

Electromagnetic Induction and Alternating Current

- Whenever there is a relative motion between a loop (or coil) and a magnet, an emf is induced in the loop (or coil) which is called **induced emf**. This phenomenon is called as electromagnetic induction.
- **Magnetic flux linked with a coil**
 - (i) Flux $\phi = NBA \cos \theta$ where
 B = strength of magnetic field
 N = number of turns in the coil
 A = area of surface
 θ = angle between normal to area and field direction.
 - (ii) When plane of coil is perpendicular to B , i.e. $\theta = 0^\circ$, $\phi = NBA$ (maximum value).
 - (iii) When plane of coil is parallel to B , i.e. $\theta = 90^\circ$,
 $\phi = 0$ (minimum value)
 - (iv) S.I. unit of ϕ = weber
c.g.s unit of ϕ = maxwell
1 weber = 10^8 maxwell.
 - (v) Dimensional formula of magnetic flux
 $[\phi] = [ML^2T^{-2}A^{-1}]$.
- **Faraday's laws of electromagnetic induction**
 - (i) Whenever magnetic flux linked with a circuit (a loop of wire or a coil or an electric circuit in general) changes, induced emf is produced.
 - (ii) The induced emf lasts as long as the change in the magnetic flux continues.
 - (iii) The magnitude of induced emf is directly proportional to the rate of change of the magnetic flux linked with the circuit.

$$\varepsilon = -\frac{Nd\phi}{dt}$$
where N is turns in a coil.
- By Faraday's second law of induction, $\varepsilon = -d\phi/dt$
Apply it to the coil.
Induced e.m.f. ε depends on rate of change of magnetic flux linked with the coil.
Flux $\phi = NBA \cos \theta$ where
 B = strength of magnetic field
 N = number of turns in the coil
 A = area of surface

θ = angle between normal to area and field direction.

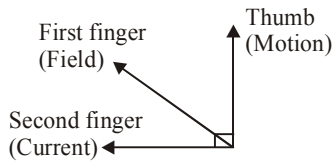
$$\varepsilon = -\frac{d}{dt}(NBA\cos\omega t) \text{ where } \theta = \omega t$$

Induced e.m.f. ε depends on N , B , A and ω .

- **Lenz's Rule**

States that the induced current produced in a circuit always flows in such a direction that it opposes the change or the cause that produce it.

- **Fleming's right hand rule**



- **Motional E.M.F.**

When a conductor of length l moves with a velocity v in a magnetic field B , so that magnetic field is perpendicular to both the length of the conductor and its direction of motion, the magnetic Lorentz force on the conductor gives rise to e.m.f. Mathematically, $\varepsilon = Blv$.

- **Eddy currents/Focault's currents**

Currents induced in conductor, when placed in a changing magnetic field are also known as **Focault's currents**.

- **Self inductance**

The phenomenon, according to which an opposing induced emf is produced in a coil as a result of change in current or magnetic flux linked with the coil is called self-inductance.

- **Coefficient of self induction or self inductance L**

$$\Rightarrow \phi = LI$$

$$\Rightarrow \varepsilon = -L \frac{dI}{dt}$$

- **Self inductance/coefficient of self induction**

(i) The self inductance L depends on geometry of coil or solenoid and the permeability of the core material of the coil or solenoid.

(ii) Unit of L = henry.

(iii) Dimensions of inductance = $[ML^2T^{-2}A^{-2}]$

(iv) For a small circular coil, $L = \frac{\mu_0\mu_r N^2 \pi r}{2}$

(v) For a solenoid, $L = \frac{\mu_0\mu_r N^2 A}{l}$.

