### **NUCLEAR PHYSICS**

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### JEE (Advance) Syllabus

Photoelectric effect; Bohr's theory of hydrogen-like atoms; characteristic and continuous X-rays, Moseley's law; de Broglie wavelength of matter waves.

### JEE (Main) Syllabus

Alpha - particle scattering experiment; Rutherford's model of atom; Bohr model, energy levels, hydrogen spectrum. Composition and size of nucleus, atomic masses, isotopes, isobars; isotones. Radioactivity – alpha, beta and gamma particles/rays and their properties; radioactive decay law. Mass-energy relation, mass defect; binding energy per nucleon and its variation with mass number; nuclear fission and fusion.

Note: Marked Questions can be used for Revision.

## **NUCLEAR PHYSICS**

It is the branch of physics which deals with the study of nucleus.

### 1. NUCLEUS:

- (a) **Discoverer**: Rutherford
- (b) Constituents: neutrons (n) and protons (p) [collectively known as nucleons]
  - 1. **Neutron**: It is a neutral particle. It was discovered by J. Chadwick. Mass of neutron,  $m_n = 1.6749286 \times 10^{-27}$  kg.
  - **2. Proton**: It has a charge equal to +e. It was discovered by Goldstein.

Mass of proton, 
$$m_D = 1.6726231 \times 10^{-27} \text{ kg}$$

$$m_p \approx m_n$$

(c) Representation:

$$_{z}X^{A}$$
 or  $_{z}^{A}X$ 

where  $X \Rightarrow symbol of the atom$ 

 $Z \Rightarrow Atomic number = number of protons$ 

A ⇒ Atomic mass number = total number

of nucleons.

= no. of protons + no. of neutrons.

#### Atomic mass number :

It is the nearest integer value of mass represented in a.m.u. (atomic mass unit).

1 a.m.u. =  $\frac{1}{12}$  [mass of one atom of  ${}_{6}C^{12}$  atom at rest and in ground state]

 $1.6603 \times 10^{-27} \text{ kg}$ ; 931.478 MeV/c<sup>2</sup>

mass of proton  $(m_p)$  = mass of neutron  $(m_p)$  = 1 a.m.u.

#### Some definitions:

(1) Isotopes:

The nuclei having the same number of protons but different number of neutrons are called isotopes.

(2) Isotones:

Nuclei with the same neutron number N but different atomic number Z are called isotones.

(3) Isobars:

The nuclei with the same mass number but different atomic number are called isobars.

(d) Size of nucleus: Order of 10<sup>-15</sup> m (fermi)

Radius of nucleus;  $R = R_0 A^{1/3}$ 

where  $R_0 = 1.1 \times 10^{-15}$  m (which is an empirical constant)

A = Atomic mass number of atom.

(e) Density: density = 
$$\frac{\text{mass}}{\text{volume}} \cong \frac{\text{Am}_p}{\frac{4}{3}\pi\text{R}^3} = \frac{\text{Am}_p}{\frac{4}{3}\pi(\text{R}_0\text{A}^{1/3})^3} = \frac{3\text{m}_p}{4\pi\text{R}_0^3}$$
$$= \frac{3\times1.67\times10^{-27}}{4\times3.14\times(1.1\times10^{-15})^3} = 3\times10^{17}\,\text{kg/m}^3$$

Nuclei of almost all atoms have almost same density as nuclear density is independent of the mass number (A) and atomic number (Z).

### SOLVED EXAMPLE \_\_\_\_\_

**Example 1.** Calculate the radius of <sup>70</sup>Ge.

**Solution:** We have,

R = 
$$R_0 A^{1/3}$$
 = (1.1 fm) (70)<sup>1/3</sup>  
= (1.1 fm) (4.12) = 4.53 fm.

**Example 2.** Calculate the electric potential energy of interaction due to the electric repulsion between two nuclei of <sup>12</sup>C when they 'touch' each other at the surface

**Solution:** The radius of a <sup>12</sup>C nucleus is

R = 
$$R_0 A^{1/3}$$
  
= (1.1 fm) (12)<sup>1/3</sup> = 2.52 fm.

The separation between the centres of the nuclei is 2R = 5.04 fm. The potential energy of the pair is

$$U = \frac{q_1 q_2}{4\pi\epsilon_0 \Gamma}$$

$$= (9 \times 10^9 \text{ N-m}^2/\text{C}^2) \frac{(6 \times 1.6 \times 10^{-19} \text{ C})^2}{5.04 \times 10^{-15} \text{ m}}$$

$$= 1.64 \times 10^{-12} \text{ J} = 10.2 \text{ MeV}.$$



#### 2. MASS DEFECT

It has been observed that there is a difference between expected mass and actual mass of a nucleus.

$$M_{\text{expected}} = Z m_{p} + (A - Z) m_{n}$$

$$M_{\text{observed}} = M_{\text{atom}} - Z m_{e}$$

It is found that

$$M_{observed} < M_{expected}$$

Hence, mass defect is defined as

$${\sf Mass \, defect = M}_{\sf expected} - {\sf M}_{\sf observed}$$

$$\Delta m = [Zm_p + (A - Z)m_n] - [M_{atom} - Zm_e]$$

### 3. BINDING ENERGY

It is the minimum energy required to break the nucleus into its constituent particles.

or

Amount of energy released during the formation of nucleus by its constituent particles and bringing them from infinite separation.

Binding Energy (B.E.) =  $\Delta mc^2$ 

BE = 
$$\Delta m$$
 (in amu) × 931.5 MeV/amu

**Note:** If binding energy per nucleon is more for a nucleus then it is more stable.

For example

$$\mathbf{f} \qquad \left(\frac{B.E_1}{A_1}\right) > \left(\frac{B.E_2}{A_2}\right)$$

then nucleus 1 would be more stable.

### SOLVED EXAMPLE \_\_\_\_\_

**Example 3.** Following data is available about 3 nuclei P, Q & R. Arrange them in decreasing order of stability

	Р	Q	R
Atomic mass number (A)	10	5	6
Binding Energy (MeV)	100	60	66

**Solution:** 
$$\left(\frac{B.E}{A}\right)_{P} = \frac{100}{10} = 10$$

$$\left(\frac{BE}{A}\right)_{O} = \frac{60}{5} = 12$$

$$\left(\frac{B.E.}{A}\right)_{R} = \frac{66}{6} = 11$$

∴ Stability order is Q > R > P.

**Example 4.** The three stable isotopes of neon:  $^{20}_{10}$ Ne ,  $^{21}_{10}$ Ne and  $^{22}_{10}$ Ne have respective abundances of 90.51% 0.27% and 9.22% . The atomic masses of three isotopes are 19.99 u. 20.99 u, respectively. Obtain the average atomic mass of neon.

**Solution**: 
$$m = \frac{90.51 \times 19.99 + 0.27 \times 20.99 + 9.22 \times 22}{100} = 20.18 \text{ u}$$

**Example 5** A nuclear reaction is given as

$$A + B \rightarrow C + D$$

Binding energies of A, B, C and D are given as

$$B_1$$
,  $B_2$ ,  $B_3$  and  $B_4$ 

Find the energy released in the reaction

**Solution:** 
$$(B_3 + B_4) - (B_1 + B_2)$$

**Example 6.** Calculate the binding energy of an alpha particle from the following data:

mass of 
$${}_{1}^{1}H$$
 atom = 1.007826 u

mass of 
$${}_{2}^{4}$$
He atom = 4.00260 u

Take 1 u = 
$$931 \text{ MeV/c}^2$$
.

**Solution:** The alpha particle contains 2 protons and 2 neutrons. The binding energy is

B = 
$$(2 \times 1.007826 \text{ u} + 2 \times 1.008665 \text{ u} - 4.00260 \text{ u})c^2$$

$$= (0.03038 \text{ u})c^2$$

$$= 0.03038 \times 931 \text{ MeV} = 28.3 \text{ MeV}.$$

**Example 7.** Find the binding energy of  ${}^{56}_{26}$ Fe . Atomic mass of  ${}^{56}$ Fe is 55.9349 u and that of  ${}^{1}$ H is 1.00783 u. Mass of neutron = 1.00867 u.

**Solution :** The number of protons in  ${}^{56}_{26}$ Fe = 26 and the number of neutrons = 56-26=30.

The binding energy of  $^{56}_{26}$ Fe is

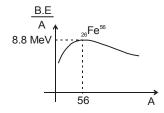
$$= (0.52878 \text{ u})c^2$$



### Variation of binding energy per nucleon with mass number :

The binding energy per nucleon first increases on an average and reaches a maximum of about 8.8 MeV for  $A \Box 50 \rightarrow 80$ . For still heavier nuclei, the binding energy per nucleon slowly decreases as A increases.

Binding energy per nucleon is maximum for  $_{26}$ Fe $^{56}$ , which is equal to 8.8 MeV. Binding energy per nucleon is more for medium nuclei than for heavy nuclei. Hence, medium nuclei are highly stable.



- \* The heavier nuclei being unstable have tendency to split into medium nuclei. This process is called Fission.
- \* The Lighter nuclei being unstable have tendency to fuse into a medium nucleus. This process is called **Fusion**.

#### **NUCLEAR COLLISIONS**

We can represent a nuclear collision or reaction by the following notation, which means X (a,b) Y

We can apply:

(i) Conservation of momentum (ii) Conservation of charge (iii) Conservation of mass-energy

By mass energy conservation

(i) 
$$K_1 + K_2 + (m_\alpha + m_x)c^2 = K_3 + K_4 + (m_y + m_b)c^2$$

(ii) Energy released in any nuclear reaction or collision is called Q value of the reaction

(iii) 
$$Q = (K_3 + K_4) - (K_1 + K_2) = \sum K_p - \sum K_p = (\sum m_p - \sum m_p)c^2$$

(iv) If Q is positive, energy is released and products are more stable in comparison to reactants.

(v) If Q is negative, energy is absorbed and products are less stable in comparison to reactants.

$$Q = \Sigma(B.E.)_{product} - \Sigma(B.E.)_{reactants}$$

### Solved Example \_\_\_\_\_

**Example 8.** Let us find the Q value of fusion reaction

$$^{4}$$
He +  $^{4}$ He  $\rightarrow$   $^{8}$ Be, if  $\frac{B.E.}{A}$  of He = X and  $\frac{B.E.}{A}$  of Be = Y  $\Longrightarrow$  Q = 8Y - 8X

Solution: Q value for  $\alpha$  decay  $_{z}X^{A} \rightarrow _{z-2}Y^{A-4} + _{2}He^{4} \Longrightarrow Q = K_{\alpha} + K_{\gamma}$  ....(i)

Momentum conservation,  $p_y = p_\alpha$  ...(ii)

$$K_{\alpha} = \frac{p^2}{2 \times m \times 4}$$
  $K_{\gamma} = \frac{p^2}{2m(A-4)} = \frac{4K_{\alpha}}{A-4}$ 

$$Q = K_{\alpha} + \frac{4K_{\alpha}}{A - 4} = \frac{A}{A - 4}K_{\alpha} \qquad K_{\alpha} = \frac{A - 4}{A}Q$$

For  $\alpha$  decay A > 210 which means maximum part of released energy is associated with K.E. of  $\alpha$ . If Q is negative, the reaction is endoergic. The minimum amount of energy that a bombarding particle must have in order to initiate an endoergic reaction is called Threshold energy E<sub>10</sub>,

given by E  $_{\rm th}$  = –Q  $\left(\frac{m_1}{m_2}+1\right)$  where  $\rm\,m_1$  = mass of the projectile.

 $E_{th}$  = minimum kinetic energy of the projectile to initiate the nuclear reaction  $m_2$  = mass of the target

**Example 9.** How much energy must a bombarding proton possess to cause the reaction  ${}_{3}\text{Li}^{7} + {}_{1}\text{H}^{1} \rightarrow {}_{4}\text{Be}^{7} + {}_{0}\text{N}^{1}$  (Mass of  ${}_{3}\text{Li}^{7}$  atom is 7.01600, mass of  ${}_{4}\text{H}^{1}$  atom is 1.0783, mass of  ${}_{4}\text{Be}^{7}$  atom is 7.01693)

**Solution:** Since the mass of an atom includes the masses of the atomic electrons, the appropriate number of electron masses must be subtracted from the given values.

**Reactants**: Total mass =  $(7.01600 - 3 \text{ m}_{\odot}) + (1.0783 - 1 \text{ m}_{\odot}) = 8.0943 - 4 \text{ m}_{\odot}$ 

**Products**: Total mass =  $(7.01693 - 4m_{g}) + 1.0087 = 8.02563 - 4m_{g}$ 

The energy is supplied as kinetic energy of the bombarding proton. The incident proton must have more than this energy because the system must possess some kinetic energy even after the reaction, so that momentum is conserved with momentum conservation taken into account, the minimum kinetic energy that the incident particle must possess can be found with the formula.

where,  $Q = -[(8.02563 - 4m_a) - (8.0943 - 4m_a)] 931.5 \text{ MeV} = -63.96 \text{ MeV}$ 

$$E_{th} = -\left(1 + \frac{m}{M}\right) Q = -\left(1 + \frac{1}{7}\right) (-63.96) = 73.1 \text{ MeV}$$

### 

#### 4. RADIOACTIVITY:

It was discovered by Henry Becquerel.

Spontaneous emission of radiations  $(\alpha, \beta, \gamma)$  from unstable nucleus is called **radioactivity**. Substances which shows radioactivity are known as **radioactive substance**.

Radioactivity was studied in detail by Rutherford.

In radioactive decay, an unstable nucleus emits  $\alpha$  particle or  $\beta$  particle. After emission of  $\alpha$  or  $\beta$  the remaining nucleus may emit  $\gamma$ -particle, and converts into more stable nucleus.

### $\alpha$ -particle:

It is a doubly charged helium nucleus. It contains two protons and two neutrons.

Mass of  $\alpha$ -particle = Mass of  $_{2}$ He<sup>4</sup> atom – 2m<sub>2</sub>  $\approx 4$  m<sub>2</sub>

Charge of  $\alpha$ -particle = + 2 e

### $\beta$ -particle:

(a)  $\beta^-$  (electron):

Mass =  $m_a$ ; Charge = -e

(b)  $\beta^+$  (positron):

Mass =  $m_a$ ; Charge = +e

positron is an antiparticle of electron.

### **Antiparticle:**

A particle is called antiparticle of other if on collision both can annihilate (destroy completely) and converts into energy. For example : (i) electron (-e,  $m_e$ ) and positron (+e,  $m_e$ ) are anti particles. (ii) neutrino (v) and antineutrino ( $\overline{v}$ ) are anti particles.

 $\gamma$ -particle: They are energetic photons of energy of the order of Mev and having rest mass zero.

### 5. RADIOACTIVE DECAY (DISPLACEMENT LAW):

#### $\alpha$ -decay:

$$_{7}X^{A}$$
  $\rightarrow$   $_{7-2}Y^{A-4} + _{2}He^{4} + Q$ 

Q value: It is defined as energy released during the decay process.

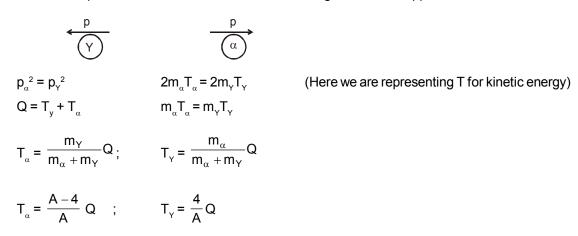
Q value = rest mass energy of reactants – rest mass energy of products.

This energy is available in the form of increase in K.E. of the products.

Let, 
$$M_x = \text{mass of atom }_Z X^A$$
  
 $M_y = \text{mass of atom }_{Z-2} Y^{A-4}$   
 $M_{He} = \text{mass of atom }_2 He^4$ .  
Q value =  $[(M_x - Zm_e) - \{(M_y - (Z-2) m_e) + (M_{He} - 2m_e)\}]c^2$   
=  $[M_x - M_y - M_{He}] c^2$   
Considering actual number of electrons in  $\alpha$ -decay  
Q value =  $[M_x - (M_y + 2m_e) - (M_{He} - 2m_e)]c^2$   
=  $[M_x - M_y - M_{He}] c^2$   
 $Z$ -electrons (it has charge + 2e)

### Calculation of kinetic energy of final products:

As atom X was initially at rest and no external forces are acting, so final momentum also has to be zero. Hence both Y and  $\alpha$ -particle will have same momentum in magnitude but in opposite direction.

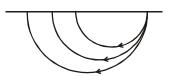


From the above calculation, one can see that all the  $\alpha$ -particles emitted should have same kinetic energy. Hence, if they are passed through a region of uniform magnetic field having direction perpendicular to velocity, they should move in a circle of same radius.

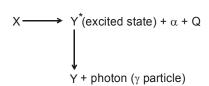
$$r = \frac{mv}{qB} = \frac{mv}{2eB} = \frac{\sqrt{2Km}}{2eB}$$

### **Experimental Observation:**

Experimentally it has been observed that all the  $\alpha$ -particles do not move in the circle of same radius, but they move in `circles having different radii.



This shows that they have different kinetic energies. But it is also observed that they follow circular paths of some fixed values of radius i.e. yet the energy of emitted  $\alpha\text{-particles}$  is not same but it is quantized. The reason behind this is that all the daughter nuclei produced are not in their ground state but some of the daughter nuclei may be produced in their



excited states and they emits photon to acquire their ground state.

The only difference between Y and Y\* is that Y\* is in excited state and Y is in ground state.

Let, the energy of emitted  $\gamma$ -particles be E

$$\therefore$$
 Q = T<sub>a</sub> + T<sub>y</sub> + E

where Q = 
$$[M_x - M_y - M_{He}] c^2$$

$$T_{\alpha} + T_{\nu} = Q - E$$

$$T_{\alpha} = \frac{m_{Y}}{m_{\alpha} + m_{Y}} (Q - E); T_{Y} = \frac{m_{\alpha}}{m_{\alpha} + m_{Y}} (Q - E)$$

### β-- decay :

$$_{z}X^{A} \longrightarrow _{z+1}Y^{A} + _{-1}e^{0} + Q$$

\_1e<sup>0</sup> can also be written as \_1β<sup>0</sup>.

Here also one can see that by momentum and energy conservation, we will get

$$T_e = \frac{m_Y}{m_e + m_Y} Q;$$

$$T_{Y} = \frac{m_{e}}{m_{e} + m_{Y}} Q$$

as m<sub>a</sub> << m<sub>y</sub>, we can consider that all the energy is taken away by the electron.

From the above results, we will find that all the  $\beta$ -particles emitted will have

same energy and hence they have same radius if passed through a region of perpendicular magnetic field. But, experimental observations were completely different. On passing through a region of uniform magnetic field perpendicular to the velocity, it was observed that  $\beta$ -particles take circular paths of different radius having a continuous spectrum.



To explain this, Paulling has introduced the extra particles called neutrino and antineutrino (antiparticle of neutrino).

