

PERCENTAGE

The term per cent means for every hundred. It can best be defined as :

“ A fraction, whose denominator is 100, is called a *percentage*, and the numerator of the fraction is called *the rate per cent*.”

Suppose, a man says that he gains forty per cent (40 %) profit after selling a watch. It means his profit is ₹ 40 for every hundred rupees.

So, by definition of the percentage, the meaning of 40 per cent of the percentage, the meaning of 40 per cent is 40/100.

To Convert Fraction into Percentage

Process : 1. Fraction is multiplied by 100.

2. Result (Fraction \times 100) takes sign of per cent (%) after it.

Therefore, Rule :

Value in % = (Fraction \times 100) %

Example :

	Value in fraction	Rule (Fraction \times 100) %	Value in per cent
1.	4/25	(4/25 \times 100) %	16 %
2.	2/3	(2/3 \times 100) %	66.66 %
3.	3/40	(3/40 \times 100) %	7.5 %

To Convert Percentage into Fraction

Process :

1. Given value or term is divided by 100.
2. Sign of per cent (%) is eliminated or removed.

Rule :

$$\text{Fraction} = \frac{\text{Digit of Per cent}}{100}$$

Example :

	Value in percentage	Rule $\left(\frac{\text{Digit of \%}}{100} \right)$	Fraction
1.	9 %	9/100	9/100
2.	0.3 %	0.3/100	3/1000
3.	36 %	36/100	9/25

To Convert Percentage into Decimal

Process :

1. Given value (in percentage) is divided by 100 and we take result in decimal.

2. Sign of per cent (%) is eliminated.

Example :

Value in per cent	Using Process	Value in decimal
0.03 %	0.03/100	= 0.0003

Rule : Short-cut Method to Convert Percentage into Decimal.

Decimal is placed at two digits from right to left side in given value eliminating sign of per cent (%).

Example : 25 %

According to rule, decimal will take place after two digits (5 and 2) from right to left. Thus decimal value of 25 % will be 0.25.

Other Example : 34 % = 0.34

126 % = 1.26

9 % = 0.09

(Here, second digit is '0')

To Convert Decimal into percentage

Process : 1. Given value is multiplied by 100.

2. Sign of per cent (%) is added after the product.

Rule :

$$\text{Value in per cent} = (\text{Value in decimal}) \times 100 \%$$

Example :

Value in decimal	Rule	Value in per cent
1. 0.218	$(0.218 \times 100) \%$	21.8 %

Memorable Point :

If Y % of X = Z, then $XY/100 = Z$

In above mathematical relation, there are three terms, X, Y and Z. If values of any two terms are known then we can obtain the value of rest term.

$$1. X = \frac{Z}{Y} \times 100 \quad 2. Y = \frac{Z}{X} \times 100$$

$$3. Z = \frac{X}{Y} \times 100$$

Example : 35 % of 160 + 60 % of 80 = ? % of 312

Solution : 35 % of 160 + 60 % of 80 = ? of 312

$$\Rightarrow 160 \times 35/100 + 80 \times 60/100 = ?/100 \times 312$$

$$\Rightarrow \frac{(56 + 48) \times 100}{312} = ?$$

$$\Rightarrow ? = \frac{100}{3} = 33 \frac{1}{3}$$

Facts To Remember

Remember the following results. Their direct use help in solving objective type problems on percentage.

Sl. No.	Value in %	Value in Fraction	Sl. No.	Value in %	Value in Fraction
1.	100%	1	11.	10 %	1/10
2.	50 %	1/2	12.	90 %	9/10
3.	25 %	1/4	13.	130 %	13/10
4.	20 %	1/5	14.	$6\frac{1}{4} \%$	1/16
5.	30 %	3/10	15.	$12\frac{1}{2} \%$	1/8
6.	40 %	2/5	16.	$37\frac{1}{2} \%$	3/8
7.	80 %	4/5	17.	$62\frac{1}{2} \%$	5/8
8.	120 %	6/5	18.	$66\frac{2}{3} \%$	2/3
9.	70 %	7/10	19.	$87\frac{1}{2} \%$	7/8
10.	1 %	1/100			

EXERCISE

1. $(?) \times 15 = 37.5 \%$ of 220

(a) 5.5 (b) 81.5

(c) 5.5 (d) 815

(e) None of these

2. 67 % of 89 ÷ 89 % of 67 = ?