(vi) For two coils connected in series when

– Current flows in same direction in both,

$$L = L_1 + L_2 + 2M$$

– When currents flow in two coils in opposite directions

$$L = L_1 + L_2 - 2M$$

$$\text{If } M = 0, L = L_1 + L_2$$

(vii) For two coils connected in parallel

$$\frac{1}{L} = \frac{1}{L_1 + M} + \frac{1}{L_2 + M} \Rightarrow L = \frac{(L_1 + M)(L_2 + M)}{L_1 + L_2 + 2M}$$

$$\text{If } M = 0, L = \frac{L_1 L_2}{L_1 + L_2}$$

$$\text{(viii) Self inductance of a toroid, } L = \frac{\mu_0 N^2 A}{2\pi r}.$$

- **Mutual inductance (M)**

(i) Mutual inductance of two coils is numerically equal to magnetic flux linked with one coil, when a unit current flows through the neighbouring coil.

$$\Rightarrow \phi = MI$$

$$\varepsilon = -M \frac{dI}{dt}$$

(ii) For two long co-axial solenoids, each of length l , common area of cross-section A wound on air core,

$$M = \frac{\mu_0 N_1 N_2 A}{l}$$

(iii) For two coupled coils, $M = K\sqrt{L_1 L_2}$ where K denotes the coefficient of coupling between the coils.

(iv) If $K = 1$, the coils are said to be tightly coupled such that magnetic flux produced in primary is fully linked with the secondary.

$$M = \sqrt{L_1 L_2} = \text{maximum value of } M.$$

- **Energy stored in an inductor**

$$\Rightarrow E = \frac{1}{2} LI^2$$

- **Induced emf due to rotation and translation**

(i) A conducting rod rotates in a perpendicular magnetic field

$$\varepsilon = -\frac{B\omega L^2}{2} = -BAf \text{ where } f = \text{frequency of rotation}$$

$$A = \text{area swept by rotating rod} = \pi L^2$$

$$L = \text{length of rod, } \omega = \text{angular/rotational speed}$$

(ii) A disc rotates in a perpendicular magnetic field

$$\varepsilon = -B\pi r^2 \cdot f = -\frac{Br^2\omega}{2} = -BAf, \text{ where}$$

$$A = \pi r^2 = \text{area of disc, } \omega = \text{angular speed of disc}$$

(iii) A rectangular coil moves linearly in a field when coil moves with constant velocity in a uniform magnetic field, flux and induced emf will be zero.

(iv) When a coil is displaced in a field B , $\varepsilon = -Bvl$ where v = velocity of coil.

(v) A rod moves, at an angle θ with the direction of magnetic field, with velocity

$$\varepsilon = -Blv \sin \theta$$

$$\varepsilon = -Blv \text{ when rod moves along normal to the field.}$$

- **An emf is induced in the following cases:**

- (i) When a train moves horizontally in any direction.
- (ii) When an aeroplane flies horizontally.
- (iii) When a conductor falls freely in east-west direction.
- (iv) When an aeroplane takes off or lands with its wings in east-west direction.
- (v) The plane of orbit of a metallic satellite is inclined to the equatorial plane at any angle.
- (vi) When a magnet is moved with respect to a coil, an emf is induced in the coil.
- (vii) When a current carrying coil is moved with respect to a stationary coil, a current is induced in the stationary coil.
- (viii) When strength of current flowing in a coil is increased or decreased induced current is developed in the coil in same or opposite direction.

Growth and decay of current

- **Growth of current in inductive circuit**

- (i) The value of current at any instant of time t is given by

$$I = I_0 \left(1 - e^{-Rt/L}\right) \text{ where}$$

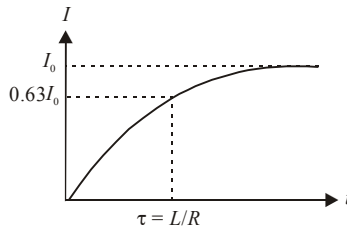
I_0 = maximum/final current

R = total resistance of circuit

- (ii) If $t = L/R$

$$I = 0.63I_0 = 63\% I_0$$

$\tau = L/R$ = time constant of circuit.



- (iii) Inductance acts as electrical inertia. It opposes growth of current as well as decay of current.