 $\overline{v} \rightarrow$  antineutrino,  $v \rightarrow$  neutrino

### Properties of antineutrino( $\overline{v}$ ) & neutrino(n) :

- (1) They are like photons having rest mass = 0
  - speed = c

Energy,  $E = mc^2$ 

- (2) They are chargeless (neutral)
- (3) They have spin quantum number,  $s = \pm \frac{1}{2}$

Considering the emission of antineutrino, the equation of  $\beta^-$  - decay can be written as

$$_{7}X^{A} \longrightarrow _{7+1}Y^{A} + _{-1}e^{0} + Q + \overline{\nu}$$

Production of antineutrino along with the electron helps to explain the continuous spectrum because the

energy is distributed randomly between electron and  $\overline{v}$  and it also helps to explain the spin quantum number balance (p, n and  $\pm$  e each has spin quantum number  $\pm$  1/2).

During  $\beta^-$  - decay, inside the nucleus a neutron is converted to a proton with emission of an electron and antineutrino.

$$n \rightarrow p + _{-1}e^{0} + \overline{\nu}$$

Let,  $M_y = \text{mass of atom }_{z}X^A$ 

 $M_v = \text{mass of atom}_{7+1} Y^A$ 

m = mass of electron

Q value = 
$$[(M_v - Zm_a) - \{(M_v - (z + 1) m_a) + m_a\}] c^2 = [M_v - M_v] c^2$$

Considering actual number of electrons.

Q value = 
$$[M_v - \{(M_v - m_a) + m_a\}] c^2 = [M_v - M_v] c^2$$

### SOLVED EXAMPLE \_\_\_\_\_

### **Example 10.** Consider the beta decay

<sup>198</sup> Au 
$$\rightarrow$$
 <sup>198</sup> Hg\* +  $\beta$ - +  $\overline{\nu}$ 

where <sup>198</sup>Hg\* represents a mercury nucleus in an excited state at energy 1.088 MeV above the ground state. What can be the maximum kinetic energy of the electron emitted? The atomic mass <sup>198</sup>Au is 197.968233 u and that of <sup>198</sup>Hg is 197.966760 u.

Solution:

If the product nucleus <sup>198</sup>Hg is formed in its ground state, the kinetic energy available to the electron and the antineutrino is

$$Q = [m(^{198}Au) - m(^{198}Hg)]c^{2}$$
.

As <sup>198</sup>Hg\* has energy 1.088 MeV more than <sup>198</sup>Hg in ground state, the kinetic energy actually available is  $Q = [m(^{198}Au) - m(^{198}Hg)]c^2 - 1.088 \text{ MeV}$ 

= (197.968233 u – 197.966760 u) 
$$\left(931\frac{\text{MeV}}{\text{u}}\right)$$
 – 1.088 MeV

This is also the maximum possible kinetic energy of the electron emitted.



#### β+ - decay:

$$_{7}X^{A} \rightarrow _{7-1}Y^{A} + _{+1}e^{0} + v + Q$$

In  $\beta^+$  decay, inside a nucleus a proton is converted into a neutron, positron and neutrino.

$$p \rightarrow n + \mu e^0 + \nu$$

As mass increases during conversion of proton to a neutron, hence it requires energy for  $\beta^+$  decay to take place,  $\beta^+$  decay is rare process. It can take place in the nucleus where a proton can take energy from the nucleus itself.

Q value = 
$$[(M_{\chi} - Zm_{e}) - \{(M_{\gamma} - (Z - 1) m_{e}) + m_{e}\}] c^{2}$$
  
=  $[M_{\chi} - M_{\gamma} - 2m_{a}] c^{2}$ 

Considering actual number of electrons.

Q value = 
$$[M_{\chi} - \{(M_{\gamma} + m_{e}) + m_{e}\}] c^{2}$$
  
=  $[M_{\chi} - M_{\gamma} - 2m_{e}] c^{2}$ 

### SOLVED EXAMPLE \_\_\_\_\_

**Example 11.** Calculate the Q-value in the following decays:

(a) 
$$^{19}\text{O} \rightarrow ^{19}\text{F} + \text{e}^- + \, \overline{\nu}$$

(b) 
$$^{25}AI \rightarrow ^{25}Mg + e^+ + \nu$$
.

The atomic masses needed are as follows:

**Solution**: (a) The Q-value of  $\beta^-$ -decay is

Q = 
$$[m(^{19}O) - m(^{19}F)]c^2$$
  
=  $[19.003576 u - 18.998403 u] (931 MeV/u)$   
=  $4.816 MeV$ 

(b) The Q-value of  $\beta^+$ -decay is

$$Q = [m(^{25}AI) - m(^{25}Mg) - 2m_e]c^2$$

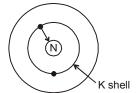
$$= \left[24.99032 \, u - 24.985839 \, u - 2 \times 0.511 \frac{\text{MeV}}{c^2}\right] c^2$$

= (0.004593 u) (931 MeV/u) - 1.022 MeV



### K capture:

It is a rare process which is found only in few nucleus. In this process the nucleus captures one of the atomic electrons from the K shell. A proton in the nucleus combines with this electron and converts itself into a neutron. A neutrino is also emitted in the process and is emitted from the nucleus.



$$p + _{-1}e^0 \rightarrow n + \nu$$

If X and Y are atoms then reaction is written as:

$$_{z}X^{A} \rightarrow_{z-1}Y^{A} + v + Q + characteristic x-rays of Y.$$

If X and Y are taken as nucleus, then reaction is written as:

$$_{Z}X^{A}$$
 +  $_{-1}e^{0}$   $ightarrow$   $_{Z-1}Y^{A}$  +  $\nu$ 

**Note:** (1) Nuclei having atomic numbers from Z = 84 to 112 shows radioactivity.

- (2) Nuclei having Z = 1 to 83 are stable (only few exceptions are there)
- (3) Whenever a neutron is produced, a neutrino is also produced.
- (4) Whenever a neutron is converted into a proton, a antineutrino is produced.

### Properties of $\alpha$ , $\beta$ and $\gamma$ rays

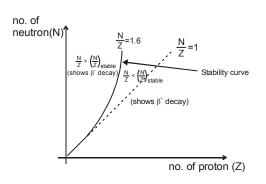
Features	α-particles	β-particles	γ–rays
Identity	Helium nucleus or doubly	Fast moving electrons	Electromagnetic wave
	ionised helium atom (,He <sup>4</sup> )	$(\beta^0 \text{ or } \beta^-)$	(photons)
Charge	Twice of proton (+2e) $\approx 4 \text{m}_{\text{p}}$	Electronic (– e)	Neutral
Mass	p	(rest mass of $\beta$ )	rest mass = 0
Widoo	m <sub>p</sub> -mass of proton	= (rest mass of electron)	Took made
Speed	1.4 × 10 <sup>7</sup> m/s. to	1% of c to 99% of c	Only c = 3 × 108 m/s
·	2.2 × 10 <sup>7</sup> m/s.	(All possible values	γ–photons come out with
	(Only certain value	between this range)	same speed from all
	between this range).	β–particles come out with	types of nucleus.
	Their speed depends on	different speeds from the	So, can not be a
	nature of the nucleus.	same type of nucleus.	characteristic speed.
	So that it is a	So that it can not	·
	characteristic speed.	be a characteristic speed.	
K.E.	≈ MeV	≈ MeV	≈ MeV
Energy	Line and discrete	Continuous	Line and discrete
spectrum	(or linear)	(or linear)	
Ionization	10,000 times	100 times of γ–rays	
power ( $\alpha$ > $\beta$ > $\gamma$ )	of γ–rays	(or $\frac{1}{100}$ times of $\alpha$ )	1 (or $\frac{1}{100}$ times of $\beta$ )
Penetration	$\frac{1}{10000}$ times of $\gamma$ -rays	$\frac{1}{100}$ times of $\gamma$ -rays	1(100 times of $\beta$ )
power ( $\gamma$ > $\beta$ > $\alpha$ )		(100 times of $\alpha$ )	
Effect of electric or magnetic field	Deflection	Deflection (More than $\alpha$ )	No deflection
Explanation of emission	By Tunnel effect (or quantum mechanics)	By weak nuclear interactions	With the help of energy levels in nucleus

### 6. **NUCLEAR STABILITY:**

Figure shows a plot of neutron number N versus proton number Z

for the nuclides found in nature. The solid line in the figure represents the stable nuclides. For light stable nuclides, the neutron number is equal to the proton number so that ratio N/Z is equal to 1. The ratio N/Z increases for the heavier nuclides and becomes about 1.6 for the heaviest stable nuclides.

The points (Z, N) for stable nuclides fall in a rather well-defined



narrow region. There are nuclides to the left of the stability belt as well as to the right of it. The nuclides to the left of the stability region have excess neutrons, whereas, those to the

right of the stability belt have excess protons. These nuclides are unstable and decay with time according to the laws of radioactive disintegration. Nuclides with excess neutrons (lying above stability belt) show  $\beta^-$  decay while nuclides with excess protons (lying below stability belt) show  $\beta^+$  decay and K - capture.

#### 7. NUCLEAR FORCE:

- (i) Nuclear forces are basically attractive and are responsible for keeping the nucleons bound in a nucleus in spite of repulsion between the positively charge protons.
- (ii) It is strongest force with in nuclear dimensions (F = 100 F = )
- (iii) It is short range force (acts only inside the nucleus)
- (iv) It acts only between neutron-neutron, neutron-proton and proton-proton i.e. between nucleons.
- (v) It does not depend on the nature of nucleons.
- (vi) An important property of nuclear force is that it is not a central force. The force between a pair of nucleons is not solely determined by the distance between the nucleons. For example, the nuclear force depends on the directions of the spins of the nucleons. The force is stronger if the spins of the nucleons are parallel (i.e., both nucleons have  $m_s = + 1/2$  or 1/2) and is weaker if the spins are antiparallel (i.e., one nucleon has  $m_s = + 1/2$  and the other has  $m_s = 1/2$ ). Here  $m_s$  is spin quantum number.

#### 8. RADIOACTIVE DECAY: STATISTICAL LAW:

(Given by Rutherford and Soddy)

Rate of radioactive decay ∞ N

where N = number of active nuclei

$$= \lambda N$$

where  $\lambda$ = decay constant of the radioactive substance.

Decay constant is different for different radioactive substances, but it does not depend on amount of substance and time.

SI unit of  $\lambda$  is s<sup>-1</sup>

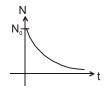
If  $\lambda_1 > \lambda_2$  then first substance is more radioactive (less stable) than the second one.

For the case, if A decays to B with decay constant  $\lambda$ 

$$A \xrightarrow{\lambda} B$$
  
 $t = 0 \quad N_0 \quad 0$  where  $N_0 =$  number of active nuclei of A at  $t = 0$   
 $t = t \quad N \quad N'$  where N = number of active nuclei of A at  $t = t$ 

Rate of radioactive decay of A =  $-\frac{dN}{dt} = \lambda N$ 

$$-\int_{N_0}^{N} \frac{dN}{N} = \int_{0}^{t} \lambda dt \implies N = N_0 e^{-\lambda t}$$
 (it is exponential decay)



Number of nuclei decayed (i.e. the number of nuclei of B formed)

$$N' = N_0 - N$$

$$= N_0 - N_0 e^{-\lambda t}$$

$$N' = N_0 (1 - e^{-\lambda t})$$



### Half life $(T_{1/2})$ :

It is the time in which number of active nuclei becomes half.

$$N = N_0 e^{-\lambda t}$$

After one half life,  $N = \frac{N_0}{2}$ 

$$N = \frac{N_0}{2}$$

$$\frac{N_0}{2} = N_0 e^{-\lambda t} \Rightarrow t = \frac{\ln 2}{\lambda} \Rightarrow \frac{0.693}{\lambda} = t_{_{1/2}}$$

$$t_{1/2} = \frac{\ln 2}{\lambda} = \frac{0.693}{\lambda}$$
 (to be remembered)

Number of nuclei present after n half lives i.e. after a time  $t = n t_{1/2}$ 

$$N = N_0 e^{-\lambda t} \qquad = N_0 e^{-\lambda n t_{1/2}} \qquad = N_0 e^{-\lambda n \frac{\ln 2}{\lambda}}$$

 $= N_0 e^{\ln 2^{(-n)}} = N_0 (2)^{-n} = N_0 (1/2)^n = \frac{N_0}{2^n}$ 

 $\{n = \frac{t}{t_{1/2}}\}$ . It may be a fraction, need not to be an integer

 $N_0 \xrightarrow{\text{after 1st}} \frac{N_0}{2} \xrightarrow{2} N_0 \left(\frac{1}{2}\right)^2 \xrightarrow{3} N_0 \left(\frac{1}{2}\right)^3 \dots \frac{n}{2} N_0 \left(\frac{1}{2}\right)^n$ 

### SOLVED EXAMPLE \_\_\_

A radioactive sample has 6.0 × 10<sup>18</sup> active nuclei at a certain instant. How many of these nuclei will Example 12. still be in the same active state after two half-lives?

Solution: In one half-life the number of active nuclei reduces to half the original number. Thus, in two half lives the number is reduced to  $\left(\frac{1}{2}\right) \times \left(\frac{1}{2}\right)$  of the original number. The number of remaining active nuclei is, therefore,  $6.0 \times 10^{18} \times \left(\frac{1}{2}\right) \times \left(\frac{1}{2}\right) = 1.5 \times 10^{18}$ .

Example 13. The number of <sup>238</sup>U atoms in an ancient rock equals the number of <sup>206</sup>Pb atoms. The half-life of decay of  $^{238}$ U is 4.5 × 10  $^{9}$  y. Estimate the age of the rock assuming that all the  $^{206}$ Pb atoms are formed from the decay of 238U.

Since the number of <sup>206</sup>Pb atoms equals the number of <sup>238</sup>U atoms, half of the original <sup>238</sup>U atoms have Solution: decayed. It takes one half-life to decay half of the active nuclei. Thus, the sample is 4.5 × 10° y old.

### Ш

### **Activity:**

Activity is defined as rate of radioactive decay of nuclei

It is denoted by A or R  $A = \lambda N$ 

If a radioactive substance changes only due to decay then

$$A = -\frac{dN}{dt}$$

As in that case,  $N = N_0 e^{-\lambda t}$ 

$$A = \lambda N = \lambda N_0 e^{-\lambda t}$$

$$A = A_0 e^{-\lambda t}$$

SI Unit of activity: becquerel (Bq) which is same as 1 dps (disintegration per second)

The popular unit of activity is curie which is defined as

1 curie = 
$$3.7 \times 10^{10}$$
 dps

(which is activity of 1 gm Radium)

### SOLVED EXAMPLE \_\_\_\_

- **Example 14.** The decay constant for the radioactive nuclide  $^{64}$ Cu is  $1.516 \times 10^{-5}$  s<sup>-1</sup>. Find the activity of a sample containing 1  $\mu$ g of  $^{64}$ Cu. Atomic weight of copper = 63.5 g/mole. Neglect the mass difference between the given radioisotope and normal copper.
- **Solution :** 63.5 g of copper has  $6 \times 10^{23}$  atoms. Thus, the number of atoms in 1  $\mu$ g of Cu is

$$N = \frac{6 \times 10^{23} \times 1 \mu g}{63.5 g} = 9.45 \times 10^{15}$$

The activity =  $\lambda N$ 

= 
$$(1.516 \times 10^{-5} \text{ s}^{-1}) \times (9.45 \times 10^{15})$$
 =  $1.43 \times 10^{11}$  disintegrations/s

$$= \frac{1.43 \times 10^{11}}{3.7 \times 10^{10}} \text{ Ci} = 3.86 \text{ Ci}.$$

## Activity after n half lives: $\frac{A_0}{2^n}$

- **Example 15.** The half-life of a radioactive nuclide is 20 hours. What fraction of original activity will remain after 40 hours?
- **Solution:** 40 hours means 2 half lives.

Thus, 
$$A = \frac{A_0}{2^2} = \frac{A_0}{4}$$
 or,

r, 
$$\frac{A}{A_0} = \frac{1}{4}$$
.

So one fourth of the original activity will remain after 40 hours.

**Specific activity:** The activity per unit mass is called specific activity.

### Average Life:

$$\mathbf{T}_{\mathsf{avg}} = \frac{\mathsf{sum of ages of all the nuclei}}{\mathsf{N}_0} = \frac{\int\limits_0^\infty \lambda \mathsf{N}_0 \mathrm{e}^{-\lambda t} \ \mathsf{dt.t}}{\mathsf{N}_0} = \frac{1}{\lambda}$$

### SOLVED EXAMPLE \_\_\_\_\_

**Example 16.** The half-life of <sup>198</sup>Au is 2.7 days. Calculate (a) the decay constant, (b) the average-life and (c) the activity of 1.00 mg of <sup>198</sup>Au. Take atomic weight of <sup>198</sup>Au to be 198 g/mol.

**Solution**: (a) The half-life and the decay constant are related as

$$t_{_{1/2}} = \frac{In2}{\lambda} \ = \frac{0.693}{\lambda} \qquad \text{ or, } \qquad \lambda = \frac{0.693}{t_{_{1/2}}} = \frac{0.693}{2.7\,\text{days}}$$

$$= \frac{0.693}{2.7 \times 24 \times 3600 \,s} = 2.9 \times 10^{-6} \,s^{-1}.$$

- (b) The average-life is  $t_{av} = \frac{1}{\lambda} = 3.9$  days.
- (c) The activity is A =  $\lambda$ N. Now, 198 g of <sup>198</sup>Au has 6 × 10<sup>23</sup> atoms.

The number of atoms in 1.00 mg of <sup>198</sup>Au is

$$N = 6 \times 10^{23} \times \frac{1.0 \text{ mg}}{198 \text{ g}} = 3.03 \times 10^{18}.$$

Thus,  $A = \lambda N = (2.9 \times 10^{-6} \text{ s}^{-1}) (3.03 \times 10^{18})$ =  $8.8 \times 10^{12}$  disintegrations/s

$$= \frac{8.8 \times 10^{12}}{3.7 \times 10^{10}}$$
 Ci = 240 Ci.

**Example 17.** Suppose, the daughter nucleus in a nuclear decay is itself radioactive. Let  $\lambda_p$  and  $\lambda_d$  be the decay constants of the parent and the daughter nuclei. Also, let  $N_p$  and  $N_d$  be the number of parent and daughter nuclei at time t. Find the condition for which the number of daughter nuclei becomes constant.

**Solution :** The number of parent nuclei decaying in a short time interval t to t + dt is  $\lambda_p N_p dt$ . This is also the number of daughter nuclei decaying during the same time interval is  $\lambda_d N_d dt$ . The number of the daughter nuclei will be constant if

$$\lambda_{p}N_{p}dt = \lambda_{d}N_{d}dt$$
or, 
$$\lambda_{p}N_{p} = \lambda_{d}N_{d}.$$

**Example 18.** A radioactive sample decays with an average-life of 20 ms. A capacitor of capacitance 100  $\mu$ F is charged to some potential and then the plates are connected through a resistance R. What should be the value of R so that the ratio of the charge on the capacitor to the activity of the radioactive sample remains constant in time?

