CHAPTER CIRCLES

Syllabus

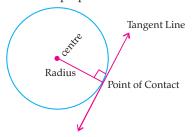
- Tangent to a circle at point of contact.
 - 1. (Prove) The tangent at any point of a circle is perpendicular to the radius through the point of contact.
 - 2. (Prove) The lengths of tangents drawn from an external point to a circle are equal.

Trend Analysis

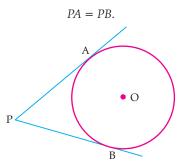
List of Concepts	2018		2019		2020	
	Delhi	Outside Delhi	Delhi	Outside Delhi	Delhi	Outside Delhi
Tangent to Circle (Theorems)	1 Q (3 M)			1 Q (3 M)	1 Q (2 M) 2 Q (3 M)	1 Q (3 M)
Question based on Properties of tangent			2 Q (3 M)		1 Q (1 M)	1 Q (1 M)

Revision Notes

- ➤ A tangent to a circle is a line that intersects the circle at one point only.
- ➤ The common point of the circle and the tangent is called the point of contact.
- Secant: Two common points (A and B) between line PQ and circle.
- ➤ A tangent to a circle is a special case of the secant when the two end points of the corresponding chord are coincide.
- ➤ There is no tangent to a circle passing through a point lying inside the circle.
- ➤ At any point on the circle there can be one and only one tangent.
- The tangent at any point of a circle is perpendicular to the radius through the point of contact.

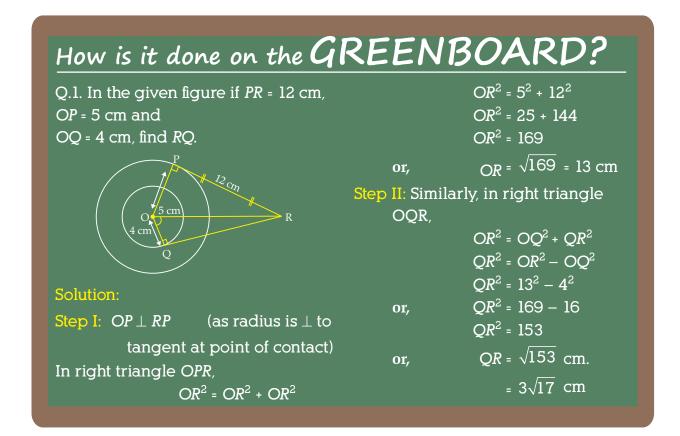


- There are exactly two tangents to a circle through a point outside the circle.
- > The length of the segment of the tangent from the external point P and the point of contact with the circle is called the length of the tangent.
- The lengths of the tangents drawn from an external point to a circle are equal.
 In the figure,

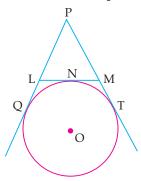


Know the Facts

- ➤ The word 'tangent' comes from the Latin word 'tangere', which means to touch and was introduced by the Danish mathematician **Thomas Fincke** in 1583.
- > The line perpendicular to the tangent and passing through the point of contact, is known as the normal.
- ➤ In two concentric circles, the chord of the larger circle, which touches the smaller circle, is bisected at the point of contact.



Q. 1. If PQ = 28 cm, then find the perimeter of ΔPLM .



A [CBSE SQP, 2020-21]

Sol. :
$$PQ = PT$$

$$PL + LQ = PM + MT$$

$$PL + LN = PM + MN$$

$$(LQ = LN, MT = MN)$$
(Tangents to a circle from a common point)
$$Perimeter (\Delta PLM)$$

$$= PL + LM + PM \qquad \frac{1}{2}$$

$$= PL + LN + MN + PM$$

$$= 2(PL + LN)$$

$$= 2(PL + LQ)$$

$$= 2 \times 28 = 56 \text{ cm} \qquad \frac{1}{2}$$
[CBSE SQP Marking Scheme, 2020-21]

Detailed Solution:

Given, PQ = 28 cm $\therefore PQ = PT$ (Length of tangents from an external point are equal) i.e., PQ = PT = 28 cmAccording to figure, Let LQ = x, then PL = (28 - x) cm

and let MT = y, then PM = (28 - y) cm and LM = LN + NM

Now, the perimeter of
$$\triangle PLM = PL + LM + PM$$

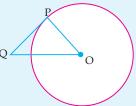
= $(28 - x) + (x + y) + (28 - y)$
= $28 + 28 = 56$ cm. ½

O

\bigcirc Q. 2. PQ is a tangent to a circle with centre O at point P. If \triangle OPQ is an isosceles triangle, then find \angle OQP.

A [CBSE SQP, 2020-21]

Sol.



In
$$\triangle OPQ$$
,
$$\angle P + \angle Q + \angle O = 180^{\circ}$$

$$(\angle O = \angle Q \text{ isosceles triangle})$$

$$2\angle Q + \angle P = 180^{\circ}$$

$$2\angle Q + 90^{\circ} = 180^{\circ}$$

$$2\angle Q = 90^{\circ}$$

$$\angle Q = 45^{\circ}$$
1
[CBSE SQP Marking Scheme, 2020-21]

Detailed Solution:

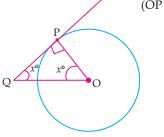
As we know that

 $\angle OPQ = 90^{\circ}$ (Angle between tangent and radius)

Let \angle PQO be x° , then

$$\angle QOP = x^{\circ}$$

Since OPQ is an isosceles triangle. (given) (OP = OQ)



In ΔOPQ,

 $\frac{1}{2}$

 $\angle OPQ + \angle PQO + \angle QOP = 180^{\circ}$ (Property of the sum of angles of a triangle)

$$0^{\circ} + x^{\circ} + x^{\circ} = 180^{\circ}$$

$$2x^{\circ} = 180^{\circ} - 90^{\circ} = 90^{\circ}$$

$$x = \frac{90}{2} = 45^{\circ}.$$

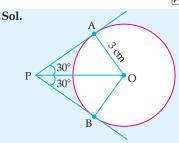
Hence, ∠OQP is 45°

Q. 3. If two tangents inclined at 60° are drawn to a circle of radius 3 cm, then find length of each tangent.

A [CBSE SQP, 2020-21]

1/2

 $\frac{1}{2}$



In ΔPAO,

$$\tan 30^\circ = \frac{AO}{PA}$$

(Using trigonometry) 1/2

$$\frac{1}{\sqrt{3}} = \frac{3}{PA}$$

$$PA = 3\sqrt{3}$$
 cm. $\frac{1}{2}$

[CBSE SQP Marking Scheme, 2020-21]

Detailed Solution:

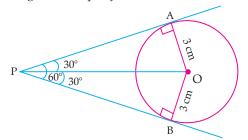
$$PA = PB = ?$$

Angle between tangents = 60°

(Given)

1/2

: Tangents are equally inclined to each other.



$$\Rightarrow$$
 $\angle OPA = \angle OPB = 30^{\circ}$

and $\angle OAP = 90^{\circ}$

(Angle between tangent and radius)

Ιη ΔΡΑΟ,

$$\tan 30^{\circ} = \frac{\text{Perpendicular}}{\text{Base}} = \frac{OA}{AP}$$

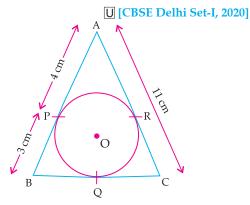
$$\Rightarrow \frac{1}{\sqrt{3}} = 3\sqrt{3}$$

(Using trigonometric Ratios)

$$\Rightarrow$$
 $AP = 3\sqrt{3}$

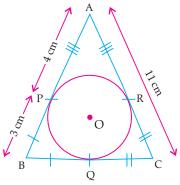
Hence, the length of each tangent is $3\sqrt{3}$ cm. $\frac{1}{2}$

\bigcirc Q. 4. In the adjoining figure, if \triangle ABC is circumscribing a circle, then find the length of BC.



