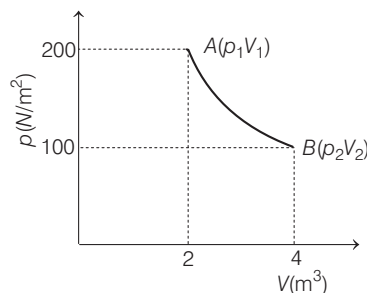
22. A body of mass  $m$  is launched up on a rough inclined plane making an angle of  $30^\circ$  with the horizontal. The coefficient of friction between the body and plane is  $\sqrt{x}/5$ . If the time of ascent is half of the time of descent. The value of  $x$  is ..... .
23. In the given figure, switches  $S_1$  and  $S_2$  are in open condition. The resistance across  $ab$  when the switches  $S_1$  and  $S_2$  are closed is .....  $\Omega$ .



24. Two bodies, a ring and a solid cylinder of same material are rolling down without slipping an inclined plane. The radii of the bodies are same. The ratio of velocity of the centre of mass at the bottom of the inclined plane of the ring to that of the cylinder is  $\sqrt{x}/2$ . Then, the value of  $x$  is ..... .
25. For the forward biased diode characteristics shown in the figure, the dynamic resistance at  $I_D = 3$  mA will be .....  $\Omega$ .



26. A series  $L$ - $C$ - $R$  circuit of  $R = 5\Omega$ ,  $L = 20$  mH and  $C = 0.5\mu\text{F}$  is connected across an AC supply of 250 V, having variable frequency. The power dissipated at resonance condition is .....  $\times 10^2$  W .
27. One mole of an ideal gas at  $27^\circ\text{C}$  is taken from A to B as shown in the given  $p$ - $V$  indicator diagram. The work done by the system will be .....  $\times 10^{-1}$  J .  
 [Take,  $R = 8.3$  J/mol-K,  $\ln 2 = 0.693$ ]  
 (Round off to the nearest integer)



28. A certain metallic surface is illuminated by monochromatic radiation of wavelength  $\lambda$ . The stopping potential for photoelectric current for this radiation is  $3V_0$ . If the same surface is illuminated with a radiation of wavelength  $2\lambda$ , the stopping potential is  $V_0$ . The threshold wavelength of this surface for photoelectric effect is .....  $\lambda$ .
29. A body rotating with an angular speed of 600 rpm is uniformly accelerated to 1800 rpm in 10 s. The number of rotations made in the process is ..... .
30. A radioactive substance decays to  $(1/16)$ th of its initial activity in 80 days. The half-life of the radioactive substance expressed in days is ..... .

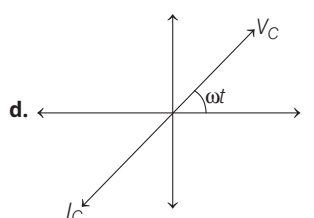
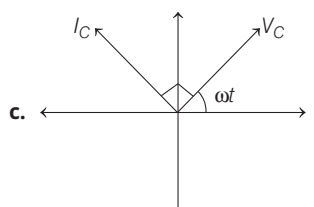
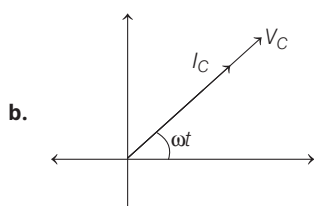
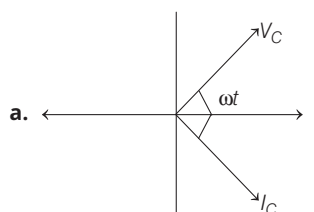
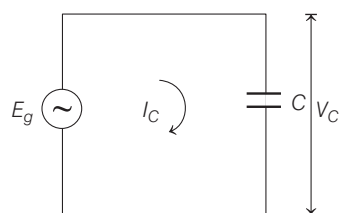
## Answers

1. (a)	2. (c)	3. (d)	4. (a)	5. (b)	6. (d)	7. (d)	8. (c)	9. (d)	10. (c)
11. (b)	12. (d)	13. (a)	14. (d)	15. (b)	16. (d)	17. (a)	18. (d)	19. (a)	20. (b)
21. (192)	22. (3)	23. (10)	24. (3)	25. (25)	26. (125)	27. (17258)	28. (4)	29. (32)	30. (20)

## 22 JULY SHIFT II

### Section A : Objective Type Questions

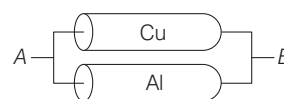
1. In a circuit consisting of a capacitance and a generator with alternating emf  $E_g = E_{g_0} \sin \omega t$ ,  $V_C$  and  $I_C$  are the voltage and current. Correct phasor diagram for such circuit is



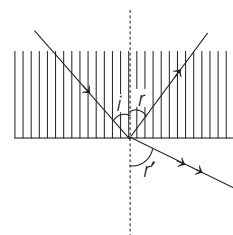
2. A copper (Cu) rod of length 25 cm and cross-sectional area  $3 \text{ mm}^2$  is joined with a similar aluminium (Al) rod as

shown in figure. Find the resistance of the combination between the ends A and B.

(Take, resistivity of copper =  $1.7 \times 10^{-8} \Omega\text{-m}$ , resistivity of aluminium =  $2.6 \times 10^{-8} \Omega\text{-m}$ )



- a. 2.170 m  $\Omega$                       b. 1.420 m  $\Omega$   
c. 0.0858 m  $\Omega$                       d. 0.858 m  $\Omega$
3. What will be the projection of vector  $\mathbf{A} = \hat{i} + \hat{j} + \hat{k}$  on vector  $\mathbf{B} = \hat{i} + \hat{j}$  ?  
a.  $\sqrt{2}(\hat{i} + \hat{j} + \hat{k})$                       b.  $2(\hat{i} + \hat{j} + \hat{k})$   
c.  $\sqrt{2}(\hat{i} + \hat{j})$                       d.  $(\hat{i} + \hat{j})$
4. A porter lifts a heavy suitcase of mass 80 kg and at the destination lowers it down by a distance of 80 cm with a constant velocity. Calculate the work done by the porter in lowering the suitcase.  
[Take,  $g = 9.8 \text{ ms}^{-2}$ ]  
a. -62720.0 J                      b. -6272 J  
c. +6272 J                      d. 784.0 J
5.  $T_0$  is the time period of a simple pendulum at a place. If the length of the pendulum is reduced to  $1/16$  times of its initial value, then the modified time period is  
a.  $T_0$                       b.  $8\pi T_0$                       c.  $4T_0$                       d.  $\frac{1}{4}T_0$
6. A ray of light passes from a denser medium to a rarer medium at an angle of incidence  $i$ . The reflected and refracted rays make an angle of  $90^\circ$  with each other. The angle of reflection and refraction are respectively  $r$  and  $r'$ . The critical angle is given by



- a.  $\sin^{-1}(\cot r)$     b.  $\tan^{-1}(\sin i)$     c.  $\sin^{-1}(\tan r')$     d.  $\sin^{-1}(\tan r)$
7. **Statement I** The ferromagnetic property depends on temperature. At high temperature, ferromagnet becomes paramagnet.



**Statement II** At high temperature, the domain wall area of a ferromagnetic substance increases.

In the light of the above statements, choose the most appropriate answer from the options given below.

- Statement I is true but Statement II is false
  - Both Statement I and Statement II are true
  - Both Statement I and Statement II are false
  - Statement I is false but Statement II is true
- 8.** A bullet of 4 g mass is fired from a gun of mass 4 kg. If the bullet moves with the muzzle speed of  $50 \text{ ms}^{-1}$ , the impulse imparted to the gun and velocity of recoil of gun are
- $0.4 \text{ kg}\cdot\text{ms}^{-1}$ ,  $0.1 \text{ ms}^{-1}$
  - $0.2 \text{ kg}\cdot\text{ms}^{-1}$ ,  $0.05 \text{ ms}^{-1}$
  - $0.2 \text{ kg}\cdot\text{ms}^{-1}$ ,  $0.1 \text{ ms}^{-1}$
  - $0.4 \text{ kg}\cdot\text{ms}^{-1}$ ,  $0.05 \text{ ms}^{-1}$
- 9.** Choose the correct option.
- True dip is not mathematically related to apparent dip.
  - True dip is less than apparent dip.
  - True dip is always greater than the apparent dip.
  - True dip is always equal to apparent dip.
- 10.** Consider a situation in which a ring, a solid cylinder and a solid sphere roll down on the same inclined plane without slipping. Assume that they start rolling from rest and having identical diameter.
- The correct statement for this situation.
- The sphere has the greatest and the ring has the least velocity of the centre of mass at the bottom of the inclined plane.
  - The ring has the greatest and the cylinder has the least velocity of the centre of mass at the bottom of the inclined plane.
  - All of them will have same velocity.
  - The cylinder has the greatest and the sphere has the least velocity of the centre of mass at the bottom of the inclined plane.
- 11.** Consider a situation in which reverse biased current of a particular  $p$ - $n$  junction increases when it is exposed to a light of wavelength  $\leq 621 \text{ nm}$ . During this process, enhancement in carrier concentration takes place due to generation of hole-electron pairs. The value of band gap is nearly
- 2 eV
  - 4 eV
  - 1 eV
  - 0.5 eV
- 12.** A nucleus with mass number 184 initially at rest emits an  $\alpha$ -particle. If the  $Q$ -value of the reaction is 5.5 MeV, calculate the kinetic energy of the  $\alpha$ -particle.
- 5.0 MeV
  - 5.5 MeV
  - 0.12 MeV
  - 5.38 MeV
- 13.** An electron of mass  $m_e$  and a proton of mass  $m_p$  are accelerated through the same potential difference. The ratio of the de-Broglie wavelength associated with the electron to that with the proton is
- $\frac{m_p}{m_e}$
  - 1
  - $\sqrt{\frac{m_p}{m_e}}$
  - $\frac{m_e}{m_p}$

**14.** Match List I with List II.

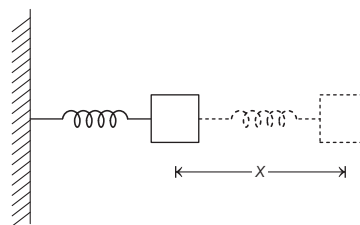
List I	List II
A. $\omega L > \frac{1}{\omega C}$	(i) Current is in phase with EMF
B. $\omega L = \frac{1}{\omega C}$	(ii) Current lags behind the applied EMF
C. $\omega L < \frac{1}{\omega C}$	(iii) Maximum current occurs
D. Resonant frequency	(iv) Current leads the EMF

Choose the correct answer from the options given below.

**Codes**

	A	B	C	D		A	B	C	D
a.	(ii)	(i)	(iv)	(iii)	b.	(ii)	(i)	(iii)	(iv)
c.	(iii)	(i)	(iv)	(ii)	d.	(iv)	(iii)	(ii)	(i)

- 15.** What should be the height of transmitting antenna and the population covered, if the television telecast is to cover a radius of 150 km? The average population density around the tower is  $2000/\text{km}^2$  and the value of  $R_e = 6.5 \times 10^6 \text{ m}$ .
- Height = 1731 m, Population covered =  $1413 \times 10^5$
  - Height = 1241 m, Population covered =  $7 \times 10^5$
  - Height = 1600 m, Population covered =  $2 \times 10^5$
  - Height = 1800 m, Population covered =  $1413 \times 10^8$
- 16.** What will be the average value of energy for a monoatomic gas in thermal equilibrium at temperature  $T$ ?
- $\frac{2}{3} K_B T$
  - $K_B T$
  - $\frac{3}{2} K_B T$
  - $\frac{1}{2} K_B T$
- 17.** Intensity of sunlight is observed as  $0.092 \text{ Wm}^{-2}$  at a point in free space. What will be the peak value of magnetic field at that point? ( $\epsilon_0 = 8.85 \times 10^{-12} \text{ C}^{-2} \text{N}^{-1} \text{m}^{-2}$ )
- $2.77 \times 10^{-8} \text{ T}$
  - $1.96 \times 10^{-8} \text{ T}$
  - 8.31 T
  - 5.88 T
- 18.** The motion of a mass on a spring, with spring constant  $k$  is as shown in figure.



The equation of motion is given by

$$x(t) = A \sin \omega t + B \cos \omega t \text{ with } \omega = \sqrt{\frac{k}{m}}$$

Suppose that at time  $t = 0$ , the position of mass is  $x(0)$  and velocity  $v(0)$ , then its displacement can also be represented as  $x(t) = C \cos(\omega t - \phi)$ , where  $C$  and  $\phi$  are

- $C = \sqrt{\frac{2v(0)^2}{\omega^2} + x(0)^2}$ ,  $\phi = \tan^{-1}\left(\frac{v(0)}{x(0)\omega}\right)$
- $C = \sqrt{\frac{2v(0)^2}{\omega^2} + x(0)^2}$ ,  $\phi = \tan^{-1}\left(\frac{x(0)\omega}{2v(0)}\right)$

$$c. C = \sqrt{\frac{v(0)^2}{\omega^2} + x(0)^2}, \phi = \tan^{-1}\left(\frac{x(0)\omega}{v(0)}\right)$$

$$d. C = \sqrt{\frac{v(0)^2}{\omega^2} + x(0)^2}, \phi = \tan^{-1}\left(\frac{v(0)}{x(0)\omega}\right)$$

19. An electric dipole is placed on  $X$ -axis in proximity to a line charge of linear charge density  $3.0 \times 10^{-6}$  C/m. Line charge is placed on  $Z$ -axis and positive and negative charge of dipole is at a distance of 10 mm and 12 mm from the origin, respectively. If total force of 4 N is exerted on the dipole, find out the amount of positive or negative charge of the dipole.

a. 815.1 nC    b.  $8.8 \mu\text{C}$     c. 0.485 nC    d.  $4.44 \mu\text{C}$

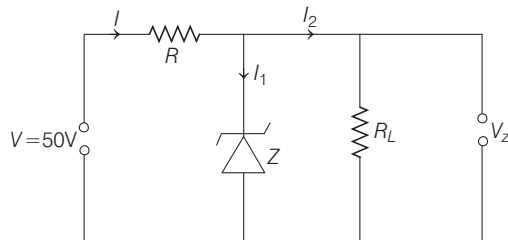
20. A body is projected vertically upwards from the surface of Earth with a velocity sufficient enough to carry it to infinity. The time taken by it to reach height  $h$  is ..... s.

$$a. \sqrt{\frac{R_e}{2g}} \left[ \left( 1 + \frac{h}{R_e} \right)^{3/2} - 1 \right] \quad b. \sqrt{\frac{2R_e}{g}} \left[ \left( 1 + \frac{h}{R_e} \right)^{3/2} - 1 \right]$$

$$c. \frac{1}{3} \sqrt{\frac{R_e}{2g}} \left[ \left( 1 + \frac{h}{R_e} \right)^{3/2} - 1 \right] \quad d. \frac{1}{3} \sqrt{\frac{2R_e}{g}} \left[ \left( 1 + \frac{h}{R_e} \right)^{3/2} - 1 \right]$$

## Section B : Numerical Type Questions

21. In a given circuit diagram, a 5 V Zener diode along with a series resistance is connected across a 50 V power supply. The minimum value of the resistance required, if the maximum Zener current is 90 mA will be .....  $\Omega$ .



22. The position of the centre of mass of a uniform semi-circular wire of radius  $R$  placed in  $XY$ -plane with its centre at the origin and the line joining its ends as  $X$ -axis is given by  $(0, xR/\pi)$ . Then, the value of  $|x|$  is ..... .
23. In an electric circuit, a cell of certain EMF provides a potential difference of 1.25 V across a load resistance of  $5 \Omega$ . However, it provides a potential difference of 1 V across a load resistance of  $2 \Omega$ . The emf of the cell is given by  $\frac{x}{10}$  V. Then, the value of  $x$  is ..... .

24. The total charge enclosed in an incremental volume of  $2 \times 10^{-9} \text{ m}^3$  located at the origin is ..... nC, if electric flux density of its field is found as  $D = e^{-x} \sin y \hat{i} - e^{-x} \cos y \hat{j} + 2z \hat{k}$  C/m<sup>2</sup>.

25. Three particles  $P$ ,  $Q$  and  $R$  are moving along the vectors  $\mathbf{A} = \hat{i} + \hat{j}$ ,  $\mathbf{B} = \hat{j} + \hat{k}$  and  $\mathbf{C} = -\hat{i} + \hat{j}$ , respectively. They strike on a point and start to move in different directions. Now, particle  $P$  is moving normal to the plane which contain vectors  $\mathbf{A}$  and  $\mathbf{B}$ . Similarly, particle  $Q$  is moving normal to the plane which contain vectors  $\mathbf{A}$  and  $\mathbf{C}$ . The angle between the direction of motion of  $P$  and  $Q$  is  $\cos^{-1}\left(\frac{1}{\sqrt{x}}\right)$ . Then, the value of  $x$  is ..... .

26. The centre of a wheel rolling on a plane surface moves with a speed  $v_0$ . A particle on the rim of the wheel at the same level as the centre will be moving at a speed  $\sqrt{x}v_0$ . Then, the value of  $x$  is ..... .

27. A ray of light passing through a prism ( $\mu = \sqrt{3}$ ) suffers minimum deviation. It is found that the angle of incidence is double the angle of refraction within the prism. Then, the angle of prism is ..... (in degrees).

28. The area of cross-section of a railway track is  $0.01 \text{ m}^2$ . The temperature variation is  $10^\circ\text{C}$ . Coefficient of linear expansion of material of track is  $10^{-5}/^\circ\text{C}$ . The energy stored per metre in the track is ..... J/m.

(Take, Young's modulus of material of track is  $10^{11} \text{ Nm}^{-2}$ )

29. Three students  $S_1$ ,  $S_2$  and  $S_3$  perform an experiment for determining the acceleration due to gravity ( $g$ ) using a simple pendulum. They use different lengths of pendulum and record time for different number of oscillations. The observations are as shown in the table.

Student No.	Length of pendulum (cm)	No. of oscillations ( $n$ )	Total time for $n$ oscillations	Time period (s)
1.	64.0	8	128.0	16.0
2.	64.0	4	64.0	16.0
3.	20.0	4	36.0	9.0

(Least count of length = 0.1m, least count for time = 0.1s)

If  $E_1$ ,  $E_2$  and  $E_3$  are the percentage errors in  $g$  for students 1, 2 and 3 respectively, then the minimum percentage error is obtained by student number ..... .

30. In 5 min, a body cools from  $75^\circ\text{C}$  to  $65^\circ\text{C}$  at room temperature of  $25^\circ\text{C}$ . The temperature of body at the end of next 5 min is .....  $^\circ\text{C}$ .

## Answers

1. (c)    2. (d)    3. (d)    4. (b)    5. (d)    6. (d)    7. (a)    8. (b)    9. (b)    10. (a)  
 11. (a)    12. (d)    13. (c)    14. (a)    15. (a)    16. (c)    17. (a)    18. (d)    19. (d)    20. (d)  
 21. (500)    22. (2)    23. (15)    24. (4)    25. (9)    26. (4)    27. (60)    28. (5)    29. (1)    30. (57)

## 25 JULY SHIFT I

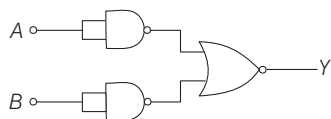
### Section A : Objective Type Questions

1. For a gas  $C_p - C_v = R$  in a state  $P$  and  $C_p - C_v = 1.10 R$  in a state  $Q$ .  $T_P$  and  $T_Q$  are the temperatures in two different states  $P$  and  $Q$ , respectively. Then,
  - a.  $T_P = T_Q$
  - b.  $T_P < T_Q$
  - c.  $T_P = 0.9T_Q$
  - d.  $T_P > T_Q$
2. **Assertion A** Moment of inertia of a circular disc of mass  $M$  and radius  $R$  about  $X$ ,  $Y$ -axes (passing through its plane) and  $Z$ -axis which is perpendicular to its plane were found to be  $I_x$ ,  $I_y$  and  $I_z$ , respectively. The respective radii of gyration about all the three axes will be the same.

**Reason R** A rigid body making rotational motion has fixed mass and shape.



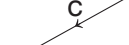
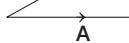
In the light of the above statements, choose the most appropriate answer from the options given below.

  - a. Both A and R are correct and R is the correct explanation of A.
  - b. Both A and R are correct but R is not the correct explanation of A.
  - c. A is correct but R is not correct.
  - d. A is not correct but R is correct.
3. What should be the order of arrangement of de-Broglie wavelength of electron ( $\lambda_e$ ), an  $\alpha$ -particle ( $\lambda_\alpha$ ) and proton ( $\lambda_p$ ) given that all have the same kinetic energy ?
  - a.  $\lambda_e = \lambda_p = \lambda_\alpha$
  - b.  $\lambda_e < \lambda_p < \lambda_\alpha$
  - c.  $\lambda_e > \lambda_p > \lambda_\alpha$
  - d.  $\lambda_e = \lambda_p > \lambda_\alpha$
4. Identify the logic operation carried out.



- a. OR  
c. NOR
- b. AND  
d. NAND
5. A particle of mass  $4M$  at rest disintegrates into two particles of masses  $M$  and  $3M$  respectively having non-zero velocities. The ratio of de-Broglie wavelength of particle of mass  $M$  to that of mass  $3M$  will be
- a. 1 : 3  
c.  $1 : \sqrt{3}$
- b. 3 : 1  
d. 1 : 1
6. Some nuclei of a radioactive material are undergoing radioactive decay. The time gap between the instances when a quarter of the nuclei have decayed and when half of the nuclei have decayed is given as (where,  $\lambda$  is the decay constant)
- a.  $\frac{1 \ln 2}{2 \lambda}$   
c.  $\frac{2 \ln 2}{\lambda}$
- b.  $\frac{\ln 2}{\lambda}$   
d.  $\frac{\ln 3}{2 \lambda}$

- 7.** Match List I with List II.

List I	List II
(A) $\mathbf{C} - \mathbf{A} - \mathbf{B} = 0$	(i) 
(B) $\mathbf{A} - \mathbf{C} - \mathbf{B} = 0$	(ii) 
(C) $\mathbf{B} - \mathbf{A} - \mathbf{C} = 0$	(iii) 
(D) $\mathbf{A} + \mathbf{B} = -\mathbf{C}$	(iv) 

Choose the correct answer from the options given below.