**Solution:** The activity of the sample at time t is given by

$$A = A_0 e^{-\lambda t}$$

where  $\lambda$  is the decay constant and  $A_0$  is the activity at time t=0 when the capacitor plates are connected. The charge on the capacitor at time t is given by

$$Q = Q_0 e^{-t/CR}$$

where  $Q_0$  is the charge at t = 0 and C = 100  $\mu F$  is the capacitance. Thus,  $\frac{Q}{A} = \frac{Q_0}{A_0} \frac{e^{-t/CR}}{e^{-\lambda t}}$ .

It is independent of t if  $\lambda = \frac{1}{CR}$ 

or, 
$$R = \frac{1}{\lambda C} = \frac{t_{av}}{C} = \frac{20 \times 10^{-3} \text{s}}{100 \times 10^{-6} \text{F}} = 200 \ \Omega.$$

**Example 19.** A radioactive nucleus can decay by two different processes. The half-life for the first process is t<sub>1</sub> and that for the second process is t<sub>2</sub>. Show that the effective half-life t of the nucleus is given by

$$\frac{1}{t} = \frac{1}{t_1} + \frac{1}{t_2} \ .$$

Solution: The decay constant for the first process is  $\lambda_1 = \frac{\ln 2}{t_1}$  and for the second process it is  $\lambda_2 = \frac{\ln 2}{t_1}$ . The probability that an active nucleus decays by the first process in a time interval dt is  $\lambda_1$ dt. Similarly, the probability that it decays by the second process is  $\lambda_2$ dt. The probability that it either decays by the first process or by the second process is  $\lambda_1$ dt +  $\lambda_2$ dt. If the effective decay constant is  $\lambda$ , this probability is also equal to  $\lambda$ dt. Thus.

$$\lambda dt = \lambda_1 dt + \lambda_2 dt$$

or, 
$$\lambda = \lambda_1 + \lambda_2$$
 or, 
$$\frac{1}{t} = \frac{1}{t_1} + \frac{1}{t_2}$$
 (To be remembered)

**Example 20.** A factory produces a radioactive substance A at a constant rate R which decays with a decay constant  $\lambda$  to form a stable substance. Find (i) the no. of nuclei of A and (ii) Number of nuclei of B, at any time t assuming the production of A starts at t = 0. (iii) Also find out the maximum number of nuclei of 'A' present at any time during its formation.

**Solution**: Factory 
$$\xrightarrow{R} A \xrightarrow{\lambda} B$$

Let N be the number of nuclei of A at any time t

$$\therefore \qquad \frac{dN}{dt} = R - \lambda N \qquad \qquad \int_{0}^{N} \frac{dN}{R - \lambda N} = \int_{0}^{t} dt$$

On solving we will get

$$N = R/\lambda(1 - e^{-\lambda t})$$

- (ii) Number of nuclei of B at any time t,  $N_B = R t N_A = R t R/\lambda(1 e^{-\lambda t}) = R/\lambda(\lambda t 1 + e^{-\lambda t})$ .
- (iii) Maximum number of nuclei of 'A' present at any time during its formation =  $R/\lambda$ .
- **Example 21.** A radioactive substance "A" having  $N_0$  active nuclei at t=0, decays to another radioactive substance "B" with decay constant  $\lambda_1$ . B further decays to a stable substance "C" with decay constant  $\lambda_2$ . (a) Find the number of nuclei of A, B and C after time t. (b) What would be the answer of part (a) if  $\lambda_1 >> \lambda_2$  and  $\lambda_1 << \lambda_2$ .

**Solution**: (a) The decay scheme is as shown

Here N<sub>1</sub>, N<sub>2</sub> and N<sub>3</sub> represent the nuclei of A, B and C at any time t.

For A, we can write

$$N_1 = N_0 e^{-\lambda_1 t}$$
 .... (1)

For B, we can write

$$\frac{dN_2}{dt} = \lambda_1 N_1 - \lambda_2 N_2 \qquad \dots (2)$$

or, 
$$\frac{dN_2}{dt} + \lambda_2 N_2 = \lambda_1 N_1$$

This is a linear differential equation with integrating factor

I.F. = 
$$e^{\lambda_2 t}$$

$$e^{\lambda_2 t} \frac{dN_2}{dt} + e^{\lambda_2 t} \lambda_2 N_2 = \lambda_1 N_1 e^{\lambda_2 t}$$

$$\int d(N_2 e^{\lambda_2 t}) = \int \lambda_1 N_1 e^{\lambda_2 t} dt$$

$$N_2 e^{\lambda_2 t} = \lambda_1 N_0 \int e^{-\lambda_1 t} e^{\lambda_2 t} dt \qquad \qquad ..... using (1)$$

$$N_2 e^{\lambda_2 t} = \lambda_1 N_0 \frac{e^{(\lambda_2 - \lambda_1)t}}{\lambda_2 - \lambda_1} + C$$
 .....(3)

At 
$$t = 0$$
,  $N_2 = 0$   $0 = \frac{\lambda_1 N_0}{\lambda_2 - \lambda_1} + C$ 

Hence 
$$C = \frac{\lambda_1 N_0}{\lambda_1 - \lambda_2}$$

Using C in eqn. (3), we get

$$N_2 = \frac{\lambda_1 N_0}{\lambda_2 - \lambda_1} \left( e^{-\lambda_1 t} - e^{-\lambda_2 t} \right)$$

and 
$$N_1 + N_2 + N_3 = N_0$$

$$N_3 = N_0 - (N_1 + N_2)$$

(b) For 
$$\lambda_1 >> \lambda_2$$
  $N_2 = \frac{\lambda_1 N_0}{-\lambda_1} (-e^{-\lambda_2 t}) = N_0 e^{-\lambda_2 t}$ 

For 
$$\lambda_1 \ll \lambda_2$$
  $N_2 = \frac{\lambda_1 N_0}{\lambda_2} (e^{-\lambda_1 t}) = 0$ 

### 

### Alternate solution of (b) part without use of answer of part (a):

If  $\lambda_1 > \lambda_2$  that means A will decay very fast to 'B' and B will then decay slowly. We can say that practically  $N_1$  vanishes in very short time & B has initial no. of atoms as  $N_0$ .

$$\therefore \qquad \text{Now} \qquad \text{N}_2 = \text{N}_0 \, \text{e}^{-\lambda_2 t} \qquad \qquad \text{\&} \qquad \text{N}_1 = \text{N}_0 \, \text{e}^{-\lambda_1 t}$$

If  $\lambda_1 \ll \lambda_2$  then B is highly unstable and it will soon decay into C.

So, it's rate of formation ≈ its rate of decay.

$$\therefore \qquad \lambda_1 N_1 \approx \lambda_2 N_2 \qquad \Rightarrow \qquad N_2 = \frac{\lambda_1 N_1}{\lambda_2} \quad = \frac{\lambda_1 N_0}{\lambda_2} \ (e^{-\lambda_1 t})$$

### 9. NUCLEAR FISSION:

In nuclear fission heavy nuclei of A, above 200, break up into two or more fragments of comparable masses. The most attractive bid, from a practical point of view, to achieve energy from nuclear fission is to use  $_{92}$ U<sup>236</sup> as the fission material. The technique is to hit a uranium sample by slow-moving neutrons (kinetic energy  $\approx 0.04$  eV, also called thermal neutrons). A  $_{92}$ U<sup>235</sup> nucleus has large probability of absorbing a slow neutron and forming  $_{92}$ U<sup>236</sup> nucleus. This nucleus then fissions into two or more parts. A variety of combinations of the middle-weight nuclei may be formed due to the fission. For example, one may have

$${}_{92}U^{235} + {}_{0}N^{1} \rightarrow {}_{92}U^{236} \rightarrow \ X + Y + 2{}_{0}N^{1},$$

or 
$${}_{92}U^{235} + {}_{0}N^{1} \rightarrow {}_{92}U^{236} \rightarrow X' + Y' + 3{}_{0}N^{1}$$

and a number of other combinations.

- \* On an average 2.5 neutrons are emitted in each fission event.
- \* Mass lost per reaction ≈ 0.2 a.m.u.
- In nuclear fission the total B.E. increases and excess energy is released.
- \* In each fission event, about 200 MeV of energy is released a large part of which appears in the form of kinetic energies of the two fragments. Neutrons take away about 5MeV.

eg. 
$${}^{235}_{92}\text{U} + {}_{0}\text{n}^{1} \rightarrow {}^{236}_{92}\text{U} \rightarrow {}^{141}_{56}\text{Ba} + {}^{92}_{36}\text{Kr} + 3{}_{0}\text{n}^{1} + \text{energy}$$

Q value = 
$$[(M_U - 92m_e + m_n) - \{(M_{Ba} - 56 m_e) + (M_{Kr} - 36m_e) + 3m_n\}]c^2$$
  
=  $[(M_U + m_n) - (M_{Ba} + M_{Kr} + 3m_n)]c^2$ 

\* A very important and interesting feature of neutron-induced fission is the chain reaction. For working of nuclear reactor refer your text book.

### 10. NUCLEAR FUSION (THERMO NUCLEAR REACTION):

(a) Some unstable light nuclei of A below 20, fuse together, the B.E. per nucleon increases and hence the excess energy is released. The easiest thermonuclear reaction that can be handled on earth is the fusion of two deuterons (D–D reaction) or fusion of a deuteron with a triton (D–T reaction).

$$\label{eq:continuous_equation} \begin{split} _1H^2 + _1H^2 &\to _2He^3 + _0n^1 + 3.3 \text{ MeV (D-D)} \\ \text{Q value} = [2(\text{M}_{\text{D}} - \text{m}_{\text{e}}) - \{(\text{M}_{\text{He}^3} - 2\text{m}_{\text{e}}) + \text{m}_{\text{n}}\}]c^2 \\ &= [2\text{M}_{\text{D}} - (\text{M}_{\text{He}^3} + \text{m}_{\text{n}})]c^2 \\ _1H^2 + _1H^2 &\to _1H^3 + _1H^1 + 4.0 \text{ MeV (D-D)} \\ \text{Q value} = [2(\text{M}_{\text{D}} - \text{m}_{\text{e}}) - \{(\text{M}_{\text{T}} - \text{m}_{\text{e}}) + (\text{M}_{\text{H}} - \text{m}_{\text{e}})\}]c^2 \\ &= [2\text{M}_{\text{D}} - (\text{M}_{\text{T}} + \text{M}_{\text{H}})]c^2 \\ _1H^2 + _1H^3 &\to _2He^4 + \text{n} + 17.6 \text{ MeV (D-T)} \\ \text{Q value} = [\{(\text{M}_{\text{D}} - \text{m}_{\text{e}}) + (\text{M}_{\text{T}} - \text{m}_{\text{e}})\} - \{(\text{M}_{\text{He}^4} - 2\text{m}_{\text{e}}) + \text{m}_{\text{n}}\}]c^2 \\ &= [(\text{M}_{\text{D}} + \text{M}_{\text{T}}) - (\text{M}_{\text{He}^4} + \text{m}_{\text{n}})]c^2 \end{split}$$

**Note:** In case of fission and fusion,  $\Delta m = \Delta m_{atom} = \Delta m_{nucleus}$ .

#### REQUIRED CONDITION FOR NUCLEAR FUSION

High temperature :

Which provide kinetic energy to nuclei to overcome the repulsive electrostatic force between them.

• High Pressure (or density) :

Which ensure frequent collision and increases the probability of fusion. The required temperature and pressure at earth (lab) are not possible. These condition exist in the sun and in many other stars. The source of energy in the sun is nuclear fusion, where hydrogen is in plasma state and there protons fuse to form helium nuclei.

### SOLVED EXAMPLE.

**Example 22.** Calculate the energy released when three alpha particles combine to form a  ${}^{12}$ C nucleus. The atomic mass of  ${}^{4}_{2}$ He is 4.002603 u.

**Solution:** The mass of a <sup>12</sup>C atom is exactly 12 u.

The energy released in the reaction  $3\binom{4}{2}He$   $\rightarrow$   $\binom{12}{6}C$  is

$$[3 \text{ m}({}_{2}^{4}\text{He}) - \text{m}({}_{6}^{12}\text{C})] c^{2}$$
  
=  $[3 \times 4.002603 \text{ u} - 12 \text{ u}] (931 \text{ MeV/u}) = 7.27 \text{ MeV}.$ 

Example 23. Consider two deuterons moving towards each other with equal speeds in a deutron gas. What should be their kinetic energies (when they are widely separated) so that the closest separation between them becomes 2fm? Assume that the nuclear force is not effective for separations greater than 2 fm. At what temperature will the deuterons have this kinetic energy on an average?

**Solution :** As the deuterons move, the Coulomb repulsion will slow them down. The loss in kinetic energy will be equal to the gain in Coulomb potential energy. At the closest separation, the kinetic energy is

zero and the potential energy is  $\frac{e^2}{4\pi\epsilon_0 r}$ . If the initial kinetic energy of each deuteron is K and the closest separation is 2fm, we shall have

$$2 \text{ K} = \frac{e^2}{4\pi\epsilon_0 (2 \text{ fm})} = \frac{(1.6 \times 10^{-19} \text{ C})^2 \times (9 \times 10^9 \text{ N} - \text{m}^2 / \text{C}^2)}{2 \times 10^{-15} \text{ m}}$$

or, 
$$K = 5.7 \times 10^{-14} \text{ J}.$$

If the temperature of the gas is T, the average kinetic energy of random motion of each nucleus will be 1.5 kT. The temperature needed for the deuterons to have the average kinetic energy of  $5.7 \times 10^{-14}$  J will be given by

$$1.5 \text{ kT} = 5.7 \times 10^{-14} \text{ J}$$

where k = Botzmann constant

or, 
$$T = \frac{5.7 \times 10^{-14} \text{ J}}{1.5 \times 1.38 \times 10^{-23} \text{ J/K}}$$
$$= 2.8 \times 10^9 \text{ K}.$$

JEE (Adv.)-Physics Nuclear physics

## **Exercise #1**

### **PART - I: SUBJECTIVE QUESTIONS**

If required, you can use the following data:

Mass of proton  $m_p = 1.007276 \text{ u}$ , Mass of  $_1\text{H}^1$  atom = 1.007825 u, Mass of neutron  $m_n = 1.008665 \text{ u}$ , Mass of electron = 0.0005486 u = 511 KeV/c<sup>2</sup>, 1 u = 931 MeV/c<sup>2</sup>.  $N_\Delta = 6.023 \times 10^{23}$ 

Atomic mass of:  $H^2 = 2.01410 \text{ u}$ ,  $Be^8 = 8.00531 \text{ u}$ ,  $B^{11} = 11.00930 \text{ u}$ ,  $Li^7 = 7.01601 \text{ u}$ ,  $He^4 = 4.002603 \text{ u}$ .

### **SECTION (A): PROPERTIES OF NUCLEUS**

- A.1 A neutron star has a density equal to that of the nuclear matter( $\approx 3 \times 10^{17} \,\text{kg/m}^3$ ). Assuming the star to be spherical, find the radius of a neutron star whose mass is (i)  $4.0 \times 10^{30} \,\text{kg}$  (twice the mass of the sun) (ii)  $6 \times 10^{24} \,\text{Kg}$  (around mass of the earth).
- **A-2.** Assuming the radius of a nucleus to be equal to R = 1.3 A<sup>1/3</sup> × 10<sup>-15</sup> m, where A is its mass number, evaluate the density of nuclei and the number of nucleons per unit volume of the nucleus. Take mass of one nucleon =  $1.67 \times 10^{-27}$  kg

### **SECTION (B): MASS DEFECT AND BINDING ENERGY**

- **B 1.** Find the binding energy of the nucleus of lithium isotope <sub>3</sub>Li<sup>7</sup> and hence find the binding energy per nucleon in it.
- **B 2.** Find the energy required for separation of a  $_{10}$ Ne $^{20}$  nucleus into two  $\alpha$  particles and a  $_6$ C<sup>12</sup> nucleus if it is known that the binding energies per nucleon in  $_{10}$ Ne $^{20}$ ,  $_2$ He $^4$  and  $_6$ C<sup>12</sup> nuclei are equal to 8.03, 7.07 and 7.68 MeV respectively.

### SECTION (C): RADIOACTIVE DECAY & DISPLACEMENT LAW

- C 1. The kinetic energy of an  $\alpha$  particle which flies out of the nucleus of a Ra<sup>226</sup> atom in radioactive disintegration is 4.78 MeV. Find the total energy evolved during the escape of the  $\alpha$  particle.
- C 2. In the decay <sup>64</sup> Cu → <sup>64</sup> Ni + e<sup>+</sup> + v, the maximum kinetic energy carried by the positron is found to be 0.680 MeV (a) Find the energy of the neutrino which was emitted together with a positron of energy 0.180 MeV (b) What is the momentum of this neutrino in kg-m /s ?Use the formula applicable to photon.

#### SECTION (D): STATISTICAL LAW OF RADIOACTIVE DECAY

- **D 1.** Beta decay of a free neutron takes place with a half life of 14 minutes. Then find (a) decay constant (b) energy liberated in the process.
- **D 2.** How many  $\beta$  particles are emitted during one hour by 1.0 μg of Na<sup>24</sup> radionuclide whose half–life is 15 hours? [Take e<sup>(-0.693/15)</sup> = 0.955, and avagadro number = 6 × 10<sup>23</sup>]
- **D 3.** Calculate the specific activities of  $Na^{24}$  &  $U^{235}$  nuclides whose half lives are 15 hours and  $7.1 \times 10^8$  years respectively.

#### **SECTION (E): NUCLEAR FISSION AND FUSION**

- Consider the case of bombardment of U<sup>235</sup> nucleus with a thermal neutron. The fission products are E 1. Mo<sup>95</sup> & La<sup>139</sup> and two neutrons. Calculate the energy released by one U<sup>235</sup> nucleus. (Rest masses of the nuclides are  $U^{235} = 235.0439 \text{ u}$ , n = 1.0087 u,  $Mo^{95} = 94.9058 \text{ u}$ ,  $La^{139} = 138.9061 \text{ u}$ ).
- E 2. Energy evolved from the fusion reaction  $2\frac{2}{1}H = \frac{4}{2}He + Q$  is to be used for the production of power. Assuming the efficiency of the process to be 30 %. Find the mass of deuterium that will be consumed in a second for an output of 50 MW.
- E 3. For the D-T fusion reaction, find the rate at which deuterium & tritium are consumed to produce 1 MW. The Q-value of D-T reaction is 17.6 MeV & assume all the energy from the fusion reaction is available.