Sol. \because AP and AR are tangents to the circle from external point A.

$$\therefore$$
 $AP = AR i.e., AR = 4 cm$



Similarly, PB and BQ are tangents.

:.
$$BP = BQ \text{ i.e., } BQ = 3 \text{ cm}$$
 1/2
Now, $CR = AC - AR = 11 - 4 = 7 \text{ cm}$

Similarly, CR and CQ are tangents.

$$\therefore \qquad CR = CQ \text{ i.e., } CQ = 7 \text{ cm}$$

Now,
$$BC = BQ + CQ = 3 + 7 = 10$$
 cm.
Hence, the length of BC is 10 cm.

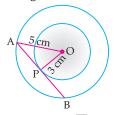
COMMONLY MADE ERROR

Some students were not versed with the properties of circle.

ANSWERING TIP

The students to learn all properties of circle.

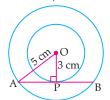
A Q. 5. In the given figure, find the length of PB.



U [CBSE OD Set-I, 2020]

Sol. Since AB is a tangent at P and OP is radius.

$$\therefore$$
 $\angle APO = 90^{\circ}, AO = 5 \text{ cm and } OP = 3 \text{ cm}$



In right angled ∆OPA,

$$AP^2 = AO^2 - OP^2$$

(By using Pythagoras theorem) ½

 $\frac{1}{2}$

$$AP^2 = (5)^2 - (3)^2 = 25 - 9 = 16$$

$$\Rightarrow AP = 4 \text{ cm}$$

 \because Perpendicular from centre to chord bisect the chord

$$\Rightarrow$$
 $AP = BP = 4 \text{ cm}.$

Q. 6. If the radii of two concentric circles are 4 cm and 5 cm, then find the length of each chord of one circle which is tangent to the other circle.

[CBSE SQP, 2020]

Sol. Length of Tangent =
$$2 \times \sqrt{5^2 - 4^2}$$

= 2×3 cm = 6 cm $\frac{1}{2} + \frac{1}{2}$
[CBSE SQP Marking Scheme, 2020]

Detailed Solution:

In ΔOBC

$$CO^{2} + BC^{2} = OB^{2}$$
 $4^{2} + BC^{2} = 5^{2}$
 $16 + BC^{2} = 25$
 $BC^{2} = 25 - 16$
 $BC^{2} = 9$
 $BC = 3$

In ΔOAC,

∴.

$$OC^{2} + AC^{2} = OA^{2}$$

$$4^{2} + AC^{2} = 5^{2}$$

$$AC^{2} = 9$$

$$AC = 3$$

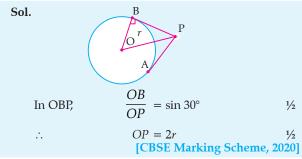
$$AB = AC + BC$$

$$= 3 + 3$$

$$= 6 \text{ cm}$$

Q. 7. If the angle between two tangents drawn from an external point 'P' to a circle of radius 'r' and centre O is 60°, then find the length of OP.

[CBSE SQP, 2020] [Foreign Set-I, II, III, 2016]



Detailed Solution:

$$OA = r$$
 $PP = ?$

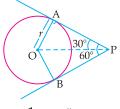
Angle between tangents = 60° Tangents are equally inclined to each other $\Rightarrow \angle OPA = \angle OPB = 30^{\circ}$ In $\triangle OPA$,

$$\angle POA = 180^{\circ} - 90^{\circ} - 30^{\circ}$$

$$= 60^{\circ}$$

$$\cos 60^{\circ} = \frac{OA}{OP}$$

 $\frac{1}{2}$

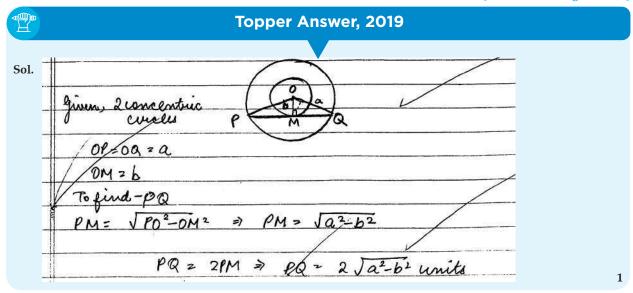


$$\frac{1}{2} = \frac{r}{OP}$$

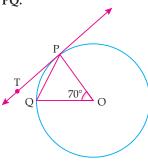
$$OP = 2r$$

Q. 8. Two concentric circles of radii a and b (a > b) are given. Find the length of the chord of the larger circle which touches the smaller circle. [CBSE, Delhi Region, 2019]

1/2



Q. 9. In given figure, O is the centre of the circle, PQ is a chord and PT is tangent to the circle at P. Find ∠TPQ.



U [CBSE, OD Set-I, II, III, 2017]

Sol.
$$\angle OPQ = \angle OQP$$
 (radius of circle)

$$= \frac{180^{\circ} - 70^{\circ}}{2} = 55^{\circ} \qquad \frac{1}{2}$$

$$\therefore \angle TPQ = 90^{\circ} - 55^{\circ}$$

$$= 35^{\circ} \qquad \frac{1}{2}$$
[CBSE Marking Scheme, 2017]

Detailed Solution:

According to the figure,

$$OP = OQ \qquad \text{(radii)}$$

$$\therefore \qquad \angle OPQ = \angle OQP \qquad \text{(Isosceles triangle property)}$$
Now, in $\triangle POQ$,
$$\angle OPQ + \angle OQP + \angle POQ = 180^{\circ} \qquad \text{(Angle sum property)}$$

$$\angle OPQ + \angle OPQ + 70^{\circ} = 180^{\circ} \qquad \text{(Angle sum property)}$$

$$\angle OPQ = 180^{\circ} - 70^{\circ} = 110^{\circ} \qquad 1/2$$

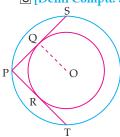
$$\angle OPQ = 55^{\circ}$$
Since
$$\angle OPT = 90^{\circ} \qquad \text{(Angle between tangent and radius)}$$
Hence,
$$\angle TPQ = 90^{\circ} - \angle OPQ$$

$$= 90^{\circ} - 55^{\circ}$$

$$= 35^{\circ}. \qquad 1/2$$

Q. 10. In the fig. there are two concentric circles with centre O. PRT and PQS are tangents to the inner circle from a point P lying on the outer circle. If PR = 5 cm, find the length of PS.

U [Delhi Comptt. Set-I, II, III, 2017]

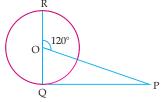


Sol.
$$PQ = PR = 5 \text{ cm}$$
 ½
and $PQ = QS$ ½
∴ $PS = 2PQ$

$$= 2 \times 5 = 10 \text{ cm}.$$
[CBSE Marking Scheme, 2017]

Q. 11. PQ is a tangent drawn from an external point P to a circle with centre O and QOR is the diameter of the circle. If ∠POR = 120°, What is the measure of ∠OPQ?