- a. (A)  $\rightarrow$  (iv), (B)  $\rightarrow$  (i), (C)  $\rightarrow$  (iii), (D)  $\rightarrow$  (ii)  
b. (A)  $\rightarrow$  (iv), (B)  $\rightarrow$  (iii), (C)  $\rightarrow$  (i), (D)  $\rightarrow$  (ii)  
c. (A)  $\rightarrow$  (iii), (B)  $\rightarrow$  (ii), (C)  $\rightarrow$  (iv), (D)  $\rightarrow$  (i)  
d. (A)  $\rightarrow$  (i), (B)  $\rightarrow$  (iv), (C)  $\rightarrow$  (ii), (D)  $\rightarrow$  (iii)
8. A parallel plate capacitor with plate area  $A$  and distance of separation  $d$  is filled with a dielectric. What is the capacity of the capacitor when permittivity of the dielectric varies as
- $\epsilon(x) = \epsilon_0 + kx$ , for  $\left(0 < x \leq \frac{d}{2}\right)$   
 $\epsilon(x) = \epsilon_0 + k(d - x)$ , for  $\left(\frac{d}{2} \leq x \leq d\right)$
- a.  $\left(\epsilon_0 + \frac{kd}{2}\right)^{2/kA}$   
b.  $\frac{kA}{2 \ln\left(\frac{2\epsilon_0 + kd}{2\epsilon_0}\right)}$   
c. zero  
d.  $\frac{kA}{2} \ln\left(\frac{2\epsilon_0}{2\epsilon_0 - kd}\right)$
9. A monoatomic ideal gas, initially at temperature  $T_1$  is enclosed in a cylinder fitted with a frictionless piston. The gas is allowed to expand adiabatically to a temperature  $T_2$  by releasing the piston suddenly. If  $l_1$  and  $l_2$  are the lengths of the gas column, before and after the expansion respectively, then the value of  $\frac{T_1}{T_2}$  will be
- a.  $\left(\frac{l_1}{l_2}\right)^{\frac{2}{3}}$   
b.  $\left(\frac{l_2}{l_1}\right)^{\frac{2}{3}}$   
c.  $\frac{l_2}{l_1}$   
d.  $\frac{l_1}{l_2}$
10. A ray of laser of a wavelength 630 nm is incident at an angle of  $30^\circ$  at the diamond-air interface. It is going from diamond to air. The refractive index of diamond is 2.42 and that of air is 1. Choose the correct option.
- a. Angle of refraction is  $24.41^\circ$   
b. Angle of refraction is  $30^\circ$   
c. Refraction is not possible  
d. Angle of refraction is  $53.4^\circ$

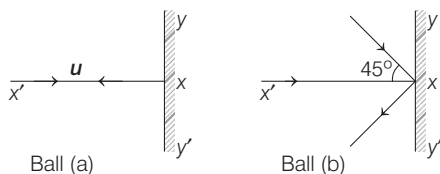
11. Two wires of same length and radius are joined end-to-end and loaded. The Young's moduli of the materials of the two wires are  $Y_1$  and  $Y_2$ . The combination behaves as a single wire, then its Young's modulus is

a.  $Y = \frac{2Y_1Y_2}{3(Y_1 + Y_2)}$       b.  $Y = \frac{2Y_1Y_2}{Y_1 + Y_2}$   
 c.  $Y = \frac{Y_1Y_2}{2(Y_1 + Y_2)}$       d.  $Y = \frac{Y_1Y_2}{Y_1 + Y_2}$

12. The half-life of  $^{198}\text{Au}$  is 3 days. If atomic weight of  $^{198}\text{Au}$  is 198 g/mol, then the activity of 2 mg of  $^{198}\text{Au}$  is [in disintegration/s]

a.  $2.67 \times 10^{12}$       b.  $6.06 \times 10^{18}$   
 c.  $32.36 \times 10^{12}$       d.  $16.18 \times 10^{12}$

13. Two billiard balls of equal mass 30 g strike a rigid wall with same speed of 108 km/h (as shown) but at different angles. If the balls get reflected with the same speed, then the ratio of the magnitude of impulses imparted to ball  $a$  and ball  $b$  by the wall along,  $x$ , direction is

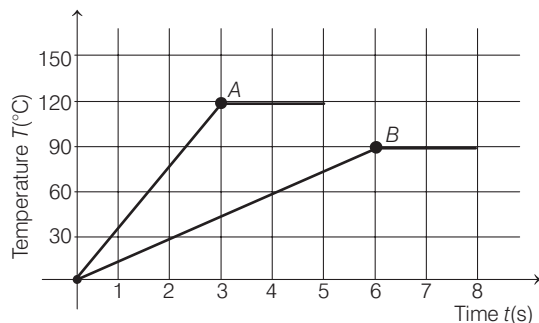


a. 1 : 1      b.  $\sqrt{2} : 1$   
 c. 2 : 1      d.  $1 : \sqrt{2}$

14. In the Young's double slit experiment, the distance between the slits varies in time as  $d(t) = d_0 + a_0 \sin \omega t$ , where  $d_0$ ,  $\omega$  and  $a_0$  are constants. The difference between the largest fringe width and the smallest fringe width obtained over time is given as

a.  $\frac{2\lambda D(d_0)}{(d_0^2 - a_0^2)}$       b.  $\frac{2\lambda D a_0}{(d_0^2 - a_0^2)}$   
 c.  $\frac{\lambda D}{d_0^2} a_0$       d.  $\frac{\lambda D}{d_0 + a_0}$

15. Two different metal bodies  $A$  and  $B$  of equal mass are heated at a uniform rate under similar conditions. The variation of temperature of the bodies is graphically represented as shown in the figure. The ratio of specific heat capacities is



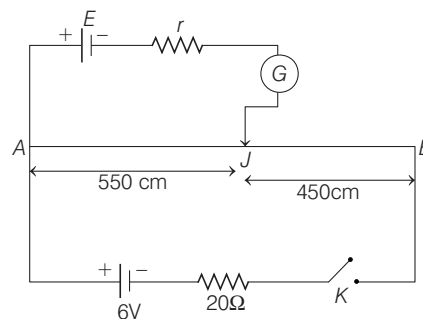
a.  $\frac{8}{3}$       b.  $\frac{3}{8}$       c.  $\frac{3}{4}$       d.  $\frac{4}{3}$

16. A linearly polarised electromagnetic wave in vacuum is  $E = 3.1 \cos[(1.8)z - (5.4 \times 10^6)t] \hat{i}$  N/C is incident normally on a perfectly reflecting wall at  $z = a$ .

Choose the correct option.

- a. The wavelength is 5.4 m  
 b. The frequency of electromagnetic wave is  $54 \times 10^4$  Hz.  
 c. The transmitted wave will be  $3.1 \cos[(1.8)z - (5.4 \times 10^6)t] \hat{i}$  N/C  
 d. The reflected wave will be  $3.1 \cos[(1.8)z + (5.4 \times 10^6)t] \hat{i}$  N/C

17. In the given figure, there is a circuit of potentiometer of length  $AB = 10$  m. The resistance per unit length is  $0.1 \Omega$  per cm. Across  $AB$ , a battery of EMF  $E$  and internal resistance  $r$  is connected. The maximum value of emf measured by this potentiometer is



- a. 5 V      b. 2.25 V      c. 6 V      d. 2.75 V

18. In amplitude modulation, the message signal

$$V_m(t) = 10 \sin(2\pi \times 10^5 t) \text{ volts}$$

and carrier signal

$$V_c(t) = 20 \sin(2\pi \times 10^7 t) \text{ volts}$$

The modulated signal now contains the message signal with lower side band and upper side band frequency.

Therefore, the bandwidth of modulated signal is  $\alpha$  kHz. The value of  $\alpha$  is

- a. 200 kHz      b. 50 kHz  
 c. 100 kHz      d. zero

19. Water droplets are coming from an open tap at a particular rate. The spacing between a droplet observed at 4th second after its fall to the next droplet is 34.3 m. At what rate, the droplets are coming from the tap? (Take,  $g = 9.8 \text{ m/s}^2$ )

- a. 3 drops / 2 s      b. 2 drops / s  
 c. 1 drop / s      d. 1 drop / 7 s

20. The minimum and maximum distances of a planet revolving around the Sun are  $x_1$  and  $x_2$ . If the minimum speed of the planet on its trajectory is  $v_0$ , then its maximum speed will be

a.  $\frac{v_0 x_1^2}{x_2^2}$       b.  $\frac{v_0 x_2^2}{x_1^2}$       c.  $\frac{v_0 x_1}{x_2}$       d.  $\frac{v_0 x_2}{x_1}$

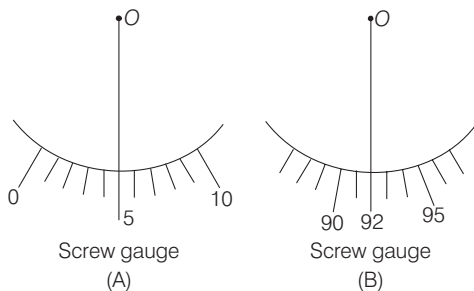
## Section B : Numerical Type Questions

21. A body of mass 2 kg moving with a speed of 4 m/s makes an elastic collision with another body at rest and continues to move in the original direction but with one-fourth of its initial speed. The speed of the two body centre of mass is  $\frac{x}{10}$  m/s. Then, the value of  $x$  is .....

22. Student A and student B used two screw gauges of equal pitch and 100 equal circular divisions to measure the radius of a given wire. The actual value of the radius of the wire is 0.322 cm. The absolute value of the difference between the final circular scale readings observed by the students A and B is .....

[Figure shows position of reference O when jaws of screw gauge are closed]

Given, pitch = 0.1 cm.



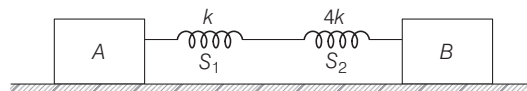
23. An inductor of 10 mH is connected to a 20 V battery through a resistor of 10 k $\Omega$  and a switch. After a long time, when maximum current is set up in the circuit, the current is switched off. The current in the circuit after 1  $\mu$ s is  $\frac{x}{100}$  mA. Then, x is equal to ..... (Take,  $e^{-1} = 0.37$ )
24. A circular conducting coil of radius 1 m is being heated by the change of magnetic field **B** passing perpendicular to the plane in which the coil is laid. The resistance of the coil is 2  $\mu\Omega$ . The magnetic field is slowly switched off such that its magnitude changes in time as

$$B = \frac{4}{\pi} \times 10^{-3} \left( 1 - \frac{t}{100} \right) \text{ T}$$

The energy dissipated by the coil before the magnetic field is switched off completely is  $E = \dots$  mJ.

25. In the reported figure, two bodies A and B of masses 200 g and 800 g are attached with the system of springs.

Springs are kept in a stretched position with some extension when the system is released. The horizontal surface is assumed to be frictionless. The angular frequency will be ..... rad/s when  $k = 20 \text{ N/m}$ .



26. The value of aluminium susceptibility is  $2.2 \times 10^{-5}$ . The percentage increase in the magnetic field, if space within a current carrying toroid is filled with aluminium is  $\frac{x}{10^4}$ , then the value of x is .....
27. A particle of mass 1 mg and charge  $q$  is lying at the mid-point of two stationary particles kept at a distance 2 m when each is carrying same charge  $q$ . If the free charged particle is displaced from its equilibrium position through distance  $x$  ( $x \ll 1 \text{ m}$ ), the particle executes SHM. Its angular frequency of oscillation will be .....  $\times 10^5 \text{ rad/s}$ , if  $q^2 = 10 \text{ C}^2$ .
28. An electric bulb rated as 200 W at 100 V is used in a circuit having 200 V supply. The resistance  $R$  that must be put in series with the bulb, so that the bulb delivers the same power is .....  $\Omega$ .
29. A pendulum bob has a speed of 3 m/s at its lowest position. The pendulum is 50 cm long. The speed of bob when the length makes an angle of  $60^\circ$  to the vertical will be ..... m/s. (Take,  $g = 10 \text{ m/s}^2$ )
30. A particle of mass  $m$  is moving in time  $t$  on a trajectory given by

$$\mathbf{r} = 10\alpha t^2 \hat{i} + 5\beta(t - 5) \hat{j}$$

where,  $\alpha$  and  $\beta$  are dimensional constants. The angular momentum of the particle becomes the same as it was for  $t = 0$  at time  $t$  is ..... s.

## Answers

- |          |          |          |          |          |          |            |          |         |          |
|----------|----------|----------|----------|----------|----------|------------|----------|---------|----------|
| 1. (d)   | 2. (d)   | 3. (c)   | 4. (b)   | 5. (d)   | 6. (d)   | 7. (b)     | 8. (b)   | 9. (b)  | 10. (c)  |
| 11. (b)  | 12. (d)  | 13. (b)  | 14. (b)  | 15. (b)  | 16. (d)  | 17. (a)    | 18. (a)  | 19. (c) | 20. (d)  |
| 21. (25) | 22. (13) | 23. (74) | 24. (80) | 25. (10) | 26. (22) | 27. (6000) | 28. (50) | 29. (2) | 30. (10) |

## 25 JULY SHIFT II

### Section A : Objective Type Questions

1. The relation between time  $t$  and distance  $x$  for a moving body is given as  $t = mx^2 + nx$ , where  $m$  and  $n$  are constants. The retardation of the motion is (when  $v$  stands for velocity)
- a.  $2mv^3$       b.  $2mnv^3$       c.  $2nv^3$       d.  $2n^2v^3$
2. In a simple harmonic oscillation, what fraction of total mechanical energy is in the form of kinetic energy, when the particle is midway between mean and extreme position.
- a.  $1/2$       b.  $3/4$   
c.  $1/3$       d.  $1/4$

3. A force  $\mathbf{F} = (40\hat{i} + 10\hat{j})$  N acts on a body of mass 5 kg. If the body starts from rest its position vector  $\mathbf{r}$  at time  $t = 10$  s, will be

a.  $(100\hat{i} + 400\hat{j})$  m                      b.  $(100\hat{i} + 100\hat{j})$  m  
c.  $(400\hat{i} + 100\hat{j})$  m                      d.  $(400\hat{i} + 400\hat{j})$  m

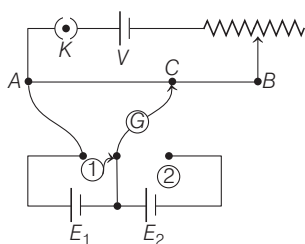
4. A prism of refractive index  $\mu$  and angle of prism  $A$  is placed in the position of minimum angle of deviation. If minimum angle of deviation is also  $A$ , then in terms of refractive index,

a.  $2\cos^{-1}\left(\frac{\mu}{2}\right)$                       b.  $\sin^{-1}\left(\frac{\mu}{2}\right)$   
c.  $\sin^{-1}\left(\sqrt{\frac{\mu-1}{2}}\right)$                       d.  $\cos^{-1}\left(\frac{\mu}{2}\right)$

5. A heat engine has an efficiency of  $1/6$ . When the temperature of sink is reduced by  $62^\circ\text{C}$ , its efficiency get doubled. The temperature of the source is

a.  $124^\circ\text{C}$                       b.  $37^\circ\text{C}$   
c.  $62^\circ\text{C}$                       d.  $99^\circ\text{C}$

6. In the given potentiometer circuit arrangement, the balancing length  $AC$  is measured to be 250 cm. When the galvanometer connection is shifted from point (1) to point (2) in the given diagram, the balancing length becomes 400 cm. The ratio of the EMF of two cells,  $\frac{E_1}{E_2}$  is



a.  $5/3$                       b.  $8/5$   
c.  $4/3$                       d.  $3/2$

7. Two ions having same mass have charges in the ratio 1 : 2. They are projected normally in a uniform magnetic field with their speeds in the ratio 2 : 3. The ratio of the radii of their circular trajectories is

a. 1 : 4                      b. 4 : 3  
c. 3 : 1                      d. 2 : 3

8. A  $10\ \Omega$  resistance is connected across 220 V - 50Hz AC supply. The time taken by the current to change from its maximum value to the rms value is

a. 2.5 ms                      b. 1.5 ms  
c. 3.0 ms                      d. 4.5 ms

9. A balloon was moving upwards with a uniform velocity of 10 m/s. An object of finite mass is dropped from the balloon when it was at a height of 75 m from the ground level. The height of the balloon from the ground when object strikes the ground was around, is (Take, the value of  $g = 10\ \text{m/s}^2$ )

a. 300 m                      b. 200 m  
c. 125 m                      d. 250 m

10. If  $q_f$  is the free charge on the capacitor plates and  $q_b$  is the bound charge on the dielectric slab of dielectric constant  $K$  placed between the capacitor plates, then bound charge  $q_b$  can be expressed as

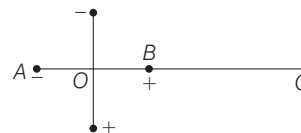
a.  $q_b = q_f\left(1 - \frac{1}{\sqrt{K}}\right)$                       b.  $q_b = q_f\left(1 - \frac{1}{K}\right)$   
c.  $q_b = q_f\left(1 + \frac{1}{\sqrt{K}}\right)$                       d.  $q_b = q_f\left(1 + \frac{1}{K}\right)$

11. Consider a planet in some solar system which has a mass double the mass of Earth and density equal to the average density of Earth. If the weight of an object on Earth is  $w$ , the weight of the same object on that planet will be

a.  $2w$                       b.  $w$                       c.  $2^{1/3}w$                       d.  $\sqrt{2}w$

12. Two ideal electric dipoles  $A$  and  $B$ , having their dipole moment  $p_1$  and  $p_2$  respectively, are placed on a plane with their centres at  $O$  as shown in the figure. At point  $C$  on the axis of dipole  $A$ , the resultant electric field is making an angle of  $37^\circ$  with the axis. The ratio of the dipole moment of  $A$  and  $B$ ,  $\frac{p_1}{p_2}$  is

(Take,  $\sin 37^\circ = \frac{3}{5}$ )



a.  $\frac{3}{8}$                       b.  $\frac{3}{2}$                       c.  $\frac{2}{3}$                       d.  $\frac{4}{3}$

13. Two spherical soap bubbles of radii  $r_1$  and  $r_2$  in vacuum combine under isothermal conditions. The resulting bubble has a radius equal to

a.  $\frac{r_1 r_2}{r_1 + r_2}$                       b.  $\sqrt{r_1 r_2}$                       c.  $\sqrt{r_1^2 + r_2^2}$                       d.  $\frac{r_1 + r_2}{2}$

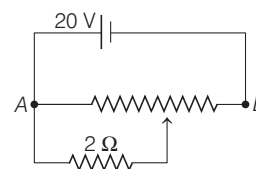
14. The force is given in terms of time  $t$  and displacement  $x$  by the equation

$$F = A \cos Bx + C \sin Dt$$

The dimensional formula of  $\frac{AD}{B}$  is

a.  $[M^0 L T^{-1}]$                       b.  $[M L^2 T^{-3}]$                       c.  $[M^1 L^1 T^{-2}]$                       d.  $[M^2 L^2 T^{-3}]$

15. The given potentiometer has its wire of resistance  $10\ \Omega$ . When the sliding contact is in the middle of the potentiometer wire, the potential drop across  $2\ \Omega$  resistor is



a. 10 V                      b. 5 V  
c.  $\frac{40}{9}$  V                      d.  $\frac{40}{11}$  V



- 28.** A solid disc of radius 20 cm and mass 10 kg is rotating with an angular velocity of 600 rpm, about an axis normal to its circular plane and passing through its centre of mass. The retarding torque required to bring the disc at rest in 10 s is  $\pi \times 10^{-1}$  N-m.

29. In a semiconductor, the number density of intrinsic charge carriers at  $27^\circ\text{C}$  is  $1.5 \times 10^{16}/\text{m}^3$ . If the semiconductor is doped with impurity atom, the hole density increases to  $4.5 \times 10^{22}/\text{m}^3$ . The electron density in the doped semiconductor is .....  $\times 10^9/\text{m}^3$ .

30. The nuclear activity of a radioactive element becomes  $(1/8)$ th of its initial value in 30 yr. The half-life of radioactive element is yr.

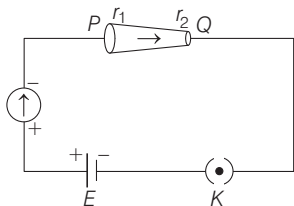
## Answers

1. (a) 2. (b) 3. (c) 4. (a) 5. (d) 6. (a) 7. (b) 8. (a) 9. (c) 10. (b)  
11. (c) 12. (c) 13. (c) 14. (b) 15. (c) 16. (c) 17. (b) 18. (a) 19. (b) 20. (b)  
21. (25) 22. (125) 23. (1) 24. (45) 25. (500) 26. (27.16) 27. (450) 28. (4) 29. (5) 30. (10)

## 27 JULY SHIFT I

### Section A : Objective Type Questions

1. In the given figure, a battery of emf  $E$  is connected across a conductor  $PQ$  of length  $l$  and different area of cross-sections having radii  $r_1$  and  $r_2$  ( $r_2 < r_1$ ).



Choose the correct option as one moves from  $P$  to  $Q$ .

- a. Drift velocity of electron increases  
b. Electric field decreases  
c. Electron current decreases  
d. All of the above
2. The number of molecules in 1 L of an ideal gas at 300 K and 2 atm pressure with mean kinetic energy  $2 \times 10^{-9}$  J per molecules is  
a.  $0.75 \times 10^{11}$  b.  $3 \times 10^{11}$   
c.  $15 \times 10^{11}$  d.  $6 \times 10^{11}$
3. The relative permittivity of distilled water is 81. The velocity of light in it will be (Take,  $\mu_r = 1$ )  
a.  $4.33 \times 10^7$  m/s b.  $2.33 \times 10^7$  m/s  
c.  $3.33 \times 10^7$  m/s d.  $5.33 \times 10^7$  m/s
- 4.

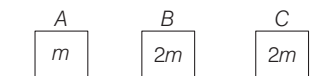
List I		List II	
A.	Moment of inertia of the rod (length $L$ , mass $M$ , about an axis perpendicular to the rod passing through the mid-point)	I.	$\frac{8ML^2}{3}$
B.	Moment of inertia of the rod (length $L$ , mass $2M$ , about an axis perpendicular to the rod passing through one of its end)	II.	$\frac{ML^2}{3}$

List I		List II	
C.	Moment of inertia of the rod (length $2L$ , mass $M$ , about an axis perpendicular to the rod passing through its midpoint)	III.	$\frac{ML^2}{12}$
D.	Moment of inertia of the rod (length $2L$ , mass $2M$ , about an axis perpendicular to the rod passing through one of its end)	IV.	$\frac{2ML^2}{3}$

Choose the correct answer from the options given below.