### PART - II: OBJECTIVE QUESTIONS

#### **SECTION (A): PROPERTIES OF NUCLEUS**

A 1.	The mass num	ber of a nuc	leus is

- (A) always less than its atomic number
- (B) always more than its atomic number
- (C) equal to its atomic number
- (D) sometimes more than and sometimes equal to its atomic number
- The stable nucleus that has a radius 1/3 that of Os189 is -A 2.

$$(A)_3Li^7$$

$$(C)_{5}B^{10}$$

 $(D)_{6}C^{12}$ 

The graph of  $\ell n(R/R_n)$  versus  $\ell nA$  (R = radius of a nucleus and A = its mass number) is A-3.

- (A) a straight line
- (B) a parabola
- (C) an ellipse

(D) none of them

A-4. For uranium nucleus how does its mass vary with volume? [ JEE 2003 (Screening) 3,-1/84 ]

(A)  $m \propto V$ 

(B) m  $\propto 1/V$ 

(C) m  $\propto \sqrt{V}$ 

(D) m  $\propto V^2$ 

A-5. Let  $F_{pp}$ ,  $F_{pn}$  and  $F_{nn}$  denote the magnitudes of the nuclear force by a proton on a proton, by a proton on a neutron and by a neutron on a neutron respectively. When the separation is 1 fm,

(A) 
$$F_{nn} > F_{nn} = F_{nn}$$

(B) 
$$F_{nn} = F_{nn} = F_{nn}$$
 (C)  $F_{nn} > F_{nn} > F_{nn}$ 

(D) 
$$F_{nn} < F_{nn} = F_{nn}$$

An  $\alpha$ -particle of energy 5 MeV is scattered through 180° by a fixed uranium nucleus. The distance of the A 6. closest approach is of the order of: (AIEEE 2004 4/300)

- (1) 1 Å
- (2) 10<sup>-10</sup> cm
- (3) 10<sup>-12</sup> cm
- (4) 10<sup>-15</sup> cm

If radius of the  $^{27}_{13}$ AI nucleus is estimated to be 3.6 Fermi, then the radius of  $^{125}_{52}$ Te nucleus be nearly : A 7.

(AIEEE 2005 4/300)

(1) 6 Fermi

(2) 8 Fermi

(3) 4 Fermi

(4) 5 Fermi

<sup>\*</sup> Marked Questions may have more than one correct option.

(A) A neutrino

(A) 0.8 MeV

C-4.

(C) An  $\alpha$ -particle

### **SECTION (B): MASS DEFECT AND BINDING ENERGY**

As the mass number A increases, the binding energy per nucleon in a nucleus (A) increases (B) decreases (C) remains the same (D) varies in a way that depends on the actual value of A. B 2. Which of the following is a wrong description of binding energy of a nucleus? (A) It is the energy required to break a nucleus into its constituent nucleons. (B) It is the energy released when free nucleons combine to from a nucleus (C) It is the sum of the rest mass energies of its nucleons minus the rest mass energy of the nucleus (D) It is the sum of the kinetic energy of all the nucleons in the nucleus B 3. The energy of the reaction  $Li^7 + p \longrightarrow 2 He^4$  is (the binding energy per nucleon in  $Li^7$  and  $He^4$ nuclei are 5.60 and 7.06 MeV respectively.) (A) 17.3 MeV (B) 1.73 MeV (C) 1.46 MeV (D) depends on binding energy of proton. B 4. The atomic weight of boron is 10.81 g/mole and it has two isotopes  ${}^{10}_{5}B$  and  ${}^{11}_{5}B$ . The ratio (by number) of  ${}^{10}_{5}B: {}^{11}_{5}B$  in nature would be: (A) 19:81 (B) 10:11 (C) 15:16 (D) 81:19 SECTION (C): RADIOACTIVE DECAY & DISPLACEMENT LAW C 1 Which of the following processes represents a gamma decay? (A)  ${}^{A}X_{7} + \gamma \longrightarrow {}^{A}X_{7-1} + a + b$ (B)  ${}^{A}X_{7} + {}^{1}n_{0} \longrightarrow {}^{A-3}X_{7-2} + c$ (D)  ${}^{A}X_{7} + e_{-1} \longrightarrow {}^{A}X_{7-1} + g$  $(C)^A X_7 \longrightarrow ^A X_7 + f$ C 2. An  $\alpha$ -particle is bombarded on <sup>14</sup>N. As a result, a <sup>17</sup>O nucleus is formed and a particle is emitted. This particle is a (A) neutron (B) proton (C) electron (D) positron C 3. A free neutron decays into a proton, an electron and:

(B) An antineutrino

(D) A β-particle

Nuclei X decay into nuclei Y by emitting  $\alpha$  particles. Energies of  $\alpha$  particle are found to be only 1 MeV

(C) 1 MeV

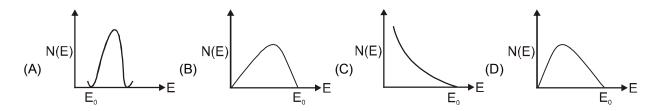
(D) 0.4 MeV

& 1.4 MeV. Disregarding the recoil of nuclei Y. The energy of  $\gamma$  photon emitted will be

(B) 1.4 MeV

C 5. A nuclear transformation is denoted by X(n,  $\alpha$ )  $\rightarrow \frac{7}{3}$ Li. Which of the following is the nucleus of element X? (AIEEE 2005 4/300) (4) <sup>11</sup><sub>4</sub>Be  $(1)_{6}^{12}C$  $(2)_{5}^{10}B$  $(3)_{5}^{9}B$ SECTION (D): STATISTICAL LAW OF RADIOACTIVE DECAY D 1. In one average-life (A) half the active nuclei decay (B) less than half the active nuclei decay (C) more than half the active nuclei decay (D) all the nuclei decay D 2. A freshly prepared radioactive source of half-life 2 h emits radiation of intensity which is 64 times the permissible safe level. The minimum time after which it would be possible to work safely with this source is -(A) 6 h (B) 12 h (C) 24 h (D) 128 h Two isotopes P and Q of atomic weight 10 and 20, respectively are mixed in equal amount by weight. After 20 D 3. days their weight ratio is found to be 1:4. Isotope P has a half-life of 10 days. The half-life of isotope Q is (C) 20 days (A) zero (B) 5 days (D) inifinite D 4. Starting with a sample of pure 66Cu, 7/8 of it decays into Zn in 15 minutes. The corresponding half-life is: (AIEEE 2005 4/300) (D)  $7\frac{1}{2}$  minute (A) 10 minute (B) 15 minute (C) 5 minute D 5. 10 grams of <sup>57</sup>Co kept in an open container beta-decays with a half-life of 270 days. The weight of the material inside the container after 540 days will be very nearly -(A) 10 g(B) 7.5 g(D) 2.5 g(C) 5 g $A \xrightarrow{\lambda} B \xrightarrow{2\lambda} C$ D-6.  $t = 0 \qquad N_0 \qquad \qquad 0$  $N_2$  $N_{_{1}}$ The ratio of  $N_1$  to  $N_2$  when  $N_2$  is maximum is: (A) at no time this is possible (D)  $\frac{\ln 2}{2}$ (B)2(C) 1/2 The half-life of  $^{131}$ I is 8 days. Given a sample of  $^{131}$ I at time t = 0, we can assert that D 7. [JEE-1999] (A) No nucleus will decay before t = 4 days (B) No nucleus will decay before t = 8 days (C) All nuclei will decay before t = 16 days (D) A given nucleus may decay at any time after t = 0.

The energy spectrum of  $\beta$ -particles (number N(E) as a function of  $\beta$ -energy E) emitted from a radioactive D 8. source is: (AIEEE 2006 3/180, -1)



### **SECTION (E): NUCLEAR FISSION AND FUSION**

The binding energy per nucleon of deuteron  $\binom{2}{1}H$  and helium nucleus  $\binom{4}{2}He$  is 1.1 MeV and 7 MeV respec-E 1. tively. If two deuteron nuclei react to form a single helium nucleus, then the energy released is :

(AIEEE 2004 4/300)

- (A) 13.9 MeV
- (B) 26.9 MeV
- (C) 23.6 MeV
- (D) 19.2 MeV

E 2.  $_{92}$ U<sup>235</sup> nucleus absorbs a slow neutron and undergoes fission into  $_{54}$ X<sup>139</sup> and  $_{38}$ Sr<sup>94</sup> nuclei. The other particles produced in this fission process are

- (A) 1  $\beta$  and 1  $\alpha$
- (B) 2  $\beta$  and 1 neutron
- (C) 2 neturons
- (D) 3 neutrons

E 2. Two lithium <sup>6</sup>Li nuclei in a lithium vapour at room temperature do not combine to form a carbon <sup>12</sup>C nucleus because

(A) a lithium nucleus is more tightly bound than a carbon nucleus

- (B) carbon nucleus is an unstable particle
- (C) it is not energetically favourable

(D) Coulomb repulsion does not allow the nuclei to come very close

E 3. In a uranium reactor whose thermal power is P = 100 MW, if the average number of neutrons liberated in each nuclear splitting is 2.5. Each splitting is assumed to release an energy E = 200 MeV. The number of neutrons generated per unit time is -

(A) 
$$4 \times 10^{18} \text{ s}^{-1}$$

(B) 
$$8 \times 10^{23} \text{ s}^{-1}$$

(C) 
$$8 \times 10^{19} \text{ s}^{-1}$$

(B) 
$$8 \times 10^{23} \text{ s}^{-1}$$
 (C)  $8 \times 10^{19} \text{ s}^{-1}$  (D)  $\frac{125}{16} \times 10^{18} \text{ s}^{-1}$ 

E 4. Choose the statement which is true.

(A) The energy released per unit mass is more in fission than in fusion

- (B) The energy released per atom is more in fusion than in fission.
- (C) The energy released per unit mass is more in fusion and that per atom is more in fission.
- (D) Both fission and fusion produce same amount of energy per atom as well as per unit mass.

E 5. Fusion reaction is possible at high temperature because -

- (A) atoms are ionised at high temperature
- (B) molecules break-up at high temperature
- (C) nuclei break-up at high temperature
- (D) kinetic energy is high enough to overcome repulsion between nuclei.

**E 6.** In a fission reaction

$$^{236}_{92}U \longrightarrow ^{117}X + ^{117}Y + n + n$$

the average binding energy per nucleon of X and Y is 8.5 MeV whereas that of  $^{236}$ U is 7.6 MeV. The total energy liberated will be about :

(A) 200 keV

(B) 2 MeV

(C) 200 MeV

(D) 2000 MeV

**E-7.** A heavy nucleus having mass number 200 gets disintegrated into two small fragments of mass number 80 and 120. If binding energy per nucleon for parent atom is 6.5 M eV and for daughter nuclei is 7 M eV and 8 M eV respectively, then the energy released in each decay will be:

(A) 200 M eV

(B) – 220 M eV

(C) 220 M eV

(D) 180 M eV

**E-8.** Assuming that about 20 MeV of energy is released per fusion reaction,  $_1H^2 + _1H^3 \rightarrow _0n^1 + _2He^4$ , the mass of  $_1H^2$  consumed per day in a future fusion reactor of power 1 MW would be approximately

(A) 0.1 gm

(B) 0.01 gm

(C) 1 gm

(D) 10 gm

E-9. A nucleus disintegrates into two nuclear parts which have their velocities in the ratio 2 : 1. The ratio of their nuclear sizes will be : (AIEEE 2004 4/300)

 $(1) 2^{1/3} : 1$ 

 $(2) 1 : 3^{1/2}$ 

(3) 31/2: 1

 $(4)\ 1:2^{1/3}$ 

### PART - III: MATCH THE COLUMN

1. Match the column-I of properties with column-II of reactions

Column-I

Column-II

(A) Mass of product formed is less than

(p)  $\alpha$ -decay

the original mass of the system in

(B) Binding energy per nucleon increase in

(q) β-decay

(C) Mass number is conserved in

(r) Nuclear fission

(D) Charge number is conserved in

- (s) Nuclear fusion
- 2. In column-I, consider each process just before and just after it occurs. Initial system is isolated from all other bodies. Consider all product particles (even those having rest mass zero) in the system. Match the system in column-I with the result they produce in column-II.

Column-I

Column-II

(A) Spontaneous radioactive decay of an uranium nucleus initially at rest

(p) Number of protons is increased

as given by reaction  $^{238}_{92}U \rightarrow ^{234}_{90}Th + ^{4}_{2}He + ...$ 

(B) Fusion reaction of two hydrogen nuclei

(g) Momentum is conserved

as given by reaction  ${}_{1}^{1}H + {}_{1}^{1}H \rightarrow {}_{1}^{2}H + ....$ 

(C) Fission of U<sup>235</sup> nucleus initiated by a thermal neutron as given by reaction

(r) Mass is converted to energy or vice versa

$$_{0}^{1}n+\ _{92}^{235}U\rightarrow \ _{56}^{144}Ba+\ _{36}^{89}Kr+3_{0}^{1}n+...$$

(D)  $\beta$  - decay (negative beta decay)

(s) Charge is conserved

3.\_ Four physical quantities are listed in column I. Their values are listed in Column II in a random order.

	Column I	Colum	าท II
(a)	Thermal energy of air molecules at room temperature	(e)	0.04 eV
(b)	Binding energy of heavy nuclei per nucleon	(f)	2 eV
(c)	X-ray photon energy	(g)	1 KeV
(d)	Photon energy of visible light	(h)	7 MeV T

The correct matching of columns I & II is given by :

(A) a - e, b - h, c - g, d - f

(B) a - e, b - g, c - f, d - h

(C) a - f, b - e, c - g, d - h

(D) a - f, b - h, c - e, d - g

#### 4. Match the following

[JEE 2006 5/184]

Column 1

Column 2

- (A) Nuclear fission (p) Converts some matter into energy
- (q) Possible for nuclei with low atomic number (B) Nuclear fusion (C) β - decay (r) Possible for nuclei with high atomic number
- (D) Exothermic nuclear reaction
- (s) Essentially proceeds by weak nuclear forces.
- Some laws / processes are given in Column I. Match these with the physical phenomena given in Column 5. II . [IIT-JEE 2007' 6/81]

Column I Column II (A) Transition between two atomic energy levels Characteristic X-rays (p) (B) Electron emission from a material Photoelectric effect (q) (C) Mosley's law Hydrogen spectrum (r) (D) Change of photon energy into kinetic energy (s) **β-decay** of electrons

Column II gives certain systems undergoing a process. Column I suggests changes in some of the parameters 6. related to the system. Match the statements in Column-I to the appropriate process(es) from Column II. [JEE 2009,8/160]

> Column-I Column-II

- (A) The energy of the system is increased.
- (p) System: A capacitor, initially uncharged

Process: It is connected to a battery.

which is converted into energy of random motion of its parts

(B) Mechanical energy is provided to the system, (q) System: A gas in an adiabatic container fitted with an adiabatic piston

Process: The gas is compressed by pushing the

piston

- (C) Internal energy of the system is converted into its mechanical energy
- (r) System: A gas in a rigid container

Process: The gas gets cooled due to colder atmosphere surrounding it

- (D) Mass of the system is decreased
- (s) System: A heavy nucleus, initially at rest

Process: The nucleus fissions into two fragments of nearly equal masses and some neutrons are emitted

(t) System: A resistive wire loop

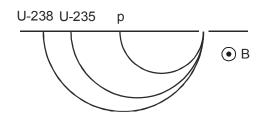
Process: The loop is placed in a time varying magnetic field perpendicular to its plane

# Exercise # 2

### PART - I: ONLY ONE OPTION CORRECT TYPE

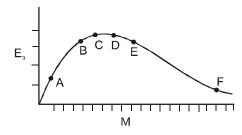
1.	The half life of $^{215}$ At is 100 $\mu$ s. The time taken for the radioactivity of a sample of $^{215}$ At to decay of its initial value is : [ JEE 2002 (Screening) 2 × 3, –1					
	(Α) 400 μs	(B) 6.3 μs	(C) 40 μs	(D) 300	) μs	
2.		umber 220 initially at rekinetic energy of the $\alpha$		rticle. If the Q		
	(A) 4.4 MeV	(B) 5.4 MeV	(C) 5.6 MeV	(D) 6.5	MeV	
3.	If the binding energy per reaction	nucleon in $^{7}_{3}$ Li and $^{4}_{2}$ He	nuclei are 5.60 Me	eV and 7.06 MeV	respectively, then in the	
	$p +_3^7 Li \rightarrow 2_2^4 He$					
	energy of proton must b	e:		(AIEEE	2006 4.5/180)	
	(A) 39.2 MeV	(B) 28.24 MeV	(C) 17.28 MeV	(D) 1.46	6 MeV	
4.	If $\rm M_{\circ}$ is the mass of an ox the nuclear binding energy		$\mathrm{d}\mathrm{M}_{_{\mathrm{N}}}$ are the masse	masses of a proton and a neutron respectively [AIEEE 2007]		
	(A) $(M_o - 8M_p)C^2$	(B) $(M_o - 8M_P - 9M_N)C^2$	$(C) M_{o}C^{2}$	(D) ( $\mathrm{M}_{\mathrm{o}}$	$-17M_N)C^2$	
5.	In the options given bell options is:	ow, let E denote the rest	mass energy of	energy of a nucleus and n a neutron. The correct		
	(A) $E \begin{pmatrix} 236 \ 92 \end{pmatrix} > E \begin{pmatrix} 137 \ 53 \end{pmatrix} + E \begin{pmatrix} 97 \ 39 \end{pmatrix} + 2E(n)$ (B) $E \begin{pmatrix} 236 \ 92 \end{pmatrix} < E \begin{pmatrix} 137 \ 53 \end{bmatrix} + E \begin{pmatrix} 97 \ 39 \end{pmatrix} + 2E(n)$ (C) $E \begin{pmatrix} 236 \ 92 \end{pmatrix} < E \begin{pmatrix} 140 \ 56 \end{pmatrix} Ba + \begin{pmatrix} 94 \ 36 \end{pmatrix} Kr + 2E(n)$					
	(D) E $\binom{236}{92}$ U) = E $\binom{140}{56}$ Ba	$+ E\left(\frac{94}{36}Kr\right) + 2E(n)$				
6.	•	ple $S_1$ having an activity of $5\mu Ci$ has twice the number of nuclei as another sample $S_2$ which $10\mu Ci$ . The half lives of $S_1$ and $S_2$ can be [JEE 2008, 3/163]				
	(A) 20 years and 5 years	s, respectively	(B) 20 years and	10 years, respe	ectively	
	(C) 10 years each		(D) 5 years each			
7.	decays with an averag	A charged capacitor of capacitance C is discharged through a resistance R. A radioactive sample decays with an average life $\tau$ . Find the value of R for which the ratio of the electrostatic field energy stored in the capacitor to the activity of the radioactive sample is independent of time.			ectrostatic field energy	
	(A) $\frac{\tau}{C}$	(B) $\frac{2\tau}{C}$	(C) $\frac{\tau}{2C}$	(D) $\frac{3\tau}{2C}$	-	

8. Protons and singly ionized atoms of U<sup>235</sup> & U<sup>238</sup> are passed in turn (which means one after the other and not at the same time) through a velocity selector and then enter a uniform magnetic field. The protons describe semicircles of radius 10 mm. The separation between the ions of  $U^{235}$  and  $U^{238}$  after describing semicircle is given by



- (A) 60 mm
- (B) 30 mm
- (C) 2350 mm
- (D) 2380 mm

9.