☐ [Foreign Set-I, II, III, 2016, 2017]



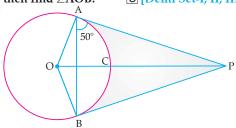
Sol. In
$$\triangle OQP$$

$$\angle POR = \angle OQP + \angle OPQ$$
(Exterior angle) ½
$$\angle OPQ = \angle POR - \angle OQP$$

$$= 120^{\circ} - 90$$

$$= 30^{\circ}$$
½

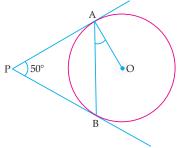
Q. 12. From an external point P, tangents PA and PB are drawn to a circle with centre O. If ∠PAB = 50°, then find ∠AOB. ☐ [Delhi Set-I, II, III, 2016]



Here,
$$\angle OAB = 90^{\circ} - 50^{\circ}$$

 $= 40^{\circ}$ (: PA \perp OA)
 $\angle OAB = \angle OBA = 40^{\circ}$
(: OA and OB are radii)
: $\angle AOB + 40^{\circ} + 40^{\circ} = 180^{\circ}$
 $\angle AOB = 180^{\circ} - 80^{\circ} = 100^{\circ}$
Hence $\angle AOB = 100^{\circ}$

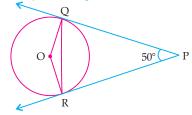
Q. 13. In fig., PA and PB are tangents to the circle with centre O such that $\angle APB = 50^{\circ}$. Write the measure of $\angle OAB$. A [CBSE, Delhi Set I, II, III, 2015]



Sol. Here,
$$\angle APB = 50^{\circ}$$

 $\angle PAB = \angle PBA = \frac{180^{\circ} - 50^{\circ}}{2} = 65^{\circ}$
 $\angle OAB = 90^{\circ} - \angle PAB$
 $= 90^{\circ} - 65^{\circ} = 25^{\circ}$
[CBSE Marking Scheme, 2015] 1

Q. 14. In the given figure, PQ and PR are tangents to the circle with centre O such that $\angle QPR = 50^{\circ}$, then find $\angle OQR$. [CBSE Delhi Set-I, II, III, 2015]



Sol.
$$\angle QPR = \angle 50^{\circ}$$
 (Given)
 $\angle QOR + \angle QPR = 180^{\circ}$ (Supplementary angles)
 $\therefore \angle QOR = 180^{\circ} - 50^{\circ} = 130^{\circ}$ ½

or,
$$\angle OQR = \angle ORQ = \frac{180^{\circ} - 130^{\circ}}{2}$$

= $\frac{50^{\circ}}{2} = 25^{\circ}$ ½

[CBSE Marking Scheme, 2015]

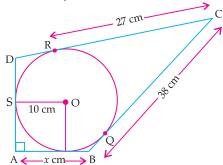


From $\triangle OQR$,

Short Answer Type Questions-I

2 marks each

Q. 1. In the figure, quadrilateral ABCD is circumscribing a circle with centre O and AD \perp AB. If radius of incircle is 10 cm, then find the value of x.



A [CBSE SQP, 2020-21]

1/2

1/2

Sol.
$$\angle A = \angle OPA = \angle OSA = 90^{\circ}$$
 ½
Hence, $\angle SOP = 90^{\circ}$
Also, $AP = AS$

Hence, OSAP is a square.
$$AP = AS = 10 \text{ cm}$$

$$CR = CQ = 27 \text{ cm}$$

 $BQ = BC - CQ$

$$= 38 - 27 = 11 \text{ cm}$$
 ¹/₂

$$BP = BQ = 11 \text{ cm}$$

$$x = AB = AP + BP$$

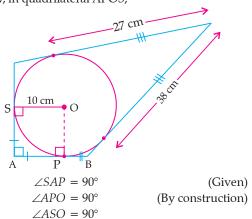
= 10 + 11 = 21 cm

[CBSE Marking Scheme, 2020-21]

Detailed Solution:

and

With O as centre, draw a perpendicular OP on AB. Now, in quadrilateral APOS,



(Angle between tangent and radius) Finally $\angle SOP = 360^{\circ} - (90^{\circ} + 90^{\circ} + 90^{\circ}) = 90^{\circ}$ AP = AS

(Tangents from external point A)

∴ *OSAP* is a square.

$$AP = AS = SO = 10 \text{ cm}$$

$$CR = CQ$$

(Tangents from external point C)

$$\therefore CR = CQ = 27 \text{ cm}$$

But
$$BC = 38 \text{ cm}$$
 (Given)

:.
$$BQ = BC - CQ = (38 - 27) \text{ cm}$$

$$BQ = 11 \text{ cm}$$
 ½

$$BP = BQ$$

(Tangent from external point B)

 $\frac{1}{2}$

$$\therefore BP = 11 \text{ cm}$$

So,
$$x = AB = AP + PB$$

$$= (10 + 11) \text{ cm} = 21 \text{ cm}$$

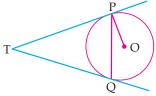
Hence, the value of \hat{x} is 21 cm.

COMMONLY MADE ERROR

Some students does not use appropriate figure to solve the question.

ANSWERING TIP

- Carefully read the question and draw the figure as per the required condition.
- \blacksquare Q. 2. In the given figure, two tangents TP and TQ are drawn to circle with centre O from an external point T. Prove that $\angle PTQ = 2\angle OPQ$.



U [CBSE Delhi Set-I, 2020] [CBSE Delhi Set-I, II, III, 2017]

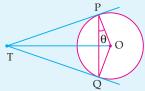
Sol. Let $\angle OPQ$ be θ , then

$$\angle TPQ = 90^{\circ} - \theta$$
 ½

Since,
$$TP = TQ$$

$$\therefore \qquad \angle TQP = 90^{\circ} - \theta \qquad \qquad \frac{1}{2}$$

(opposite angles of equal sides)



Now,
$$\angle TPQ + \angle TQP + \angle PTQ = 180^{\circ}$$
 1/2

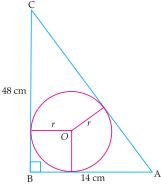
(Angle sum property of a Triangle)
$$\Rightarrow 90^{\circ} - \theta + 90^{\circ} - \theta + \angle PTQ = 180^{\circ}$$

$$\Rightarrow \angle PTQ = 180^{\circ} - 180^{\circ} + 2\theta$$

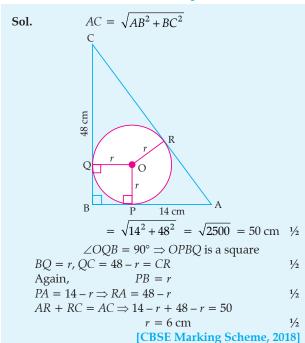
$$\Rightarrow \angle PTQ = 2\theta$$
Hence,
$$\angle PTQ = 2 \angle OPQ$$
Hence Proved.

[CBSE Marking Scheme, 2020]

Q. 3. In Fig, ABC is a triangle in which $\angle B = 90^{\circ}$, BC = 48 cm and AB = 14 cm. A circle is inscribed in the triangle, whose centre is O. Find radius of incircle.



A [CBSE Comptt. Set I, II, III, 2018]



Detailed Solution:

In
$$\triangle ABC$$
, $\angle B = 90^{\circ}$ (Given)
 $AC^2 = AB^2 + BC^2$ (By using pythagoras theorem)
 $= (14)^2 + (48)^2 = 196 + 2304$
 $= 2500$

∴
$$AC = \sqrt{2500} = 50 \text{ cm}$$
 ½

Here, $\angle OQB = \angle OPB = 90^\circ$
(Radius is perpendicular to tangent)
∴ In Quadrilateral OPBQ,
 $\angle POQ = 360^\circ - (OQB + \angle OPB + \angle PBQ)$
 $= 360^\circ - (90^\circ + 90^\circ + 90^\circ) = 90^\circ$

So, $OPBQ$ is a square.

Then $OP = QB = BP = OQ = r$ ½

Thus, $CQ = BC - QB = 48 - r$

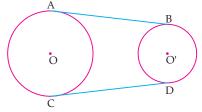
But $CQ = CR$
(Tangents from external point C)
∴ $CR = 48 - r$

and $AP = AB - BP = 14 - r$ ½

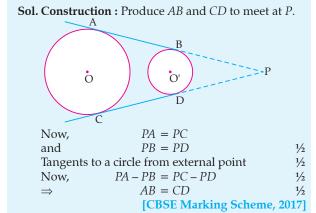
But $AP = AR$
(Tangents from external point A)
∴ $AR = 14 - r$

Now $AC = 50 \text{ cm}$ (proved above)
⇒ $AR + RC = 50$
⇒ $14 - r + 48 - r = 50$
⇒ $-2r = 50 - 62 = -12$
⇒ $r = 6 \text{ cm}$. ½

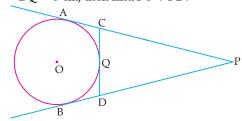
Q. 4. In the fig, AB and CD are common tangents to two circles of unequal radii. Prove that AB = CD.