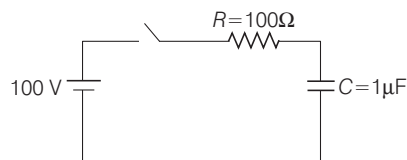
- A B C D A B C D  
a. (II) (III) (I) (IV) b. (II) (I) (III) (IV)  
c. (III) (IV) (II) (I) d. (III) (IV) (I) (II)

5. Three objects  $A$ ,  $B$  and  $C$  are kept in a straight line on a frictionless horizontal surface. The masses of  $A$ ,  $B$  and  $C$  are  $m$ ,  $2m$  and  $2m$ , respectively.  $A$  moves towards  $B$  with a speed of 9 m/s and makes an elastic collision with it. There after  $B$  makes a completely inelastic collision with  $C$ . All motions occur along same straight line. The final speed of  $C$  is



- a. 6 m/s b. 9 m/s c. 4 m/s d. 3 m/s

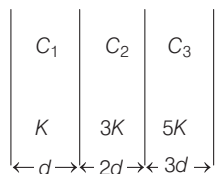
6. A capacitor of capacitance  $C = 1\mu\text{F}$  is suddenly connected to a battery of 100 V through a resistance  $R = 100\Omega$ . The time taken for the capacitor to be charged to get 50 V is



[Take,  $\ln 2 = 0.69$ ]

- a.  $1.44 \times 10^{-4}$  s b.  $3.33 \times 10^{-4}$  s  
c.  $0.69 \times 10^{-4}$  s d.  $0.30 \times 10^{-4}$  s

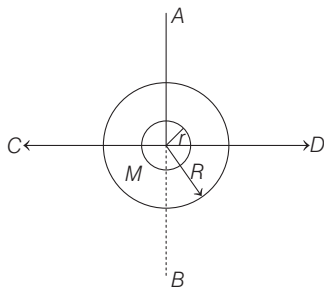
7. In the reported figure, a capacitor is formed by placing a compound dielectric between the plates of parallel plate capacitor. The expression for the capacity of the said capacitor will be (Take, area of plate =  $A$ )



- a.  $\frac{15 K \epsilon_0 A}{34 d}$     b.  $\frac{15 K \epsilon_0 A}{6 d}$     c.  $\frac{25 K \epsilon_0 A}{6 d}$     d.  $\frac{9 K \epsilon_0 A}{6 d}$

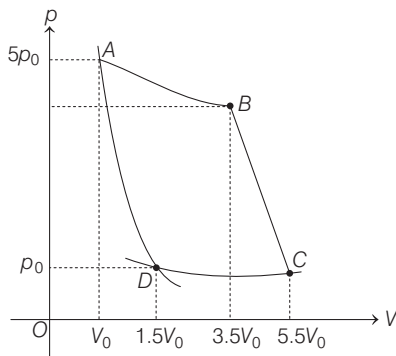
8. The figure shows two solid discs with radius  $R$  and  $r$ , respectively. If mass per unit area is same for both, what is the ratio of MI of bigger disc around axis  $AB$  (which is perpendicular to the plane of the disc and passing through its centre) of MI of smaller disc around one of its diameters lying on its plane?

Given,  $M$  is the mass of the larger disc. (MI stands for moment of inertia)



- a.  $R^2 : r^2$     b.  $2R^4 : r^4$     c.  $2R^2 : r^2$     d.  $2R^4 : r^4$

9. In Young's double slit experiment, if the source of light changes from orange to blue, then  
a. the central bright fringe will become a dark fringe  
b. the distance between consecutive fringes will decrease  
c. the distance between consecutive fringes will increase  
d. the intensity of the minima will increase
10. In the reported figure, there is a cyclic process  $ABCD$  on a sample of 1 mol of a diatomic gas. The temperature of the gas during the process  $A \rightarrow B$  and  $C \rightarrow D$  are  $T_1$  and  $T_2$  ( $T_1 > T_2$ ), respectively.



Choose the correct option out of the following for work done, if processes  $BC$  and  $DA$  are adiabatic.

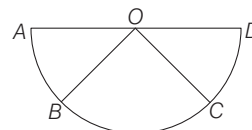
- a.  $W_{AB} = W_{DC}$     b.  $W_{AD} = W_{BC}$   
c.  $W_{BC} + W_{DA} > 0$     d.  $W_{AB} < W_{CD}$

11. **Assertion A** If  $A, B, C, D$  are four points on a semi-circular arc with centre at  $O$  such that  $|AB| = |BC| = |CD|$ , then

$$AB + AC + AD = 4AO + OB + OC$$

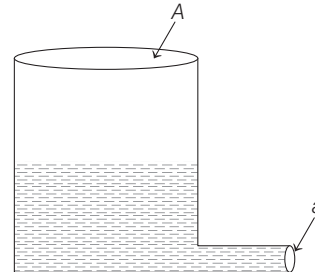
**Reason R** Polygon law of vector addition yields

$$AB + BC + CD + AD = 2AO$$



In the light of the above statements, choose the most appropriate answer from the options given below.

- a. Both A and R are correct and R is the correct explanation of A.  
b. Both A and R are correct but R is not the correct explanation of A.  
c. A is correct but R is not correct.  
d. A is not correct but R is correct.
12. A light cylindrical vessel is kept on a horizontal surface. Area of base is  $A$ . A hole of cross-sectional area  $a$  is made just at its bottom side. The minimum coefficient of friction necessary to prevent sliding the vessel due to the impact force of the emerging liquid is ( $a \ll A$ ).



- a.  $\frac{A}{2a}$     b. None of these  
c.  $\frac{2a}{A}$     d.  $\frac{a}{A}$

13. A particle starts executing simple harmonic motion (SHM) of amplitude  $a$  and total energy  $E$ . At any instant, its kinetic energy is  $\frac{3E}{4}$ , then its displacement  $y$  is given by

- a.  $y = a$     b.  $y = \frac{a}{\sqrt{2}}$   
c.  $y = \frac{a\sqrt{3}}{2}$     d.  $y = \frac{a}{2}$

14. If  $f$  denotes the ratio of the number of nuclei decayed ( $N_d$ ) to the number of nuclei at  $t = 0$  ( $N_0$ ), then for a collection of radioactive nuclei, the rate of change of  $f$  with respect to time is given as [ $\lambda$  is the radioactive decay constant]

- a.  $-\lambda(1 - e^{-\lambda t})$     b.  $\lambda(1 - e^{-\lambda t})$   
c.  $\lambda e^{-\lambda t}$     d.  $-\lambda e^{-\lambda t}$

15. Two capacitors of capacities  $2C$  and  $C$  are joined in parallel and charged upto potential  $V$ . The battery is removed and the capacitor of capacity  $C$  is filled completely with a medium of dielectric constant  $K$ . The potential difference across the capacitors will now be

a.  $\frac{V}{K+2}$                       b.  $\frac{V}{K}$   
c.  $\frac{3V}{K+2}$                       d.  $\frac{3V}{K}$

16. A ball is thrown up with a certain velocity, so that it reaches a height  $h$ . Find the ratio of the two different times of the ball reaching  $\frac{h}{3}$  in both the directions.

a.  $\frac{\sqrt{2}-1}{\sqrt{2}+1}$                       b.  $\frac{1}{3}$   
c.  $\frac{\sqrt{3}-\sqrt{2}}{\sqrt{3}+\sqrt{2}}$                       d.  $\frac{\sqrt{3}-1}{\sqrt{3}+1}$

17. A  $0.07 \text{ H}$  inductor and a  $12 \Omega$  resistor are connected in series to a  $220 \text{ V}$ ,  $50 \text{ Hz}$  AC source. The approximate current in the circuit and the phase angle between current and source voltage are, respectively. [Take,  $\pi$  as  $\frac{22}{7}$ ]

a.  $8.8 \text{ A}$  and  $\tan^{-1}\left(\frac{11}{6}\right)$                       b.  $88 \text{ A}$  and  $\tan^{-1}\left(\frac{11}{6}\right)$   
c.  $0.88 \text{ A}$  and  $\tan^{-1}\left(\frac{11}{6}\right)$                       d.  $8.8 \text{ A}$  and  $\tan^{-1}\left(\frac{6}{11}\right)$

18. Two identical tennis balls each having mass  $m$  and charge  $q$  are suspended from a fixed point by threads of length  $l$ . What is the equilibrium separation when each thread makes a small angle  $\theta$  with the vertical?

a.  $d = \left( \frac{q^2 l}{2\pi\epsilon_0 m g} \right)^{\frac{1}{2}}$                       b.  $d = \left( \frac{q^2 l}{2\pi\epsilon_0 m g} \right)^{\frac{1}{3}}$   
c.  $d = \left( \frac{q^2 l^2}{2\pi\epsilon_0 m^2 g} \right)^{\frac{1}{3}}$                       d.  $d = \left( \frac{q^2 l^2}{2\pi\epsilon_0 m^2 g^2} \right)^{\frac{1}{3}}$

19. **Assertion A** If in five complete rotations of the circular scale, the distance travelled on main scale of the screw gauge is  $5 \text{ mm}$  and there are  $50$  total divisions on circular scale, then least count is  $0.001 \text{ cm}$ .

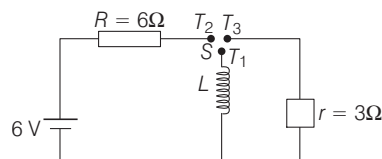
**Reason R** Least count =  $\frac{\text{Pitch}}{\text{Total divisions on circular scale}}$

In the light of the above statements, choose the most appropriate answer from the options given below.

- a. Both A and R are correct and R is the correct explanation of A.  
b. Both A and R are correct and R is not the correct explanation of A.  
c. A is correct but R is not correct.  
d. A is not correct but R is correct.
20. A body takes  $4 \text{ min}$  to cool from  $61^\circ \text{ C}$  to  $59^\circ \text{ C}$ . If the temperature of the surroundings is  $30^\circ \text{ C}$ , then the time taken by the body to cool from  $51^\circ \text{ C}$  to  $49^\circ \text{ C}$  is
- a.  $4 \text{ min}$                       b.  $3 \text{ min}$   
c.  $8 \text{ min}$                       d.  $6 \text{ min}$

## Section B : Numerical Type Questions

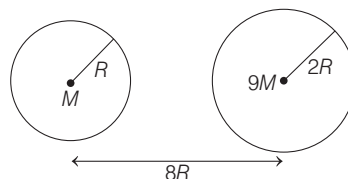
21. Consider an electrical circuit containing a two way switch  $S$ . Initially  $S$  is open and then  $T_1$  is connected to  $T_2$ . As the current in  $R = 6 \Omega$  attains a maximum value of steady state level,  $T_1$  is disconnected from  $T_2$  and immediately connected to  $T_3$ . Potential drop across  $r = 3 \Omega$  resistor immediately after  $T_1$  is connected to  $T_3$  is ..... V. (Round off to the nearest integer)



22. Suppose two planets (spherical in shape) of radii  $R$  and  $2R$ , but mass  $M$  and  $9M$  respectively have a centre to centre separation  $8R$  as shown in the figure. A satellite of mass  $m$  is projected from the surface of the planet of mass  $M$  directly towards the centre of the second planet. The minimum speed  $v$  required for the satellite to reach the surface of the second planet is  $\sqrt{\frac{a}{7} \frac{GM}{R}}$ , then the

value of  $a$  is .....

[Take, the two planets are fixed in their position]



23. In Bohr's atomic model, the electron is assumed to revolve in a circular orbit of radius  $0.5 \text{ Å}$ . If the speed of electron is  $2.2 \times 10^6 \text{ m/s}$ , then the current associated with the electron will be .....  $\times 10^{-2} \text{ mA}$ .

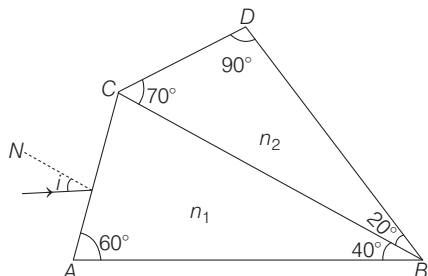
[Take,  $\pi$  as  $\frac{22}{7}$ ]

24. A radioactive sample has an average life of  $30 \text{ ms}$  and is decaying. A capacitor of capacitance  $200 \mu\text{F}$  is first charged and later connected with resistor  $R$ . If the ratio of charge on capacitor to the activity of radioactive sample is fixed with respect to time, then the value of  $R$  should be .....  $\Omega$ .
25. A particle of mass  $9.1 \times 10^{-31} \text{ kg}$  travels in a medium with a speed of  $10^6 \text{ m/s}$  and a photon of a radiation of linear momentum  $10^{-27} \text{ kg-m/s}$  travels in vacuum. The wavelength of photon is ..... times the wavelength of the particle.
26. A prism of refractive index  $n_1$  and another prism of refractive index  $n_2$  are stuck together (as shown in the figure).  $n_1$  and  $n_2$  depend on  $\lambda$ , the wavelength of light, according to the relation

$$n_1 = 1.2 + \frac{10.8 \times 10^{-14}}{\lambda^2}$$

$$\text{and } n_2 = 1.45 + \frac{18 \times 10^{-14}}{\lambda^2}$$

The wavelength for which rays incident at any angle on the interface  $BC$  pass through without bending at that interface will be ..... nm.



27. A stone of mass 20 g is projected from a rubber catapult of length 0.1 m and area of cross-section  $10^{-6} \text{ m}^2$  stretched by an amount 0.04 m. The velocity of the projected stone is ..... m/s.

(Take, Young's modulus of rubber =  $0.5 \times 10^9 \text{ N/m}^2$ )

28. A transistor is connected in common emitter circuit configuration, the collector supply voltage is 10 V and the voltage drop across a resistor of  $1000 \Omega$  in the collector circuit is 0.6 V. If the current gain factor ( $\beta$ ) is 24, then the base current is .....  $\mu\text{A}$ . (Round off to the nearest integer)
29. The amplitude of upper and lower side bands of AM wave, where a carrier signal with frequency 11.21 MHz, peak voltage 15 V is amplitude modulated by a 7.7 kHz sine wave of 5 V amplitude are  $\frac{a}{10} \text{ V}$  and  $\frac{b}{10} \text{ V}$ , respectively. Then, the value of  $\frac{a}{b}$  is .....
30. In a uniform magnetic field, the magnetic needle has a magnetic moment  $9.85 \times 10^{-2} \text{ A/m}^2$  and moment of inertia  $5 \times 10^{-6} \text{ kg-m}^2$ . If it performs 10 complete oscillations in 5 s, then the magnitude of the magnetic field is ..... mT. [Take,  $\pi^2$  as 9.85]

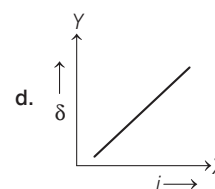
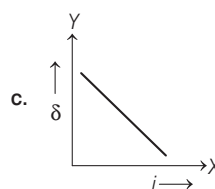
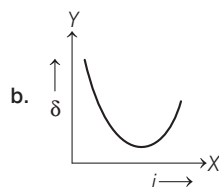
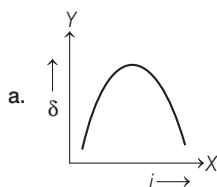
## Answers

- |         |         |           |           |           |           |          |          |         |         |
|---------|---------|-----------|-----------|-----------|-----------|----------|----------|---------|---------|
| 1. (a)  | 2. (c)  | 3. (c)    | 4. (c)    | 5. (d)    | 6. (c)    | 7. (a)   | 8. (d)   | 9. (b)  | 10. (b) |
| 11. (c) | 12. (c) | 13. (d)   | 14. (c)   | 15. (c)   | 16. (c)   | 17. (a)  | 18. (b)  | 19. (d) | 20. (d) |
| 21. (3) | 22. (4) | 23. (112) | 24. (150) | 25. (910) | 26. (600) | 27. (20) | 28. (25) | 29. (1) | 30. (8) |

## 27 JULY SHIFT II

### Objective Type Questions

- An electron and proton are separated by a large distance. The electron starts approaching the proton with energy 3 eV. The proton captures the electrons and forms a hydrogen atom in second excited state. The resulting photon is incident on a photosensitive metal of threshold wavelength  $4000 \text{ \AA}$ . What is the maximum kinetic energy of the emitted photoelectron?
  - 7.61 eV
  - 1.41 eV
  - 3.3 eV
  - No photoelectron would be emitted
- The expected graphical representation of the variation of angle of deviation  $\delta$  with angle of incidence  $i$  in a prism is



- A raindrop with radius  $R = 0.2 \text{ mm}$  falls from a cloud at a height  $h = 2000 \text{ m}$  above the ground. Assume that, the drop is spherical throughout its fall and the force of buoyancy may be neglected, then the terminal speed attained by the raindrop is  
(Take, density of water,  $\rho_w = 1000 \text{ kg m}^{-3}$  and density of air,  $\rho_a = 1.2 \text{ kg m}^{-3}$ ,  $g = 10 \text{ m/s}^2$ , coefficient of viscosity of air,  $\eta = 1.8 \times 10^{-5} \text{ N-s m}^{-2}$ )
  - $250.6 \text{ ms}^{-1}$
  - $43.56 \text{ ms}^{-1}$
  - $4.94 \text{ ms}^{-1}$
  - $14.4 \text{ ms}^{-1}$
- One mole of an ideal gas is taken through an adiabatic process, where the temperature rises from  $27^\circ\text{C}$  to  $37^\circ\text{C}$ . If the ideal gas is composed of polyatomic molecule that has 4 vibrational modes, which of the following is true? [Take,  $R = 8.314 \text{ J mol}^{-1} \text{ K}^{-1}$ ]

- a. Work done by the gas is close to 332 J  
b. Work done on the gas is close to 582 J  
c. Work done by the gas is close to 582 J  
d. Work done on the gas is close to 332 J

5. An object of mass 0.5 kg is executing simple harmonic motion. Its amplitude is 5 cm and time period ( $T$ ) is 0.2 s. What will be the potential energy of the object at an instant  $t = \frac{T}{4}$  s starting from mean position? Assume that, the initial phase of the oscillation is zero.

- a. 0.62 J      b.  $6.2 \times 10^{-3}$  J      c.  $1.2 \times 10^3$  J      d.  $6.2 \times 10^3$  J

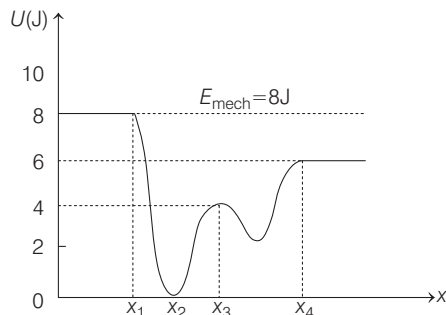
6. Match List I with List II.

List I	List II
A. Capacitance, $C$	I. $M^1 L^1 T^{-3} A^{-1}$
B. Permittivity of free space, $\epsilon_0$	II. $M^{-1} L^{-3} T^4 A^2$
C. Permeability of free space, $\mu_0$	III. $M^{-1} L^{-2} T^4 A^2$
D. Electric field, $E$	IV. $M^1 L^1 T^{-2} A^{-2}$

Choose the correct answer from the options given below.

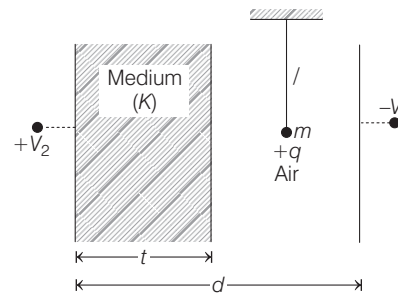
- a. III    II    IV    I      b. III    IV    II    I  
c. IV    II    III    I      d. IV    III    II    I

7. Given below is the plot of a potential energy function  $U(x)$  for a system, in which a particle is in one-dimensional motion, while a conservative force  $F(x)$  acts on it. Suppose that  $E_{\text{mech}} = 8$  J, the incorrect statement for this system is



[where, KE = kinetic energy]

- a. at  $x > x_4$ , KE is constant throughout the region.  
b. at  $x < x_1$ , KE is smallest and the particle is moving at the slowest speed.  
c. at  $x = x_2$ , KE is greatest and the particle is moving at the fastest speed.  
d. at  $x = x_3$ , KE = 4 J.
8. A 100  $\Omega$  resistance, a 0.1  $\mu\text{F}$  capacitor and an inductor are connected in series across a 250 V supply at variable frequency. Calculate the value of inductance of inductor at which resonance will occur. Given that the resonant frequency is 60 Hz.
- a. 0.70 H      b. 70.3 mH  
c.  $7.03 \times 10^{-5}$  H      d. 70.3 H
9. A simple pendulum of mass  $m$ , length  $l$  and charge  $+q$  suspended in the electric field produced by two conducting parallel plates as shown. The value of deflection of pendulum in equilibrium position will be

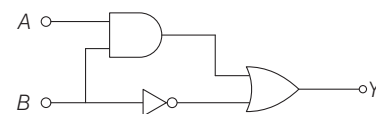


- a.  $\tan^{-1} \left[ \frac{q}{mg} \times \frac{C_1 (V_2 - V_1)}{(C_1 + C_2) (d - t)} \right]$   
b.  $\tan^{-1} \left[ \frac{q}{mg} \times \frac{C_2 (V_2 - V_1)}{(C_1 + C_2) (d - t)} \right]$   
c.  $\tan^{-1} \left[ \frac{q}{mg} \times \frac{C_2 (V_1 + V_2)}{(C_1 + C_2) (d - t)} \right]$   
d.  $\tan^{-1} \left[ \frac{q}{mg} \times \frac{C_1 (V_1 + V_2)}{(C_1 + C_2) (d - t)} \right]$

10. Two Carnot engines A and B operate in series such that engine A absorbs heat at  $T_1$  and rejects heat to a sink at temperature  $T$ . engine B absorbs half of the heat rejected by engine A and rejects heat to the sink at  $T_3$ . When work done in both the cases is equal, then the value of  $T$  is

- a.  $\frac{2}{3}T_1 + \frac{3}{2}T_3$       b.  $\frac{1}{3}T_1 + \frac{2}{3}T_3$   
c.  $\frac{3}{2}T_1 + \frac{1}{3}T_3$       d.  $\frac{2}{3}T_1 + \frac{1}{3}T_3$

11. Find the truth table for the function  $Y$  of  $A$  and  $B$  represented in the following figure.



a.

A	B	Y
0	0	0
0	1	1
1	0	0
1	1	0

b.

A	B	Y
0	0	1
0	1	0
1	0	1
1	1	1

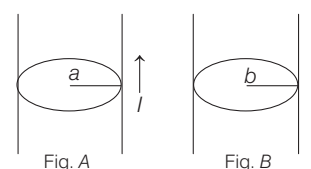
c.