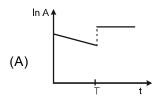


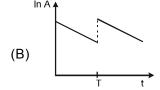
The above is a plot of binding energy per nucleon E<sub>b</sub>, agains the nuclear mass M; A, B, C, D, E, correspond to different nuclei. Consider four reactions: [AIEEE 2009 4/144]

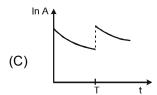
- (i)  $A + B \rightarrow C + \varepsilon$
- (ii)  $C \rightarrow A + B + \varepsilon$
- (iii) D + E  $\rightarrow$  F +  $\epsilon$  and (iv) F  $\rightarrow$  D + E +  $\epsilon$ ,

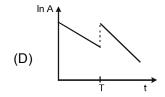
where  $\varepsilon$  is the energy released? In which reactions is  $\varepsilon$  positive?

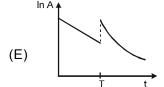
- (A) (i) and (iii)
- (B) (ii) and (iv)
- (C) (ii) and (iii)
- (D) (i) and (iv)
- 10. When a  $\beta^-$ -particle is emitted from a nucleus, the neutron-proton ratio :
  - (A) is decreased
- (B) is increased
- (C) remains the same
- (D) first (A) then (B)
- 11. At time t = 0, some radioactive gas is injected into a sealed vessel. At time T, some more of the same gas is injected into the same vessel. Which one of the following graphs best represents the variation of the logarithm of the activity A of the gas with time t?











### 12. Match the following:

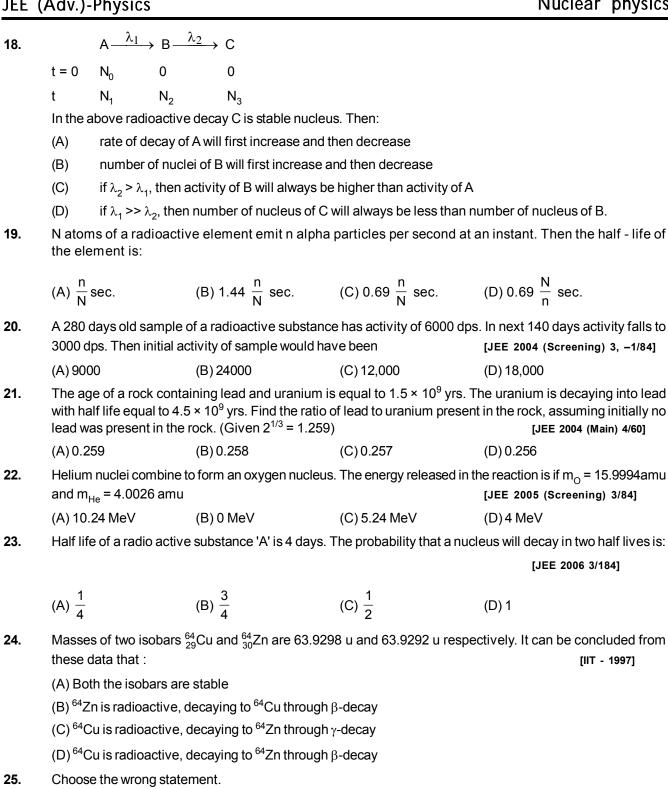
Column I Column II (a) Photoelectric effect I. Photon (b) Wave Π. Frequency (c) X rays Ш. K capture (d) Nucleus IV. γ -rays (A) a - I, b - II, c - III, d - IV(B) a - II, b - I, c - IV, d - III

- (2) 4 11, 5 1, 6 10, 4
- (C) a II, b I, c III, d IV
- (D) None of these
- 13. A sample of radioactive material has mass m, decay constant  $\lambda$ , and molecular weight M. Avogadro constant  $= N_A$ . The initial acitvity of the sample is :
  - (A)  $\lambda m$  (B)  $\frac{\lambda m}{M}$  (C)  $\frac{\lambda m N_A}{M}$  (D)  $mN_A e^{\lambda}$
- **14.** Two radioactive sources *A* and *B* initially contain equal number of radioactive atoms. Source *A* has a half-life of 1 hour and source *B* has a half-life of 2 hours. At the end of 2 hours, the ratio of the rate of disintegration of *A* to that of *B* is :
  - (A) 1:2 (B) 2:1 (C) 1:1 (D) 1:4
- **15.** A free neutron decays to a proton but a free proton does not decay to a neutron. This is because
  - (A) neutron is a composite particle made of a proton and an electron whereas proton is fundamental particle
  - (B) neutron is an uncharged particle whereas proton is a charged particle
  - (C) neutron has larger rest mass than the proton
  - (D) weak forces can operate in a neutron but not in a proton.
- **16.** Consider a sample of a pure beta-active material
  - (A) All the beta particles emitted have the same energy
  - (B) The beta particles originally exist inside the nucleus and are ejected at the time of beta decay
  - (C) The antineutrino emitted in a beta decay has zero rest mass and hence zero momentum.
  - (D) The active nucleus changes to one of its isobars after the beta decay
- 17. Two identical samples (same material and same amount initially) P and Q of a radioactive substance having mean life T are observed to have activities  $A_p \& A_Q$  respectively at the time of observation. If P is older than Q, then the difference in their ages is:

$$\text{(A)} \, \mathsf{T} \, \ell \mathsf{n} \left( \frac{A_P}{A_Q} \right) \qquad \qquad \text{(B)} \, \mathsf{T} \, \ell \mathsf{n} \left( \frac{A_Q}{A_P} \right) \qquad \qquad \text{(C)} \, \frac{1}{T} \, \ell \mathsf{n} \left( \frac{A_P}{A_Q} \right) \qquad \qquad \text{(D)} \, \mathsf{T} \left( \frac{A_P}{A_Q} \right)$$

neutrons

protons.



(A) The nuclear force becomes weak if the nucleus contains too many protons compared to the number of

(B) The nuclear force becomes weak if the nucleus contains too many neutrons compared to the number of

(C) Nuclei with atomic number greater than 82 show a tendency to disintegrate.

(D) The nuclear force becomes very strong if the nucleus contains a large number of nucleons.

- 26. The radioactivity of an old sample of whisky due to tritium (half life 12.5 years) was found to be only about 3% of that measured in a recently purchased bottle marked '7 year old'. The sample must have been prepared about:
  - (A) 70 years
- (B) 220 years
- (C) 420 years

(D) 300 years

### **PART - II: INTEGER TYPE QUESTIONS**

- 1. Consider a point source emitting  $\alpha$ -particles and receptor of area 1 cm² placed 1 m away from source. Receptor records any  $\alpha$ -particle falling on it. If the source contains  $N_0 = 3.0 \times 10^{16}$  active nuclei and the receptor records a rate of A = 50000 counts/second, if the decay constant is  $2.1 \times 10^{-x}$  find x. Assume that the source emits alpha particles uniformly in all directions and the alpha particles fall nearly normally on the window.
- In an ore containing uranium, the ratio (by number) of U-238 to Pb-206 is 3. If the age of the ore (assuming that all the lead present in the ore is the final stable product of U-238) is approximately  $z \times 10^9$  y. Take the half life of U-238 to be  $4.5 \times 10^9$  years. ( $\ell$ n 4/3 = 0.2876) find z? [IIT 1997]
- Radium being a member of the uranium series occurs in uranium ores. The half lives of uranium and radium are respectively  $4.5 \times 10^9$  and 1620 years. If the  $\frac{N_{radiun}}{N_{Uranium}}$  in Uranium ore at equilibrium is approaximately is  $1/x \times 10^6$  find x.
- **4.** A radioactive material decays by β-particle emission. During the first 2 seconds of a measurement, n β-particles are emitted and the next 2 seconds 0.75 n β-particles are emitted. Calculate the mean-life of this material in seconds to the nearest whole number. ( $\ell$ n 3 = 1.0986 and  $\ell$ n 2 = 0.6931). [JEE 2003 Main) 2/60]
- 5. The half-life of  $^{40}$ K is T = 1.30 × 10  $^{9}$  y. A sample of m = 1.00 g of pure KCl gives c = 480 counts/s. Calculate the relative percentage abundance of  $^{40}$ K (fraction of  $^{40}$ K present in term of number of atoms) in natural potassium. Molecular weight of KCl is M = 74.5 , Avogadro number N<sub>A</sub> = 6.02 × 10<sup>23</sup> , 1y = 3.15 × 10<sup>7</sup> s
- A radioactive isotope is being produced at a constant rate dN/dt = R in an experiment . The isotope has a half-life  $t_{1/2}$ . Suppose the production of the radioactive isotope starts at t = 0. If the number of active nuclei at time t is  $\frac{xR}{3\lambda}(1-e^{-\lambda t})$  find x?
- 7. A Bi<sup>210</sup> radionuclide decays via the chain Bi<sup>210</sup>  $\frac{\beta^- \text{decay}}{\lambda_1}$  Po<sup>210</sup>  $\frac{\alpha \text{decay}}{\lambda_2}$  Pb<sup>206</sup> (stable), where the decay constants are  $\lambda_1$  = 1.6 x 10<sup>-6</sup> s<sup>-1</sup>, T<sub>1/2</sub>  $\approx$  5 days ,  $\lambda_2$  = 5.8 x 10<sup>-8</sup> s<sup>-1</sup>, T<sub>1/2</sub>  $\approx$  4.6 months. If  $\alpha$  &  $\beta$  activities of the Bi<sup>210</sup> sample of mass 1.00 mg a month after its manufacture is.x × 10<sup>11</sup> s<sup>-1</sup> find x. (2 $\frac{1}{4.6}$  = 0.86)
- 8. Knowing the decay constant  $\lambda$  of a substance, if the probability of decay of a nucleus during the time from 0 to t is.  $x e^{-\lambda t}$  find x
- About 185 MeV of usable energy is released in the neutron induced fissioning of a  $^{235}_{92}U$  nucleus. If the reactor using  $^{235}_{92}U$  as fuel continuously generates 100 MW of power how long (days) will it take for 1 Kg of the uranium  $^{235}_{92}U$  to be used up?

- 10. The  $_{92}$ U<sup>235</sup> absorbs a slow neutron (thermal neutron) & undergoes a fission represented by  $_{92}$ U<sup>235</sup> +  $_{0}$ n<sup>1</sup>  $\longrightarrow$   $_{92}$ U<sup>236</sup>  $\longrightarrow$   $_{56}$ Ba<sup>141</sup> +  $_{36}$ Kr<sup>92</sup> + 3  $_{0}$ n<sup>1</sup> + E. Calculate:
  - (i) The energy released E (Mev) per fission.
  - (ii) The energy (MWh) released when 1 g of <sub>92</sub>U<sup>235</sup> undergoes complete fission.

```
Given _{92}U^{235} = 235.1175 \text{ amu (atom)};

_{56}Ba^{141} = 140.9577 \text{ amu (atom)};

_{36}Kr^{92} = 91.9264 \text{ amu (atom)}; _{0}n^{1} = 1.00898 \text{ amu, 1 amu} = 931 \text{ MeV/C}^{2}
```

- 11. A sample has two isotopes  $A^{150}$  and B having masses 50 g and 30 g respectively. A is radioactive and B is stable. A decays to A' by emitting  $\alpha$  particles. The half life of A is 2 hrs. After 4 hours and number of  $\alpha$  particles emitted is.  $x \times 10^{23}$  find x.
- Consider a nuclear reaction A + B → C. A nucleus 'A' moving with kinetic energy of 5 MeV collides with a nucleus 'B' moving with kinetic energy of 3 MeV and form a nucleus 'C' in excited state. Find the kinetic energy (MeV) of nucleus 'C' just after its formation, if it is formed in a state with excitation energy 10 MeV. Take masses of nuclei of A, B and C as 25.0, 10.0, 34.995 amu respectively. 1 amu = 930 MeV/c².
- 13. To activate the reaction  $(n, \alpha)$  with stationary B<sup>11</sup> nuclei, neutrons must have the activation kinetic energy  $T_{th} = 4.0$  MeV.  $(n, \alpha)$  means that n is bombarded to obtain  $\alpha$ . If the energy of this reaction is -x(MeV), find x
- **14.** Find the Q value of the reaction

$$N^{14} + \alpha \longrightarrow O^{17} + p$$

The masses of N<sup>14</sup>, He<sup>4</sup>, H<sup>1</sup>, O<sup>17</sup> are respectively

14.00307 u, 4.00260 u, 1.00783 u and 16.99913 u.

Find the total kinetic energy of the products if the striking  $\alpha$  particle has the minimum kinetic energy (MeV) required to initiate the reaction. 1 amu = 931.5 MeV/C<sup>2</sup>

- A radionuclide with half life T = 693.1 days emits β-particles of average kinetic energy E = 8.4 ×  $10^{-14}$  joule. This radionuclide is used as source in a machine which generates electrical energy with efficiency η = 12.6%. Calculate number of moles of the nuclide required to generate electrical energy at an initial rate P = 441 KW. (log<sub>a</sub> 2 = 0.6931) N<sub>a</sub> = 6.023 ×  $10^{23}$
- The element Curium  $^{248}_{96}$ Cm has a mean life of  $10^{13}$  seconds. Its primary decay modes are spontaneous fission and  $\alpha$ -decay, the former with a probability of 8% and the latter with a probability of 92%. Each fission releases 200 MeV of energy. The masses involved in  $\alpha$ -decay are as follows: atomic masses of atoms are  $^{248}_{96}$ Cm = 248.072220 u, He<sup>4</sup> = 4.002603 u & Pu<sup>244</sup> = 244.064100 u. (1 u = 931 MeV/ $c^2$ ). Calculate the power output ( $\mu$ W) from a sample of  $10^{20}$  Cm atoms.
- Nucleus  $_3A^7$  has binding energy per nucleon of 10 MeV. It absorbs a proton and its mass increases by  $\frac{99}{100}$  times the mass of proton. Find the new binding energy (MeV) of the nucleus so formed. [Take energy equivalent of proton = 930 MeV]
- There is a stream of neutrons with a kinetic energy of 0.0327 eV. If the half-life of neutrons is 700 seconds,  $x \times 10^{-6}$  fraction of neutrons will decay before they travel a distance of 10 m? find x [1986; 6M]

19. Calculate the electronstatic potential energy (Mev) between two identical nuclei produced in the fission of  $^{235}_{92}$ U at the moment of their separation. Given  $R_0 = 1.3 \times 10^{-15}$  m and  $\varepsilon_0 = 8.85 \times 10^{-12}$  F m<sup>-1</sup>

- 20. The binding energy per nucleon of  ${}^{16}_{8}$ O is 7.97 MeV and that of  ${}^{17}_{8}$ O of 7.75 MeV. Find the energy (Mev) required to remove a neutron from  ${}^{17}_{8}$ O.
- 21. The nucleus of  $^{230}_{90}$  Th is unstable against  $\alpha$ -decay with a half-life of 7.6 × 10<sup>3</sup> years. Using the decay reaction estimate the kinetic energy (Mev) of the emitted  $\alpha$ -particle from the following data : m ( $^{230}_{90}$  Th)=230.0381 amu, m ( $^{226}_{88}$  Ra) = 226.0254 amu and m ( $^{4}_{2}$ He) = 4.0026 amu.
- 22. A  $\pi^{\circ}$  meson at rest decays into two photons of equal energy if the wavelength (in m) of the photons is?  $x \times 10^{-14}$  m (The mass of the  $\pi^{\circ}$  is 135 Me V/c) find x.
- 23. A positive ion of kinetic energy  $1 \times 10^{-19}$  J collides with a stationary molecule of the same mass and forms a single excited composite molecule. Assuming the initial internal energies of the ion and neutral molecule were zero, if the internal energy of the molecule  $x \times 10^{-20}$  J find x.
- A sealed box was found which stated to have contained alloy composed of equal parts by weight of two metals A and B. These metals are radioactive, with half lives of 12 years and 18 years, respectively and when the container was opened it was found to contain 0.53 kg of A and 2.20 kg of B. Deduce the age (years) of the alloy.
- **25.** Find the mean-life (h) of <sup>55</sup>Co-radionuclide if its activity to decrease 4.0% per hour. The decay product is non-radioactive.
- When <sup>30</sup>Si is bombarded with a deuteron. <sup>31</sup>Si is formed in its ground state with the emission of a proton. Determine the energy (Mev) released in this reaction from the following information:

$$^{31}$$
Si  $\rightarrow$   $^{31}$  p +  $\beta^-$  +1.51 MeV  
 $^{30}$ Si + d  $\rightarrow$   $^{31}$  p + n + 5.10 MeV  
 $^{30}$ P +  $\beta^-$  +  $\overline{v}$  + 0.78 MeV

### PART - III: ONE OR MORE THAN ONE CORRECT OPTIONS

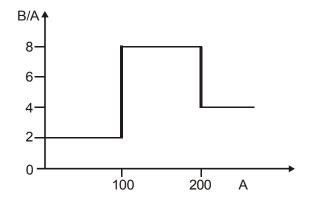
- 1.\* If a nucleus  $\frac{A}{Z}x$  emits one  $\alpha$  particle and one  $\beta$  (negative  $\beta$ ) particle in succession, then the daughter nucleus will have which of the following configurations?
  - (A) A-4 nucleons
- (B) 4 nucleons
- (C)A-Z-3 neutrons
- (D) Z-2 protons
- 2.\* The heavier stable nuclei tend to have larger N/Z ratio because -
  - (A) a neutron is heavier than a proton
  - (B) a neutron is an unstable particle
  - (C) a neutron does not exert electric repulsion
  - (D) Coulomb forces have longer range compared to nuclear forces

- 3\*. A U<sup>238</sup> sample of mass 1.0 g emits alpha particles at the rate 1.24 x 10<sup>4</sup> particles per second. (N<sub>A</sub> =  $6.023 \times 10^{23}$ )
  - (A) The half life of this nuclide is  $4.5 \times 10^9$  years
  - (B) The half life of this nuclide is  $9 \times 10^9$  years
  - (C) The activity of the prepared sample is  $2.48 \times 10^4$  particles/sec
  - (D) The activity of the prepared sample is  $1.24 \times 10^4$  particles/sec.
- **4\*.** A nitrogen nucleus <sub>7</sub>N<sup>14</sup> absorbs a neutron and can transform into lithium nucleus <sub>3</sub>Li<sup>7</sup> under suitable conditions, after emitting
  - (A) 4 protons and 4 neutrons
  - (B) 5 protons and 1 negative beta particle
  - (C) 2 alpha particles and 2 gamma particles
  - (D) 1 alpha particle, 4 protons and 2 negative beta particles.
- 5\*. Assume that the nuclear binding energy per nucleon (B/A) versus mass number (A) is as shown in the figure.

  Use this plot to choose the correct choice(s) given below.