(a) 5163 (b) 5963

(c) 0 (d) 1

(e) None of these

3. 80 % of 1200 + 40 % of 20 = ?

(a) 960 (b) 1760

(c) 968 (d) 96,800

(e) None of these

4. $0.75 + ? = 1350 \%$ of 50

(a) 746.25 (b) 674.25

(c) 576.25 (d) 467.25

(e) None of these

5. 10 % of ? = 0.101

(a) 10.1 (b) 0.101

(c) 101 (d) 1.01

(e) None of these

EXPLANATORY ANSWERS

1. (c) : In the given expression

$$? = 220 \times \frac{37.5}{100} \times \frac{1}{15} = 5.5$$

2. (d) : The given expression can be written as

$$? = 89 \times 67/100 \div 67 \times 89/100$$

$$= 89 \times 67/100 \times 100/67 \times 89 = 1$$

3. (c) : In the given expression

$$? = 1200 \times 80/100 + 20 \times 40/100$$

$$= 960 + 8 = 968.$$

4. (b) : In the given expression

$$? = 1350 \%$$
 of 50 – 0.75
$$= 1350/100 \times 50 - 0.75$$

$$= 675 - 0.75$$

$$= 674.25.$$

5. (d) : Given expression can be written as

$$? \times 10/100 = 0.101$$

$$\Rightarrow ? = \frac{0.101 \times 100}{10} = 1.01.$$

Some Special Rules For Quantitative Questions

Rule I :

First time $X\%$ is increased and second time $X\%$ is decreased, then loss $\% = [X^2/100]\%$

Example : The price of a book is increased by 30% and after some days decreased by 30%. Decreased or increase per cent is :

- (a) 0.0009% increase (b) 0.09% decrease
(c) 90% decrease (d) 9% increase
(e) None of these

Solution : (e) Loss $\% = [(30)^2/100] = 9\%$.

Rule II :

In price increase of $x\%$ reduced per cent to have no extra expenditure $= [x/(100 + x) \times 100] \%$

Example : If the price of milk is increased by 1%, how much per cent must a man reduce his consumption of milk to have no extra expenditure?

- (a) 100/101 % (b) 101/100 %
(c) 1/101 % (d) 1 %
(e) None of these

Solution. (a) : Reduced per cent
 $= [1/100 + 1 \times 100]\% = 100/101\%$.

Rule III :

(1) If P 's salary is $r\%$ more than Q 's, then Q 's salary less than P 's

$$= \left[\frac{r}{(100 + r)} \times 100 \right] \%$$

(2) If P 's salary is $r\%$ less than Q 's, then Q 's salary more than P 's

$$= \left[\frac{r}{(100 - r)} \times 100 \right] \%$$

Example : P 's salary is 50 % below Q 's. How much per cent is Q 's salary above P 's ?

- (a) 0 % (b) $16\frac{2}{3}\%$
(c) 50 % (d) 100 %
(e) None of these

Solution. (d) : Q 's salary above P 's

$$= \left[\frac{50}{(100 - 50)} \times 100 \right] \% = 100 \%$$

Rule IV :

In price decrease of $x\%$, increase per cent in consumption to maintain same expenditure

$$= \left[\frac{x}{(100 - x)} \times 100 \right] \%$$

Example : The price of sugar is reduced by 40 %. Find by how much per cent must its consumption be increased so that the expenditure remains the same as before?