A	B	Y
0	0	0
0	1	0
1	0	0
1	1	1

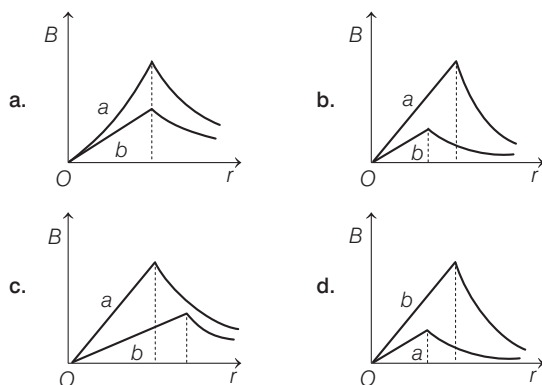
d.

A	B	Y
0	0	0
0	1	1
1	0	1
1	1	1

12. Figures A and B shown two long straight wires of circular cross-section ( $a$  and  $b$  with  $a < b$ ), carrying current  $I$  which is uniformly distributed across the cross-section. The magnitude of magnetic field  $B$  varies with radius  $r$  and can be represented as







13. Two identical particles of mass 1 kg each go round a circle of radius  $R$ , under the action of their mutual gravitational attraction. The angular speed of each particle is

a.  $\sqrt{\frac{G}{2R^3}}$       b.  $\frac{1}{2}\sqrt{\frac{G}{R^3}}$       c.  $\frac{1}{2R}\sqrt{\frac{1}{G}}$       d.  $\sqrt{\frac{2G}{R^3}}$

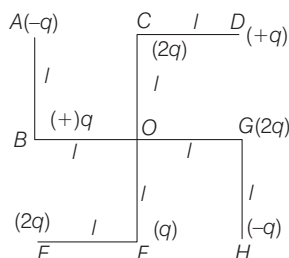
14. Consider the following statements.

- A. Atoms of each element emit characteristics spectrum.  
B. According to Bohr's postulate, an electron in a hydrogen atom, revolves in a certain stationary orbit.  
C. The density of nuclear matter depends on the size of the nucleus.  
D. A free neutron is stable but a free proton decay is possible.  
E. Radioactivity is an indication of the instability of nuclei.

Choose the correct answer from the options given below.

- a. A, B, C, D and E      b. A, B and E  
c. B and D      d. A, C and E

15. What will be the magnitude of electric field at point O as shown in figure? Each side of the figure is  $l$  and perpendicular to each other.



a.  $\frac{1}{4\pi\epsilon_0} \frac{q}{l^2}$       b.  $\frac{1}{4\pi\epsilon_0} \frac{q}{(2l^2)} (2\sqrt{2} - 1)$   
c.  $\frac{q}{4\pi\epsilon_0 (2l)^2}$       d.  $\frac{1}{4\pi\epsilon_0} \frac{2q}{2l^2} (\sqrt{2})$

16. A physical quantity  $y$  is represented by the formula  $y = m^2 r^{-4} g^x l^{-3/2}$ . If the percentage errors found in  $y, m, r, l$  and  $g$  are 18, 1, 0.5, 4 and  $p$  respectively, then find the value of  $x$  and  $p$ .

- a. 5 and  $\pm 2$       b. 4 and  $\pm 3$   
c.  $\frac{16}{3}$  and  $\pm \frac{3}{2}$       d. 8 and  $\pm 2$

17. An automobile of mass  $m$  accelerates starting from origin and initially at rest, while the engine supplies constant power  $P$ . The position is given as a function of time by

a.  $\left(\frac{9P}{8m}\right)^{\frac{1}{2}} \cdot t^{\frac{3}{2}}$       b.  $\left(\frac{8P}{9m}\right)^{\frac{1}{2}} \cdot t^{\frac{2}{3}}$   
c.  $\left(\frac{9m}{8P}\right)^{\frac{1}{2}} \cdot t^{\frac{3}{2}}$       d.  $\left(\frac{8P}{9m}\right)^{\frac{1}{2}} \cdot t^{\frac{3}{2}}$

18. The planet Mars has two Moons, if one of them has a period 7 h, 30 min and an orbital radius of  $9.0 \times 10^3$  km. Find the mass of Mars.

[Take,  $\frac{4\pi^2}{G} = 6 \times 10^{11} \text{ N}^{-1} \text{ m}^{-2} \text{ kg}^2$ ]

- a.  $5.96 \times 10^{19} \text{ kg}$       b.  $3.25 \times 10^{21} \text{ kg}$   
c.  $7.02 \times 10^{25} \text{ kg}$       d.  $6.00 \times 10^{23} \text{ kg}$

19. A particle of mass  $M$  originally at rest is subjected to a force whose direction is constant but magnitude varies with time according to the relation

$$F = F_0 \left[ 1 - \left( \frac{t - T}{T} \right)^2 \right]$$

where,  $F_0$  and  $T$  are constants. The force acts only for the time interval  $2T$ . The velocity  $v$  of the particle after time  $2T$  is

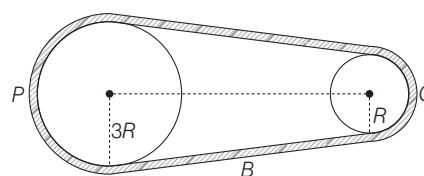
a.  $\frac{2F_0 T}{M}$       b.  $\frac{F_0 T}{2M}$   
c.  $\frac{4F_0 T}{3M}$       d.  $\frac{F_0 T}{3M}$

20. The resistance of a conductor at  $15^\circ\text{C}$  is  $16 \Omega$  and at  $100^\circ\text{C}$  is  $20 \Omega$ . What will be the temperature coefficient of resistance of the conductor?

- a.  $0.010^\circ\text{C}^{-1}$       b.  $0.033^\circ\text{C}^{-1}$   
c.  $0.003^\circ\text{C}^{-1}$       d.  $0.042^\circ\text{C}^{-1}$

## Section B : Numerical Type Questions

21. In the given figure, two wheels  $P$  and  $Q$  are connected by a belt  $B$ . The radius of  $P$  is three times as that of  $Q$ . In case of same rotational kinetic energy, the ratio of rotational inertias  $\left(\frac{I_1}{I_2}\right)$  will be  $x : 1$ . The value of  $x$  will be



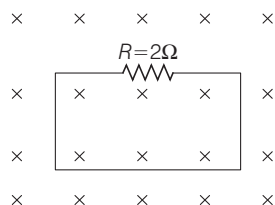
22. The difference in the number of waves when yellow light propagates through air and vacuum columns of the same thickness is one. The thickness of the air column is ..... mm.

[Take, refractive index of air = 1.0003, wavelength of yellow light in vacuum = 6000 Å]

23. The maximum amplitude for an amplitude modulated wave is found to be 12 V, while the minimum amplitude is found to be 3 V. The modulation index is  $0.6x$ , where  $x$  is .....

24. In the given figure, the magnetic flux through the loop increases according to the relation  $\phi_B(t) = 10t^2 + 20t$ , where  $\phi_B$  is in milliwebers and  $t$  is in seconds.

The magnitude of current through  $R = 2\Omega$  resistor at  $t = 5$  s is ..... mA.

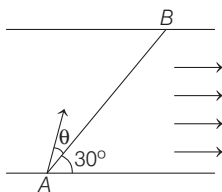


25. A particle executes simple harmonic motion represented by displacement function as

$$x(t) = A \sin(\omega t + \phi)$$

If the position and velocity of the particle at  $t = 0$  s are 2 cm and  $2\omega$  cm s<sup>-1</sup> respectively, then its amplitude is  $x\sqrt{2}$  cm, where the value of  $x$  is .....

26. A swimmer wants to cross a river from point A to point B. Line AB makes an angle of 30° with the flow of river. Magnitude of velocity of the swimmer is same as that of the river. The angle  $\theta$  with the line AB should be .....°, so that the swimmer reaches point B.



27. For the circuit shown, the value of current at time  $t = 3.2$  s will be ..... A.

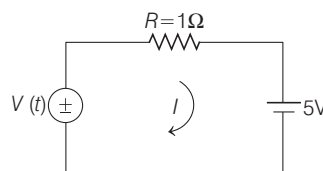
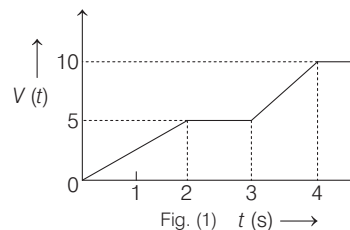
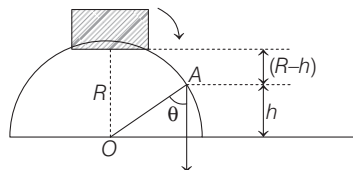


Fig. (2)

[Voltage distribution  $V(t)$  is shown by Fig. (1) and the circuit is shown in Fig. (2).]

28. A small block slides down from the top of hemisphere of radius  $R = 3$  m as shown in the figure. The height  $h$  at which the block will lose contact with the surface of the sphere is ..... m. (Assume there is no friction between the block and the hemisphere)



29. The  $K_\alpha$  X-ray of molybdenum has wavelength 0.071 nm. If the energy of a molybdenum atom with a  $K$  electron knocked out is 27.5 keV, the energy of this atom when an  $L$  electron is knocked out will be ..... keV. (Round off to the nearest integer)

[Take,  $h = 4.14 \times 10^{-15}$  eV-s,  $c = 3 \times 10^8$  ms<sup>-1</sup>]

30. The water is filled upto height of 12 m in a tank having vertical sidewalls. A hole is made in one of the walls at a depth  $h$  below the water level. The value of  $h$  for which the emerging stream of water strikes the ground at the maximum range is ..... m.

## Answers

- |         |         |         |          |         |          |         |         |          |         |
|---------|---------|---------|----------|---------|----------|---------|---------|----------|---------|
| 1. (b)  | 2. (b)  | 3. (c)  | 4. (b)   | 5. (a)  | 6. (a)   | 7. (b)  | 8. (d)  | 9. (c)   | 10. (d) |
| 11. (b) | 12. (c) | 13. (b) | 14. (b)  | 15. (d) | 16. (c)  | 17. (d) | 18. (d) | 19. (c)  | 20. (c) |
| 21. (9) | 22. (2) | 23. (1) | 24. (60) | 25. (2) | 26. (30) | 27. (1) | 28. (2) | 29. (10) | 30. (6) |

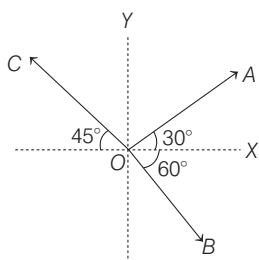
## 26 AUGUST SHIFT I

### Section A : Objective Type Questions

1. The fractional change in the magnetic field intensity at a distance  $r$  from centre on the axis of current carrying coil of radius  $a$  to the magnetic field intensity at the centre of the same coil is (Take,  $r < a$ )

a.  $\frac{3a^2}{2r^2}$       b.  $\frac{2a^2}{3r^2}$       c.  $\frac{2r^2}{3a^2}$       d.  $\frac{3r^2}{2a^2}$

2. The magnitude of vectors  $\vec{OA}$ ,  $\vec{OB}$ , and  $\vec{OC}$  in the given figure are equal. The direction of  $\vec{OA} + \vec{OB} - \vec{OC}$  with X-axis will be



a.  $\tan^{-1} \frac{(1 - \sqrt{3} - \sqrt{2})}{(1 + \sqrt{3} + \sqrt{2})}$       b.  $\tan^{-1} \frac{(\sqrt{3} - 1 + \sqrt{2})}{(1 + \sqrt{3} - \sqrt{2})}$   
 c.  $\tan^{-1} \frac{(\sqrt{3} - 1 + \sqrt{2})}{(1 - \sqrt{3} + \sqrt{2})}$       d.  $\tan^{-1} \frac{(1 + \sqrt{3} - \sqrt{2})}{(1 - \sqrt{3} - \sqrt{2})}$

3. Car B overtakes another car A at a relative speed of  $40 \text{ ms}^{-1}$ . How fast will the image of car B appear to move in the mirror of focal length 10 cm fitted in car A, when the car B is 1.9 m away from the car A?

a.  $4 \text{ ms}^{-1}$       b.  $0.2 \text{ ms}^{-1}$   
 c.  $40 \text{ ms}^{-1}$       d.  $0.1 \text{ ms}^{-1}$

4. Inside a uniform spherical shell

- I. the gravitational field is zero.
- II. the gravitational potential is zero.
- III. the gravitational field is same everywhere.
- IV. the gravitation potential is same everywhere.
- V. All of the above

Choose the most appropriate answer from the options given below .

a. I, III and IV      b. Only V  
 c. I, II and III      d. II, III and IV

5. Two narrow bores of diameter 5.0 mm and 8.0 mm are joined together to form a U-shaped tube open at both ends. If this U-tube contains water, what is the difference in the level of two limbs of the tube.

[Take surface tension of water  $T = 73 \times 10^{-2} \text{ Nm}^{-1}$ , angle of contact = 0,  $g = 10 \text{ ms}^{-2}$  and density of water  $= 1.0 \times 10^3 \text{ kg m}^{-3}$ ]

a. 3.62 mm      b. 2.19 mm  
 c. 5.34 mm      d. 4.97 mm

6. An electric appliance supplies 6000 J/min heat to the system. If the system delivers a power of 90W. How long it would take to increase the internal energy by  $25 \times 10^3 \text{ J}$ ?

a.  $25 \times 10^2 \text{ s}$       b.  $4.1 \times 10^1 \text{ s}$   
 c.  $24 \times 10^3 \text{ s}$       d.  $25 \times 10^1 \text{ s}$

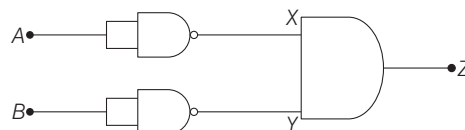
7. An inductor coil stores 64 J of magnetic field energy and dissipates energy at the rate of 640 W when a current of 8A is passed through it. If this coil is joined across an ideal battery, find the time constant of the circuit in seconds.

a. 0.4      b. 0.8      c. 0.125      d. 0.2

8. A series L-C-R circuit driven by 300 V at a frequency of 50 Hz contains a resistance  $R = 3 \text{ k}\Omega$ , an inductor of inductive reactance  $X_L = 250 \pi \Omega$  and an unknown capacitor. The value of capacitance to maximise the average power should be (Take,  $\pi^2 = 10$ )

a.  $4 \mu\text{F}$       b.  $25 \mu\text{F}$       c.  $400 \mu\text{F}$       d.  $40 \mu\text{F}$

9. Identify the logic operation carried out by the given circuit.



a. OR      b. AND      c. NOR      d. NAND

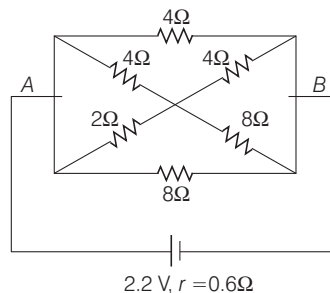
10. A particular hydrogen like ion emits radiation of frequency  $2.92 \times 10^{15} \text{ Hz}$  when it makes transition from  $n = 3$  to  $n = 1$ . The frequency in Hz of radiation emitted in transition from  $n = 2$  to  $n = 1$  will be

a.  $0.44 \times 10^{15}$       b.  $6.57 \times 10^{15}$       c.  $4.38 \times 10^{15}$       d.  $2.46 \times 10^{15}$

11. In a photoelectric experiment ultraviolet light of wavelength 280 nm is used with lithium cathode having work-function  $\phi = 2.5 \text{ eV}$ . If the wavelength of incident light is switched to 400 nm, find out the change in the stopping potential. ( $h = 6.63 \times 10^{-34} \text{ Js}$ , and  $c = 3 \times 10^8 \text{ ms}^{-1}$ )

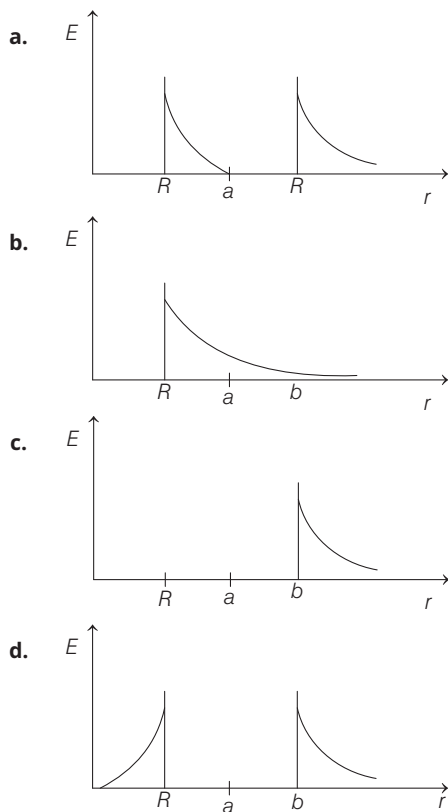
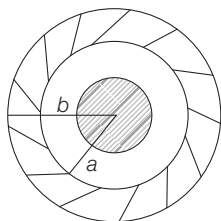
a. 1.3 V      b. 1.1 V      c. 1.9 V      d. 0.6 V

12. In the given figure, the emf of the cell is 2.2 V and if internal resistance is  $0.6 \Omega$ . Calculate the power dissipated in the whole circuit



a. 1.32 W      b. 0.65 W      c. 2.2 W      d. 4.4 W

13. A solid metal sphere of radius  $R$  having charge  $q$  is enclosed inside the concentric spherical shell of inner radius  $a$  and outer radius  $b$  as shown in figure. The approximate variation electric field as a function of distance  $r$  from centre  $O$  is given by



14. The rms speeds of the molecules of hydrogen, oxygen and carbondioxide at the same temperature are  $v_H$ ,  $v_O$  and  $v_{CO_2}$  respectively, then
- a.  $v_H > v_O > v_{CO_2}$       b.  $v_{CO_2} > v_O > v_H$   
c.  $v_H = v_O > v_{CO_2}$       d.  $v_H = v_O = v_{CO_2}$
15. In a screw gauge, 5th division of the circular scale coincides with the reference line when the ratchet is closed. There are 50 divisions on the circular scale, and the main scale moves by 0.5 mm on a complete rotation. For a particular observation the reading on the main scale is 5 mm and the 20th division of the circular scale coincides with reference line. Calculate the true reading.
- a. 5.00 mm      b. 5.25 mm      c. 5.15 mm      d. 5.20 mm
16. What equal length of an iron wire and a copper-nickel alloy wire, each of 2 mm diameter connected parallel to give an equivalent resistance of  $3\Omega$ ?

(Given, resistivities of iron and copper-nickel alloy wire are  $12\mu\Omega\text{ cm}$  and  $51\mu\Omega\text{ cm}$  respectively)

- a. 82 m      b. 97 m      c. 110 m      d. 90 m

17. The initial mass of a rocket is 1000 kg. Calculate at what rate the fuel should be burnt, so that the rocket is given an acceleration of  $20\text{ ms}^{-1}$ . The gases come out at a relative speed of  $500\text{ ms}^{-1}$  with respect to the rocket [Use,  $g = 10\text{ m/s}^2$ ]

- a.  $60 \times 10^2\text{ kg s}^{-1}$       b.  $500\text{ kg s}^{-1}$   
c.  $10\text{ kg s}^{-1}$       d.  $60\text{ kg s}^{-1}$

18. If  $E$ ,  $L$ ,  $M$  and  $G$  denote the quantities as energy, angular momentum, mass and constant of gravitation respectively, then the dimension of  $P$  in the formula  $P = EL^2M^{-5}G^{-2}$  is

- a.  $[M^0L^1T^0]$       b.  $[M^{-1}L^{-1}T^2]$       c.  $[ML^1T^{-2}]$       d.  $[M^0L^0T^0]$

19. The material filled between the plates of a parallel plate capacitor has resistivity  $200\Omega\text{m}$ . The value of capacitance of the capacitor is  $2\text{pF}$ . If a potential difference of  $40\text{ V}$  is applied across the plates of the capacitor, then the value of leakage current flowing out of the capacitor is (Given, the value of relative permittivity of material is 50.)

- a.  $9.0\mu\text{A}$       b.  $9.0\text{ mA}$       c.  $0.9\text{ mA}$       d.  $0.9\mu\text{A}$

20. **Statement I** By doping silicon semiconductor with pentavalent material, the electrons density increases. **Statement II** The  $n$ -type semiconductor has net negative charge.

In the light of the above statements, choose the most appropriate answer from the options given below.

- a. Statement I is true but statement II is false.  
b. Statement I is false but statement II is true.  
c. Both statement I and statement II are true.  
d. Both statement I and statement II are false.

## Section B : Numerical Type Questions

21. A uniform chain of length 3 m and mass 3 kg overhangs a smooth table with 2 m laying on the table. If  $k$  is the kinetic energy of the chain in joule as it completely slips off the table, then the value of  $k$  is ..... (Take,  $g = 10\text{ m/s}^2$ )

22. The electric field in a plane electromagnetic wave is given by

$$\mathbf{E} = 200\cos\left[\left(\frac{0.5 \times 10^3}{m}\right)x - \left(1.5 \times 10^{11}\frac{\text{rad}}{s} \times t\right)\right] \frac{\text{V}}{\text{m}} \hat{j}$$

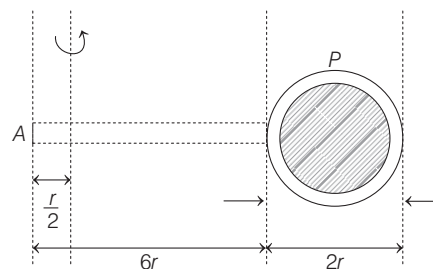
If this wave falls normally on a perfectly reflecting surface having an area of  $100\text{ cm}^2$ . If the radiation pressure exerted by the EM wave on the surface during a 10 min exposure is  $\frac{x}{10^9}$ . Find the value of  $x$ .

23. A source and a detector move away from each other in absence of wind with a speed of  $20\text{ m/s}$  with respect to the ground. If the detector detects a frequency of  $1800\text{ Hz}$  of the sound coming from the source, then the

original frequency of source considering speed of sound in air 340 m/s will be ..... Hz.