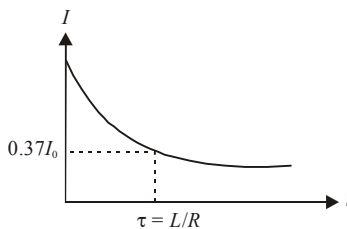
- **Decay of current in inductive circuit**

- (i) During decay, current at any instant of time is given by

$$I = I_0 \cdot e^{-Rt/L}$$

- (ii) If $t = L/R = \tau$ = time constant of circuit,

$$I = I_0/e = 37\% I_0.$$



Charge and discharge of a capacitor

• Charge of condenser

- (i) *Instantaneous charge* : When the key K_1 is closed, the capacitor gets charged. Finite time is taken in the charging process.

Instantaneous charge = q

$$\therefore q = q_0 [1 - e^{-(t/RC)}]$$

where q_0 = maximum final value of charge at $t = \text{infinity}$ and R = resistance of whole circuit.

The equation reveals that q increases exponentially with increase of time.

- (ii) If $t = RC = \tau$ = time constant.

$$q = q_0 [1 - e^{-(RC/RC)}] = q_0 \left[1 - \frac{1}{e} \right]$$

$$\text{or } q = q_0 (1 - 0.37) = 0.63 q_0$$

$$\text{or } q = 63\% \text{ of } q_0.$$

Time $\tau = RC$ is known as time-constant.

- (iii) Dimensions of $RC = [T] = [M^0 L^0 T^1]$

- (iv) Potential difference across condenser plates = V

$$\therefore V = V_0 [1 - e^{-(t/RC)}]$$

- (v) $I = I_0 [e^{-(t/RC)}]$.

If $t = RC$, then transient current I is given by

$$I = I_0 / e = 0.37 I_0$$

$$\text{or } I = 37\% \text{ of } I_0.$$

• Discharge of condenser

If key K_1 is opened and key K_2 is closed, then the capacitor gets discharged.

- (i) *Instantaneous charge* : $q = q_0 e^{-(t/RC)}$

The charge decays exponentially.

- (ii) Time constant = τ

$$\text{If } t = RC = \tau$$

$$q = q_0 / e = 0.37 q_0 = 37\% \text{ of } q_0.$$

The time constant is that time during which the charge on capacitor plates, during discharge process, decays to 37% of its maximum value.

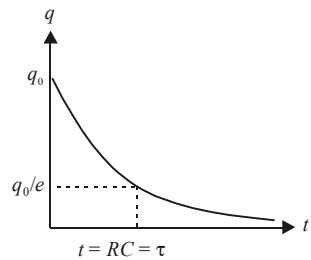
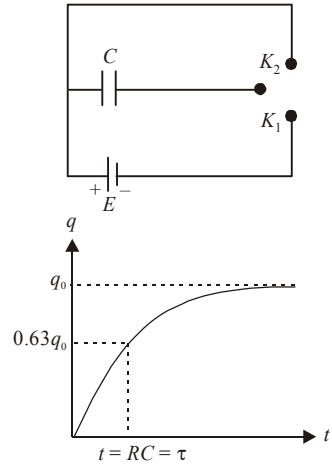
- (iii) The dimensions of RC are those of time i.e. $M^0 L^0 T^1$.

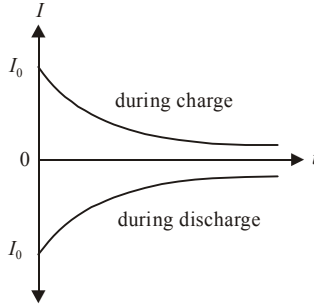
- (iv) The potential difference across the capacitor plates at any instant of time is given by

$$V = V_0 e^{-(t/RC)}$$

- (v) Transient current I at any instant of time is given by $I = -I_0 e^{-(t/RC)}$

The current in the circuit decays exponentially but its direction is opposite to that of charging current.





Alternating current and alternating e.m.f

- Instantaneous values (I and E)**

$$I = I_0 \sin \omega t \quad \text{or} \quad I = I_0 \cos \omega t$$

$$E = E_0 \sin \omega t \quad \text{or} \quad E = E_0 \cos \omega t \quad \text{where}$$

I, E = instantaneous values of current and e.m.f.