- (a) 45 % (b) $66\frac{2}{3}\%$
(c) $16\frac{2}{3}\%$ (d) $33\frac{1}{3}\%$
(e) None of these

Solution. (b) : Increase per cent

$$= \left[\frac{40}{100 - 40} \times 100 \right] \% = \frac{200}{3} \% = 66\frac{2}{3} \%$$

Rule V :

First time $x\%$ is increased and second time $y\%$ is increased, then increase in per cent

$$= \left[(x + y) + \frac{xy}{100} \right] \%$$

Example : The price of a TV is increased by 30 % before budget and 20 % after budget. Then total increase in price will be

- (a) 50 % (b) 56 %
(c) 55 % (d) 59 %
(e) None of these

Solution. (b) : Increase per cent

$$= \left[(30 + 20) + \frac{30 \times 20}{100} \right] \% \\ = 50 + 6 = 56 \%$$

Rule VI :

First time $x\%$ decreased and second time $y\%$ decreased, then decrease per cent

$$= \left[(x + y) - \frac{xy}{100} \right] \%$$

Example : The price of a commodity is reduced two times as 40% and 10% respectively. What is percentage decrease in the price?

- (a) 48 (b) 46
(c) 45 (d) 51
(e) None of these

Solution. (b) : Percentage decrease

$$= \left[(40 + 10) - \frac{40 \times 10}{100} \right] \% = 46\%$$

EXERCISE

1. $\frac{20\% \text{ of } 740}{?} = 1036$
 (a) 7 (b) 2/7
 (c) 1/7 (d) 3/7
 (e) None of these
2. 12 % of 200 = ?
 (a) 24 (b) 25
 (c) 27 (d) 28
 (e) 23
3. The tax on a commodity is diminished by 10% and its consumption increased by 10%. The effect on the revenue derived from it is :
 (a) 0.1% decrease (b) 1% decrease
 (c) 1% increase (d) 0.1% increase
 (e) None of these
4. A reduction of 20% in the price of coffee enables a purchaser to obtain 4 kg more for ₹ 80. The reduced price per kg of coffee is
 (a) ₹ 5 (b) ₹ 6
 (c) ₹ 4 (d) ₹ 5.50
 (e) None of these
5. A student has to secure 40% marks to get through. If he gets 40 marks and fails by 40 marks, find the maximum marks set for the examination.
 (a) 200 (b) 150
 (c) 300 (d) 100
 (e) None of these
6. Due to increase of 40% in the price of a radio, selling is reduced 60%, then how much percentage increase or decrease will be in income?
 (a) 74% increase (b) 44% increase
 (c) 44% decrease (d) 62% increase
 (e) None of these
7. If the length of a rectangle is decreased by 40 % and the breadth is increased by 30 %, then what is increase or decrease per cent in the area of rectangle?
 (a) 22% increase (b) 22% decrease
 (c) 28% increase (d) 27% decrease
 (e) None of these

EXPLANATORY ANSWERS

1. (c): $= \frac{740 \times 20}{? \times 100} = 1036$
 $\Rightarrow ? \times 1036 = 74 \times 2$
 $? = \frac{74 \times 2}{1036} = \frac{1}{7}$
 2. (a): $\frac{12}{100} \times 200 = 24$
 3. (b): **Trick** : Effect = $(10^2/100) \% = 1 \% \text{ decrease}$.
 4. (c): **Trick** : Reduced price per kg
 $= \frac{80 \times 20}{100 \times 4} = ₹ 4$
 5. (a): Maximum marks = $\frac{100(40 + 40)}{40} = 200$
 6. (c): **Trick** : $= \left[(40 - 60) - \frac{40 \times 60}{100} \right] \%$
 $= -20 - 24$
 $= -44 = 44 \% \text{ decrease}$,
 7. (b): **Trick** : Percentage increase or decrease
 $= \left[(30 - 40) - \frac{30 \times 40}{100} \right] \%$
 $= -22 = 22 \% \text{ decrease}$
- Note:** Negative sign shows decrease and positive sign shows increase.