24. Two spherical balls having equal masses with radius of 5 cm each are thrown upwards along the same vertical direction at an interval of 3s with the same initial velocity of 35 m/s, then these balls collide at a height of ..... m. (Take,  $g = 10 \text{ m/s}^2$ )
25. A soap bubble of radius 3 cm is formed inside the another soap bubble of radius 6 cm. The radius of an equivalent soap bubble which has the same excess pressure as inside the smaller bubble with respect to the atmospheric pressure is ..... cm.
26. An amplitude modulated wave is represented by  $C_m(t) = 10(1 + 0.2\cos 12560t)\sin(111 \times 10^4 t) \text{ V}$ . The modulating frequency in kHz will be .....
27. Two short magnetic dipoles  $m_1$  and  $m_2$  each having magnetic moment of  $1 \text{ Am}^2$  are placed at point O and P, respectively. The distance between OP is 1 m. The torque experienced by the magnetic dipole  $m_2$  due to the presence of  $m_1$  is .....  $\times 10^{-7} \text{ Nm}$ .
28. Two travelling waves produces a standing wave represented by equation.  
 $y = 1.0 \text{ mm} \cos(1.57 \text{ cm}^{-1}x) \sin(785 \text{ s}^{-1}t)$ .  
 The node closest to the origin in the region  $x > 0$  will be at x is ..... cm.

29. White light is passed through a double slit and interference is observed on a screen 1.5 m away. The separation between the slits is 0.3 mm. The first violet and red fringes are formed 2.0 mm and 3.5 mm away from the central white fringes. The difference in wavelengths of red and violet light is ..... nm.
30. Consider a badminton racket with length scales as shown in the figure.



If the mass of the linear and circular portions of the badminton racket are same ( $M$ ) and the mass of the threads are negligible, the moment of inertia of the racket about an axis perpendicular to the handle and in the plane of the ring at,  $\frac{r}{2}$  distance from the end A of the handle will be .....  $Mr^2$ .

## Answers

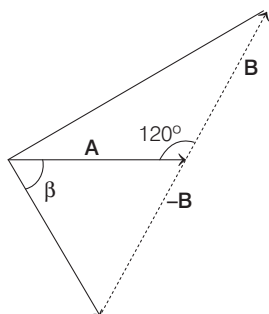
1. (d)	2. (a)	3. (d)	4. (a)	5. (b)	6. (a)	7. (d)	8. (a)	9. (c)	10. (d)
11. (a)	12. (c)	13. (a, b)	14. (a)	15. (c)	16. (b)	17. (d)	18. (d)	19. (c)	20. (a)
21. (40)	22. (354)	23. (2025)	24. (50)	25. (2)	26. (2)	27. (1)	28. (1)	29. (300)	30. (52)

## 26 AUGUST SHIFT II

### Objective Type Questions

1. The temperature of equal masses of three different liquids x, y and z are  $10^\circ\text{C}$ ,  $20^\circ\text{C}$  and  $30^\circ\text{C}$ , respectively. The temperature of mixture when x is mixed with y is  $16^\circ\text{C}$  and that when y is mixed with z is  $26^\circ\text{C}$ . The temperature of mixture when x and z are mixed will be  
 a.  $28.32^\circ\text{C}$     b.  $25.62^\circ\text{C}$     c.  $23.84^\circ\text{C}$     d.  $20.28^\circ\text{C}$
2. The de-Broglie wavelength of a particle having kinetic energy  $E$  is  $\lambda$ . How much extra energy must be given to this particle, so that the de-Broglie wavelength reduces to 75% of the initial value ?  
 a.  $\frac{1}{9}E$     b.  $\frac{7}{9}E$     c.  $E$     d.  $\frac{16}{9}E$
3. A particle of mass  $m$  is suspended from a ceiling through a string of length  $L$ . The particle moves in a horizontal circle of radius  $r$  such that  $r = \frac{L}{\sqrt{2}}$ . The speed of particle will be  
 a.  $\sqrt{rg}$     b.  $\sqrt{2rg}$     c.  $2\sqrt{rg}$     d.  $\sqrt{rg/2}$
4. A cylindrical container of volume  $4.0 \times 10^{-3} \text{ m}^3$  contains one mole of hydrogen and two moles of carbon dioxide. Assume the temperature of the mixture is 400 K. The pressure of the mixture of gases is  
 [Take, gas constant  $= 8.3 \text{ J mol}^{-1} \text{ K}^{-1}$ ]  
 a.  $249 \times 10^1 \text{ Pa}$     b.  $24.9 \times 10^3 \text{ Pa}$   
 c.  $24.9 \times 10^5 \text{ Pa}$     d.  $24.9 \text{ Pa}$

5. The angle between vector  $\mathbf{A}$  and  $(\mathbf{A} - \mathbf{B})$  is



- a.  $\tan^{-1}\left(\frac{-\frac{B}{2}}{A - B\frac{\sqrt{3}}{2}}\right)$   
b.  $\tan^{-1}\left(\frac{A}{0.7B}\right)$   
c.  $\tan^{-1}\left(\frac{\sqrt{3}B}{2A - B}\right)$   
d.  $\tan^{-1}\left(\frac{B\cos\theta}{A - B\sin\theta}\right)$

6. A light beam is described by  $E = 800 \sin\left(\omega t - \frac{x}{c}\right)$ . An electron is allowed to move normal to the propagation of light beam with a speed  $3 \times 10^7 \text{ ms}^{-1}$ . What is the maximum magnetic force exerted on the electron?  
a.  $1.28 \times 10^{-17} \text{ N}$   
b.  $1.28 \times 10^{-18} \text{ N}$   
c.  $12.8 \times 10^{-17} \text{ N}$   
d.  $12.8 \times 10^{-18} \text{ N}$

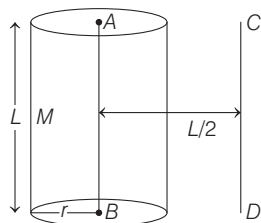
7. The two thin co-axial rings, each of radius  $a$  and having charges  $+Q$  and  $-Q$  respectively, are separated by a distance of  $s$ . The potential difference between the centres of the two rings is

- a.  $\frac{Q}{2\pi\epsilon_0} \left[ \frac{1}{a} + \frac{1}{\sqrt{s^2 + a^2}} \right]$   
b.  $\frac{Q}{4\pi\epsilon_0} \left[ \frac{1}{a} + \frac{1}{\sqrt{s^2 + a^2}} \right]$   
c.  $\frac{Q}{4\pi\epsilon_0} \left[ \frac{1}{a} - \frac{1}{\sqrt{s^2 + a^2}} \right]$   
d.  $\frac{Q}{2\pi\epsilon_0} \left[ \frac{1}{a} - \frac{1}{\sqrt{s^2 + a^2}} \right]$

8. If you are provided a set of resistances  $2\Omega$ ,  $4\Omega$ ,  $6\Omega$  and  $8\Omega$ . Connect these resistances, so as to obtain an equivalent resistance of  $\frac{46}{3} \Omega$ .

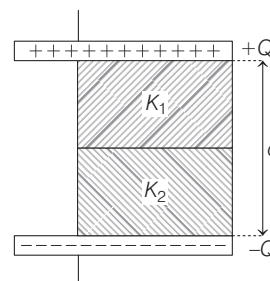
- a.  $4 \Omega$  and  $6 \Omega$  are in parallel with  $2 \Omega$  and  $8 \Omega$  in series.  
b.  $6 \Omega$  and  $8 \Omega$  are in parallel with  $2 \Omega$  and  $4 \Omega$  in series.  
c.  $2 \Omega$  and  $6 \Omega$  are in parallel with  $4 \Omega$  and  $8 \Omega$  in series.  
d.  $2 \Omega$  and  $4 \Omega$  are in parallel with  $6 \Omega$  and  $8 \Omega$  in series.

9. The solid cylinder of length  $80 \text{ cm}$  and mass  $M$  has a radius of  $20 \text{ cm}$ . Calculate the density of the material used, if the moment of inertia of the cylinder about an axis  $CD$  parallel to  $AB$  as shown in figure is  $2.7 \text{ kg m}^2$ .



- a.  $14.9 \text{ kg / m}^3$   
b.  $7.5 \times 10^1 \text{ kg / m}^3$   
c.  $7.5 \times 10^2 \text{ kg / m}^3$   
d.  $1.49 \times 10^2 \text{ kg / m}^3$

10. A parallel-plate capacitor with plate area  $A$  has separation  $d$  between the plates. Two dielectric slabs of dielectric constant  $K_1$  and  $K_2$  of same area  $A/2$  and thickness  $d/2$  are inserted in the space between the plates. The capacitance of the capacitor will be given by



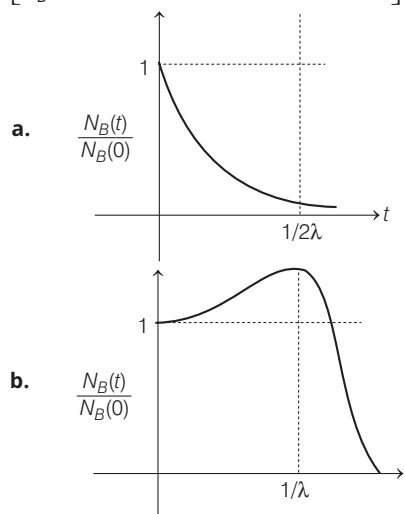
- a.  $\frac{\epsilon_0 A}{d} \left( \frac{1}{2} + \frac{K_1 K_2}{K_1 + K_2} \right)$   
b.  $\frac{\epsilon_0 A}{d} \left( \frac{1}{2} + \frac{K_1 K_2}{2(K_1 + K_2)} \right)$   
c.  $\frac{\epsilon_0 A}{d} \left( \frac{1}{2} + \frac{K_1 + K_2}{K_1 K_2} \right)$   
d.  $\frac{\epsilon_0 A}{d} \left( \frac{1}{2} + \frac{2(K_1 + K_2)}{K_1 K_2} \right)$

11. A bomb is dropped by fighter plane flying horizontally. To an observer sitting in the plane, the trajectory of the bomb is a

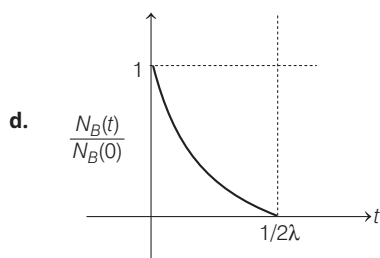
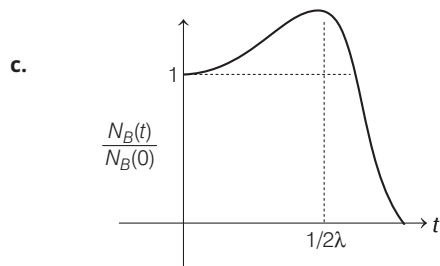
- a. hyperbola  
b. parabola in the direction of motion of plane  
c. straight line vertically down the plane  
d. parabola in a direction opposite to the motion of plane

12. At time  $t = 0$ , a material is composed of two radioactive atoms  $A$  and  $B$ , where  $N_A(0) = 2N_B(0)$ . The decay constant of both kind of radioactive atoms is  $\lambda$ . However,  $A$  disintegrates to  $B$  and  $B$  disintegrates to  $C$ . Which of the following figures represents the evolution of  $N_B(t) / N_B(0)$  with respect to time  $t$ ?

$[N_A(0) = \text{Number of } A \text{ atoms at } t = 0]$   
 $[N_B(0) = \text{Number of } B \text{ atoms at } t = 0]$







13. A transmitting antenna at top of a tower has a height of 50 m and the height of receiving antenna is 80 m. What is range of communication for line of sight (LOS) mode ?  
[Use radius of Earth = 6400 km]

a. 45.5 km    b. 80.2 km    c. 144.1 km    d. 57.28 km

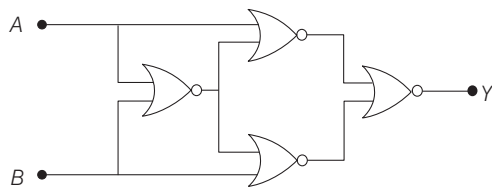
14. A refrigerator consumes an average 35 W power to operate between temperature  $-10^{\circ}\text{C}$  to  $25^{\circ}\text{C}$ . If there is no loss of energy, then how much average heat per second does it transfer ?

a. 263 J/s    b. 298 J/s    c. 350 J/s    d. 35 J/s

15. An electric bulb of 500 W at 100 V is used in a circuit having a 200 V supply. Calculate the resistance  $R$  to be connected in series with the bulb, so that the power delivered by the bulb is 500 W.

a. 20  $\Omega$     b. 30  $\Omega$     c. 5  $\Omega$     d. 10  $\Omega$

16. Four NOR gates are connected as shown in figure. The truth table for the given figure is



a.

A	B	Y
0	0	1
0	1	0
1	0	1
1	1	0

b.

A	B	Y
0	0	0
0	1	1
1	0	1
1	1	0

c.

A	B	Y
0	0	0
0	1	1
1	0	0
1	1	1

d.

A	B	Y
0	0	1
0	1	0
1	0	0
1	1	1

17. Match List-I with List-II.

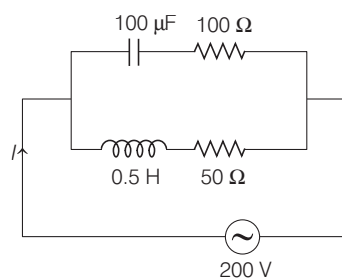
List-I	List-II
A. Magnetic induction	1. $[\text{ML}^2\text{T}^{-2}\text{A}^{-1}]$
B. Magnetic flux	2. $[\text{ML}^{-1}\text{A}]$
C. Magnetic permeability	3. $[\text{MT}^{-2}\text{A}^{-1}]$
D. Magnetisation	4. $[\text{MLT}^{-2}\text{A}^{-2}]$

Choose the most appropriate answer from the options given below.

	A	B	C	D		A	B	C	D
a.	2	4	1	3	b.	2	1	4	3
c.	3	2	4	1	d.	3	1	4	2

18. In the given circuit the AC source has  $\omega = 100 \text{ rad s}^{-1}$ .

Considering the inductor and capacitor to be ideal, what will be the current  $I$  flowing through the circuit?



a. 5.9 A    b. 4.24 A    c. 0.94 A    d. 6 A

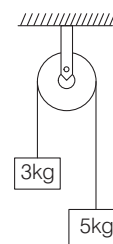
19. If the length of the pendulum in pendulum clock increases by 0.1%, then the error in time per day is

a. 86.4 s    b. 4.32 s  
c. 43.2 s    d. 8.64 s

20. Two blocks of masses 3 kg and 5 kg are connected by a metal wire going over a smooth pulley. The breaking stress of the metal is  $(24/\pi) \times 10^2 \text{ Nm}^{-2}$ . What is the minimum radius of the wire?

(Take,  $g = 10 \text{ ms}^{-2}$ )

a. 125 cm    b. 1250 cm  
c. 12.5 cm    d. 1.25 cm



## Section B : Numerical Type Questions

21. Two waves are simultaneously passing through a string and their equations are  $y_1 = A_1 \sin k(x - vt)$ ,  $y_2 = A_2 \sin k(x - vt + x_0)$ .

[Given, amplitudes  $A_1 = 12 \text{ mm}$  and  $A_2 = 5 \text{ mm}$ ,  $x_0 = 3.5 \text{ cm}$  and wave number  $k = 6.28 \text{ cm}^{-1}$ ]. The amplitude of resulting wave will be ..... mm.

22. A source of light is placed in front of a screen. Intensity of light on the screen is  $I$ . Two polaroids  $P_1$  and  $P_2$  are so placed in between the source of light and screen that the intensity of light on screen is  $I/2$ .  $P_2$  should be rotated by an angle of ..... (degrees), so that the intensity of light on the screen becomes  $3I/8$ .

23. If the maximum value of accelerating potential provided by a radio frequency oscillator is 12 kV. The number of revolution made by a proton in a cyclotron to achieve one sixth of the speed of light is .....

[Given,  $m_p = 1.67 \times 10^{-27}$  kg,  $e = 1.6 \times 10^{-19}$  C,  $c = 3 \times 10^8$  m/s]

24. The acceleration due to gravity is found upto an accuracy of 4% on a planet. The energy supplied to a simple pendulum to known mass  $m$  to undertake oscillations of time period  $T$  is being estimated. If time period is measured to an accuracy of 3%, the accuracy to which  $E$  is known as .....%.

25. A circular coil of radius 8.0 cm and 20 turns is rotated about its vertical diameter with an angular speed of  $50 \text{ rad s}^{-1}$  in a uniform horizontal magnetic field of  $3.0 \times 10^{-2}$  T. The maximum emf induced in the coil will be .....  $\times 10^{-2}$  V.

(rounded off to the nearest integer.)

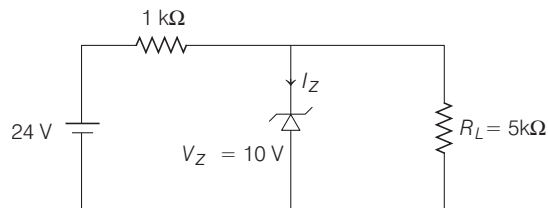
26. Two simple harmonic motions are represented by the equations

$$x_1 = 5 \sin\left(2\pi t + \frac{\pi}{4}\right) \text{ and } x_2 = 5\sqrt{2}(\sin 2\pi t + \cos 2\pi t)$$

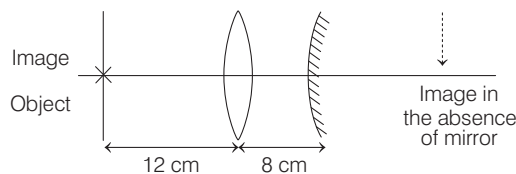
The amplitude of second motion is ..... times the amplitude in first motion.

27. A coil in the shape of an equilateral triangle of side 10 cm lies in a vertical plane between the pole pieces of permanent magnet producing a horizontal magnetic field 20 mT. The torque acting on the coil when a current of 0.2 A is passed through it and its plane becomes parallel to the magnetic field will be  $\sqrt{x} \times 10^{-5}$  Nm. The value of  $x$  is.....

28. For the given circuit, the power across Zener diode is ..... mW.

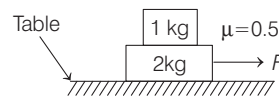


29. An object is placed at a distance of 12 cm from a convex lens. A convex mirror of focal length 15 cm is placed on other side of lens at 8 cm as shown in the figure. Image of object coincides with the object.



When the convex mirror is removed, a real and inverted image is formed at a position. The distance of the image from the object will be ..... cm.

30. The coefficient of static friction between two blocks is 0.5 and the table is smooth. The maximum horizontal force that can be applied to move the blocks together is .....N. (Take,  $g = 10 \text{ ms}^{-2}$ )



## Answers

- |         |          |           |          |          |           |         |           |          |          |
|---------|----------|-----------|----------|----------|-----------|---------|-----------|----------|----------|
| 1. (c)  | 2. (b)   | 3. (a)    | 4. (c)   | 5. (c)   | 6. (a, b) | 7. (d)  | 8. (d)    | 9. (d)   | 10. (a)  |
| 11. (c) | 12. (c)  | 13. (d)   | 14. (a)  | 15. (a)  | 16. (d)   | 17. (*) | 18. (*)   | 19. (c)  | 20. (c)  |
| 21. (7) | 22. (30) | 23. (543) | 24. (14) | 25. (60) | 26. (2)   | 27. (3) | 28. (120) | 29. (50) | 30. (15) |

## 27 AUGUST SHIFT I

### Section A : Objective Type Questions

1. A uniformly charged disc of radius  $R$  having surface charge density  $\sigma$  is placed in the  $xy$ -plane with its centre at the origin. Find the electric field intensity along the  $Z$ -axis at a distance  $Z$  from origin

a.  $E = \frac{\sigma}{2\epsilon_0} \left(1 - \frac{Z}{\sqrt{Z^2 + R^2}}\right)$       b.  $E = \frac{\sigma}{2\epsilon_0} \left(1 + \frac{Z}{\sqrt{Z^2 + R^2}}\right)$

c.  $E = \frac{2\epsilon_0}{\sigma} \left(\frac{1}{\sqrt{Z^2 + R^2}} + Z\right)$       d.  $E = \frac{\sigma}{2\epsilon_0} \left(\frac{1}{\sqrt{Z^2 + R^2}} + \frac{1}{Z^2}\right)$

2. There are  $10^{10}$  radioactive nuclei in a given radioactive element. Its half-life time is 1 min.

How many nuclei will remain after 30 s? ( $\sqrt{2} = 1.414$ )

- a.  $2 \times 10^{10}$       b.  $7 \times 10^9$       c.  $10^5$       d.  $4 \times 10^{10}$

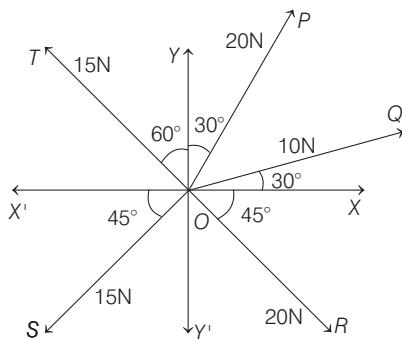
3. Which of the following is not a dimensionless quantity?

- a. Relative magnetic permeability ( $\mu_r$ )  
b. Power factor  
c. Permeability of free space ( $\mu_0$ )  
d. Quality factor

4. If  $E$  and  $H$  represent the intensity of electric field and magnetising field respectively, then the unit of  $E/H$  will be  
 a. ohm      b. mho      c. joule      d. newton

5. The resultant of these forces  $\vec{OP}$ ,  $\vec{OQ}$ ,  $\vec{OR}$ ,  $\vec{OS}$  and  $\vec{OT}$  is approximately ..... N.

[Take,  $\sqrt{3} = 1.7$ ,  $\sqrt{2} = 1.4$  and given  $\hat{i}$  and  $\hat{j}$  unit vectors along  $X, Y$  axis]



- a.  $9.25\hat{i} + 5\hat{j}$       b.  $3\hat{i} + 15\hat{j}$       c.  $2.5\hat{i} - 14.5\hat{j}$       d.  $-1.5\hat{i} - 15.5\hat{j}$

6. A balloon carries a total load of 185 kg at normal pressure and temperature of  $27^\circ\text{C}$ . What load will the balloon carry on rising to a height at which the barometric pressure is 45 cm of Hg and the temperature is  $-7^\circ\text{C}$ ? [Assuming, the volume constant.]

- a. 181.46 kg      b. 214.15 kg      c. 219.07 kg      d. 123.54 kg

7. An object is placed beyond the centre of curvature  $C$  of the given concave mirror. If the distance of the object is  $d_1$  from  $C$  and the distance of the image formed is  $d_2$  from  $C$ , the radius of curvature of this mirror is

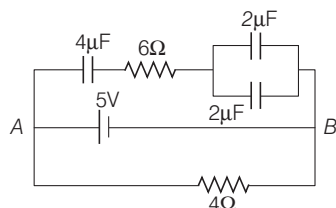
- a.  $\frac{2dd_2}{d_1 - d_2}$       b.  $\frac{2dd_2}{d_1 + d_2}$       c.  $\frac{dd_2}{d_1 + d_2}$       d.  $\frac{dd_2}{d_1 - d_2}$

8. A huge circular arc of length 4.4 ly subtends an angle  $4s$  at the centre of the circle. How long it would take for a body to complete 4 rev if its speed is 8 AU per sec?

