

## Chapter-01

### Relation and Function

#### TYPES OF RELATIONS:

- A relation  $R$  in a set  $A$  is called reflexive if  $(a, a) \in R$  for every  $a \in A$ .
- A relation  $R$  in a set  $A$  is called symmetric if  $(a_1, a_2) \in R$  implies that  $(a_2, a_1) \in R$ , for all  $a_1, a_2 \in A$ .
- A relation  $R$  in a set  $A$  is called transitive if  $(a_1, a_2) \in R$ , and  $(a_2, a_3) \in R$  together imply that  $(a_1, a_3) \in R$ .
- all  $a_1, a_2, a_3 \in A$ .

#### EQUIVALENCE RELATION

- A relation  $R$  in a set  $A$  is said to be an equivalence relation if  $R$  is reflexive, symmetric and transitive.

##### Equivalence Classes

- Every arbitrary equivalence relation  $R$  in a set  $X$  divides  $X$  into mutually disjoint subsets  $(A_i)$  called partitions or subdivisions of  $X$  satisfying the following conditions:
- All elements of  $A_i$  are related to each other for all  $i$
- No element of  $A_i$  is related to any element of  $A_j$  whenever  $i \neq j$
- $A_i \cup A_j = X$  and  $A_i \cap A_j = \Phi$ ,  $i \neq j$ . These subsets  $(A_i)$  are called equivalence classes.
- For an equivalence relation in a set  $X$ , the equivalence class containing  $a \in X$ , denoted by  $[a]$ , is the subset of  $X$  containing all elements  $b$  related to  $a$ .

**\*\*Function: A relation  $f: A \longrightarrow B$  is said to be a function if every element of  $A$  is correlated to a**

Unique element in  $B$ .

**\*A is domain**

**\* B is codomain**