  [JEE 2008, 4/163]

Figure:



- (A) Fusion of two nuclei with mass numbers lying in the range of 1 < A < 50 will release energy
- (B) Fusion of two nuclei with mass numbers lying in the range of 51 < A < 100 will release energy
- (C) Fission of a nucleus lying in the mass range of 100 < A < 200 will release energy when broken into two equal fragments
- (D) Fission of a nucleus lying in the mass range of 200 < A < 260 will release energy when broken into two equal fragments
- **6.\*** The decay constant of a radio active substance is 0.173 (years)<sup>-1</sup>. Therefore:
  - (A) Nearly 63% of the radioactive substance will decay in (1/0.173) year.
  - (B) half life of the radio active substance is (1/0.173) year.
  - (C) one -forth of the radioactive substance will be left after nearly 8 years.
  - (D) half of the substance will decay in one average life time.

Use approximation  $\ell$ n2 = 0.692

- 7.\* Let  $m_p$  be the mass of a proton,  $m_n$  the mass of a neutron,  $M_1$  the mass of a  $^{20}_{10}$  Ne nucleus &  $M_2$  the mass of a  $^{40}_{20}$  Ca nucleus. Then : [JEE '98, 2]
  - (A)  $M_2 = 2 M_1$
- (B)  $M_2 > 2 M_1$
- (C)  $M_2 < 2 M_1$
- (D)  $M_1 < 10 (m_n + m_p)$

### **PART - IV : COMPREHENSION**

#### Comprehension #1

The radionuclide <sup>56</sup>Mn is being produced in a cyclotron at a constant rate P by bombarding a maganese target with deutrons. <sup>56</sup>Mn has a half life of 2.5 hours and the target contains large number of only the stable maganese isotope <sup>55</sup>Mn. The reaction that produces <sup>56</sup>Mn is:

$$^{55}$$
Mn + d  $\rightarrow$   $^{56}$ Mn + p

After being bombarded for a long time, the activity of  $^{56}$ Mn becomes constant equal to  $13.86 \times 10^{10}$ s<sup>-1</sup>. (Use  $\ell$ n2 = 0.693; Avogadro No = 6 × 10<sup>23</sup>; atomic weight  $^{56}$ Mn = 56 gm/mole)

- 1. At what constant rate P, 56Mn nuclei are being produced in the cyclotron during the bombardment?
  - (A)  $2 \times 10^{11}$  nuclei/s

(B)  $13.86 \times 10^{10}$  nuclei/s

(C)  $9.6 \times 10^{10}$  nuclei/s

- (D)  $6.93 \times 10^{10}$  nuclei/s
- 2. After the activity of <sup>56</sup>Mn becomes constant, number of <sup>56</sup>Mn nuclei present in the target, is equal to
  - $(A) 5 \times 10^{11}$
- (B)  $20 \times 10^{11}$
- (C)  $1.2 \times 10^{14}$
- (D)  $1.8 \times 10^{15}$
- 3. After a long time bombardment, number of <sup>56</sup>Mn nuclei present in the target depends upon
  - (a) the number of <sup>56</sup>Mn nuclei present at the start of the process.
  - (b) half life of the <sup>56</sup>Mn
  - (c) the constant rate of production P.
  - (A) All (a), (b) and (c) are correct

(B) only (a) and (b) are correct

(C) only (b) and (c) are correct

(D) only (a) and (c) are correct

#### Comprehension #2

Consider the following nuclear decay: (initially <sup>236</sup>U<sub>02</sub> is at rest)

$$^{236}_{92}U \longrightarrow ^{232}_{90}Th + X$$

- **4.** Regarding this nuclear decay select the correct statement :
  - (A) The nucleus X may be at rest.
  - (B) The  $_{90}^{232}$  Th nucleus may be in excited state.
  - (C) The X may have kinetic energy but  $^{232}_{90}$  Th will be at rest
  - (D) The Q value is  $\Delta mc^2$  where  $\Delta m$  is mass difference of (  $^{236}_{92}$ U and  $^{232}_{90}$  Th ) and c is speed of light.

- 5. If the uranium nucleus is at rest before its decay, which one of the following statement is true concerning the final nuclei?
  - (A) They have equal kinetic energies, but the thorium nucleus has much more momentum.
  - (B) They have equal kinetic energies and momenta of equal magnitudes.
  - (C) The have momenta of equal magnitudes, but the thorium nucleus has much more kinetic energy.
  - (D) They have momentum of equal magnitudes, but X has much more kinetic energy.
- **6.** Following atomic masses and conversion factor are provided

```
^{236}_{92}U = 236.045\ 562\ u;

^{232}_{90}Th = 232.038054\ u;

^{1}_{0}n = 1.008665\ u; ^{1}_{1}P = 1.007277\ u;

^{4}_{2}He = 4.002603\ u and

^{1}_{2}u = 1.5\times 10^{-10}\ J
```

The amount of energy released in this decay is equal to:

- (A)  $3.5 \times 10^{-8}$  J
- (B)  $4.6 \times 10^{-12}$  J
- (C)  $6.0 \times 10^{-10}$  J
- (D)  $7.4 \times 10^{-13} \text{ J}$
- 7. For high principal quantum number(n) for hydrogen atom the spacing between the neighboring energy levels is proportional to
  - (A)  $\frac{1}{n^3}$
- (B)  $\frac{1}{n^2}$
- (C)  $\frac{1}{n}$
- (D)  $\frac{1}{n^0}$

#### Paragraph for Question Nos. 8 to 9

[JEE 2009, 4/160, -1]

Scientists are working hard to develop nuclear fusion reactor. Nuclei of heavy hydrogen,  ${}_1^2H$ , known as deuteron and denoted by D, can be thought of as a candidate for fusion reactor. The D-D reaction is  ${}_1^2H + {}_1^2H \rightarrow {}_2^3He + n + energy$ . In the core of fusion reactor, a gas of heavy hydrogen is fully ionized into deuteron nuclei and electrons. This collection of  ${}_1^2H$  nuclei and electrons is known as plasma. The nuclei move randomly in the reactor core and occasionally come close enough for nuclear fusion to take place. Usually, the temperatures in the reactor core are too high and no material wall can be used to confine the plasma. Special techniques are used which confine the plasma for a time  $t_0$  before the particles fly away from the core. If n is the density (number/volume) of deuterons, the product  $n_0$  is called Lawson number. In one of the criteria, a reactor is termed successful if Lawson number is greater than  $5 \times 10^{14}$  s/cm³.

It may be helpful to use the following: Boltzman constant  $k = 8.6 \times 10^{-5} \text{ eV/K}$ ;  $\frac{e^2}{4\pi\epsilon_0} = 1.44 \times 10^{-9} \text{ eVm}$ .

- 8. In the core of nuclear fusion reactor, the gas becomes plasma because of
  - (A) strong nuclear force acting between the deuterons
  - (B) Coulomb force acting between the deuterons
  - (C) Coulomb force acting between deuterons-electrons pairs
  - (D) the high temperature maintained inside the reactor core

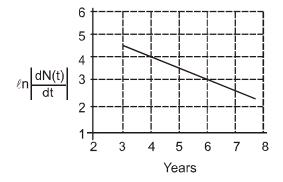
- 9. Assume that two deuteron nuclei in the core of fusion reactor at temperature T are moving towards each other, each with kinetic energy 1.5 kT, when the separation between them is large enough to neglect Coulomb potential energy. Also neglect any interaction from other particles in the core. The minimum temperature T required for them to reach a separation of  $4 \times 10^{-15}$  m in the range.
  - (A)  $1.0 \times 10^9 \text{ K} < T < 2.0 \times 10^9 \text{ K}$
- (B)  $2.0 \times 10^9 \text{ K} < T < 3.0 \times 10^9 \text{ K}$
- (C)  $3.0 \times 10^9 \text{ K} < T < 4.0 \times 10^9 \text{ K}$
- (D)  $4.0 \times 10^9 \text{ K} < T < 5.0 \times 10^9 \text{ K}$
- **10.** Results of calculations for four different designs of a fusion reactor using D-D reaction are given below. Which of these is most promising based on Lawson criterion?
  - (A) deuteron density =  $2.0 \times 10^{12}$  cm<sup>-3</sup>, confinement time =  $5.0 \times 10^{-3}$  s
  - (B) deuteron density =  $8.0 \times 10^{14}$  cm<sup>-3</sup>, confinement time =  $9.0 \times 10^{-1}$  s
  - (C) deuteron density =  $4.0 \times 10^{23}$  cm<sup>-3</sup>, confinement time =  $1.0 \times 10^{-11}$  s
  - (D) deuteron density =  $1.0 \times 10^{24}$  cm<sup>-3</sup>, confinement time =  $4.0 \times 10^{-12}$  s

# **Exercise #3**

### PART - I : JEE (ADVANCED) / IIT-JEE PROBLEMS (PREVIOUS YEARS)

- \* Marked Questions may have more than one correct option.
- 1. To determine the half life of a radioactive element, a student plots a graph of  $\ell n \left| \frac{dN(t)}{dt} \right|$  versus t. Here  $\frac{dN(t)}{dt}$

is the rate of radioactive decay at time t. If the number of radioactive nuclei of this element decreases by a factor of p after 4.16 years, the value of p is : [JEE 2010, 3/163]



2. The activity of a freshly prepared radioactive sample is  $10^{10}$  disintegrations per second, whose mean life is  $10^9$  s. The mass of an atom of this radioisotope is  $10^{-25}$  kg. The mass (in mg) of the radioactive sample is

[IIT-JEE 2011; 4/160]

3. A proton is fired from very far away towards a nucleus with charge Q = 120 e, where e is the electronic charge. It makes a closest approach of 10 fm to the nucleus. The de Brogle wavelength (in units of fm) of the proton at its start is:

(take the proton mass, 
$$m_p = (5/3) \times 10^{-27} \text{kg}$$
,  $h/e = 4.2 \times 10^{-15} \text{J.s/C}$ ;  $\frac{1}{4\pi\epsilon_0} = 9 \times 10^9 \text{ m/F}$ ; 1 fm =  $10^{-15} \text{m}$ )

[IIT-JEE-2012, Paper-1; 4/70]

#### Paragraph for Questions 4 and 5

The  $\beta$ - decay process, discovered around 1900, is basically the decay of a neutron (n), In the laboratory, a proton (p) and an electron (e<sup>-</sup>) are observed as the decay products of the neutron. therefore, considering the decay of a neutron as a tro-body decay process, it was predicted theoretically that thekinetic energy of the electron should be a constant. But experimentally, it was observed that the electron kinetic energy has a continuous spectrum. Considering a three-body decay process, i.e.  $n \to p + e^- + \overline{v}_e$ , around 1930, Pauli explained the observed electron energy spectrum. Assuming the anti-neutrino ( $\overline{v}_e$ ) to be massless and possessing negligible energy, and neutron to be at rest, momentum and energy conservation principles are applied. From this calculation, the maximum kinetic energy of the lectron is 0.8 × 10<sup>6</sup> eV. The kinetic energy carried by the proton is only the recoil energy.

**4.** What is the maximum energy of the anti-neutrino?

[IIT-JEE-2012, Paper-2; 4/66]

(A) Zero

(B) Much less than 0.8 × 10<sup>6</sup> eV

(C) Nearly  $0.8 \times 10^6$  eV

- (D) Much larger than 0.8 × 10<sup>6</sup> eV
- 5. If the anti-neutrino had a mass of 3eV/c² (where c is the speed of light) instead of zero mass, what should be the range of the kinetic energy, K, of the electron? [IIT-JEE-2012, Paper-2; 4/66]
  - (A)  $0 \le K \le 0.8 \times 10^6 \text{ eV}$

(B)  $3.0 \text{ eV} \le K \le 0.8 \times 10^6 \text{ eV}$ 

(C)  $3.0 \text{ eV} \le \text{K} < 0.8 \times 10^6 \text{ eV}$ 

- (D)  $0 \le K < 0.8 \times 10^6 \text{ eV}$
- 6. A freshly prepared sample of a radioisotope of half-life 1386 s has activity 10<sup>3</sup> disintegrations per second. Given that ln 2 = 0.693, the fraction of the initial number of nuclei (expressed in nearest integer percentage) that will decay in the first 80s after preparation of the sample is: [JEE(Advanced) 2013; 3/60]
- 7. Match List I of the nuclear processes with List II containing parent nucleus and one of the end products of each process and then select the correct answer using the codes given below the lists:

[JEE(Advanced) 2013; 5/60]

#### List I List II $_{8}^{15}0 \rightarrow_{7}^{15} N + \dots$ P. Alpha decay 1. $^{238}_{92}U \rightarrow^{234}_{90} Th + .....$ 2. Q. β+decay $^{185}_{83}$ Bi $\rightarrow^{184}_{82}$ Pb + ...... R. Fission 3. $^{239}_{94}$ Pu $\rightarrow^{140}_{57}$ La +...... S. Proton emission 4. Codes: Ρ Q R S 2 3 (A) 4 1 1 2 (B) 3 4 (C) 2 1 4 3 (D) 4 3 2 1

(B) The nucleus  $^{210}_{84}P_0$  can emit a proton

(C) Deuteron and alpha particle can undergo complete fusion.

(D) The nuclei  $_{30}^{70}$ Zn and  $_{34}^{82}$ Se can undergo complete fusion.

(B) 5422

(C) Deuteron and alpha particle can undergo complete fusion

(D) The nuclei  $^{70}_{30}$ Zn and  $^{82}_{34}$ Se can undergo complete fusion

(B) 2.14

(B) 3.2 eV

 $u_1$ :  $u_2$  = 2:1 and hc = 1240 eV nm, the work function of the metal is nearly:

(A) The nucleus  ${}_{3}^{6}$ Li can emit an alpha particle

(B) The nucleus  $^{210}_{84}\,P_{O}\,$  can emit a proton

8.

9.

10.

11.

12.

(A) 5319

(A) 1.99

(A) 3.7 eV

The correct statement is :-

#### Paragraph for Questions 8 and 9

The mass of a nucleus  $\frac{A}{7}X$  is less that the sum of the masses of (A-Z) number of neutrons and Z number of protons in the nucleus. The energy equivalent to the corresponding mass difference is known as the binding energy of the nucleus. A heavy nucleus of mass M can break into two light nuclei of masses m, and  $m_2$  only if  $(m_1 + m_2) < M$ . Also two light nuclei of masses  $m_3$  and  $m_4$  can undergo complete fusion and form a heavy nucleus of mass M' only if  $(m_3 + m_4) > M'$ . The masses of some neutral atoms are given in the table [JEE(Advanced) 2013; 2×3/60] below:

The kinetic energy (in keV) of the alpha particle, when the nucleus  $^{210}_{84}P_0$  at rest undergoes alpha decay, is:

If  $\lambda_{Cu}$  is the wavelength of  $K_{\alpha}$  X-ray line of copper (atomic number 29) and  $\lambda_{Mo}$  is the wavelength of the  $K_{\alpha}$  X-

ray line of molybdenum (atomic number 42), then the ratio  $\frac{\lambda_{Cu}}{\lambda_{Mo}}$  is close to :- [JEE Advance-2014]

(C)0.50

A metal surface is illuminated by light of two different wavelength 248 nm and 310 nm. The maximum speeds

of the photoelectrons corresponding to these wavelengths are u, and u, respectively. If the ratio

(C) 2.8 eV

(C) 5707

(D) 5818

(D) 2.5 eV

[JEE(Advanced) 2014]

<sup>1</sup> H	1.007825u	<sup>2</sup> H	2.014102u	<sup>3</sup> H	3.016050u	<sup>4</sup> <sub>2</sub> He	4.002603u
<sup>6</sup> <sub>3</sub> Li	6.015123u	<sup>7</sup> ₃Li	7.016004u	<sup>70</sup> <sub>30</sub> Zn	69.925325u	<sup>82</sup> <sub>34</sub> Se	81.916709u
<sup>152</sup> <sub>64</sub> Gd	151.919803u	<sup>206</sup> <sub>82</sub> Pb	205.974455u	<sup>209</sup> <sub>83</sub> Bi	208.980388u	<sup>210</sup> <sub>84</sub> Po	209.982876u

							_	1 1		
	<sup>6</sup> 3Li	6.015123u	<sup>7</sup> ₃Li	7.016004u	<sup>70</sup> <sub>30</sub> Zn	69.925325u	<sup>82</sup> <sub>34</sub> Se	81.916709u		
	<sup>152</sup> <sub>64</sub> Gd	151.919803u	<sup>206</sup> <sub>82</sub> Pb	205.974455u	<sup>209</sup> <sub>83</sub> Bi	208.980388u	<sup>210</sup> <sub>84</sub> Po	209.982876u		
T	The correct statement is :									
(A	(A) The nucleus $^6_3$ Li can emit an alpha particle									

- A nuclear power plant supplying electrical power to a village uses a radioactive material of half life T years as the fuel. The amount of fuel at the beginning is such that the total power requirement of the village is 12.5% of the electrical power available from the plant at that time. If the plant is able to meet the total power needs of the village for a maximum period of nT years, then the value of n is.

  [JEE(Advanced) 2015]
- **14.** Match the nuclear processes given in column-I with the appropriate option(s) in column-II.