[Given, 1 ly =  $9.46 \times 10^{15}$  m, 1 AU =  $1.5 \times 10^{11}$  m]

- a.  $4.1 \times 10^8$  s      b.  $4.5 \times 10^{10}$  s      c.  $3.5 \times 10^6$  s      d.  $7.2 \times 10^8$  s

9. Calculate the amount of charge on capacitor of  $4\mu\text{F}$ . The internal resistance of battery is  $1\Omega$ .



- a.  $8\mu\text{C}$       b. zero      c.  $16\mu\text{C}$       d.  $4\mu\text{C}$

10. Moment of inertia of a square plate of side  $l$  about the axis passing through one of the corner and perpendicular to the plane of square plate is given by

- a.  $\frac{Ml^2}{6}$       b.  $Ml^2$       c.  $\frac{Ml^2}{12}$       d.  $\frac{2}{3}Ml^2$

11. For a transistor in  $CE$  mode to be used as an amplifier, it must be operated in

- a. both cut-off and saturation      b. saturation region only  
 c. cut-off region only      d. the active region only

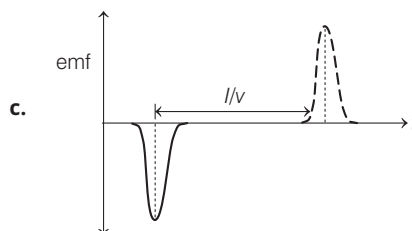
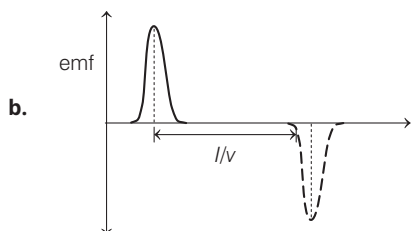
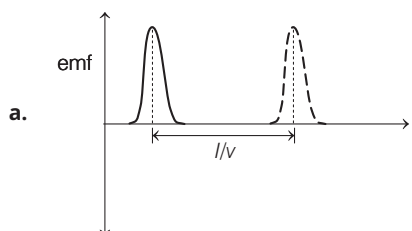
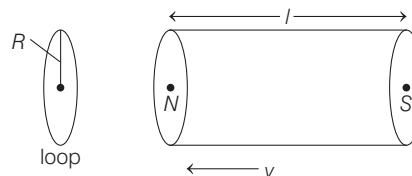
12. An ideal gas is expanding such that  $pT^3 = \text{constant}$ . The coefficient of volume expansion of the gas is

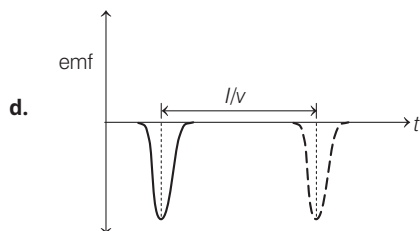
- a.  $1/T$       b.  $2/T$       c.  $4/T$       d.  $3/T$

13. In a photoelectric experiment, increasing the intensity of incident light

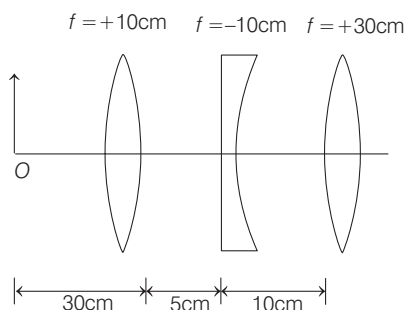
- a. increases the number of photons incident and also increases the KE of the ejected electrons.  
 b. increases the frequency of photons incident and increases the KE of the ejected electrons.  
 c. increases the frequency of photons incident and the KE of the ejected electrons remains unchanged.  
 d. increases the number of photons incident and the KE of the ejected electrons remains unchanged.

14. A bar magnet is passing through a conducting loop of radius  $R$  with velocity  $v$ . The radius of the bar magnet is such that it just passes through the loop. The induced emf in the loop can be represented by the approximate curve

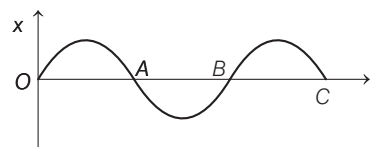




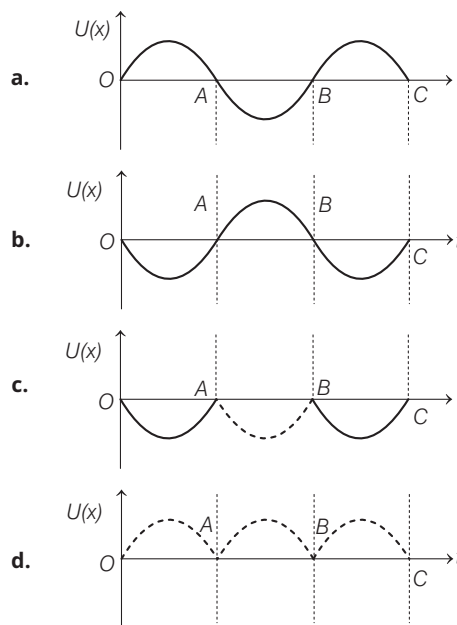
15. Two ions of masses 4 amu and 16 amu have charges  $+2e$  and  $+3e$ , respectively. These ions pass through the region of constant perpendicular magnetic field. The kinetic energy of both ions is same. Then,
- lighter ion will be deflected less than heavier ion
  - lighter ion will be deflected more than heavier ion
  - both ions will be deflected equally
  - no ion will be deflected
16. Find the distance of the image from object  $O$ , formed by the combination of lenses in the figure.



- 75 cm
  - 10 cm
  - 20 cm
  - infinity
17. In Millikan's oil drop experiment, what is viscous force acting on an uncharged drop of radius  $2.0 \times 10^{-5}$  m and density  $1.2 \times 10^3 \text{ kg m}^{-3}$ ? Take viscosity of liquid  $= 1.8 \times 10^{-5} \text{ N s m}^{-2}$ . (Neglect buoyancy due to air).
- $3.8 \times 10^{-11} \text{ N}$
  - $3.9 \times 10^{-10} \text{ N}$
  - $1.8 \times 10^{-10} \text{ N}$
  - $5.8 \times 10^{-10} \text{ N}$
18. Electric field in a plane electromagnetic wave is given by  $E = 50 \sin(500x - 10 \times 10^{10}t) \text{ V/m}$ . The velocity of electromagnetic wave in this medium is (Given,  $c$  = speed of light in vacuum)
- $\frac{3}{2}c$
  - $c$
  - $\frac{2}{3}c$
  - $\frac{c}{2}$
19. Five identical cells each of internal resistance  $1 \Omega$  and emf  $5 \text{ V}$  are connected in series and in parallel with an external resistance  $R$ . For what value of  $R$ , current in series and parallel combination will remain the same?
- $1 \Omega$
  - $25 \Omega$
  - $5 \Omega$
  - $10 \Omega$
20. The variation of displacement with time of a particle executing free simple harmonic motion is shown in the figure.

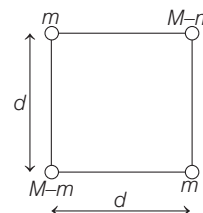


The potential energy  $U(x)$  versus time ( $t$ ) plot of the particle is correctly shown in figure :



## Section B : Numerical Type Questions

21. A body of mass  $2M$  splits into four masses  $\{m, M - m, m, M - m\}$ , which are rearranged to form a square as shown in the figure. The ratio of  $\frac{M}{m}$  for which, the gravitational potential energy of the system becomes maximum is  $x : 1$ . The value of  $x$  is..... .



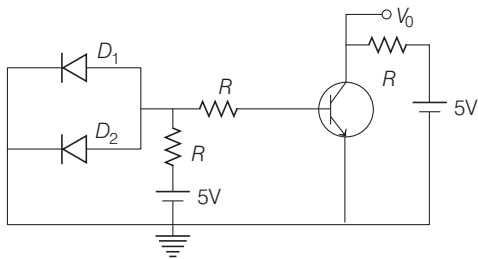
22. The alternating current is given by

$$i = \left\{ \sqrt{42} \sin\left(\frac{2\pi}{T}t\right) + 10 \right\} \text{ A}$$

The rms value of this current is ..... A.

23. A uniform conducting wire of length is  $24a$ , and resistance  $R$  is wound up as a current carrying coil in the shape of an equilateral triangle of side  $a$  and then in the form of a square of side  $a$ . The coil is connected to a voltage source  $V_0$ . The ratio of magnetic moment of the coils in case of equilateral triangle to that for square is  $1 : \sqrt{y}$ . The value of where  $y$  is ..... .

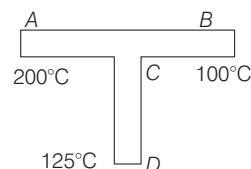
24. A circuit is arranged as shown in figure. The output voltage  $V_0$  is equal to ..... V.



25. First, a set of  $n$  equal resistors of  $10\ \Omega$  each are connected in series to a battery of emf  $20\text{ V}$  and internal resistance  $10\ \Omega$ . A current  $I$  is observed to flow. Then, the  $n$  resistors are connected in parallel to the same battery. It is observed that the current is increased 20 times, then the value of  $n$  is .....
26. Two cars  $X$  and  $Y$  are approaching each other with velocities  $36\text{ km/h}$  and  $72\text{ km/h}$  respectively. The frequency of a whistle sound as emitted by a passenger in car  $X$ , heard by the passenger in car  $Y$  is  $1320\text{ Hz}$ . If the velocity of sound in air is  $340\text{ m/s}$ , the actual frequency of the whistle sound produced is ..... Hz.

27. If the velocity of a body related to displacement  $x$  is given by  $v = \sqrt{5000 + 24x}\text{ m/s}$ , then the acceleration of the body is .....  $\text{m/s}^2$ .

28. A rod  $CD$  of thermal resistance  $10.0\text{ kW}^{-1}$  is joined at the middle of an identical rod  $AB$  as shown in figure. The end  $A, B$  and  $D$  are maintained at  $200^\circ\text{C}$ ,  $100^\circ\text{C}$  and  $125^\circ\text{C}$  respectively. The heat current in  $CD$  is  $P$  watt. The value of  $P$  is .....



29. Two persons  $A$  and  $B$  perform same amount of work in moving a body through a certain distance  $d$  with application of forces acting at angle  $45^\circ$  and  $60^\circ$  with the direction of displacement respectively. The ratio of force applied by person  $A$  to the force applied by person  $B$  is  $1/\sqrt{x}$ . The value of  $x$  is .....
30. A transmitting antenna has a height of  $320\text{ m}$  and that of receiving antenna is  $2000\text{ m}$ . The maximum distance between them for satisfactory communication in line of sight mode is  $d$ . The value of  $d$  is ..... km.

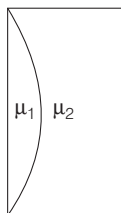
## Answers

- |         |          |         |         |          |            |          |         |         |           |
|---------|----------|---------|---------|----------|------------|----------|---------|---------|-----------|
| 1. (a)  | 2. (b)   | 3. (c)  | 4. (a)  | 5. (a)   | 6. (d)     | 7. (a)   | 8. (b)  | 9. (a)  | 10. (d)   |
| 11. (d) | 12. (c)  | 13. (d) | 14. (c) | 15. (b)  | 16. (a)    | 17. (b)  | 18. (c) | 19. (a) | 20. (d)   |
| 21. (2) | 22. (11) | 23. (3) | 24. (5) | 25. (20) | 26. (1210) | 27. (12) | 28. (2) | 29. (2) | 30. (224) |

## 27 AUGUST SHIFT II

### Section A : Objective Type Questions

1. Curved surfaces of a plano-convex lens of refractive index  $\mu_1$  and a plano-concave lens of refractive index  $\mu_2$  have equal radius of curvature as shown in figure. Find the ratio of radius of curvature to the focal length of the combined lenses.



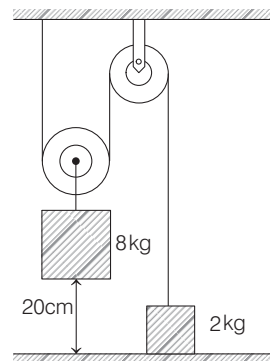
a.  $\frac{1}{\mu_2 - \mu_1}$

c.  $\frac{1}{\mu_1 - \mu_2}$

b.  $\mu_1 - \mu_2$

d.  $\mu_2 - \mu_1$

2. The boxes of masses  $2\text{ kg}$  and  $8\text{ kg}$  are connected by a massless string passing over smooth pulleys. Calculate the time taken by box of mass  $8\text{ kg}$  to strike the ground starting from rest. (Use,  $g = 10\text{ m/s}^2$ )



- a.  $0.34\text{ s}$       b.  $0.2\text{ s}$       c.  $0.25\text{ s}$       d.  $0.4\text{ s}$

3. For a transistor  $\alpha$  and  $\beta$  are given as  $\alpha = \frac{I_C}{I_E}$  and  $\beta = \frac{I_C}{I_B}$ .

Then, the correct relation between  $\alpha$  and  $\beta$  will be

- a.  $\alpha = \frac{1-\beta}{\beta}$     b.  $\beta = \frac{\alpha}{1-\alpha}$     c.  $\alpha\beta = 1$     d.  $\alpha = \frac{\beta}{1-\beta}$

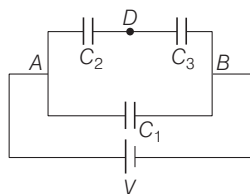
4. Water drops are falling from a nozzle of a shower onto the floor, from a height of 9.8 m. The drops fall at a regular interval of time. When the first drop strikes the floor, at that instant, the third drop begins to fall. Locate the position of second drop from the floor when the first drop strikes the floor.

- a. 4.18 m    b. 2.94 m    c. 2.45 m    d. 7.35 m

5. Two discs have moments of inertia  $I_1$  and  $I_2$  about their respective axes perpendicular to the plane and passing through the centre. They are rotating with angular speeds,  $\omega_1$  and  $\omega_2$  respectively and are brought into contact face to face with their axes of rotation co-axial. The loss in kinetic energy of the system in the process is given by

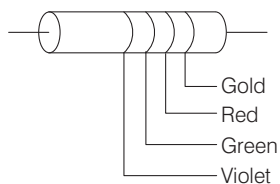
- a.  $\frac{I_1 I_2}{(I_1 + I_2)} (\omega_1 - \omega_2)^2$     b.  $\frac{(I_1 - I_2)^2 \omega_1 \omega_2}{2(I_1 + I_2)}$   
c.  $\frac{I_1 I_2}{2(I_1 + I_2)} (\omega_1 - \omega_2)^2$     d.  $\frac{(\omega_1 - \omega_2)^2}{2(I_1 + I_2)}$

6. Three capacitors  $C_1 = 2\mu\text{F}$ ,  $C_2 = 6\mu\text{F}$  and  $C_3 = 12\mu\text{F}$  are connected as shown in figure. Find the ratio of the charges on capacitors  $C_1$ ,  $C_2$  and  $C_3$ , respectively.



- a. 2 : 1 : 1    b. 2 : 3 : 3  
c. 1 : 2 : 2    d. 3 : 4 : 4

7. The colour coding on a carbon resistor is shown in the given figure. The resistance value of the given resistor is



- a.  $(5700 \pm 285)\Omega$     b.  $(7500 \pm 750)\Omega$   
c.  $(5700 \pm 375)\Omega$     d.  $(7500 \pm 375)\Omega$

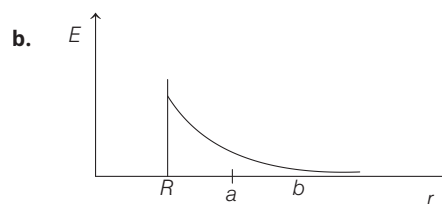
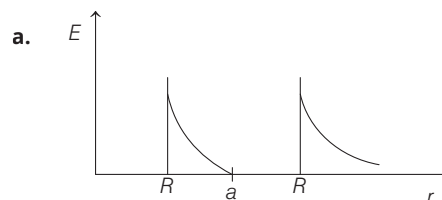
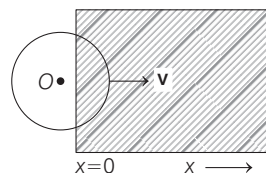
8. An antenna is mounted on a 400 m tall building. What will be the wavelength of signal that can be radiated effectively by the transmission tower upto a range of 44 km?

- a. 37.8 m    b. 605 m    c. 75.6 m    d. 302 m

9. If the rms speed of oxygen molecules at  $0^\circ\text{C}$  is 160 m/s, find the rms speed of hydrogen molecules at  $0^\circ\text{C}$ .

- a. 640 m/s    b. 40 m/s    c. 80 m/s    d. 332 m/s

10. A constant magnetic field of 1 T is applied in the  $x > 0$  region. A metallic circular ring of radius 1 m is moving with a constant velocity of 1 m/s along the X-axis. At  $t = 0$  s, the centre of O of the ring is at  $x = -1$  m. What will be the value of the induced emf in the ring at  $t = 1$  s? (Assume the velocity of the ring does not change.)



- a. 1 V    b.  $2\pi$  V    c. 2 V    d. 0

11. A mass of 50 kg is placed at the centre of a uniform spherical shell of mass 100 kg and radius 50 m. If the gravitational potential at a point, 25 m from the centre is  $V$  kg/m. The value of  $V$  is

- a. -60 G    b. +2 G    c. -20 G    d. -4 G

12. For full scale deflection of total 50 divisions, 50 mV voltage is required in galvanometer. The resistance of galvanometer if its current sensitivity is 2 div/mA will be

- a. 1  $\Omega$     b. 5  $\Omega$     c. 4  $\Omega$     d. 2  $\Omega$

13. A monochromatic neon lamp with wavelength of 670.5 nm illuminates a photo-sensitive material which has a stopping voltage of 0.48 V. What will be the stopping voltage if the source light is changed with another source of wavelength of 474.6 nm?

- a. 0.96 V    b. 1.25 V    c. 0.24 V    d. 1.5 V

14. Match List-I with List-II.

List-I	List-II
A. $R_H$ (Rydberg constant)	1. $\text{kg m}^{-1}\text{s}^{-1}$
B. $h$ (Planck's constant)	2. $\text{kg m}^2\text{s}^{-1}$
C. $\mu_B$ (Magnetic field energy density)	3. $\text{m}^{-1}$
D. $\eta$ (Coefficient of viscosity)	4. $\text{kg m}^{-1}\text{s}^{-2}$

Choose the most appropriate answer from the options given below.

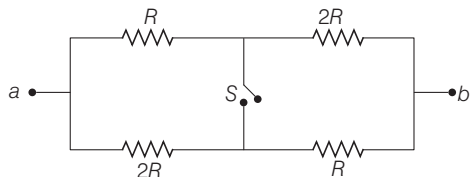
- |      |   |   |   |      |   |   |   |
|------|---|---|---|------|---|---|---|
| A    | B | C | D | A    | B | C | D |
| a. 2 | 3 | 4 | 1 | b. 3 | 2 | 4 | 1 |
| c. 4 | 2 | 1 | 3 | d. 3 | 2 | 1 | 4 |



- 

- 27.** An AC circuit has an inductor and a resistor of resistance  $R$  in series, such that  $X_L = 3R$ . Now, a capacitor is added in series such that  $X_C = 2R$ . The ratio of new power factor with the old power factor of the circuit is  $\sqrt{5} : x$ . The value of  $x$  is.

28. The ratio of the equivalent resistance of the network (shown in figure) between the points  $a$  and  $b$  when switch is open and switch is closed is  $x : 8$ . The value of  $x$  is



29. A plane electromagnetic wave with frequency of 30 MHz travels in free space. At particular point in space and time, electric field is 6 V/m. The magnetic field at this point will be  $x \times 10^{-8}$  T. The value of  $x$  is.
30. A tuning fork is vibrating at 250 Hz. The length of the shortest closed organ pipe that will resonate with the tuning fork will be ..... cm.  
(Take, speed of sound in air as  $340 \text{ ms}^{-1}$ )

## Answers

1. (b)	2. (d)	3. (b)	4. (d)	5. (c)	6. (c)	7. (d)	8. (b)	9. (a)	10. (c)
11. (d)	12. (d)	13. (b)	14. (b)	15. (a)	16. (a)	17. (a)	18. (c)	19. (d)	20. (d)
21. (500)	22. (1)	23. (15)	24. (20)	25. (40)	26. (400)	27. (1)	28. (9)	29. (2)	30. (34)

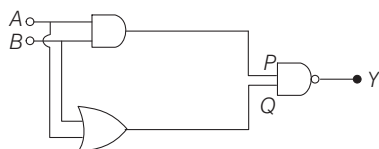
## 31 AUGUST SHIFT I

### Objective Type Questions

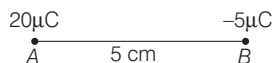
1. A helicopter is flying horizontally with a speed  $v$  at an altitude  $h$  has to drop a food packet for a man on the ground. What is the distance of helicopter from the man when the food packet is dropped?

a.  $\sqrt{\frac{2ghv^2 + 1}{h^2}}$       b.  $\sqrt{2ghv^2 + h^2}$   
c.  $\sqrt{\frac{2v^2h}{g} + h^2}$       d.  $\sqrt{\frac{2gh}{v^2} + h^2}$

2. In the following logic circuit, the sequence of the inputs  $A, B$  are (0, 0), (0, 1), (1, 0) and (1, 1). The output  $Y$  for this sequence will be



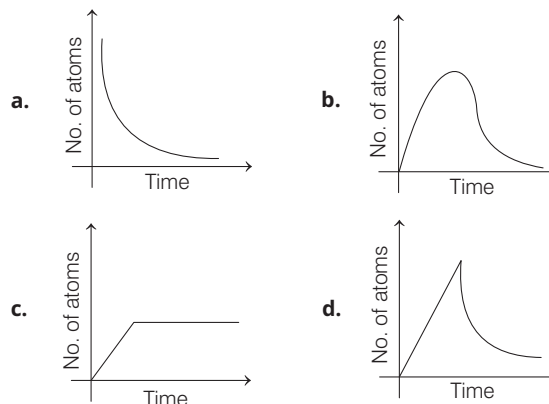
- a. 1, 0, 1, 0      b. 0, 1, 0, 1  
c. 1, 1, 1, 0      d. 0, 0, 1, 1
3. Two particles  $A$  and  $B$  having charges  $20 \mu\text{C}$  and  $-5 \mu\text{C}$  respectively are held fixed with a separation of 5 cm. At what position a third charged particle should be placed, so that it does not experience a net electric force?