A [Delhi Comptt. Set-III, 2017]



Q. 5. In the given figure, PA and PB are tangents to the circle from an external point P. CD is another tangent touching the circle at Q. If PA = 12 cm, QC = DQ = 3 cm, then find PC + PD.



A [Delhi Comptt. Set-I, II, III, 2017]

Sol. Here,
$$AC = CQ$$
 (Tangents from external point to a circle)
$$PA = PC + CA = PC + CQ$$

$$(\because CA = CQ)$$

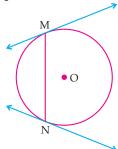
$$\Rightarrow 12 = PC + 3$$

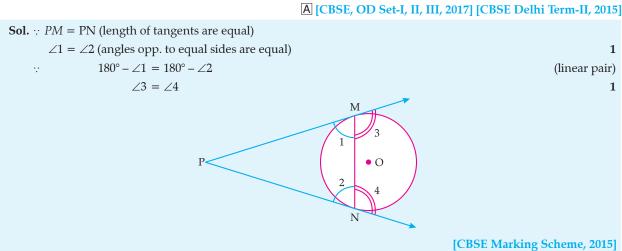
$$\Rightarrow PC = 12 - 3 = 9 \text{ cm}$$
1 PB = PD + BD
$$PA = PD + DQ$$

$$12 - 3 = PD = 9 \text{ cm}$$

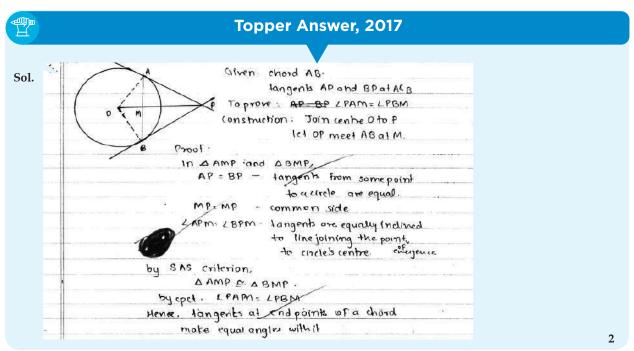
$$PC + PD = 9 + 9 = 18 \text{ cm}$$
1 [CBSE Marking Scheme, 2017]

Q. 6. Prove that the tangents drawn at the end points of a chord of a circle make equal angles with the chord.

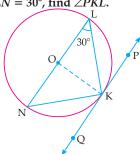




Detailed Solution:



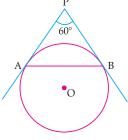
Q. 7. In given figure, O is the centre of the circle and LN is a diameter. If PQ is a tangent to the circle at K and $\angle KLN = 30^{\circ}$, find $\angle PKL$.



U [CBSE OD Comptt. Set-I, II, III, 2017]

Sol. Here,
$$OK = OL$$
 (radii)
 $\angle OKL = \angle OLK = 30^{\circ}$ (Opposite angles of equal sides) 1
Since $\angle OKP = 90^{\circ}$ (Tangent)
 $\therefore \angle PKL = 90^{\circ} - 30^{\circ} = 60^{\circ}$ 1
[CBSE Marking Scheme, 2017]

Q. 8. In Fig., AP and BP are tangents to a circle with centre O, such that AP = 5 cm and $\angle APB = 60^{\circ}$. Find the length of chord AB.



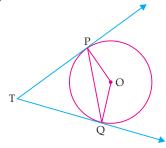
U [CBSE Delhi Set I, II, III, 2016]

Sol.
$$PA = PB$$
 ½
or, $\angle PAB = \angle PBA = 60^{\circ}$ ½

∴
$$\triangle PAB$$
 is an equilateral triangle. ½ Hence, $AB = PA = 5$ cm. ½

[CBSE Marking Scheme, 2016]

Q. 9. In the given figure PQ is chord of length 6 cm of the circle of radius 6 cm. TP and TQ are tangents to the circle at points P and Q respectively. Find $\angle PTQ$.



U [CBSE S.A.II, 2016]

Sol. Here,
$$PQ = 6$$
 cm, $OP = OQ = 6$ cm

$$PQ = OP = OQ$$

$$\angle POO = 60^{\circ}$$

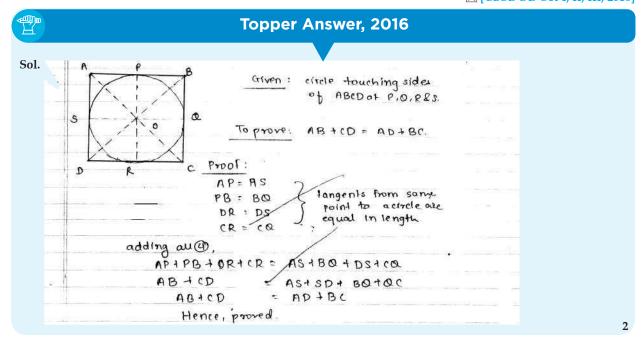
$$\angle OPT = \angle OQT = 90^{\circ}$$

$$\therefore \angle PTQ + 90^{\circ} + 90^{\circ} + 60^{\circ} = 360^{\circ}$$

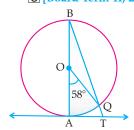
$$\angle PTO = 120^{\circ}$$
 1

Q. 10. A circle touches all the four sides of a quadrilateral ABCD. Prove that AB + CD = BC + DA.

A [CBSE OD Set-I, II, III, 2016]

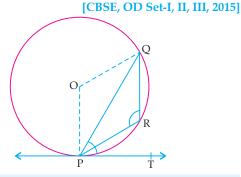


Q. 11. In given figure, AB is the diameter of a circle with center O and AT is a tangent. If $\angle AOQ = 58^{\circ}$, find $\angle ATQ$. U [Board Term-II, 2015 Set-I, II, III]



Sol.
$$\angle AOQ = 58^{\circ}$$
 (Given)
 $\angle ABQ = \frac{1}{2} \angle AOQ$
(Angle on the circumference of the circle by the same arc)
 $= \frac{1}{2} \times 58^{\circ}$
 $= 29^{\circ}$ 1
 $\angle BAT = 90^{\circ}$ ($\because OA \perp AT$)
 $\therefore \angle ATQ = 90^{\circ} - 29^{\circ}$
 $= 61^{\circ}$ 1
[CBSE Marking Scheme, 2015]

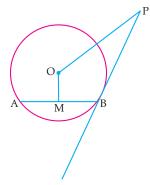
Q. 12. In figure, PQ is a chord of a circle centre O and PT is a tangent. If $\angle QPT = 60^{\circ}$, find $\angle PRQ$.



Sol. Given,
$$\angle QPT = 60^{\circ}$$

 $\angle OPQ = \angle OQP = 90^{\circ} - 60^{\circ} = 30^{\circ}$
 $\angle POQ = 180^{\circ} - (30^{\circ} + 30^{\circ})$
 $= 180^{\circ} - 60^{\circ} = 120^{\circ}$
 $\angle PRQ = \frac{1}{2} \text{ Reflex } \angle POQ$ 1
[:: Reflex $\angle POQ = 360^{\circ} - 120^{\circ} = 240^{\circ}$]
 $= \frac{1}{2} \times 240^{\circ} = 120^{\circ}$
[CBSE Marking Scheme, 2015] 1

Q. 13. PB is a tangent to the circle with centre O to B. AB is a chord of length 24 cm at a distance of 5 cm from the centre. If the tangent is of length 20 cm, find the length of PO.



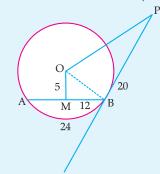
A [Delhi Board Term-2, 2015]

Sol. Construction : Join *OB*.