[JEE(Advanced)-2015]

	Column-I		Column-II
(A)	Nuclearfusion	(P)	Absorption of thermal neutrons by $^{235}_{92}\mathrm{U}$
(B)	Fission in a nuclear reactor	(Q)	$^{60}_{27}\mathrm{C_{0}}$ nucleus
(C)	β-decay	(R)	Energy production in stars via hydrogen
			conversion to helium
(D)	γ-ray emission	(S)	Heavy water
		(T)	Neutrino emission

- For a radioactive material, its activity A and rate of change of its activity R are defined as  $A=-\frac{dN}{dt}$  and  $R=-\frac{dA}{dt}$ , where N(t) is the number of nuclei at time t. Two radioactive sources P (mean life  $\tau$ ) and Q (mean life  $2\tau$ ) have the same activity at t = 0. Their rates of change of activities at  $t=2\tau$  are  $R_p$  and  $R_Q$ , respectively. If  $\frac{R_P}{R_Q}=\frac{n}{e}$ , then the value of n is: [JEE(Advanced) 2015]
- A fission reaction is given by  ${}^{236}_{92}U \rightarrow {}^{140}_{54}Xe + {}^{94}_{38}Sr + x + y$ , where x and y are two particles. Considering  ${}^{236}_{92}U$  to be at rest, the kinetic energies of the products are denoted by  $K_{xe}$ ,  $K_{sr}$ ,  $K_{x}$  (2MeV) and  $K_{y}$ (2MeV), respectively. Let the binding energies per nucleon of  ${}^{236}_{92}U$ ,  ${}^{140}_{54}Xe$  and  ${}^{94}_{38}Sr$  be 7.5 MeV, 8.5 MeV and 8.5 MeV, respectively. Considering different conservation laws, the correct options(s) is (are):

[JEE(Advanced)-2015]

(A) 
$$x = n$$
,  $y = n$ ,  $K_{sr} = 129$  MeV,  $K_{ye} = 86$  MeV

(B) 
$$x = p$$
,  $y = e^-$ ,  $K_{Sr} = 129$  MeV,  $K_{xe} = 86$  MeV

(C) 
$$x = p$$
,  $y = n$ ,  $K_{sr} = 129$  MeV,  $K_{ve} = 86$  MeV

(D) 
$$x = n$$
,  $y = n$ ,  $K_{Sr} = 86$  MeV,  $K_{xe} = 129$  MeV

The isotope  $_5^{12}$ B having a mass 12.014 u undergoes β-decay to  $_6^{12}$ C.  $_6^{12}$ C has an excited state of the nucleus  $(_6^{12}$ C) at 4.041 MeV above its ground state. If  $_5^{12}$ B decays to  $_6^{12}$ C\*, the maximum kinetic energy of the β-particle in units of MeV is  $(1u = 931.5 \text{ MeV/c}^2, \text{ where c is the speed of light in vacuum})$ :

[JEE Advance-2016]

18. The electrostatic energy of Z protons uniformly distributed throughout a spherical nucleus of radius R is

given by 
$$\label{eq:E} E = \frac{3}{5} \frac{Z(Z-1)e^2}{4\pi\epsilon_0 R}$$

[JEE Advance-2016]

The measured masses of the neutron,  ${}^{1}_{1}H$ ,  ${}^{15}_{7}N$  and  ${}^{15}_{8}O$  are 1.008665 u, 1.007825 u, 15.000109 u and 15.003065 u respectively. Given that the radii of both the  ${}^{15}_{7}N$  and  ${}^{15}_{8}O$  nuclei are same, 1u = 931.5 MeV/c<sup>2</sup> (c is

the speed of light) and  $\frac{e^2}{(4\pi\epsilon_0)}$  = 1.44 MeV fm. Assuming that the difference between the binding energies

of  $^{15}_{7}\mathrm{N}$  and  $^{15}_{8}\mathrm{O}$  is purely due to the electrostatic energy, the radius of either of the nuclei is (1fm =  $10^{-15}$ m)

- (A) 2.85 fm
- (B) 3.03 fm
- (C) 3.42 fm
- (D) 3.80 fm

An accident in a nuclear laboratory resulted in deposition of a certain amount of radioactive material of halflife 18 days inside the laboratory. Tests revealed that the radiation was 64 times more than the permissible level required for safe operation of the laboratory. What is the minimum number of days after which the laboratory can be considered safe for use?

[JEE Advance-2016]

- (A)64
- (B) 90
- (C) 108
- (D) 120

20.  $^{131}$ l is an isotope of lodine that  $\beta$  decays to an isotope of Xenon with a half-life of 8 days. A small amount of a serum labelled with  $^{131}$ l is injected into the blood of a person. The activity of the amount of  $^{131}$ l injected was  $2.4 \times 10^5$  Becquerel (Bq). It is known that the injected serum will get distributed uniformly in the blood stream in less than half an hour. After 11.5 hours, 2.5 ml of blood is drawn from the person's body, and gives an activity of 115 Bq. The total volume of blood in the person's body, in liters is approximately (you may use  $e^x \approx 1 + x$  for |x| << 1 and |x| << 0.7). [JEE Advance-2017]

21. In a radioactive decay chain,  $^{232}_{90}$ Th nucleus decays to  $^{212}_{82}$ Pb nucleus. Let N $_{\alpha}$  and N $_{\beta}$  be the number of  $\alpha$  and  $\beta^-$  particles, respectively, emitted in this decay process. Which of the following statements is (are) true ? [JEE Advance-2018]

- (A)  $N_{\alpha} = 5$
- (B)  $N_{\alpha} = 6$
- (C)  $N_B = 2$
- (D)  $N_{B} = 4$

22. In a radioactive sample,  $^{40}_{19} \rm K$  nuclei either decay into stable  $^{40}_{20} \rm Ca$  nuclei with decay constant  $4.5 \times 10^{-10}$  per year or into stable  $^{40}_{18} \rm Ar$  nuclei with decay constant  $0.5 \times 10^{-10}$  per year. Given that in this sample all the stable  $^{40}_{20} \rm Ca$  and  $^{40}_{18} \rm Ar$  nuclei are produced by the  $^{40}_{19} \rm K$  nuclei only. In time t × 10<sup>9</sup> years, if the ratio of the sum of stable  $^{40}_{20} \rm Ca$  and  $^{40}_{18} \rm Ar$  nuclei to the radioactive  $^{40}_{19} \rm K$  nuclei is 99, the value of t will be : [Given In 10 = 2.3] [JEE(Advanced) 2019; P-1]

- (A) 9.2
- (B) 1.15
- (C) 4.6
- (D) 2.3

Suppose a  $^{226}_{88}$  Ra nucleus at rest and in ground state undergoes  $\alpha$ -decay to a  $^{222}_{86}$  Rn nucleus in its excited 23. state. The kinetic energy of the emitted  $\alpha$  particle is found to be 4.44 MeV.  $^{222}_{86}Rn$  nucleus then goes to its ground state by  $\gamma$ -decay. The energy of the emitted  $\gamma$ -photon is \_\_\_\_\_ keV,

[JEE(Advanced) 2019; P-2]

[Given: atomic mass of  $^{226}_{88}Ra=226.005u$  , atomic mass of  $^{222}_{86}Rn=222.000u$  , atomic mass of  $\alpha$ particle = 4.000u,  $1u = 931 \text{ MeV/c}^2$ , c is speed of the light]

## PART - II : JEE(MAIN) / AIEEE PROBLEMS (PREVIOUS YEARS)

**Directions**: Question number 1 – 2 are based on the following paragraph.

The nucleus of mass M +  $\Delta$ m is at rest and decays into two daughter nuclei of equal mass  $\frac{M}{2}$  each.. Speed [AIEEE 2010 3/144, -1] of light is c.

- This binding energy per nucleon for the parent nucleus is  $E_1$  and that for the daughter nuclei is  $E_2$ . Then : 1.
  - $(1) E_1 = 2E_2$
- $(2) E_1 > E_2$
- $(3) E_2 > E_1$
- $(4) E_2 = 2E_1$

2. The speed of daughter nuclei is

(1) c 
$$\frac{\Delta m}{M + \Delta m}$$

(2) c 
$$\sqrt{\frac{2\Delta m}{M}}$$
 (3) c  $\sqrt{\frac{\Delta m}{M}}$ 

(3) c 
$$\sqrt{\frac{\Delta m}{M}}$$

(4) c 
$$\sqrt{\frac{\Delta m}{M + \Delta m}}$$

- A radioactive nucleus (initial mass number A and atomic number Z) emits 3  $\alpha$ -particles and 2 positrons. The 3. ratio of number of neutrons to that of protons in the final nucleus will be
  - (1)  $\frac{A-Z-8}{7-4}$
- (2)  $\frac{A-Z-4}{7-8}$  (3)  $\frac{A-Z-12}{7-4}$  (4)  $\frac{A-Z-4}{7-2}$
- The half life of a radioactive substance is 20 minutes. The approximate time interval  $(t_2 t_1)$  between the time 4.

 $t_2$  when  $\frac{2}{3}$  of it has decayed and time  $t_1$  when  $\frac{1}{3}$  of it had decayed is : [AIEEE 2011, 1 May; 4/120, -1]

- (1) 7 min
- (2) 14 min
- (3) 20 min
- (4) 28 min

#### 5. Statement - 1:

A nucleus having energy  $E_1$  decays by  $\beta$ -emission to daughter nucleus having energy  $E_2$ , but the  $\beta$ -rays are emitted with a continuous energy spectrum having end point energy E<sub>1</sub> – E<sub>2</sub>.

#### Statement - 2:

To conserve energy and momentum in  $\beta$ -decay at least three particles must take part in the transformation.

[AIEEE 2011, 11 May; 4/120, -1]

- (1) Statement-1 is correct but statement-2 is not correct.
- (2) Statement-1 and statement-2 both are correct and stateemnt-2 is the correct explanation of statement-1.
- (3) Statement-1 is correct, statement-2 is correct and statement-2 is not the correct explanation of statement-1
- (4) Statement-1 is incorrect, statement-2 is correct.

[AIEEE 2012; 4/120, -1]

	(1) 0.73 MeV	(2) 7.10 MeV	(3) 6.30 MeV	(4) 5.4 MeV			
7.			om an energy level with q radiation emitted is propo	uantum number n to another with ortional to :			
				[JEE (Main) 2013; 4/120, -1]			
	(1) $\frac{1}{n}$	(2) $\frac{1}{n^2}$	(3) $\frac{1}{n^{3/2}}$	(4) $\frac{1}{n^3}$			
8.	( <sub>3</sub> Li <sup>6</sup> ) <sup>+ +</sup> all have one ele	ctron around the nucleus	. Consider an electron tra	and doubly ionised lithium ansition from n = 2 to n = 1. If the approximately which one of the [JEE (Main) 2014; 4/120, -1]			
	(1) $\lambda_1 = \lambda_2 = 4\lambda_3 = 9\lambda_4$		$(2) \lambda_1 = 2\lambda_2 = 3\lambda_3 = 4\lambda$	4			
	(3) $4\lambda_1 = 2\lambda_2 = 2\lambda_3 = \lambda$	4	(4) $\lambda_1 = 2\lambda_2 = 2\lambda_3 = \lambda_4$				
9.	photoelectrons. These e	electrons are made to ent		on a metal surface to produce 10-4T. If the radius of the largest the metal is close to:			
				[JEE(Main) 2014; 4/120, -1]			
	(1) 0.8 eV	(2) 1.6 eV	(3) 1.8 eV	(4) 1.1 eV			
10.				inutes, respectively. Initially, the ed numbers of A and B nuclei will [JEE(Main) 2016; 4/120, -1]			
	(1) 5 : 4	(2) 1 : 16	(3) 4 : 1	(4) 1 : 4			
11.			-	t = 0, there is no nucleus B. At by: [JEE(Main) 2017; 4/120, -1]			
	$(1) t = T \log (1.3)$	(2) $t = \frac{T}{\log(1.3)}$	(3) $t = \frac{T}{2} \frac{\log 2}{\log 1.3}$	$(4) t = T \frac{\log 1.3}{\log 2}$			
12.	An electron from various excited states of hydrogen atom emit radiation to come to the ground state. $\lambda_n$ , $\lambda_g$ be the de Broglie wavelength of the electron in the n <sup>th</sup> state and the ground state respectively. $\Lambda_n$ be the wavelength of the emitted photon in the transition from the n <sup>th</sup> state to the ground state. For land, (A, B are constants) [JEE(Main) 2018; 4/120, –1]						
	(1) $\Lambda_n \approx A + B\lambda_n$	(2) $\Lambda_n^2 \approx A + B\lambda_n^2$	(3) $\Lambda_n^2 \approx \lambda$	$(4) \Lambda_n \approx A + \frac{B}{\lambda_n^2}$			

Assume that a neutron breaks into a proton and an electron. The energy released during this process is :

(mass of neutron =  $1.6725 \times 10^{-27}$  kg, Mass of proton =  $1.6725 \times 10^{-27}$  kg, mass of electron =  $9 \times 10^{-31}$  kg)

- A sample of radioactive material A, that has an activity of 10 mCi(I Ci = 3.7 × I010 decays/s), has twice the 13. number of nuclei as another sample of a different radioactive maternal B which has an activity of 20 mCi. The correct choices for hall-lives of A and B would then be respectively: [JEE(Main) 2019; 4/120, -1]
  - (1) 20 days and 5 days

(2) 20 days and 10 days

(3) 5 days and 10 days

(4) 10 days and 40 days

14. Consider the nuclear fission [JEE(Main) 2019, Jan.; 4/120, -1]

$$Ne^{20} \rightarrow 2He^4 + C^{12}$$

Given that the binding energy/nucleon of Ne<sup>20</sup>, He<sup>4</sup> and C<sup>12</sup> are, respectively, 8.03 MeV, 7.07 MeV and 7.86 MeV, identify the correct statement:

- (1) 8.3 MeV energy will be released
- (2) energy of 12.4 MeV will be supplied
- (3) energy of 11.9 MeV has to be supplied
- (4) energy of 3.6 MeV will be released
- In a radioactive decay chain, the initial nucleus is  $^{232}_{90}$ Th . At the end there are 6 lpha-particles and 4 eta-particles 15. which are emitted. If the end nucleus, If  ${}_{7}^{A}X$ , A and Z are given by : [JEE(Main) 2019, Jan.; 4/120, -1]
  - (1) A = 208; Z = 80
- (2) A = 202; Z = 80 (3) A = 200; Z = 81
- (4) A = 208; Z = 82
- An alpha-particle of mass m suffers 1-dimensional elastic coolision with a nucleus at rest of unknown mass. 16. It is scattered directly backwards losing, 64% of its initial kinetic energy. The mass of the nucleus is :-

[JEE(Main) 2019, Jan.; 4/120, -1]

- (1) 4 m
- (2) 3.5 m
- (3) 2 m
- (4) 1.5 m
- Given the masses of various atomic particles  $m_p = 1.0072u$ ,  $m_n = 1.0087u$ ,  $m_e = 0.000548u$ , 17.  $m_{\overline{v}}$  = 0,  $m_{d}$  = 2.0141u, where p = proton, n = neutron, e = electron,  $\overline{v}$  = antineutrino and d = deuteron. Which of the following process is allowed by momentum and energy conservation?
  - (1) n + p  $\rightarrow$  d +  $\gamma$

[JEE(Main) 2020, Sep.; 4/100, -1]

- (2)  $e^+ + e^- \rightarrow \gamma$
- (3)  $n + n \rightarrow$  deuterium atom (electron bound to the nucleus)
- (4) p  $\rightarrow$  n + e<sup>+</sup> +  $\overline{v}$
- In a reactor, 2 kg of <sub>92</sub>U<sup>235</sup> fuel is fully used up in 30 days. The energy released per fission is 200 MeV. Given 18. that the Avogadro number,  $N = 6.023 \times 10^{26}$  per kilo mole and  $1 \text{ eV} = 1.6 \times 10^{-19}$  J. The power output of the reactor is close to: [JEE(Main) 2020, Sep.; 4/100, -1]
  - (1) 125 MW
- (2) 60 MW
- (3) 35 MW
- (4) 54 MW

# **Answers**

## Exercise # 1

#### PART - I

#### SECTION (A):

**A.1** (i) 
$$r_1 = \left[ \frac{4 \times 10^{30}}{3 \times 10^{17}} \times \frac{3}{4\pi} \right]^{1/3} = 14.71 \text{ km}$$

(ii) 
$$r_2 = \left[ \frac{6 \times 10^{24}}{3 \times 10^{17}} \times \frac{3}{4\pi} \right]^{1/3} = 168.4 \text{ m}$$

**A-2.** 2 ×10<sup>11</sup> kg/cm<sup>3</sup>, 1×10<sup>38</sup> nucl./cm<sup>3</sup>

### SECTION (B):

**B 1.** B.E. = 
$$\left[3M_{_{1}H^{1}} + 4m_{_{0}n^{1}} - M_{_{3}Li^{7}}\right]931$$

MeV = 
$$39.22 \text{ MeV}$$
,  $\frac{\text{B.E.}}{\text{A}} = \frac{39.22}{7} = 5.6 \text{ MeV}$ 

**B 2.**  $E = 20 \times (8.03) - 2 \times 4(7.07) - 2(7.68) = 11.9 \text{MeV}$ **SECTION (C):** 

**C 1.** 
$$\frac{226}{222} \times 4.78 = 4.87 \text{ MeV}.$$

**C 2.** (a) 
$$(0.680 - 0.180)$$
 Me V = 500 ke V

(b) 
$$\frac{500 \times 10^3 \text{ e}}{\text{C}} = 2.67 \times 10^{-22} \text{ kg-m/s}$$

### SECTION (D):

**D 1.** (a) 
$$\frac{0.693}{14 \times 60} = 8.25 \times 10^{-4} \text{ s}^{-1}$$

(b) 
$$(m_n - m_p - m_e)$$
 931 = 782 keV

**D 2.** 
$$\frac{6 \times 10^{23} \times 10^{-6}}{24} \left[ 1 - e^{-0.693/15} \right] = 1.128 \times 10^{15}$$

**D 3.** 
$$\frac{N_A}{24} \times \frac{0.693}{15 \times 60 \times 60} = 3.2 \times 10^{17} \text{ dps}$$

$$\& \frac{N_A}{235} \times \frac{0.693}{7.1 \times 10^8 \times 365 \times 86400} = 0.8 \times 10^5 \, dps$$

#### SECTION (E):

**E 1.** 
$$[M_U + m_n - M_{Mo} - M_{La} - 2m_n] 931 = 207.9 \text{ MeV}$$

**E 2.** 
$$\frac{2}{Q} \times \frac{100}{30} \times \frac{50}{1.6 \times 10^{-19}} \times \frac{2}{N_A} \times 10^{-3} \text{Kg}$$

$$= 2.9 \times 10^{-7} \text{ kg}$$
;

where Q =  $(2M_{1H}^2 - M_{2He}^4) \times 931 = 23.834531$ MeV

**E 3.** 
$$\frac{2}{N_A} \times \frac{1}{17.6 \,\text{e}} \times 10^{-3} \,\text{Kg/s} = 1.179 \times 10^{-9} \,\text{kg/s},$$

$$\frac{3}{N_{\Delta}} \times \frac{1}{17.6 \,\text{e}} \times 10^{-3} \text{ Kg/s} = 1.769 \times 10^{-9} \,\text{kg/s}$$

#### PART - II

#### SECTION (A):

- **A 1.** (D) **A 2.** 
  - (A)
- **A-3**. (A)

- **A-4.** (A)
- A-5.
- (B)
- **A 6**. (3)

**A** 7. (1)

### SECTION (B):

- **B 1**. (D)
- B 2.
- (D)
- **B 3**. (A)

**B 4.** (A)

### SECTION (C):

- **C 1** (C)
- C 2.
- (B)
- **C 3**. (B)

- **C-4.** (D)
- **C** 5. (2)

### SECTION (D):

- **D 1**. (C)
- D 2.
- (B)
- **D** 3. (D)

- **D 4**. (3)
- D 5.
- (A)
- **D-6.** (B)

- **D** 7. (D)
- **D 8.** (D)

### SECTION (E):

- **E 1**. (C)
- E 2.
- (D)
- **E 2**. (D)

- **E 3**. (D)
- E 4.
- (C)
- **E 5**. (D)

- **E 6.** (C)
- E-7.
- (C)
- **E-8.** (A)

**E-9.** (D)

#### PART - III

- $(A) \rightarrow p,q,r,s; (B) \rightarrow p,q,r,s; (C) \rightarrow p,q,r,s;$ 1.  $(D) \rightarrow p,q,r,s$
- 2. (A) q,r,s, (B) q,r,s (C) q,r,s (D) p,q,r,s
- (A) 3.\_
- 4.  $(A) \rightarrow (p,r); \ (B) \rightarrow (p,q); \quad \ (C) \rightarrow (p,q,r\&s); \ (D) \rightarrow$ (p,q&r)
- $(\mathsf{A}) \to (\mathsf{p}),\, (\mathsf{r});\, (\mathsf{B}) \to (\mathsf{q}),\, (\mathsf{s});\, (\mathsf{C}) \to (\mathsf{p});\, (\mathsf{D}) \to (\mathsf{q})$ 5.
- 6.  $(A) \rightarrow p, \, q, \, t; \, (B) \rightarrow q, \, t; \, (C) \rightarrow s; \, (D) \rightarrow s$

## Exercise # 2

	PART - I								
1.	(A)	2.	(B)	3.	(C)				
4.	(B)	5.	(A)	6.	(A)				
7.	(B)	8.	(A)	9.	(D)				
10.	(A)	11.	(B)	12.	(A)				
13.	(C)	14.	(C)	15.	(C)				
16.	(D)	17.	(B)	18.	(B)				
19.	(D)	20.	(B)	21.	(A)				
22.	(A)	23.	(B)	24.	(D)				
25.	(D)	26.	(A)						

#### PART - II 2 3. 1. 7 2. 3 4. 6.954 5. 0.36 6. 3 7. 1.40 8. 1 8.781 9. 10. (i) 200.57; (ii) 22.84 11. 1.5 12. 2.65 13. 3.7 14. 0.34 15. 6000 33.16 79.3 16. 17. 18. 3.96 19. 240 20. 4.23 21. 9.25 22. 1.84 23. 5 24. 74 25. 26. 4.37 24.5

## **PART - III**

- (C,D) 1. (A,C)2. 3. (A,D)
- (A,C,D) **5.** 4. (B,D) (A,C)6.
- 7. (C,D)

	F	PART -	- IV		
(B)	2.	(D)	3.	(C)	
(B)	5.	(D)	6.	(D)	

- 7. (A) 8. (D) 9. (A)
- 10. (B)

1.