I_0, E_0 = peak values of current and e.m.f.

ω = angular velocity

$\omega = 2\pi f$ where f denotes frequency.

$\omega = 2\pi/T$ where T denotes periodic time.

- Mean or average values**

(i) In first half-cycle,

$$I_m = \frac{2}{\pi} I_0 \quad \text{and} \quad E_m = \frac{2}{\pi} E_0 \Rightarrow I_m = 0.637 I_0, E_m = 0.637 E_0$$

(ii) In second half-cycle,

$$I_m = -\frac{2}{\pi} I_0 = -0.637 I_0, E_m = -\frac{2}{\pi} E_0 = -0.637 E_0$$

(iii) Over a complete cycle,

$$I_m = 0 \quad \text{and} \quad E_m = 0.$$

- Root mean square (RMS = r.m.s.) value**

(i) RMS value is also known as virtual value or effective value.

(ii) All A.C. instruments measure virtual value.

$$(iii) I_v = \frac{I_0}{\sqrt{2}} = 0.707 I_0, E_v = \frac{E_0}{\sqrt{2}} = 0.707 E_0$$

$$(iv) \text{Form factor of A.C. } (K) = \frac{I_v}{I_m} = \frac{0.707 I_0}{0.637 I_0} = 1.11$$

- Reactance**

(i) It is the opposition offered to A.C. by a coil of inductance L or by a capacitor of capacitance C .

(ii) Reactance arises on account of induction effects.

- Inductive reactance (X_L)**

$$(i) X_L = \omega L = 2\pi f L = \frac{2\pi}{T} L$$

(ii) Alternating current lags behind the alternating e.m.f. applied to a pure inductor by phase angle of 90° .

(iii) For direct current (d.c.), frequency $f = 0$.

$$\therefore X_L = \text{zero}.$$

An inductor thus behaves like a perfect conductor for d.c.

(iv) For a.c., higher the frequency f , greater is the inductive reactance.

(v) Average power over one full cycle of a.c.

$$P_{av} = E_v I_v \cos\theta = E_v I_v \cos 90^\circ = \text{zero}.$$

(vi) Energy stored in inductor $= \frac{1}{2} L I_0^2$.

(vii) **Choke coil:** It is a pure inductance coil. Since power consumed in it is zero, the current in choke coil is known as wattless current.

$$\text{(viii) Susceptance} = \frac{1}{\text{reactance}} \Rightarrow S_L = \frac{1}{X_L} = \frac{1}{\omega L}$$

It is measured in siemen or $(\text{ohm})^{-1}$.

- **Capacitive reactance (X_C)**

$$(i) X_C = \frac{1}{\omega C} = \frac{1}{2\pi f C}$$

(ii) Alternating current leads the alternating e.m.f. in a pure capacitor by phase angle of 90° .

(iii) For d.c., $X_C = \frac{1}{2\pi f C} = \frac{1}{0} = \infty$.

A condenser blocks d.c.

(iv) For a.c., higher the frequency f , lower is the capacitive reactance.

(v) Average power or true power over one full cycle of a.c.

$$P_{av} = E_v I_v \cos\theta = E_v I_v \cos 90^\circ = \text{zero}.$$

(vi) Energy stored in a capacitor $= \frac{1}{2} C V^2 = \frac{QV}{2} = \frac{Q^2}{2C}$

(vii) Susceptance is reciprocal of reactance.

$$S_C = \frac{1}{X_C} = \omega C.$$

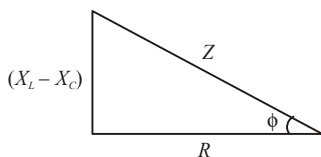
Susceptance is measured in $(\text{ohm})^{-1}$ or siemen.

- **Impedance**

(i) The total effective opposition in LCR circuit is called impedance (Z).

$$(ii) Z = \sqrt{R^2 + (X_L - X_C)^2}$$

$$\tan \phi = \frac{X_L - X_C}{R}$$



ϕ = angle by which e.m.f. leads the current in LCR circuit.