In rt. $\triangle OMB$,

$$OB^2 = 5^2 + 12^2 = 13^2$$

 $\therefore OB = 13 \text{ cm}$ 1
Since $OB \perp PB$ (radius \perp tangent)

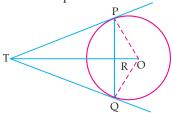


$$ΩP2 = OB2 + BP2
= 132 + 202
= 569
or,
$$OP = \sqrt{569} = 23.85 \text{ cm.} \quad \mathbf{1}$$
[CBSE Marking Scheme, 2015]$$

Q. 14. From a point T outside a circle of centre O, tangents TP and TQ are drawn to the circle. Prove that OT is the right bisector of line segment PQ.

A [CBSE Delhi Term-2, 2015 Set-I, II, III]

Sol. Given: *A* circle with centre *O*. Tangents *TP* and *TQ* are drawn from a point *T* outside a circle.



To Prove: *OT* is the right bisector of line segment *PO*.

Construction: Join OP and OQ

Proof:
$$\triangle$$
 OPT and \triangle *OTQ* $PT = PQ$

(Tangents of the circle)

$$OT = OT$$
 (Common side)
 $\angle OPT = \angle OQR = 90^{\circ}$

$$\triangle OPT \cong \triangle OQT$$

$$(R.H.S. Congruency)$$

$$\angle PTO = \angle QTO \qquad (C.P.C.T)$$

$$\triangle PTR \text{ and } \triangle TRQ$$

$$TP = TQ \qquad (Tangents of circle)$$

$$TR = TR \qquad (Common)$$

$$\triangle PTR \cong \triangle QTR \text{ (SAS congruency)}$$

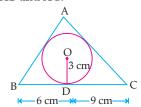
$$\angle PRT = \angle TRQ \qquad (c.p.c.t.)$$

$$PR = QR \qquad (c.p.c.t.)$$

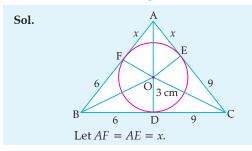
$$\angle PRT + \angle TRQ = 180^{\circ}$$

$$\therefore \qquad \angle PRT = \angle TRQ = 90^{\circ}$$

Q. 15. In figure, a triangle ABC is drawn to circumscribe a circle of radius 3 cm, such that the segments BD and DC are respectively of lengths 6 cm and 9 cm. If the area of \triangle ABC is 54 cm², then find the lengths of sides AB and AC.

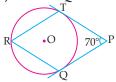


A [CBSE, OD Set-I, II, III, 2015]



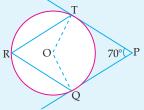
∴
$$AB = 6 + x$$
, $AC = 9 + x$ and $BC = 15 \frac{1}{2}$
ar $\triangle ABC = \frac{1}{2} [15 + 6 + x + 9 + x].3 = 54$
 $45 + 3x = 54$ 1
or, $x = 3$
∴ $AB = 9 \text{ cm}$, $AC = 12 \text{ cm}$ ½
and $BC = 15 \text{ cm}$.
[CBSE Marking Scheme, 2015]

Q. 16. In figure, O is the centre of a circle. PT and PQ are tangents to the circle from an external point P. If $\angle TPQ = 70^{\circ}$, find $\angle TRQ$.



U [Foreign Set-I, II, III, 2015]

Sol.
$$\angle TOQ = 180^{\circ} - 70^{\circ} = 110^{\circ}$$
 (angle of supplementary)



Then,
$$\angle TRQ = \frac{1}{2} \angle TOQ$$

(angle at the circumference of the circle by same arc)

$$= \frac{1}{2} \times 110^{\circ} = 55^{\circ}.$$
 1

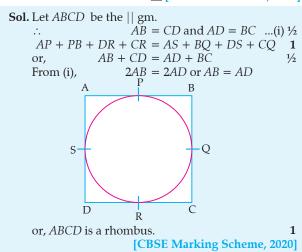
[CBSE Marking Scheme, 2015]



Short Answer Type Questions-II

3 marks each

Q. 1. Prove that the parallelogram circumscribing a circle is a rhombus. A [CBSE Delhi Set-II, 2020]



Detailed Solution:

Let *ABCD* be the parallelogram.

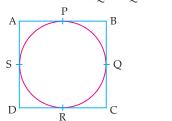
$$\therefore AB = CD \text{ and } AD = BC$$
 ...(i) ½

We know that the tangents drawn to a circle from an exterior point are equal in length.

Therefore, AP = AS, BP = BQ, CR = CQ and DR = DS.

Adding the above equations.

$$AP + BP + CR + DR = AS + BQ + CQ + DS$$
 ½



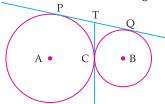
 $\frac{1}{2}$

$$\Rightarrow (AP + BP) + (CR + DR) = (AS + DS) + (BQ + CQ)$$

$$\Rightarrow AB + CD = AD + BC$$
From eq. (i),
$$2AB = 2AD$$
or,
$$AB = AD$$

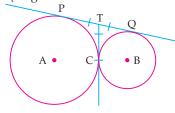
Hence, ABCD is a rhombus. Hence Proved. 1/2

🔃 Q. 2. In given Fig., two circles touch each other at the point C. Prove that the common tangent to the circles at C, bisects the common tangent at P and Q.



A [CBSE Delhi Set-III, 2020]

Sol. Since, PT = TC(tangents of circle) QT = TCand (tangents of circle from extended point) 1



So,
$$PT = QT$$
 1/2
Now $PQ = PT + TQ$ 1/2
 $\Rightarrow PQ = PT + PT$
 $\Rightarrow PQ = 2PT$
 $\Rightarrow \frac{1}{2}PQ = PT$

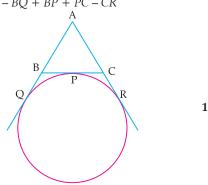
Hence, the common tangent to the circle at C, bisects the common tangents at P and Q.

 $\mathbf{\overline{AI}}$ Q. 3. If a circle touches the side BC of a triangle ABC at P and extended sides AB and AC at Q and R, respectively, prove that $AQ = \frac{1}{2}(BC + CA + AB)$.

A [CBSE OD Set-I, 2020]

Sol.
$$BC + CA + AB$$

= $(BP + PC) + (AR - CR) + (AQ - BQ)$
= $AQ + AR - BQ + BP + PC - CR$



: From the same external point, the tangent segments drawn to a circle are equal. 1/2 From the point B, BQ = BP

From the point A, AQ = AR

From the point C, CP = CR

 \therefore Perimeter of $\triangle ABC$, *i.e.*,

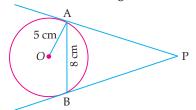
$$AB + BC + CA = 2AQ - BQ + BQ + CR - CR$$

$$\Rightarrow \qquad 2AQ = AB + BC + CA$$

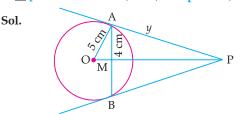
$$\Rightarrow \qquad AQ = \frac{1}{2} (BC + CA + AB)$$

Hence proved. 1

Q. 4. In figure AB is a chord of length 8 cm of a circle of radius 5 cm. The tangents to the circle at A and B intersect at P. Find the length of AP.



A [CBSE Delhi Set-I, 2019, Compt. Set I, II, III 2018]



Given,
$$AB = 8 \text{ cm} \Rightarrow AM = 4 \text{ cm}$$
.

$$\therefore OM = \sqrt{OA^2 - AM^2}$$

(By using Pythagoras theorem)

$$OM = \sqrt{5^2 - 4^2} = 3 \text{ cm}.$$

Let AP = y cm, PM = x cm.