- a. At 5 cm from  $20 \mu\text{C}$  on the left side of system  
b. At 5 cm from  $-5 \mu\text{C}$  on the right side  
c. At 1.25 cm from  $-5 \mu\text{C}$  between two charges  
d. At mid-point between two charges

4. A reversible engine has an efficiency of  $\frac{1}{4}$ . If the temperature of the sink is reduced by  $58^\circ\text{C}$ , its efficiency becomes double. Calculate the temperature of the sink.  
a.  $174^\circ\text{C}$       b.  $280^\circ\text{C}$   
c.  $180.4^\circ\text{C}$       d.  $382^\circ\text{C}$
5. An object is placed at the focus of concave lens having focal length  $f$ . What is the magnification and distance of the image from the optical centre of the lens?  
a. 1,  $\infty$       b. Very high,  $\infty$   
c.  $\frac{1}{2}$ ,  $\frac{f}{2}$       d.  $\frac{1}{4}$ ,  $\frac{f}{4}$
6. A sample of a radioactive nucleus  $A$  disintegrates to another radioactive nucleus  $B$ , which in turn disintegrates to some other stable nucleus  $C$ . Plot of a graph showing the variation of number of atoms of nucleus  $B$  versus time is

(Assume that at  $t = 0$ , there are no  $B$  atoms in the sample)



7. A coil having  $N$  turns is wound tightly in the form of a spiral with inner and outer radii  $a$  and  $b$ , respectively. Find the magnetic field at centre, when a current  $I$  passes through coil

a.  $\frac{\mu_0 I N}{2(b-a)} \ln\left(\frac{b}{a}\right)$       b.  $\frac{\mu_0 I}{8} \ln\left[\frac{a+b}{a-b}\right]$   
 c.  $\frac{\mu_0 I}{4(a-b)} \ln\left[\frac{1}{a} - \frac{1}{b}\right]$       d.  $\frac{\mu_0 I}{8} \ln\left(\frac{a-b}{a+b}\right)$

8. A body of mass  $M$  moving at speed  $v_0$  collides elastically with a mass  $m$  at rest. After the collision, the two masses move at angles  $\theta_1$  and  $\theta_2$  with respect to the initial direction of motion of the body of mass  $M$ . The largest possible value of the ratio  $M/m$ , for which the angles  $\theta_1$  and  $\theta_2$  will be equal, is

a. 4      b. 1      c. 3      d. 2

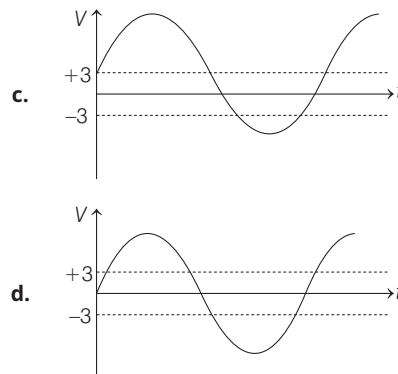
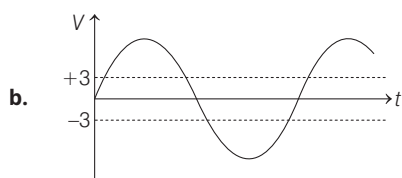
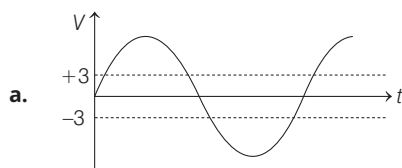
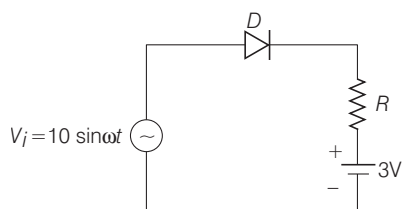
9. The masses and radii of the Earth and Moon are  $(m_1, R_1)$  and  $(m_2, R_2)$ , respectively. Their centres are at a distance  $r$  apart. Find the minimum escape velocity for a particle of mass  $m$  to be projected from the middle of these two masses.

a.  $v = \frac{1}{2} \sqrt{\frac{4G(m_1 + m_2)}{r}}$       b.  $v = \sqrt{\frac{4G(m_1 + m_2)}{r}}$   
 c.  $v = \frac{1}{2} \sqrt{\frac{2G(m_1 + m_2)}{r}}$       d.  $v = \sqrt{2G(m_1 + m_2)/r}$

10. A small square loop of side  $a$  and one turn is placed inside a larger square loop of side  $b$  and one turn ( $b \gg a$ ). The two loops are coplanar with their centres coinciding. If a current  $I$  is passed in the square loop of side  $b$ , then the coefficient of mutual inductance between the two loops is

a.  $\frac{\mu_0}{4\pi} 8\sqrt{2} \frac{a^2}{b}$       b.  $\frac{\mu_0}{4\pi} 8\sqrt{2} \frac{a}{b}$       c.  $\frac{\mu_0}{4\pi} 8\sqrt{2} \frac{b^2}{a}$       d.  $\frac{\mu_0}{4\pi} 8\sqrt{2} \frac{b}{a}$

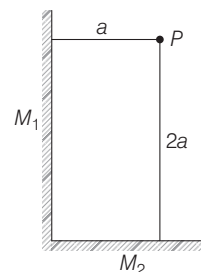
11. Choose the correct wave form that can represent the voltage across  $R$  of the following circuit, assuming the diode is ideal one.



12. A uniform heavy rod of weight  $10 \text{ kg ms}^{-2}$ , cross-sectional area  $100 \text{ cm}^2$  and length  $20 \text{ cm}$  is hanging from a fixed support. Young's modulus of the material of the rod is  $2 \times 10^{11} \text{ Nm}^{-2}$ . Neglecting the lateral contraction, find the elongation of rod due to its own weight.

a.  $2 \times 10^{-9} \text{ m}$       b.  $5 \times 10^{-8} \text{ m}$   
 c.  $4 \times 10^{-8} \text{ m}$       d.  $5 \times 10^{-10} \text{ m}$

13. Two plane mirrors  $M_1$  and  $M_2$  are at right angle to each other shown. A point source  $P$  is placed at  $a$  and  $2a$  meter away from  $M_1$  and  $M_2$ , respectively. The shortest distance between the images thus formed is (Take  $\sqrt{5} = 2.3$ )



a.  $3a$       b.  $4.6a$       c.  $2.3a$       d.  $2\sqrt{10}a$

14. Match List-I with List-II.

List-I	List-II
A. Torque	1. $\text{MLT}^{-1}$
B. Impulse	2. $\text{MT}^{-2}$
C. Tension	3. $\text{ML}^2\text{T}^{-2}$
D. Surface tension	4. $\text{MLT}^{-2}$

Choose the most appropriate answer from the options given below.

A	B	C	D	A	B	C	D
a. 3	1	4	2	b. 2	1	4	3
c. 1	3	4	2	d. 3	4	1	2

15. For an ideal gas the instantaneous change in pressure  $p$  with volume  $V$  is given by the equation  $\frac{dp}{dV} = -ap$ . If  $p = p_0$  at  $V = 0$  is the given boundary condition, then the maximum temperature one mole of gas can attain is (Here  $R$  is the gas constant)

a.  $\frac{p_0}{aeR}$       b.  $\frac{ap_0}{cR}$       c. infinity      d.  $0^\circ\text{C}$

16. Which of the following equations is dimensionally incorrect ?

Where,  $t$  = time,  $h$  = height,  $s$  = surface tension,  $\theta$  = angle,  $\rho$  = density,  $a, r$  = radius,  $g$  = acceleration due to gravity,  $V$  = volume,  $p$  = pressure,  $W$  = work done,  $\tau$  = torque,  $\epsilon$  = permittivity,  $E$  = electric field,  $J$  = current density,  $L$  = length.

a.  $V = \frac{\pi \rho a^4}{8\eta L}$                       b.  $h = \frac{2s \cos \theta}{\rho r g}$   
 c.  $J = \epsilon \frac{\partial E}{\partial t}$                       d.  $W = \tau \theta$

17. Angular momentum of a single particle moving with constant speed along circular path  
 a. changes in magnitude but remains same in the direction  
 b. remains same in magnitude and direction  
 c. remains same in magnitude but changes in the direction  
 d. is zero

18. In an AC-circuit, an inductor, a capacitor and a resistor are connected in series with  $X_L = R = X_C$ . Impedance of this circuit is  
 a.  $2R^2$                       b. Zero  
 c.  $R$                       d.  $R\sqrt{2}$

19. A moving proton and electron have the same de-Broglie wavelength. If  $k$  and  $p$  denote the KE and momentum, respectively. Then, choose the correct option.

a.  $K_p < K_e$  and  $p_p = p_e$                       b.  $K_p = K_e$  and  $p_p = p_e$   
 c.  $K_p < K_e$  and  $p_p < p_e$                       d.  $K_p > K_e$  and  $p_p = p_e$

20. Consider a galvanometer shunted with  $5 \Omega$  resistance and 2% of current passes through it. What is the resistance of the given galvanometer ?

a.  $300 \Omega$                       b.  $344 \Omega$   
 c.  $245 \Omega$                       d.  $226 \Omega$

## Section B : Numerical Type Questions

21. When a rubber ball is taken to a depth of ..... m in deep sea, its volume decreases by 0.5%. (The bulk modulus of rubber =  $9.8 \times 10^8 \text{ Nm}^{-2}$ . Density of sea water =  $10^3 \text{ kg m}^{-3}$ ,  $g = 9.8 \text{ m/s}^2$ )

22. A particle of mass 1 kg is hanging from a spring of force constant  $100 \text{ Nm}^{-1}$ . The mass is pulled slightly downward and released, so that it executes free simple harmonic motion with time period  $T$ . The time when the kinetic energy and potential energy of the system will become equal, is  $T/x$ . The value of  $x$  is.

23. If the sum of the heights of transmitting and receiving antennas in the line of sight of communication is fixed at 160 m, then the maximum range of LOS communication is ..... km.

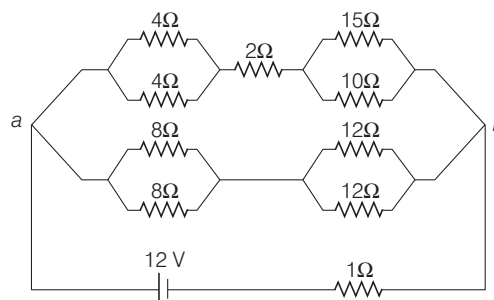
(Take, radius of Earth = 6400 km)

24. A square shaped wire with resistance of each side  $3 \Omega$  is bent to form a complete circle. The resistance between

two diametrically opposite points of the circle in unit of  $\Omega$  will be

25. A wire having a linear mass density  $9.0 \times 10^{-4} \text{ kg/m}$  is stretched between two rigid supports with a tension of 900 N. The wire resonates at a frequency of 500 Hz. The next higher frequency at which the same wire resonates is 550 Hz. The length of the wire is ..... m.

26. The voltage drop across  $15 \Omega$  resistance in the given figure will be ..... V.



27. A block moving horizontally on a smooth surface with a speed of  $40 \text{ ms}^{-1}$  splits into two equal parts. If one of the parts moves at  $60 \text{ ms}^{-1}$  in the same direction, then the fractional change in the kinetic energy will be  $x : 4$ , where  $x$  is

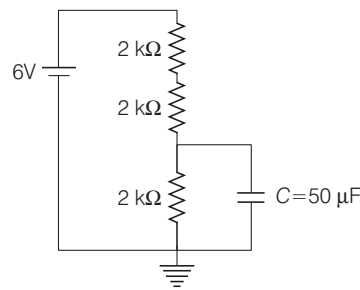
28. The electric field in an electromagnetic wave

is given by  $E = (50 \text{ NC}^{-1}) \sin \omega \left( t - \frac{x}{c} \right)$ .

The energy contained in a cylinder of volume  $V$  is  $5.5 \times 10^{-12} \text{ J}$ . The value of  $V$  is .....  $\text{cm}^3$ .

(Given  $\epsilon_0 = 8.85 \times 10^{-12} \text{ C}^2 \text{ N}^{-1} \text{ m}^{-2}$ ).

29. A capacitor of  $50 \mu\text{F}$  is connected in a circuit as shown in figure. The charge on the upper plate of the capacitor is .....  $\mu\text{C}$ .



30. A car is moving on a plane inclined at  $30^\circ$  to the horizontal with an acceleration of  $10 \text{ ms}^{-2}$  parallel to the plane upward. A bob is suspended by a string from the roof of the car. The angle in degrees which the string makes with the vertical is .....

(Take,  $g = 10 \text{ ms}^{-2}$ )

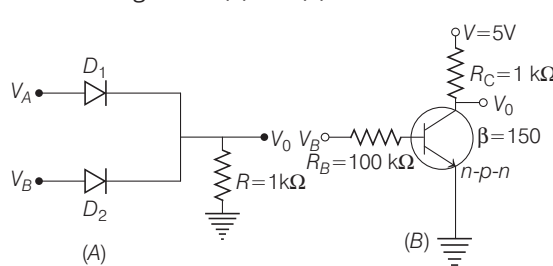
## Answers

- |           |         |          |         |          |         |         |           |           |          |
|-----------|---------|----------|---------|----------|---------|---------|-----------|-----------|----------|
| 1. (c)    | 2. (c)  | 3. (b)   | 4. (a)  | 5. (c)   | 6. (b)  | 7. (a)  | 8. (c)    | 9. (b)    | 10. (a)  |
| 11. (*)   | 12. (d) | 13. (b)  | 14. (a) | 15. (a)  | 16. (a) | 17. (b) | 18. (c)   | 19. (a)   | 20. (c)  |
| 21. (500) | 22. (8) | 23. (64) | 24. (3) | 25. (10) | 26. (6) | 27. (5) | 28. (500) | 29. (100) | 30. (30) |

**Note** (\*) None of the option is correct.

## 31 AUGUST SHIFT II

### Section A : Objective Type Questions

- Four identical hollow cylindrical columns of mild steel support a big structure of mass  $50 \times 10^3$  kg. The inner and outer radii of each column are 50 cm and 100 cm, respectively. Assuming, uniform local distribution, calculate the compression strain of each column. [Use,  $Y = 2.0 \times 10^{11}$  Pa,  $g = 9.8$  m/s<sup>2</sup>].  
 a.  $3.60 \times 10^{-8}$                       b.  $2.60 \times 10^{-7}$   
 c.  $1.87 \times 10^{-3}$                       d.  $7.07 \times 10^{-4}$
- A current of 1.5 A is flowing through a triangle, of side 9 cm each. The magnetic field at the centroid of the triangle is  
 (Assume that, the current is flowing in the clockwise direction.)  
 a.  $3 \times 10^{-7}$  T, outside the plane of triangle  
 b.  $2\sqrt{3} \times 10^{-7}$  T, outside the plane of triangle  
 c.  $2\sqrt{3} \times 10^{-5}$  T, inside the plane of triangle  
 d.  $3 \times 10^{-5}$  T, inside the plane of triangle
- A system consists of two identical spheres each of mass 1.5 kg and radius 50 cm at the end of light rod. The distance between the centres of the two spheres is 5 m. What will be the moment of inertia of the system about an axis perpendicular to the rod passing through its mid-point?  
 a.  $18.75 \text{ kgm}^2$   
 b.  $1.905 \times 10^5 \text{ kgm}^2$   
 c.  $19.05 \text{ kgm}^2$   
 d.  $1.875 \times 10^5 \text{ kgm}^2$
- Statement I** Two forces  $(\mathbf{P} + \mathbf{Q})$  and  $(\mathbf{P} - \mathbf{Q})$  where  $\mathbf{P} \perp \mathbf{Q}$ , when act at an angle  $\theta_1$  to each other, the magnitude of their resultant is  $\sqrt{3(P^2 + Q^2)}$ , when they act at an angle  $\theta_2$ , the magnitude of their resultant becomes  $\sqrt{2(P^2 + Q^2)}$ . This is possible only when  $\theta_1 < \theta_2$ .  
**Statement II** In the situation given above,  $\theta_1 = 60^\circ$  and  $\theta_2 = 90^\circ$ .  
 In the light of the above statements, choose the most appropriate answer from the options given below.  
 a. Statement I is false but statement II is true.  
 b. Both statement I and statement II are true.  
 c. Statement I is true but statement II is false.  
 d. Both statement I and statement II are false.
- A free electron of 2.6 eV energy collides with a  $\text{H}^+$  ion. This results in the formation of a hydrogen atom in the first excited state and a photon is released. Find the frequency of the emitted photon.  
 ( $h = 6.6 \times 10^{-34}$  Js)  
 a.  $1.45 \times 10^{16}$  MHz                      b.  $0.19 \times 10^{15}$  MHz  
 c.  $1.45 \times 10^9$  MHz                      d.  $9.0 \times 10^{27}$  MHz
- Two thin metallic spherical shells of radii  $r_1$  and  $r_2$  ( $r_1 < r_2$ ) are placed with their centres coinciding. A material of thermal conductivity  $K$  is filled in the space between the shells. The inner shell is maintained at temperature  $\theta_1$  and the outer shell at temperature  $\theta_2$  ( $\theta_1 < \theta_2$ ). The rate at which heat flows radially through the material is  
 a.  $\frac{4\pi K r_1 r_2 (\theta_2 - \theta_1)}{r_2 - r_1}$                       b.  $\frac{\pi r_1 r_2 (\theta_2 - \theta_1)}{r_2 - r_1}$   
 c.  $\frac{K (\theta_2 - \theta_1)}{r_2 - r_1}$                       d.  $\frac{K (\theta_2 - \theta_1) (r_2 - r_1)}{4\pi r_1 r_2}$
- If  $V_A$  and  $V_B$  are the input voltages (either 5V or 0V) and  $V_0$  is the output voltage then the two gates represented in the following circuit (A) and (B) are  

 a. AND and OR gate                      b. OR and NOT gate  
 c. NAND and NOR gate                      d. AND and NOT gate
- Consider two separate ideal gases of electrons and protons having same number of particles. The temperature of both the gases are same. The ratio of the uncertainty in determining the position of an electron to that of a proton is proportional to  
 a.  $\left(\frac{m_p}{m_e}\right)^{\frac{3}{2}}$                       b.  $\sqrt{\frac{m_e}{m_p}}$   
 c.  $\sqrt{\frac{m_p}{m_e}}$                       d.  $\frac{m_p}{m_e}$

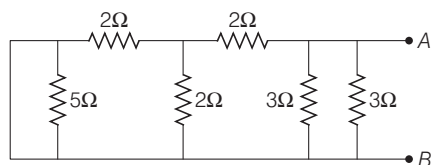
9. A bob of mass  $m$  suspended by a thread of length  $l$  undergoes simple harmonic oscillations with time period  $T$ . If the bob is immersed in a liquid that has density  $1/4$  times that of the bob and the length of the thread is increased by  $1/3$ rd of the original length, then the time period of the simple harmonic oscillations will be
- a.  $T$       b.  $\frac{3}{2}T$       c.  $\frac{3}{4}T$       d.  $\frac{4}{3}T$

10. **Statement I** If three forces  $\mathbf{F}_1$ ,  $\mathbf{F}_2$  and  $\mathbf{F}_3$  are represented by three sides of a triangle and  $\mathbf{F}_1 + \mathbf{F}_2 = -\mathbf{F}_3$ , then these three forces are concurrent forces and satisfy the condition for equilibrium.

**Statement II** A triangle made up of three forces  $\mathbf{F}_1$ ,  $\mathbf{F}_2$  and  $\mathbf{F}_3$  as its sides taken in the same order, satisfy the condition for translatory equilibrium.

In the light of the above statements, choose the most appropriate answer from the options given below.

- a. Statement I is false but statement II is true.  
b. Statement I is true but statement II is false.  
c. Both statement I and statement II are false.  
d. Both statement I and statement II are true.
11. If velocity  $[v]$ , time  $[T]$  and force  $[F]$  are chosen as the base quantities, the dimensions of the mass will be
- a.  $[FT^{-1}v^{-1}]$       b.  $[FTv^{-1}]$   
c.  $[FT^2v]$       d.  $[FvT^{-1}]$
12. The magnetic field vector of an electromagnetic wave is given by  $\mathbf{B} = B_0 \frac{\hat{i} + \hat{j}}{\sqrt{2}} \cos(kz - \omega t)T$  where  $\hat{i}$ ,  $\hat{j}$  represents unit vector along  $X$  and  $Y$ -axis respectively. At  $t = 0$ , two electric charges  $q_1$  of  $4\pi$  C and  $q_2$  of  $2\pi$  C located at  $(0, 0, \frac{\pi}{k})$  and  $(0, 0, \frac{3\pi}{k})$  respectively, have the same velocity of  $0.5c\hat{i}$ . (where,  $c$  is the velocity of light). The ratio of the force acting on charge  $q_1$  to  $q_2$  is
- a.  $2\sqrt{2}:1$       b.  $1:\sqrt{2}$       c.  $2:1$       d.  $\sqrt{2}:1$
13. The equivalent resistance of the given circuit between the terminals  $A$  and  $B$  is



- a. 0      b.  $3\Omega$       c.  $9/2\Omega$       d.  $1\Omega$
14. Choose the incorrect statement.
- A. The electric lines of force entering into a Gaussian surface provide negative flux.  
B. A charge  $q$  is placed at the centre of a cube. The flux through all the faces will be the same.  
C. In a uniform electric field net flux through a closed Gaussian surface containing no net charge is zero.  
D. When electric field is parallel to a Gaussian surface, it provides a finite non-zero flux.

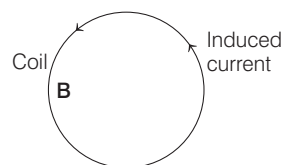
Choose the most appropriate answer from the options given below.

- a. (C) and (D)      b. (B) and (D)      c. Only (D)      d. (A) and (C)

15. A mixture of hydrogen and oxygen has volume  $500\text{ cm}^3$ , temperature  $300\text{ K}$ , pressure  $400\text{ kPa}$  and mass  $0.76\text{ g}$ . The ratio of masses of oxygen to hydrogen will be
- a. 3 : 8      b. 3 : 16      c. 16 : 3      d. 8 : 3

16. A block moving horizontally on a smooth surface with a speed of  $40\text{ m/s}$  splits into two parts with masses in the ratio of 1 : 2. If the smaller part moves at  $60\text{ m/s}$  in the same direction, then the fractional change in kinetic energy is
- a.  $1/3$       b.  $2/3$       c.  $1/8$       d.  $1/4$

17. A coil is placed in a magnetic field  $\mathbf{B}$  as shown below.



A current is induced in the coil because  $\mathbf{B}$  is

- a. outward and decreasing with time  
b. parallel to the plane of coil and decreasing with time  
c. outward and increasing with time  
d. parallel to the plane of coil and increasing with time
18. For a body executing SHM
- A. potential energy is always equal to its kinetic energy.  
B. average potential and kinetic energy over any given time interval are always equal.  
C. sum of the kinetic and potential energy at any point of time is constant.  
D. average kinetic energy in one time period is equal to average potential energy in one time period.
- Choose the most appropriate option from the options given below.
- a. (C) and (D)      b. Only (C)      c. (B) and (C)      d. Only (B)

19. **Statement I** To get a steady DC output from the pulsating voltage received from a full wave rectifier we can connect a capacitor across the output parallel to the load  $R_L$ .