(iii) Admittance (K)

Reciprocal of impedance is called admittance. $K = \frac{1}{Z} = \frac{1}{\sqrt{R^2 + (X_L - X_C)^2}}$

It is measured in $(\text{ohm})^{-1}$ or siemen.

- **Power in a.c. circuit**

(i) Instantaneous power $= P_{in} = EI$

$$P_{in} = (E_0 \sin \omega t) I_0 \sin(\omega t \pm \theta)$$

(ii) Average power or true power

$$P_{av} \text{ or } \langle P \rangle = E_v I_v \cos \theta = \frac{E_0 I_0}{2} \cos \theta$$

(iii) Apparent power (P_v)

$$P_v = E_v \cdot I_v = \frac{E_0 I_0}{2}$$

It is equal to maximum value of average power.

- **Power factor**

(i) Power factor of an a.c. circuit $= \frac{\text{true power}}{\text{apparent power}}$

$$\Rightarrow \text{Power factor} = \cos \theta = R/Z.$$

(ii) It is a unitless and dimensionless quantity.

(iii) Its value lies between 0 and 1.

(iv) Power lost in the circuit is the meaning of power factor of the circuit.

- **Purely resistive circuit**

(i) $E = E_0 \sin \omega t$

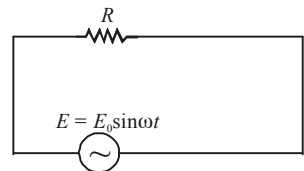
(ii) $I = I_0 \sin \omega t$

(iii) Phase difference between I and E is zero.

(iv) Peak current $I_0 = E_0/R$

(v) Average power = true power $= E_v I_v$

(v) Power factor $= \cos \theta = \cos 0 = 1$.



- **Pure inductive circuit**

(i) $E = E_0 \sin \omega t$

(ii) $I = I_0 \sin \left(\omega t - \frac{\pi}{2} \right)$

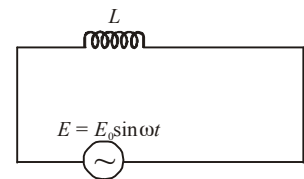
(iii) Current lags behind e.m.f. by $\pi/2$ or e.m.f. leads over current by $\pi/2$

(iv) Reactance $X_L = \omega L = 2\pi f L$

(v) Peak current $I_0 = E_0/X_L$

(vi) Average power = zero.

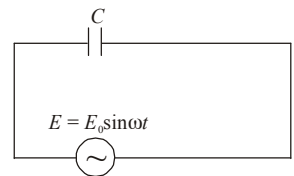
(vii) Power factor $= \cos \theta = \cos 90^\circ = \text{zero}$.



- **Pure capacitive circuit**

(i) $E = E_0 \sin \omega t$

(ii) $I = I_0 \sin \left(\omega t + \frac{\pi}{2} \right)$



(iii) Current leads the e.m.f. by $\pi/2$ or e.m.f. lags behind the current by $\pi/2$

(iv) Reactance $= X_C = \frac{1}{\omega C} = \frac{1}{2\pi f C}$

(v) Peak current $= I_0 = E_0/X_C$

(vi) Average power = zero

(vii) Power factor $= \cos\theta = \cos 90^\circ = \text{zero}$.

• **L-R circuit**

(i) Equations of E and I

$$E = E_0 \sin \omega t$$

$$I = I_0 \sin(\omega t - \theta)$$

Current I lags behind the applied e.m.f. E by θ .

It means that the e.m.f. leads over current by θ .

