

1. If t_n denotes the n th term of the series $2 + 3 + 6 + 11 + 18 + \dots$ then t_{50} is
 (A) $49^2 - 1$ (B) 49^2 (C) $50^2 + 1$ (D) $49^2 + 2$
2. Let $x = 1 + 3a + 6a^2 + 10a^3 + \dots$ $|a| < 1$, $y = 1 + 4b + 10b^2 + 20b^3 + \dots$ $|b| < 1$.
 Then $S = 1 + 3(ab) + 5(ab)^2 + \dots$ in terms of x and y is
 (A) $\frac{1+(1-x^{-1/3})(1-y^{-1/4})}{\{1-(1-x^{-1/3})(1-y^{-1/4})\}^2}$ (B) $\frac{1+(1+x^{-1/3})(1+y^{-1/4})}{\{1-(1+x^{-1/3})(1+y^{-1/4})\}^2}$
 (C) $\frac{1+(1-x^{-1/3})(1-y^{-1/4})}{\{1+(1-x^{-1/3})(1-y^{-1/4})\}^2}$ (D) None of these
3. If $\frac{1}{1^2} + \frac{1}{2^2} + \frac{1}{3^2} + \dots$ upto $\infty = \frac{\pi^2}{6}$ then, $\frac{1}{1^2} + \frac{1}{3^2} + \frac{1}{5^2} + \dots \infty =$
 (A) $\frac{\pi^2}{6}$ (B) $\frac{\pi^2}{8}$ (C) $\frac{\pi^2}{4}$ (D) π^2
4. The sum of infinite terms of the series $\frac{1}{1+1^2+1^4} + \frac{2}{1+2^2+2^4} + \frac{3}{1+3^2+3^4} + \dots \infty$ is :
 (A) $\frac{1}{2}$ (B) $\frac{1}{3}$ (C) 1 (D) $\frac{1}{4}$
5. The sum of the series $1.3^2 + 2.5^2 + 3.7^2 + \dots$ upto 20 terms is
 (A) 188090 (B) 180890 (C) 189820 (D) None of these
6. The sum of series $\frac{3}{1^2} + \frac{5}{1^2+2^2} + \frac{7}{1^2+2^2+3^2} + \frac{9}{1^2+2^2+3^2+4^2} + \dots$ to n terms equals
 (A) $\frac{6n}{n+1}$ (B) $\frac{6n}{n^2+1}$ (C) $\frac{n+1}{n^2+1}$ (D) None of these
7. Sum to infinite of the series $1 + \frac{2}{5} + \frac{3}{5^2} + \frac{4}{5^3} + \dots$ is
 (A) $5/4$ (B) $6/5$ (C) $25/16$ (D) $16/9$
8. The sum of the infinite series $\frac{1}{10} + \frac{2}{10^2} + \frac{3}{10^3} + \dots$ is equal to :
 (A) $\frac{1}{9}$ (B) $\frac{10}{81}$ (C) $\frac{1}{8}$ (D) $\frac{17}{72}$
9. The sum of the series, $1 + 2 \cdot \left(1 + \frac{1}{n}\right) + 3 \cdot \left(1 + \frac{1}{n}\right)^2 + \dots \infty$ is (where $|n| > 1$).
 (A) n^2 (B) $n(n+1)$ (C) $n \left(1 + \frac{1}{n}\right)^2$ (D) $(n+1)(n+2)$
10. Sum of infinite terms of the series $\left[\frac{1}{5} - \frac{2}{7^2} + \frac{3}{5^3} - \frac{4}{7^4} + \dots \right]$ is
 (A) $\frac{211}{1152}$ (B) $\frac{220}{1811}$ (C) $\frac{2}{311}$ (D) None of these.

11. If the sum to infinity of the series $1 + 4x + 7x^2 + 10x^3 + \dots$ is $\frac{35}{16}$ then find x.
- (A) $\frac{1}{5}$ (B) $\frac{19}{7}$ (C) $\frac{15}{12}$ (D) None of these
12. The sum of $0.2 + 0.004 + 0.00006 + 0.0000008 + \dots$ to ∞ is
- (A) $\frac{200}{891}$ (B) $\frac{2000}{9801}$ (C) $\frac{1000}{9801}$ (D) None of these
13. The sum of the series $\frac{1}{\log_2 4} + \frac{1}{\log_4 4} + \frac{1}{\log_8 4} + \dots + \frac{1}{\log_{2^n} 4}$ is
- (A) $\frac{n(n+1)}{2}$ (B) $\frac{n(n+1)+(2n+1)}{12}$ (C) $\frac{1}{n(n+1)}$ (D) $\frac{n(n+1)}{4}$
14. The sum to infinity of the series $\frac{1}{2.4} + \frac{1}{4.6} + \frac{1}{6.8} + \frac{1}{8.10} + \dots$ is
- (A) $1/4$ (B) $1/8$ (C) $1/2$ (D) $1/16$
15. The sum of $\frac{3}{1.2} \cdot \frac{1}{2} + \frac{4}{2.3} \cdot \left(\frac{1}{2}\right)^2 + \frac{5}{3.4} \cdot \left(\frac{1}{2}\right)^3 + \dots$ to n terms is equal to
- (A) $1 - \frac{1}{(n+1)2^n}$ (B) $1 - \frac{1}{n \cdot 2^{n-1}}$ (C) $1 + \frac{1}{(n+1)2^n}$ (D) none of these
16. The value of $\sum_{n=3}^{\infty} \frac{1}{n^5 - 5n^3 + 4n}$ is equal to
- (A) $\frac{1}{120}$ (B) $\frac{1}{96}$ (C) $\frac{1}{24}$ (D) $\frac{1}{144}$
17. The value of $\sum_{r=1}^n \frac{1}{\sqrt{a+rx} + \sqrt{a+(r-1)x}}$ is
- (A) $\frac{n}{\sqrt{a} - \sqrt{a+nx}}$ (B) $\frac{\sqrt{a+nx} - \sqrt{a}}{x}$ (C) $\frac{n(\sqrt{a+nx} - a)}{x}$ (D) None of these
18. If the sum $\sum_{k=1}^{\infty} \frac{1}{(k+2)\sqrt{k} + k\sqrt{k+2}} = \frac{\sqrt{a} + \sqrt{b}}{\sqrt{c}}$ where a, b, c $\in \mathbb{N}$ and lie in [1, 15], then a + b + c equals to
- (A) 6 (B) 8 (C) 10 (D) 11
19. The value of $\frac{1}{1.3.5} + \frac{1}{3.5.7} + \frac{1}{5.7.9} + \frac{1}{9.11.13} + \dots$ equals
- (A) $\frac{1}{12}$ (B) $\frac{53}{249}$ (C) $\frac{35}{429}$ (D) $\frac{35}{249}$
20. The value of $\sum_{k=1}^{\infty} \frac{6^k}{(3^k - 2^k)(3^{k+1} - 2^{k+1})}$ is
- (A) 1 (B) 2 (C) 3 (D) 4

Answers

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1. (D) 2. (A) 3. (B) 4. (A) 5. (A) 6. (A) 7. (C) 8. (B) 9. (A) 10. (A)
11. (A) 12. (B) 13. (D) 14. (A) 15. (A) 16. (B) 17. (B) 18. (D) 19. (A) 20. (B)