**Statement II** To get a steady DC output from the pulsating voltage received from a full wave rectifier we can connect an inductor in series with  $R_L$ .

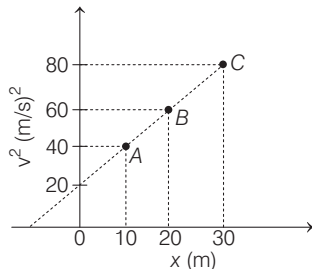
In the light of the above statements, choose the most appropriate answer from the options given below.

- a. Statement I is true but statement II is false.  
b. Statement I is false but statement II is true.  
c. Both statement I and statement II are false.  
d. Both statement I and statement II are true.
20. If  $R_E$  be the radius of Earth, then the ratio between the acceleration due to gravity at a depth  $r$  below and a height  $r$  above the Earth surface is (Given,  $r < R_E$ )
- a.  $1 - \frac{r}{R_E} - \frac{r^2}{R_E^2} - \frac{r^3}{R_E^3}$       b.  $1 + \frac{r}{R_E} + \frac{r^2}{R_E^2} + \frac{r^3}{R_E^3}$   
c.  $1 + \frac{r}{R_E} - \frac{r^2}{R_E^2} + \frac{r^3}{R_E^3}$       d.  $1 + \frac{r}{R_E} - \frac{r^2}{R_E^2} - \frac{r^3}{R_E^3}$



## Section B : Numerical Type Questions

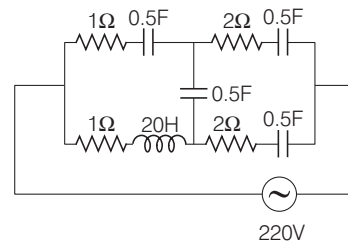
- 21.** A bandwidth of 6 MHz is available for AM transmission. If the maximum audio signal frequency used for modulating the carrier wave is not to exceed 6 kHz. The number of stations that can be broadcasted within this band simultaneously without interfering with each other will be .....
- 22.** A parallel plate capacitor of capacitance  $200\ \mu\text{F}$  is connected to a battery of 200 V. A dielectric slab of dielectric constant 2 is now inserted into the space between plates of capacitor while the battery remain connected. The change in the electrostatic energy in the capacitor will be ..... J.
- 23.** A long solenoid with 1000 turns/m has a core material with relative permeability 500 and volume  $10^3\text{cm}^3$ . If the core material is replaced by another material having relative permeability of 750 with same volume maintaining same current of 0.75 A in the solenoid, the fractional change in the magnetic moment of the core would be approximately  $\left(\frac{\chi}{499}\right)$ . Find the value of  $\chi$ .
- 24.** A particle is moving with constant acceleration  $a$ . Following graph shows  $v^2$  versus  $x$  (displacement) plot. The acceleration of the particle is .....  $\text{m/s}^2$



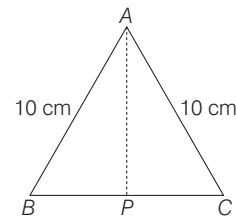
- 25.** In a Young's double slit experiment, the slits are separated by 0.3 mm and the screen is 1.5 m away from the plane of slits. Distance between fourth bright fringes on both sides of central bright is 2.4 cm. The frequency of light used is .....  $\times 10^{14}$  Hz.
- 26.** The diameter of a spherical bob is measured using a Vernier callipers. 9 divisions of the main scale, in the vernier calipers, are equal to 10 divisions of vernier scale.

One main scale division is 1 mm. The main scale reading is 10 mm and 8th division of vernier scale was found to coincide exactly with one of the main scale division. If the given vernier callipers has positive zero error of 0.04 cm, then the radius of the bob is .....  $\times 10^{-2}$  cm.

- 27.** A sample of gas with  $\gamma = 1.5$  is taken through an adiabatic process in which the volume is compressed from  $1200\text{ cm}^3$  to  $300\text{ cm}^3$ . If the initial pressure is 200 kPa. The absolute value of the work done by the gas in the process is ..... J.
- 28.** At very high frequencies, the effective impedance of the given circuit will be .....  $\Omega$ .



- 29.** Cross-section view of a prism is the equilateral triangle ABC in the figure. The minimum deviation is observed using this prism when the angle of incidence is equal to the prism angle. The time taken by light to travel from P (mid-point of BC) to A is .....  $\times 10^{-10}$  s.  
(Given, speed of light in vacuum =  $3 \times 10^8$  m/s and  $\cos 30^\circ = \frac{\sqrt{3}}{2}$ )



- 30.** A resistor dissipates 192 J of energy in 1 s when a current of 4 A is passed through it. Now, when the current is doubled, the amount of thermal energy dissipated in 5 s is ..... J.

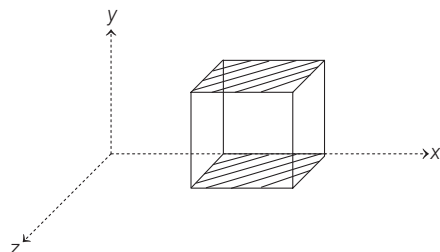
## Answers

- |           |         |           |         |         |          |           |         |         |            |
|-----------|---------|-----------|---------|---------|----------|-----------|---------|---------|------------|
| 1. (b)    | 2. (d)  | 3. (c)    | 4. (b)  | 5. (c)  | 6. (a)   | 7. (b)    | 8. (c)  | 9. (d)  | 10. (d)    |
| 11. (b)   | 12. (c) | 13. (d)   | 14. (c) | 15. (c) | 16. (c)  | 17. (a)   | 18. (a) | 19. (d) | 20. (d)    |
| 21. (500) | 22. (4) | 23. (250) | 24. (1) | 25. (5) | 26. (52) | 27. (480) | 28. (2) | 29. (5) | 30. (3840) |

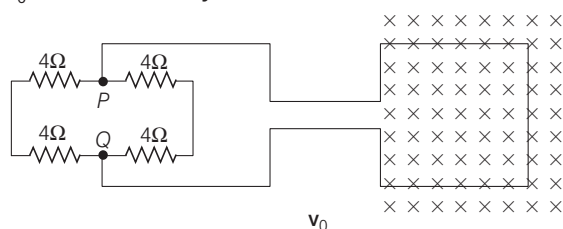
# 1 SEPTEMBER SHIFT II

## Section A : Objective Type Questions

1. A cube is placed inside an electric field,  $\mathbf{E} = 150y^2\hat{j}$ . The side of the cube is 0.5 m and is placed in the field as shown in the given figure. The charge inside the cube is

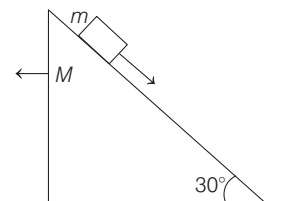


- a.  $3.8 \times 10^{-11} \text{ C}$       b.  $8.3 \times 10^{-11} \text{ C}$   
c.  $3.8 \times 10^{-12} \text{ C}$       d.  $8.3 \times 10^{-12} \text{ C}$
2. A square loop of side 20 cm and resistance  $1 \Omega$  is moved towards right with a constant speed  $v_0$ . The right arm of the loop is in a uniform magnetic field of 5 T. The field is perpendicular to the plane of the loop and is going into it. The loop is connected to a network of resistors each of value  $4 \Omega$ . What should be the value of  $v_0$ , so that a steady current of 2 mA flows in the loop?



- a. 1 m/s      b. 1 cm/s      c.  $10^2 \text{ m/s}$       d.  $10^{-2} \text{ cm/s}$
3. The temperature of an ideal gas in 3-dimensions is 300 K. The corresponding de-Broglie wavelength of the electron approximately at 300 K, is  
[ $m_e$  = mass of electron =  $9 \times 10^{-31} \text{ kg}$   
 $h$  = Planck's constant =  $6.6 \times 10^{-34} \text{ Js}$   
 $K_B$  = Boltzmann constant =  $1.38 \times 10^{-23} \text{ JK}^{-1}$ ]
- a. 6.26 nm      b. 8.46 nm      c. 2.26 nm      d. 3.25 nm
4. A body of mass  $m$  dropped from a height  $h$  reaches the ground with a speed of  $0.8\sqrt{gh}$ . The value of workdone by the air-friction is
- a.  $-0.68 mgh$       b.  $mgh$       c.  $1.64 mgh$       d.  $0.64 mgh$
5. The ranges and heights for two projectiles projected with the same initial velocity at angles  $42^\circ$  and  $48^\circ$  with the horizontal are  $R_1, R_2$  and  $H_1, H_2$ , respectively. Choose the correct option.
- a.  $R_1 > R_2$  and  $H_1 = H_2$       b.  $R_1 = R_2$  and  $H_1 < H_2$   
c.  $R_1 < R_2$  and  $H_1 < H_2$       d.  $R_1 = R_2$  and  $H_1 = H_2$

6. A block of mass  $m$  slides on the wooden wedge, which in turn slides backward on the horizontal surface. The acceleration of the block with respect to the wedge is [Given,  $m = 8 \text{ kg}$ ,  $M = 16 \text{ kg}$ ]



Assume all the surfaces shown in the figure to be frictionless.

- a.  $\frac{4}{3}g$       b.  $\frac{6}{5}g$       c.  $\frac{3}{5}g$       d.  $\frac{2}{3}g$

7. Due to cold weather a 1 m water pipe of cross-sectional area  $1 \text{ cm}^2$  is filled with ice at  $-10^\circ\text{C}$ . Resistive heating is used to melt the ice. Current of 0.5 A is passed through  $4 \text{ k}\Omega$  resistance. Assuming that, all the heat produced is used for melting, what is the minimum time required? [Given, latent heat of fusion for water/ice =  $333 \times 10^5 \text{ J kg}^{-1}$ , specific heat of ice =  $2 \times 10^3 \text{ J kg}^{-1}$  and density of ice =  $10^3 \text{ kg/m}^3$ ]

- a. 0.353 s      b. 35.3 s      c. 3.53 s      d. 70.6 s

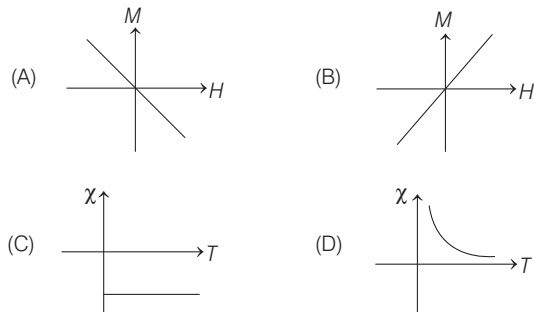
8. A student determined Young's modulus of elasticity using the formula  $Y = \frac{MgL^3}{4bd^3\delta}$ . The value of  $g$  is taken to be  $9.8 \text{ m/s}^2$ , without any significant error, his observations are as following.

Physical quantity	Least count of the equipment used for measurement	Observed value
Mass ( $M$ )	1 g	2 kg
Length of bar ( $L$ )	1 mm	1 m
Breadth of bar ( $b$ )	0.1 mm	4 cm
Thickness of bar ( $d$ )	0.01 mm	0.4 cm
Depression ( $\delta$ )	0.01 mm	5 mm

Then, the fractional error in the measurement of  $Y$  is

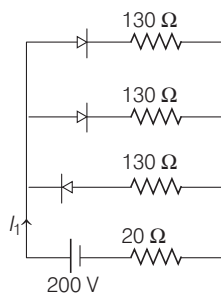
- a. 0.0083      b. 0.0155      c. 0.155      d. 0.083
9. Two resistors  $R_1 = (4 \pm 0.8) \Omega$  and  $R_2 = (4 \pm 0.4) \Omega$  are connected in parallel. The equivalent resistance of their parallel combination will be
- a.  $(4 \pm 0.4) \Omega$       b.  $(2 \pm 0.4) \Omega$   
c.  $(2 \pm 0.3) \Omega$       d.  $(4 \pm 0.3) \Omega$
10. The half life period of radioactive element  $x$  is same as the mean life time of another radioactive element  $y$ . Initially they have the same number of atoms. Then,
- a.  $x$  will decay faster than  $y$   
b.  $y$  will decay faster than  $x$   
c.  $x$  and  $y$  have same decay rate initially and later on different decay rate  
d.  $x$  and  $y$  decay at the same rate always

11. Following plots show magnetisation ( $M$ ) versus magnetising field ( $H$ ) and magnetic susceptibility ( $\chi$ ) versus temperature ( $T$ ) graph

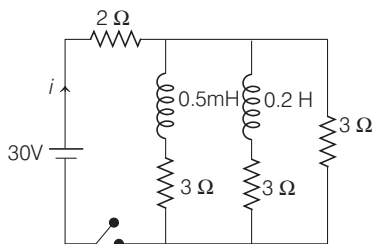


Which of the following combination will be represented by a diamagnetic material?

- a. (A) and (C)   b. (A) and (D)   c. (B) and (D)   d. (B) and (C)
12. A glass tumbler having inner depth of 17.5 cm is kept on a table. A student starts pouring water ( $\mu = 4/3$ ) into it while looking at the surface of water from the above. When he feels that the tumbler is half filled, he stops pouring water. Up to what height, the tumbler is actually filled?
- a. 11.7 cm   b. 10 cm   c. 7.5 cm   d. 8.75 cm
13. In the given figure, each diode has a forward bias resistance of  $30\ \Omega$  and infinite resistance in reverse bias. The current  $I_1$  will be

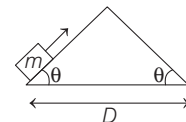


- a. 3.75 A   b. 2.35 A   c. 2 A   d. 2.73 A
14. For the given circuit the current  $i$  through the battery when the key is closed and the steady state has been reached is

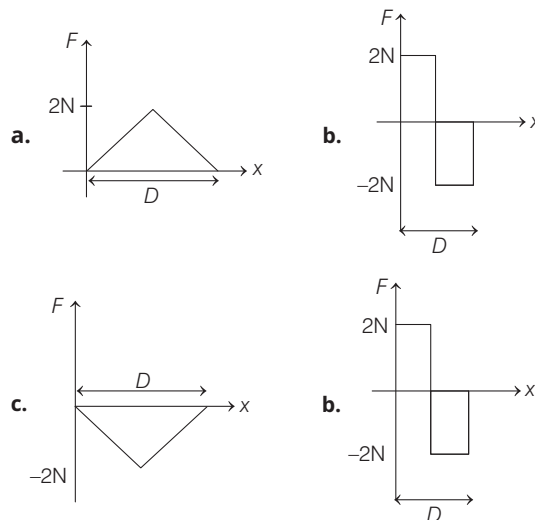


- a. 6 A   b. 25 A   c. 10 A   d. 0

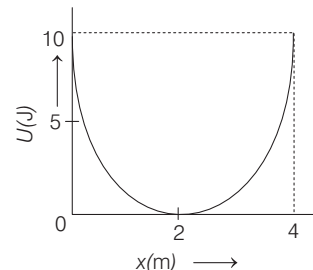
15. An object of mass  $m$  is being moved with a constant velocity under the action of an applied force of 2 N along a frictionless surface with following surface profile.



The correct applied force versus distance graph will be

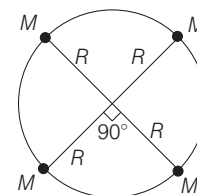


16. A mass of 5 kg is connected to a spring. The potential energy curve of the simple harmonic motion executed by the system is shown in the figure. A simple pendulum of length 4 m has the same period of oscillation as the spring system. What is the value of acceleration due to gravity on the planet where these experiments are performed?
- a.  $10\ \text{m/s}^2$    b.  $5\ \text{m/s}^2$    c.  $4\ \text{m/s}^2$    d.  $9.8\ \text{m/s}^2$
17. A capacitor is connected to a 20 V battery through a resistance of  $10\ \Omega$ . It is found that the potential difference across the capacitor rises to 2 V in  $1\ \mu\text{s}$ . The capacitance of the capacitor in .....  $\mu\text{F}$ . [Given,  $\ln\left(\frac{10}{9}\right) = 0.105$ ]



- a. 9.52   b. 0.95   c. 0.105   d. 1.85

18. Four particles each of mass  $M$ , move along a circle of radius  $R$  under the action of their mutual gravitational attraction as shown in figure. The speed of each particle is



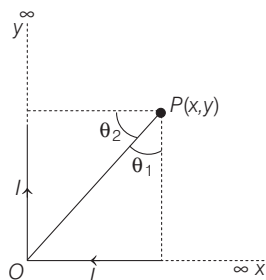
- a.  $\frac{1}{2}\sqrt{\frac{GM}{R(2\sqrt{2}+1)}}$    b.  $\frac{1}{2}\sqrt{\frac{GM}{R(2\sqrt{2}-1)}}$   
c.  $\frac{1}{2}\sqrt{\frac{GM}{R(2\sqrt{2}-1)}}$    d.  $\sqrt{\frac{GM}{R}}$

19. Electric field of plane electromagnetic wave propagating through a non-magnetic medium is given by  $E = 20\cos(2 \times 10^{10}t - 200x)$  V/m. The dielectric constant of the medium is equal to

(Take,  $\mu_r = 1$ )

- a. 9      b. 2      c. 1/3      d. 3

20. There are two infinitely long straight current carrying conductors and they are held at right angles to each other so that their common ends meet at the origin as shown in the figure given below. The ratio of current in both conductors is 1 : 1. The magnetic field at point P is



- a.  $\frac{\mu_0 I}{4\pi xy} [\sqrt{x^2 + y^2} + (x + y)]$       b.  $\frac{\mu_0 I}{4\pi xy} [\sqrt{x^2 + y^2} - (x + y)]$   
c.  $\frac{\mu_0 I xy}{4\pi} [\sqrt{x^2 + y^2} - (x + y)]$       d.  $\frac{\mu_0 I xy}{4\pi} [\sqrt{x^2 + y^2} + (x + y)]$

## Section B : Numerical Type Questions

21. The temperature of 3.00 mol of an ideal diatomic gas is increased by 40.0 °C without changing the pressure of the gas. The molecules in the gas rotate but do not oscillate. If the ratio of change in internal energy of the gas to the amount of workdone by the gas is  $\frac{x}{10}$ , then the value of x (round off to the nearest integer) is .....  
(Given,  $R = 8.31 \text{ J mol}^{-1} \text{ K}^{-1}$ )
22. The width of one of the two slits in a Young's double slit experiment is three times the other slit. If the amplitude of the light coming from a slit is proportional to the slit-width, the ratio of minimum to maximum intensity in the interference pattern is x : 4 where x is .....
23. Two satellites revolve around a planet in coplanar circular orbits in anti-clockwise direction. Their period of revolutions are 1 h and 8 h, respectively. The radius of the orbit of nearer satellite is  $2 \times 10^3 \text{ km}$ . The angular speed of the farther satellite as observed from the nearer satellite at the instant when both the satellites are closest is  $\frac{\pi}{x} \text{ rad h}^{-1}$ , where x is .....
24. When a body slides down from rest along a smooth inclined plane making an angle of 30° with the horizontal, it takes time T. When the same body slides down from the rest along a rough inclined plane making the same angle and through the same distance, it takes time  $\alpha T$ , where  $\alpha$  is a constant greater than 1. The coefficient of friction between the body and the rough plane is  $\frac{1}{\sqrt{x}} \left( \frac{\alpha^2 - 1}{\alpha^2} \right)$ , where x is .....
25. The average translational kinetic energy of  $\text{N}_2$  gas molecules at ..... °C becomes equal to the KE of an electron accelerated from rest through a potential difference of 0.1 V.  
[Given,  $K_B = 1.38 \times 10^{-23} \text{ J/K}$ ]
26. A uniform heating wire of resistance 36 Ω is connected across a potential difference of 240 V. The wire is then cut into half and potential difference of 240 V is applied across each half separately. The ratio of power dissipation in first case to the total power dissipation in the second case would be 1 : x, where x is .....
27. A steel rod with  $Y = 2.0 \times 10^{11} \text{ Nm}^{-2}$  and  $\alpha = 10^5 \text{ °C}^{-1}$  of length 4 m and area of cross-section  $10 \text{ cm}^2$  is heated from 0°C to 400°C without being allowed to extend. The tension produced in the rod is  $x \times 10^5 \text{ N}$ , where the value of x is .....
28. A 2 kg steel rod of length 0.6 m is clamped on a table vertically at its lower end and is free to rotate in vertical plane. The upper end is pushed so that the rod falls under gravity. Ignoring the friction due to clamping at its lower end, the speed of the free end of rod when it passes through its lowest position is .....  $\text{ms}^{-1}$ .  
(Take,  $g = 10 \text{ ms}^{-2}$ )
29. A carrier wave with amplitude of 250 V is amplitude modulated by a sinusoidal base band signal of amplitude 150 V. The ratio of minimum amplitude to maximum amplitude for the amplitude modulated wave is 50 : x, then value of x is .....
30. An engine is attached to a wagon through a shock absorber of length 1.5 m. The system with a total mass of 40000 kg is moving with a speed of  $72 \text{ kmh}^{-1}$ , when the brakes are applied to bring it to rest. In the process of the system being brought to rest, the spring of the shock absorber gets compressed by 1.0 m. If 90% of energy of the wagon is lost due to friction, the spring constant is .....  $\times 10^5 \text{ N/m}$ .

## Answers

- |          |         |         |         |           |         |         |         |         |          |
|----------|---------|---------|---------|-----------|---------|---------|---------|---------|----------|
| 1. (b)   | 2. (b)  | 3. (a)  | 4. (a)  | 5. (b)    | 6. (d)  | 7. (b)  | 8. (b)  | 9. (c)  | 10. (b)  |
| 11. (a)  | 12. (b) | 13. (c) | 14. (c) | 15. (b)   | 16. (c) | 17. (b) | 18. (b) | 19. (a) | 20. (a)  |
| 21. (25) | 22. (1) | 23. (3) | 24. (3) | 25. (500) | 26. (4) | 27. (8) | 28. (6) | 29. (4) | 30. (16) |