Equations can also be represented as

$$E = E_0 \sin(\omega t + \theta) \text{ and}$$

$$I = I_0 \sin \omega t.$$

(ii) Resultant voltage

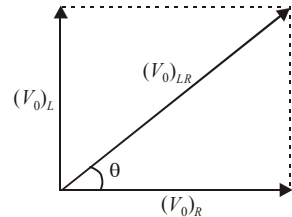
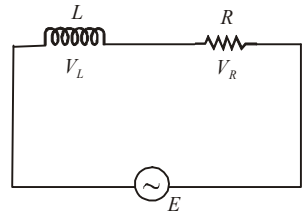
$$\begin{aligned} (V_0)_{LR}^2 &= (V_0)_L^2 + (V_0)_R^2 \\ &= I_0^2 (R^2 + X_L^2) \end{aligned}$$

$$\text{or, } (V_0)_{LR} = I_0 \sqrt{R^2 + \omega^2 L^2}$$

(iii) Power factor $(\cos\theta) = \frac{R}{\sqrt{R^2 + \omega^2 L^2}} = \frac{R}{Z_{LR}}$

(iv) Average power $< P >$

$$< P > = E_{\text{rms}} I_{\text{rms}} \cos\theta.$$



• **R-C circuit**

(i) Equations of E and I

$$E = E_0 \sin \omega t$$

$$I = I_0 \sin(\omega t + \theta)$$

$$\text{or } E = E_0 \sin(\omega t - \theta),$$

$$I = I_0 \sin \omega t.$$

emf E lags behind the current I by θ

or current I leads over e.m.f. by θ

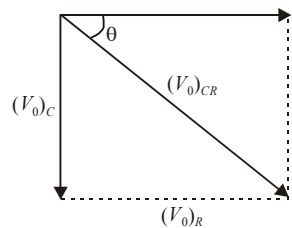
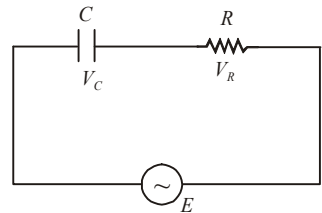
(ii) Resultant voltage $(V_0)_{CR}$

$$\begin{aligned} (V_0)_{CR}^2 &= (V_0)_R^2 + (V_0)_C^2 \\ &= I_0^2 (R^2 + X_C^2) \end{aligned}$$

$$\text{or } (V_0)_{CR} = I_0 \sqrt{R^2 + \frac{1}{\omega^2 C^2}}$$

(iii) Power factor $(\cos\theta)$

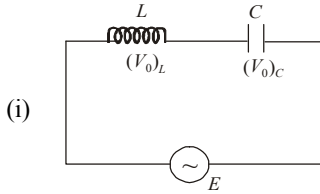
$$\cos\theta = \frac{R}{Z_{CR}} = \frac{R}{\sqrt{R^2 + X_C^2}}$$



(iv) Average power, $\langle P \rangle$

$$\langle P \rangle = \frac{E_{\text{rms}} I_{\text{rms}} R}{Z_{CR}}$$

- **L-C circuit**



(ii) Resultant voltage

$$(V_0)_{LC} = (V_0)_L \sim (V_0)_C$$

$$= I_0(X_L \sim X_C) = I_0\left(\omega L \sim \frac{1}{\omega C}\right)$$

$$= I_0\left[2\pi f L \sim \frac{1}{2\pi f C}\right]$$

- **Phase relations**

- (i) The phase difference between V_L and V_C is 180° *i.e.* they are in mutually opposite phase.
- (ii) V_L leads I by a phase angle of 90° .
- (iii) V_C lags behind I by a phase angle of 90° .
- (iv) I will lead E by 90° if $X_C > X_L$.
- (v) I will lag behind E by 90° if $X_C < X_L$.

- **Impedance or reactance**

(i) $Z = X_L \sim X_C$

(ii) $Z = L\omega \sim \frac{1}{C\omega}$

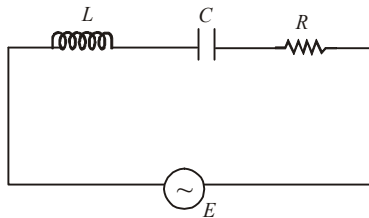
(iii) $Z = 2\pi f L \sim \frac{1}{2\pi f C}$

(iv) If $X_L > X_C$, then $Z = X_L - X_C = \omega L - \frac{1}{\omega C}$

(v) If $X_L < X_C$, then $Z = X_C - X_L = \frac{1}{\omega C} - \omega L$

(vi) If $X_L = X_C$, then $Z = 0$.