 \therefore $\triangle OAP$ is a right angle triangle.

$$\therefore OP^2 = OA^2 + AP^2$$

(Again using Pythagoras theorem)

$$(x+3)^2 = y^2 + 25$$

$$\Rightarrow$$
 $x^2 + 9 + 6x = y^2 + 25$...(i) $\frac{1}{2}$

Also,
$$x^2 + 4^2 = y^2$$
 ...(ii) $\frac{1}{2}$
 $x^2 + 6x + 9 = x^2 + 16 + 25$

$$6x = 32$$

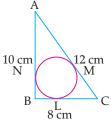
$$x = \frac{32}{6} \text{ i.e., } \frac{16}{3} \text{ cm}$$
$$y^2 = x^2 + 16 = \frac{256}{9} + 16$$

$$y^{2} = x^{2} + 16 = \frac{9}{9} + 16$$

$$= \frac{400}{9}$$
1

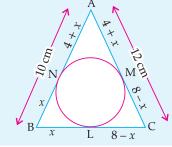
$$y = \frac{20}{3}$$
 cm or $6\frac{2}{3}$ cm. 1

 $\mathbf{\widehat{\mathbf{HI}}}$ Q. 5. In the given figure a circle is inscribed in a ΔABC having sides BC = 8 cm, AB = 10 cm and AC = 12cm. Find the length BL, CM and AN.



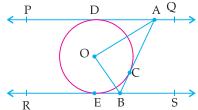
A [CBSE Delhi Set-II, 2019] [Delhi Set-I, II, III, 2016]

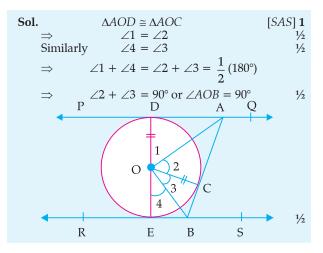
Sol. Let
$$BL = x = BN$$
 (Tangent from external point B)
 $\therefore CL = 8 - x = CM$ (Tangent from external point C)
 $\therefore AC = 12$
 $\Rightarrow AM = 4 + x = AN$ 1 (Tangent from external point A)
Now $AB = AN + NB = 10$
 $\Rightarrow x + 4 + x = 10$
 $\Rightarrow x = 3$ 1
 $\therefore BL = 3 \text{ cm}, CM = 5 \text{ cm} \text{ and } AN = 7 \text{ cm}.$ 1



O. 6. In Figure PO and RS are two parallel tangents to a circle with centre O and another tangent AB with point of contact C intersecting PQ at A and RS at B. Prove that $\angle AOB = 90^{\circ}$.

> [CBSE Delhi Set-I, II, III, 2017] A [CBSE OD Set-1, 2019]





Alternate method:

$$\triangle OAD \cong \triangle AOC \qquad \text{(By SAS)}$$

$$\Rightarrow \qquad \angle 1 = \angle 2 \qquad \qquad 1$$
Similarly, \(\angle 4 = \angle 3 \)
But \(\angle 1 + \angle 2 + \angle 3 + \angle 4 = 180^{\circ} \)
$$\Rightarrow \qquad \angle 2 + \angle 3 = \angle 1 + \angle 4 = \frac{1}{2} (180^{\circ}) = 90^{\circ}$$

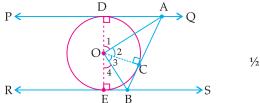
$$\therefore \text{ In } \triangle AOB, \angle AOB = 180^{\circ} - (\angle 2 + \angle 3) = 90^{\circ} \qquad \frac{1}{2}$$

$$P \qquad D \qquad A \qquad Q$$

Ε

Detailed Solution:

R



В

In \triangle DOA and \triangle COA

In
$$\triangle DOA$$
 and $\triangle COA$

$$DA = AC$$
(Tangents drawn from common point)
$$\angle ODA = \angle OCA = 90^{\circ}$$
(angle between tangent and radius)
$$OD = OC \text{ (radius of circle)}$$

$$\therefore \triangle DOA \cong \triangle COA \qquad \text{(By SAS) } \frac{1}{2}$$
Hence, $\angle 1 = \angle 2 \text{ i.e., } \angle DOA = \angle COA \text{ (By cpct) ...(i)}$

S

[CBSE Marking Scheme, 2019]

Similarly,
$$\Delta BOC \cong \Delta BOE \qquad \text{(By SAS) } \frac{1}{2}$$

$$\therefore \quad \angle 3 = \angle 4 \text{ i.e., } \angle COB = \angle BOE \qquad \text{(By cpct)}$$
...(ii)

Now, $\angle 1 + \angle 2 + \angle 3 + \angle 4 = 180^{\circ} \qquad \frac{1}{2}$
(angles on a straight line)
$$2 \angle 2 + 2 \angle 3 = 180^{\circ} \qquad \text{[from eq. (i) \& eq. (ii)]}$$

$$\angle 2 + \angle 3 = 90^{\circ}$$
i.e., $\angle AOC + \angle BOC = 90^{\circ}$
or $\angle AOB = 90^{\circ}$ Hence Proved. 1

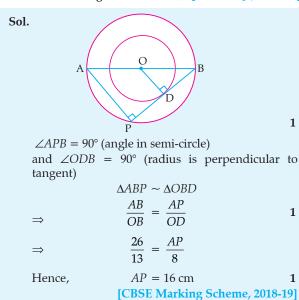
COMMONLY MADE ERROR

Some candidates could not apply the appropriate theorem to find out the unknown angles.

ANSWERING TIP

Learn circle and related angle properties, cyclic properties, tangent and secant properties thoroughly.

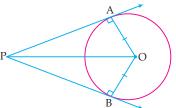
Q. 7. The radii of two concentric circles are 13 cm and 8 cm. AB is a diameter of the bigger circle and BD is a tangent to the smaller circle touching it at D and intersecting the larger circle at P on producing. Find the length of AP. U [CBSE SQP, 2018-19]



Q. 8. Prove that the lengths of two tangents drawn from an external point to a circle are equal.

A [CBSE OD Set-I, II, III, 2018]

Sol. Given: AP and BP are tangents of circle having centre O. ½



Construction : Join *OP, AO* and *BO*

Proof: $\triangle OAP$ and $\triangle OBP$

OA = OB (Radius of circle) OP = OP (Common side)

 $\angle OAP = \angle OBP = 90^{\circ}$

(Radius – tangent angle)

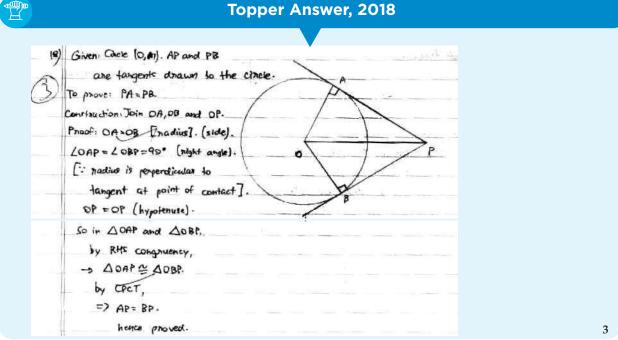
 $\triangle OAP = \triangle OBP$ (RHS congruency rule)

AP = BP (By cpct) 1

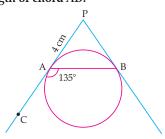
Hence Proved.

 $\frac{1}{2}$

Detailed Solution:



Q. 9. In the given figure, PA and PB are tangents to a circle from an external point P such that PA = 4 cm and $\angle BAC = 135^{\circ}$. Find the length of chord AB.