- **LCR series circuit**



- (i) The alternating e.m.f. leads/lags behind the current by a phase angle ϕ given by

$$\tan \phi = \frac{\omega L - 1/\omega C}{R}$$

- (ii) The e.m.f. leads the current, if $\omega L > 1/\omega C$ and it lags behind the current, if $\omega L < 1/\omega C$.

- (iii) Impedance of LCR -circuit, $Z = \sqrt{R^2 + (\omega L - 1/\omega C)^2}$

- (iv) Power factor, $\cos \phi = \frac{R}{\sqrt{R^2 + (\omega L - 1/\omega C)^2}} = \frac{R}{Z}$

• **Series resonant circuit**

- (i) L , C and R are connected in series.

- (ii) Condition of resonance is $X_L = X_C$.

$$\Rightarrow L\omega = \frac{1}{C\omega} \Rightarrow LC\omega^2 = 1 \Rightarrow \omega = \frac{1}{\sqrt{LC}}$$

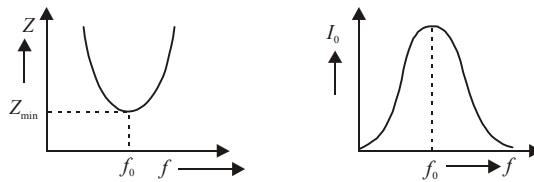
$$\Rightarrow 2\pi f = \frac{1}{\sqrt{LC}} \Rightarrow f = \frac{1}{2\pi\sqrt{LC}}$$

This means that frequency of a.c. applied to circuit becomes equal to natural frequency of energy oscillations in the circuit.

- (iii) $Z = R$ at resonance

$$I_0 = \frac{E_0}{2} = \frac{E_0}{R} = \text{circuit admits maximum current.}$$

The following figures indicate variation of Z and current with frequency.



- (iv) *Acceptor circuit* : Series resonance circuit is known as acceptor circuit.

- (v) *Sharpness at resonance or Q-factor* : Q should be higher for sharper resonance.

$$Q = \frac{1}{R} \sqrt{\frac{L}{C}}$$

• **Parallel resonant circuit**

- (i) It is known as rejector circuit.

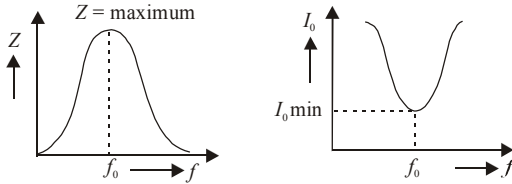
- (ii) L and C are connected in parallel with each other.

- (iii) At resonance, $X_L = X_C$

Impedance Z is maximum.

Current I_0 is minimum.

The figures indicate the variations.



Transformer

- It is based on the phenomenon of mutual induction between two coils known as the primary coil and the secondary coil.
- It is used for transmission of a.c. over long distances at high voltages. The energy losses and cost of transmission are reduced by this device.

• Step-up transformer:

- The output voltage E_s across secondary coil is greater than input voltage E_p in primary coil.
- But $I_s < I_p$.
- $N_s > N_p$ where N denotes the number of turns in the coils.

$$(iv) \frac{E_s}{E_p} = \frac{I_p}{I_s} = \frac{N_s}{N_p} > 1.$$

• Step-down transformer

- The output voltage $E_s < E_p$
- The output current $I_s > I_p$
- The number of turns $N_s < N_p$

$$(iv) \frac{E_s}{E_p} = \frac{I_p}{I_s} = \frac{N_s}{N_p} < 1.$$

• Transformation ratio (K)

$$K = \frac{E_s}{E_p} = \frac{I_p}{I_s} = \frac{N_s}{N_p}.$$

- Efficiency of transformer = $\frac{\text{output power}}{\text{input power}}$

$$\eta = \frac{E_s I_s}{E_p I_p}$$

Energy losses in transformer

- For an ideal transformer,
output power = input power
 $E_s I_s = E_p I_p$

$$\frac{E_s}{E_p} = \frac{I_p}{I_s} = \frac{N_s}{N_p}$$

But in practice, these are losses.