Sol.
$$PA = PB = 4 \text{ cm}$$
(Tangents from external point) $\frac{1}{2}$
 $\angle PAB = 180^{\circ} - 135^{\circ} = 45^{\circ}$
(Supplementary angles)
$$\angle ABP = \angle PAB = 45^{\circ}$$
(Opposite angles of equal sides) $\frac{1}{2}$

$$\therefore \angle APB = 180^{\circ} - 45^{\circ} - 45^{\circ}$$

$$= 90^{\circ}$$
So, $\triangle ABP$ is an isosceles right angled triangle.
$$\Rightarrow AB^{2} = 2AP^{2} \qquad 1$$

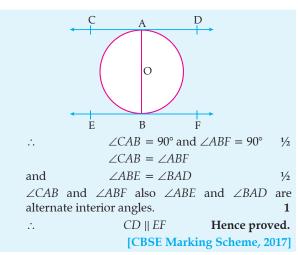
$$\Rightarrow AB^{2} = 32 \qquad 1$$
Hence, $AB = \sqrt{32} = 4\sqrt{2} \text{ cm}$

Q. 10. Prove that the tangents drawn at the ends of the diameter of a circle are parallel.

[CBSE Marking Scheme, 2017]

Sol. Let *AB* be the diameter of a given circle and let *CD* and *EF* be the tangents drawn to the circle at A and *B* respectively.

$$AB \perp CD$$
 and $AB \perp EF$



Q. 11. ABC is a triangle. A circle touches sides AB and AC produced and side BC at X, Y and Z respectively. Show that

$$AX = \frac{1}{2}$$
 perimeter of $\triangle ABC$.

A [Board Term-2, 2016]

Sol. See Q.3. from SATQ-II.



5 marks each

Q. 1. Prove that opposite sides of a quadrilateral circumscribing a circle subtend supplementary angles at the centre of the circle.

A [CBSE Delhi Region, 2019] [Foreign Set-I, II, III, 2017]

Sol. Given: A circle with centre *O* is inscribed in a quadrilateral *ABCD*.

In $\triangle AEO$ and $\triangle AFO$,

$$OE = OF$$
 (radii of circle)
 $\angle OEA = \angle OFA = 90^{\circ}$ (radius is \bot^r to tangent) 1

(laddiss 1 to targett) 1

A

E

8 1

7 0 2

H

1

The point of contact is perpendicular to the tangent. OA = OA (common side)

 $\Delta AEO \cong \Delta AFO$

(R.H.S. congruency)

...(ii)

1

$$\angle 7 = \angle 8$$
 (By cpct) ...(i) 1

Similarly,

$$\angle 1 = \angle 2$$

$$\angle 3 = \angle 4$$
 ...(iii)

$$\angle 5 = \angle 6$$
 ...(iv)

$$\angle 1 + \angle 2 + \angle 3 + \angle 4 + \angle 5 + \angle 6 + \angle 7 + \angle 8 = 360^{\circ}$$
1

(angle around a point is 360°)

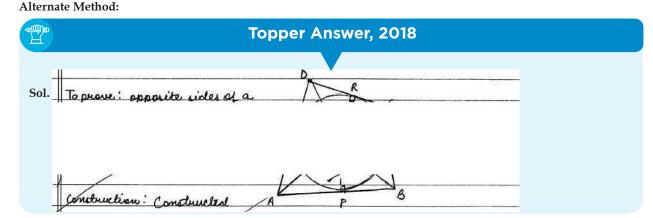
$$2 \angle 1 + 2 \angle 8 + 2 \angle 4 + 2 \angle 5 = 360^{\circ}$$

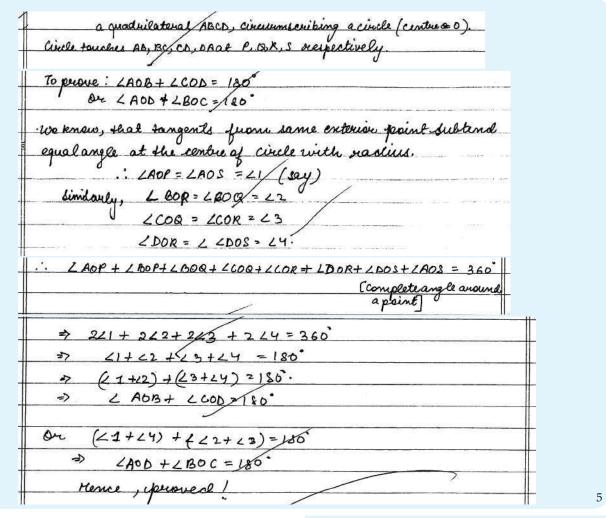
$$\angle 1 + \angle 8 + \angle 4 + \angle 5 = 180^{\circ}$$

$$(\angle 1 + \angle 8) + (\angle 4 + \angle 5) = 180^{\circ}$$

$$\angle AOB + \angle COD = 180^{\circ}$$

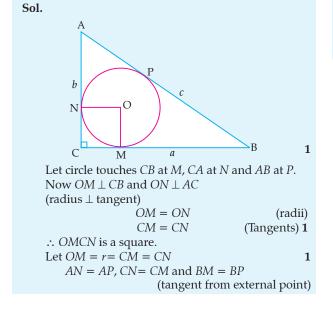
Hence Proved.





Q. 2. a, b and c are the sides of a right triangle, where c is the hypotenuse. A circle, of radius r, touches the sides of the triangle. Prove that $r = \frac{a+b-c}{2}$.

A [CBSE SA-2, 2016]



$$AN = AP$$

$$AC - CN = AB - BP$$

$$b - r = c - BM$$

$$b - r = c - (a - r)$$

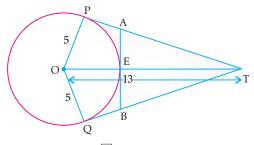
$$b - r = c - a + r$$

$$2r = a + b - c$$

$$r = \frac{a + b - c}{2}$$

Hence Proved. [CBSE Marking Scheme, 2016]

Q. 3. In Fig. O is the centre of a circle of radius 5 cm. T is a point such that OT = 13 cm and OT intersects circle at E. If AB is a tangent to the circle at E, find the length of AB, where TP and TQ are two tangents to the circle.



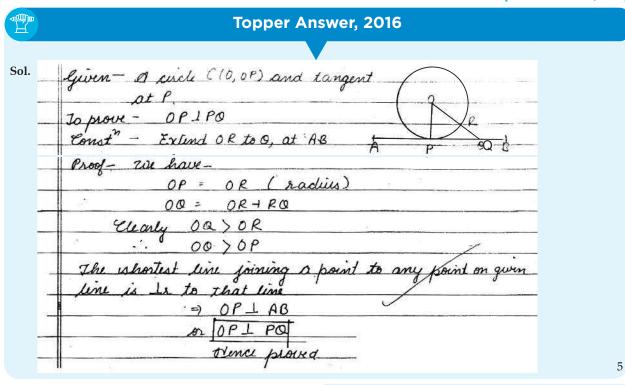
U [CBSE Delhi Set I, II, III, 2016]

Sol.
$$PT = \sqrt{169 - 25} = 12 \text{ cm}$$
 or, and $TE = \text{OT} - \text{OE} = 13 - 5$ or, $\frac{1}{2} + \frac{1}{2}$ Or, Then, $TA^2 = TE^2 + EA^2$ 1

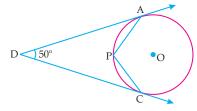
or,
$$(12-x)^2 = 8^2 + x^2$$
 1
 $24x = 80$
or, $x = 3.3 \text{ cm. (Approx.)}$ 1
Thus $AB = 2 \times x = 2 \times 3.3$
 $= 6.6 \text{ cm. (Approx.)}$ 1
[CBSE Marking Scheme, 2016]

Q. 4. Prove that tangent drawn at any point of a circle is perpendicular to the radius through the point of contact.

[CBSE OD Set II, 2016]

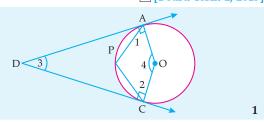


Q. 5. In the given figure, O is the centre of the circle. Determine $\angle APC$, if DA and DC are tangents and $\angle ADC = 50^{\circ}$.



Sol.