Output power < input power.

The losses are discussed along with remedy.

- **Copper losses**

- (i) Windings are made of copper wire. Energy is lost as heat in resistance of copper wire.

- (ii) It is reduced by use of thick wires of copper.

- **Iron losses/eddy current losses**

- (i) Energy is lost due to eddy currents in the core of transformer.

- (ii) It is reduced by using laminated soft iron core.

- **Flux leakage**

- (i) Some magnetic flux leaks in air between primary and secondary coils.

- (ii) It is reduced by winding the secondary coil over a primary coil using insulator between them.

- **Hysteresis loss**

- (i) The core is magnetised and demagnetised and energy is lost as heat.

- (ii) It is reduced by using soft iron core.

Various material points about transformer

- There is a phase difference of π radian between E_s and E_p . Obviously they are in opposite phases.
- Transformer, a device based on mutual induction, converts magnetic energy into electrical energy.
- Transformer does not amplify power as a vacuum tube (triode) does.
- Law of conservation of energy holds good for a transformer.
- It does not operate on d.c. or direct voltages. It operates only on alternating voltages at input as well as at output.
- Frequency of output voltage across secondary coil is same as that of input voltage across primary coil.

- Efficiency = $\frac{\text{Output power}}{\text{Input power}} = \frac{\text{power in secondary}}{\text{power in primary}}$

Power available in secondary can never be greater than power fed in primary.

At the most, efficiency = 1 = 100%.

Generally, efficiency ranges from 70% to 90%.

Some salient features about a.c., transformer and inductance

- The dimensions of L/R , RC and \sqrt{LC} are the dimensions of time. Their reciprocal have dimensions of frequency.
- Form factor of a.c. is $K = \frac{I_v}{I_m} = \frac{0.707I_0}{0.637I_0} = 1.11$

- The direction of induced e.m.f. depends on
 - (i) direction of magnetic flux
 - (ii) rate of change of magnetic flux *i.e.* $d\phi/dt$ is increasing or decreasing
- An induction coil generates high voltages of the order of 10^5 volts from a battery. It is based on the phenomenon of mutual induction.
- A choke coil is a pure inductor. Average power consumed per cycle is zero in a choke coil.
- For reducing low frequency a.c., choke coil with laminated soft iron cores are used.
- For reducing high frequency a.c., air cored chokes are used.
- A d.c. motor converts d.c. energy from a battery into mechanical energy of rotation.
- A motor starter is a variable resistance connected in series with the motor coil. It protects the motor from damage when it is switched on.
- A d.c. dynamo/generator produces d.c. energy from mechanical energy of rotation of a coil.
- An a.c. dynamo/generator produces a.c. energy from mechanical energy of rotation of a coil.
- **Effective current**
 - (i) The component of a.c. which remains in phase with the alternating e.m.f. is defined as the effective current.
 - (ii) The power lost due to effective current is given by $E_v I_v \cos\theta$.
 - (iii) The peak value of effective current is $I_0 \cos\theta$. Its r.m.s. value is $\frac{I_0}{\sqrt{2}} \cos\theta$.
- Lenz's law is based on the law of conservation of energy.
- $$\text{henry} = \frac{\text{volt}}{\text{amp/sec}} = \frac{\text{volt} \times \text{sec}}{\text{amp}} = \text{ohm} \times \text{sec}$$
- If a solenoid is placed partly in different media, then

$$M = \frac{\mu_0 N_1 N_2}{l} (\mu_1 A_1 + \mu_2 A_2 + \dots)$$
- **Reciprocity relation** : Mutual inductance M depends on two coils. It does not matter which one of them acts as the primary or the secondary coil. The relation

$$M = \frac{\mu_0 A N_1 N_2}{l}$$
 for a solenoid is known as reciprocity relation.