A [Board Term-2, 2015]



Given *DA* and *DC* are tangents from point *D* to a circle with centre *O*.

$$\angle APC = \frac{1}{2} \text{ reflex } \angle 4$$

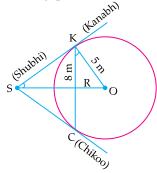
(angle subtended at centre)

$$\angle APC = \frac{1}{2} \times 230^{\circ} = 115^{\circ}$$

[CBSE Marking Scheme, 2015]

Note: Attempt any four sub parts from each question. Each sub part carries 1 mark

🛍 Q. 1. There is a circular filed of radius 5 m. Kanabh, Chikoo and Shubhi are playing with ball, in which Kanabh and Chikoo are standing on the boundary of the circle. The distance between Kanabh and Chikoo is 8 m. From Shubhi point S, two tangents are drawn as shown in the figure. Give the answer C + AEof the following questions.



- (i) What is the relation between the lengths of SK and SC?
 - (a) SK ≠ SC
- (b) SK = SC
- (c) SK > SC
- (d) SK < SC.

Sol. Correct Option: (b)

Explanation: We know that the lengths of tangents drawn from an external point to a circle are equal. So SK and SC are tangents to a circle with centre O.

$$SK = SC$$

- (ii) The length (distance) of OR is:
 - (a) 3 m
- (b) 4 m
- (c) 5 m
- (d) 6 m.

Sol. Correct Option: (a)

Explanation: In question 1, we have proved

$$SK = SC$$

Then ASKC is an isosceles triangle and SO is the angle bisector of ∠KSC. So, OS

 \therefore OS bisects KC, gives KR = RC = 4 cm.

Now,

$$OR = \sqrt{OK^2 - KR^2}$$
(By using Pythagoras theorem)

$$= \sqrt{5^2 - 4^2} = \sqrt{25 - 16}$$

$$= \sqrt{25 - 16}$$

$$= \sqrt{9}$$

$$= 3 \text{ m.}$$
1

- (iii) The sum of angles SKR and OKR is:
 - (a) 45°
- (b)
- (c) 90°
- none of these (d)
- Sol. Correct Option: (c)

Explanation:

$$\angle SKR + \angle OKR = \angle OKR$$

= 90° (Radius is \perp^r to tangent) **1**

- (iv) The distance between Kanabh and Shubhi is:
- (c) $\frac{16}{3}$ m
- Sol. Correct Option: (d)

Explanation: ΔSKR and ΔRKO ,

$$\angle RKO = \angle KSR$$

and

$$\angle SRK = \angle ORK$$

٠. Then

$$\Delta KSR \sim \Delta OKR$$

 $\frac{SK}{} = \frac{RK}{}$ \overline{KO}

$$\frac{SK}{5} = \frac{4}{3}$$

(RO = 3 m, proved in Q.2.)

(By AA Similarity)

3SK = 20

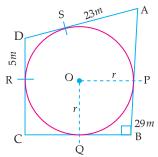
 $SK = \frac{20}{3}$

Hence, the distance between Kanabh and Shubhi is

- (v) What is the mathematical concept related to this question?
 - (a) Constructions
- (b) Area
- (c) Circle
- (d) none of these
- **Sol.** Correct Option: **(c)**

Explanation: The mathematical concept (Circle) is related to this question.

 $oxed{oxed{oxed{A}}}$ $oxed{Q}$. $oxed{Q}$. ABCD is a playground. Inside the playground a circular track is present such that it touches AB at point P, BC at Q, CD at R and DA at S.



See the above figure and give answer of the C + AEfollowing questions:

- (i) If DR = 5 m, then DS is equal to:
 - (a) 6 m
- (b) 11 m
- (c) 5 m
- (d) 18 m

Sol. Correct Option: (c)

Explanation:

$$DR = 5 \text{ m (given)}$$

$$\therefore$$
 $DR = DS$

(Length of tangents are equal)

i.e.,
$$DS = 5 \text{ m}.$$

(ii) The length of AS is:

- (a) 18 m
- (b) 13 m
- (c) 14 m
- (d) 12 m

Sol. Correct Option: (a)

Explanation: We have AD = 23 m.

and
$$DS = 5 \text{ m}$$
 (Proved in Q.1)

$$\therefore AS = AD - DS$$

$$= (23 - 5) \text{ m} = 18 \text{ m}.$$

- (a) 12 m
- (b) 11 m
- (c) 13 m
- (d) 20 m

Sol. Correct Option: (b)

Explanation: We have,

$$AB = 29 \text{ m}$$

But AS = AP

(lengths of tangents are equal)

1

and
$$AS = 18 \text{ m}$$

(Proved in Q.2)

$$\therefore$$
 $AP = 18 \text{ m}$

$$PB = AB - AP$$

$$= (29 - 18) \text{ m}$$

$$= 11 \text{ m}.$$

(iv) What is the angle of OQB?

(a) 60°

Now,

- 30°
- (c) 45°
- 90° (d)

Sol. Correct Option: **(d)**

Explanation: $\angle OQB = 90^{\circ}$ (Radius is \perp^r to tangent)

- (v) What is the diameter of given circle?
 - (a) 22 m
- (b) 33 m
- (c) 20 m
- (d) 30 m

Sol. Correct Option: (a)

Explanation:

$$PB = 11 \text{ m} \qquad \text{(proved in Q.3)}$$
But
$$PB = BQ \qquad \text{(lengths of PB)}$$

tangents are equal)

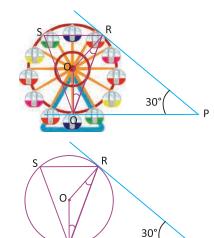
$$\therefore$$
 BQ = 11 m

or
$$r = OQ = QB = 11 \text{ m}$$

Hence, diameter = $2r = 2 \times 11 = 22$ m.

Q. 3. A Ferris wheel (or a big wheel in the United Kingdom) is an amusement ride consisting of a rotating upright wheel with multiple passengercarrying components (commonly referred to as passenger cars, cabins, tubs, capsules, gondolas, or pods) attached to the rim in such a way that as the wheel turns, they are kept upright, usually by gravity.

After taking a ride in Ferris wheel, Aarti came out from the crowd and was observing her friends who were enjoying the ride. She was curious about the different angles and measures that the wheel will form. She forms the figure as given below.



- (i) In the given figure find $\angle ROQ$.
 - (a) 60
- (b) 100
- (c) 150
- (d) 90

Sol. Correct option: (c).

- (ii) Find ∠RQP.
 - (a) 75
- 60 (b)
- (c) 30
- (d) 90

Sol. Correct option: (a).

- (iii) Find ∠RSQ.
 - (a) 60
- 75 (b)
- (c) 100
- (d) 30
- **Sol.** Correct option: **(b)**.
- (iv) Find \angle ORP.
 - (a) 90
- (b) 70 (d)

60

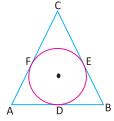
- (c) 100
- **Sol.** Correct option: (a).

Explanation: $\angle ORP = 90^{\circ}$

Because, radius of circle is perpendicular to tangent.

Q. 4. Varun has been selected by his School to design logo for Sports Day T-shirts for students and staff. The logo design is as given in the figure and he is working on the fonts and different colours according to the theme. In given figure, a circle with centre O is inscribed in a $\triangle ABC_r$, such that it touches the sides AB, BC and CA at points D, E and F respectively. The lengths of sides AB, BC and CA are 12 cm, 8 cm and 10 cm respectively.





- (i) Find the length of AD.
 - (a) 7
- (b) 8
- (c) 5
- (d) 9
- Sol. Correct option: (a).
- (ii) Find the Length of BE.
 - (a) 8
- (b) 5
- (c) 2
- (d) 9
- Sol. Correct option: (b).

- (iii) Find the length of CF.
 - (a) 9
- (b) 5
- (c) 2
- (d) 3

Sol. Correct option: (d).

- (iv) If radius of the circle is 4 cm, find the area of $\Delta \text{OAB}.$
 - (a) 20
- (b) 36
- (c) 24
- (d) 48

Sol. Correct option: (c).

- (v) Find area of $\triangle ABC$
 - (a) 50
- (b) 60
- (c) 100
- (d) 90

Sol. Correct option: (b).