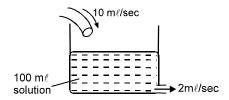
4.

			PART	<b>- I</b>	
1.	8	2.	1	3.	7
4.	(C)	5.	(D)	6.	4
7.	(C)	8.	(C)	9.	(A)
10.	(C)	11.	(B)	12.	(A)
13.	3				
14.	(A)-R o	r R,T; (B	)-P&S	(C)-Q &	T; (D)-R
15.	2	16.	(A)	17.	9
18.	(C)	19.	(C)	20.	5
21.	(A,C)	22.	(A)	23.	130 to 140
		F	PART	- II	
1.	(3)	2.	(2)	3.	(2)
4.	(3)	5.	(2)	6.	(1)
7.	(4)	8.	(1)	9.	(4)
10.	(1)	11.	(4)	12.	(4)
13.	(1)	14.	(3)	15.	(4)
16.	(1)	17.	(1)	18.	(2)

# **RANKER PROBLEMS**

#### SUBJECTIVE QUESTIONS

- Nuclei of radioactive element A are being produced at a constant rate  $\alpha$ . The element has a decay constant  $\lambda$ . At time t = 0, there are  $N_0$  nuclei of the element. [IIT 1998]
  - (a) Calculate the number N of nuclei of A at time t.
  - (b) If  $\alpha = 2N_0\lambda$ , calculate the number of nuclei of A after one half-life of A and also the limiting value of N as  $t \to \infty$ .
- 2. A 100 m $\ell$  solution having activity 50 dps is kept in a beaker. It is now constantly diluted by adding water at a constant rate of 10 m $\ell$ /sec and 2 m $\ell$ /sec of solution is constantly being taken out. Find the activity of 10 m $\ell$  solution which is taken out, assuming half life to be effectively very large.



- 3. What kinetic energy must an  $\alpha$ -particle possess to split a deuteron H² whose binding energy is  $E_h = 2.2 \text{MeV}$ ?
- **4.** A nucleus at rest undergoes  $\alpha$  decay according to the equation ,  ${}^{225}_{92}$  X  $\longrightarrow$  Y +  $\alpha$  .

At time t = 0 , the emitted  $\alpha$  – particle enters in a region of space where a uniform magnetic field  $\vec{B} = B_0 \, \hat{i}$  and electric field  $\vec{E} = E_0 \, \hat{i}$  exist . The  $\alpha$  – particle enters in the region with velocity  $\vec{v} = v_0 \, \hat{j}$  from origin . At time t =  $\sqrt{3} \times 10^7 \frac{m_\alpha}{q_\alpha \, E_0}$  sec. , where  $m_\alpha$  is the mass and  $q_\alpha$  is the charge of  $\alpha$  – particle . The particle was observed to have speed twice the initial speed  $v_0$ . Then find :

- (a) the initial speed  $v_0$  of the  $\alpha$  particle
- **(b)** the velocity of  $\alpha$  particle at time t
- (c) the binding energy per nucleon of X.

**Given that** : m (Y) = 221.03 u, m (He) = 4.003 u , m (n) = 1.009 u, m (p) = 1.0084 u and 1 u =  $1.67 \times 10^{-27}$  kg = 931 MeV/c<sup>2</sup>

- 5. A neutron collides elastically with an initially stationary deuteron. Find the fraction of the kinetic energy lost by the neutron (a) in a head-on collision; (b) in scattering at right angles.
- **6.** Find the binding energy of a nucleus consisting of equal numbers of protons and neutrons and having the radius one and a half time smaller than that of Al<sup>27</sup> nucleus.

- 7. A radio nuclide with half life T = 69.31 second emits β-particles of average kinetic energy E = 11.25 eV. At an instant concentration of β-particles at distance, r = 2 m from nuclide is  $n = 3 \times 10^{13}$  per  $m^3$ .
  - (i) Calculate number of nuclei in the nuclide at that instant.
  - (ii) If a small circular plate is placed at distance r from nuclide such that  $\beta$ -particles strike the plate normally and come to rest, calculate pressure experienced by the plate due to collision of  $\beta$ -particle. (Mass of  $\beta$ -particle = 9 × 10<sup>-31</sup> kg) (log<sub>e</sub> 2 = 0.693)
- 8. (a) Find the energy needed to remove a neutron from the nucleus of the calcium isotope  ${}^{42}_{20}$ Ca
  - (b) Find the energy needed to remove a proton from this nucleus
  - (c) Why are these energies different?

Atomic masses of  $^{41}_{20}$ Ca and  $^{42}_{20}$ Ca are 40.962278 u and 41.958622 u respectively.

9. A nucleus X, initially at rest, undergoes alpha-decay according to the equation. [JEE 1991; 2+4+2M]

$$_{92}^{A}X \rightarrow + _{Z}^{228}Y + \alpha$$

- (a) Find the values of A and Z in the above process.
- (b) The alpha particle produced in the above process is found to move in a circular track of radius 0.11 m in a uniform magnetic field of 3 tesla. Find the energy (in MeV) released during the process and the binding energy of the parent nucleus X.

Given that m (Y) = 228.03 u;  $m({}_{0}^{1}n)$  = 1.009 u.

$$m_{2}^{4}He = 4.003 \text{ u}; m(_{1}^{1}H) = 1.008 \text{ u}.$$

10. 100 millicuries of radon which emits  $5.5 \text{ MeV} \alpha$  - particles are contained in a glass capillary tube 5 cm long with internal and external diameters 2 and 6 mm respectively Neglecting and effects and assuming that the inside of the tube is uniformly irrandicated by the particles which are stopped at the surface calculate the temperature difference between the walls of a tube when steady thermal conditions have been reached.

Thermal conductivity of glass = 0.025 Cal cm<sup>-2</sup> s<sup>-1</sup> C<sup>-1</sup>

Curie =  $3.7 \times 10^{10}$  disintergration per second

11.  $^{90}$ Sr decays to  $^{90}$ Y by  $\beta$  decay with a half-life of 28 years.  $^{90}$ Y decays by  $\beta$  decay to  $^{90}$ Zr with a half-life of 64h.

A pure sample of  ${}^{90}$ Sr is allowed to decay. What is the value of  $\frac{N_{Sr}}{N_y}$  after (a) 1h (b) 10 years?

# **Answers**

**1.** (a) 
$$N = \frac{1}{\lambda} [\alpha - (\alpha - \lambda N_0) e^{-\lambda t}]$$
, (b)  $2 N_0$ 

**2.** 6.6 MeV

**4.** (a) 
$$v_0 = 10^7 \text{ m/s}$$
; (b)  $\vec{v}$  (t)  $= \frac{q E_0}{m} t \hat{i} + 10^7 \cos \omega t \hat{j} - 10^7 \sin \omega t \hat{k}$  where  $\omega = q B/m$ 

(c) 8.11 MeV/nucleon

5. (a) 
$$\eta = 4\text{mM/(m + M)}^2 = 0.89$$
; (b)  $\eta = 2\text{m/(m + M)} = 2/3$ .

Here m and M are the masses of a neutron and deuteron.

**6.** Be<sup>8</sup>, 
$$E_b = 56.5$$
 MeV.

7. (i) 
$$9.6 \pi \times 10^{22}$$
,

- (b) Removing a proton from  ${}^{42}_{20}$ Ca leaves the potassium isotope  ${}^{41}_{19}$ K. A similar calculation gives a binding energy of 10.27 MeV for the missing proton.
- (c) The neutron was acted upon only by attractive nuclear forces whereas the proton was also acted upon by repulsive electric forces that decrease its binding energy.
- **9.** (a) 232, 90 (b) 5.3 MeV, 1823.2 MeV
- **10.** The flow of heat in a material placed between the walls of a coaxial cylinder is given by

$$\frac{dQ}{dt} = \frac{2\pi KL(T_1 - T_2)}{\ell n \left(\frac{r_2}{r_1}\right)}$$

Number of decays of radon atoms per second

$$\frac{dN}{dt} = 100 \times 10^{-3} \times 3.7 \times 10^{10} = 3.7 \times 10^{9}$$
 disintegration/second

Energy deposited by  $\alpha'$  s =3.7 × 10 $^{9}$  × 5.5 MeV/s

= 
$$2.035 \times 10^{10}$$
 MeV/s =  $3.256 \times 10^{-7}$  J =  $0.779 \times 10^{-3}$  Cal/s

Using the values.  $k = 0.025 \text{ Cal cm}^{-2} \text{ s}^{-1} \text{ C}^{-1}$ , L = 5 cm,  $r_1 = 2 \text{ mm}$  and

$$r_2 = 6 \text{ mm in (1)}$$
, and solving for  $(T_1 - T_2)$  we find  $(T_1 - T_2) = 1.09 \,^{\circ}\text{C}$ 

11. (a) For t = 1 h and using the values for the decay constans  $N_{sf}/N_v = 3.56 \times 10^5$ 

(b) For t = 10 years, 
$$N_{sr}/N_{v} = 3823$$

# **SELF ASSESSMENT PAPER**

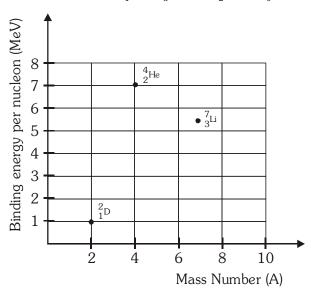
## **JEE (ADVANCED) PAPER-1**

### SECTION-1: ONE OPTION CORRECT TYPE (Maximum Marks - 12)

- Binding Energy per nucleon of a fixed nucleus X<sup>A</sup> is 6 MeV. It absorbs a neutron moving with KE = 2MeV, 1. and converts into Y at ground state, emitting a photon of energy 1 MeV. The Binding Energy per nucleon of Y (in MeV) is -
  - (A)  $\frac{(6A+1)}{(A+1)}$  (B)  $\frac{(6A-1)}{(A+1)}$  (C) 7

- (D)  $\frac{7}{6}$
- 2. The positions of  ${}_{1}^{2}D$ ,  ${}_{2}^{4}He$  and  ${}_{3}^{7}Li$  are shown on the binding energy curve as shown in figure.

The energy released in the fusion reaction.  $^2_1D + ^7_3\text{Li} \rightarrow 2 \ ^4_2\text{He} \ + \ ^1_0\text{n}$ 



- (A) 20 MeV
- (B) 16 MeV
- (C) 8 MeV
- (D) 1.6 MeV

- $A \xrightarrow{\lambda_1} B \xrightarrow{\lambda_2} C$ 3.
  - t = 0 $N_0$
- 0
- $N_1$
- $N_2$
- $N_3$

In the above radioactive decay C is stable nucleus. Then:

- (A) rate of decay of A will first increase and then decrease
- (B) number of nuclei of B will first increase and then decrease
- if  $\lambda_2 > \lambda_1$ , then activity of B will always be higher than activity of A (C)
- if  $\lambda_1 >> \lambda_2$ , then number of nucleus of C will always be less than number of nucleus of B. (D)

4.  $A \xrightarrow{\lambda} B \xrightarrow{2\lambda} C$   $t = 0 \quad N_0 \qquad 0 \qquad 0$   $t \quad N_1 \qquad N_2 \qquad N_3$ 

The ratio of  $N_1$  to  $N_2$  when  $N_2$  is maximum is :

- (A) at no time this is possible
- (B) 2
- (C) 1/2
- (D)  $\frac{\ell n \, 2}{2}$

### SECTION-2: ONE OR MORE THAN ONE CORRECT TYPE (Maximum Marks - 32)

- In the  $\alpha$ -decay of a U-238 nucleus the energy released in the decay is Q. The U-238 nucleus was initially stationary. Which of the following is (are) true?
  - (A) Ratio of K.E. of  $\alpha$ -particle and Thorium nucleus is 117 : 2
  - (B) Ratio of K.E. of Thorium nucleus and  $\alpha$ -particle is 1 : 234
  - (C) Momentum of  $\alpha\text{-particle}$  is  $\sqrt{\frac{234Qm_{\alpha}}{119}}$
  - (D) Recoil velocity of Thorium nucleus is  $\sqrt{\frac{234Q}{119\times117m_{Th}}}$
- A stationary nucleus  $^{226}_{88}$ Ra (ground state) decays into the nucleus  $^{222}_{86}$ Rn (ground state) by emitting an α-particle. (Given that  $m(^{226}_{88}$ Ra) = 226.02540 u,  $m(^4_2$ He) = 4.00260 u,  $m(^{222}_{86}$ Rn) = 222.01750 u.) and Take 1amu = 931 MeV/c².
  - (A) The Q-value for the  $\alpha\text{-decay}$  of  $\binom{226}{88}Ra)$  is (approximately) 4.93 MeV
  - (B) The Q-value for the  $\alpha\text{-decay}$  of  $\binom{226}{88}Ra)$  is (approximately) 9.8 MeV
  - (C) The K.E. of the emitted  $\alpha$ -particle in the decay of  $^{226}_{88}Ra$  is (approximately) 4.85 MeV
  - (D) The K.E. of the emitted  $\alpha$ -particle in the decay of  $^{226}_{88}\,Ra\,$  is (approximately) 9.7 MeV
- 7. A nucleus has a radius of 7.2 × 10<sup>-15</sup> m. When an  $\alpha$ -decay takes place from this nucleus, ratio of number of neutrons and number of protons in the daughter nucleus becomes  $\frac{65}{41}$ :
  - (A) Parent nucleus is 84Po.

- (B) Daughter nucleus is <sub>82</sub>Pb.
- (C) Mass number of daughter nucleus is 216.
- (D) Mass number of parent nucleus is 216.

- 8. The mass of <sup>11</sup>C and <sup>11</sup>B are respectively 11.0114 amu and 11.0093 amu respectively. Mass of electron is 0.0005486 amu. If carbon converts to boron by  $\beta^+$  decay, (Take : 1 amu = 931 MeV)
  - (A) Maximum energy of positron is measured to be 933.6 keV
  - (B) Maximum energy of positron is measured to be 1955.6 keV
  - (C) Minimum energy of positron is measured to be zero.
  - (D) A zero rest mass particle is also emitted in the decay
- 9. A radioactive sample has a half life of 40 seconds. When its activity is measured 80 seconds after the begining, it is found to be  $6.932 \times 10^{18}$  dps. During this time total energy released is  $6 \times 10^{8}$  joule ( $\ell$ n2 = 0.6932):
  - (A) The initial number of atoms in the sample is  $1.6 \times 10^{20}$
  - (B) The initial number of atoms in the sample is  $1.6 \times 10^{21}$
  - (C) Energy released per fission is  $5 \times 10^{-13}$  J
  - (D) Energy released per fission is  $\frac{5}{3}$  × 10<sup>-13</sup> J
- **10.** Choose the **CORRECT** option(s):
  - (A) Strong nuclear force is a spin dependent force.
  - (B) Strong nuclear force between an electron and proton is same as between a proton and neutron.
  - (C) Strong nuclear force is a short range force.
  - (D) Strong nuclear force is always attractive in nature.
- 11. It is proposed to use the nuclear fusion reaction  $1H^2 + 1H^2 \rightarrow 2He^4$  in a nuclear reactor of 200 MW rating.
  - (A) The mass defect for this reaction is 0.0256 a.m.u.
  - (B) The energy released in this reaction is 23.8336 MeV
  - (C) The number of deuterium needed per day is  $36.35 \times 10^{24}$
  - (D) None of these
- 12. Consider the following nuclear reactions and select the correct statements from the options that follow.

**Reaction I**: 
$$n \rightarrow p + e^- + \overline{\nu}$$
 **Reaction II**:  $p \rightarrow n + e^+ + \nu$ 

- (A) Free neutron has higher mass than proton, therefore reaction I is possible
- (B) Free proton has less mass than neutron, therefore reaction II is not possible
- (C) Inside a nucleus, both decays (reaction I and II) are possible
- (D) Inside a nucleus, reaction I is not possible but reaction II is possible.

## **SECTION-3: NUMERICAL VALUE TYPE (Maximum Marks - 18)**

- 13. A neutron of energy 2 MeV and mass  $1.6 \times 10^{-27}$  kg passes a proton at such a distance that the angular momentum of neutron relative to proton approximately equals  $4 \times 10^{-34}$  Js. The distance of closest approach neglecting the interaction between particles is given by  $\alpha \times 10^{-16}$  m. Find the value of  $\alpha$ .
- 14. Consider the following fussion raction  $_1H^2 + _1H^3 \rightarrow 2He^4$ . If 20 MeV of energy is released per fusion reaction. Mass of  $_1H^2$  consumed per day is 0.1 gm. What is the (approx) power of the reactor in MW?
- $\begin{array}{ll} \textbf{15.} & \text{The reaction } {}^7_3\text{Li} + {}^1_1\text{ H} \rightarrow {}^7_4\text{ Be} + {}^1_0\text{ n} \text{ is endothermic. Assuming that Li nuclei is free and at rest. What is the minimum kinetic energy (in keV) of incident proton so that this reaction occurs ? Take Q value of this reaction <math display="block"> \text{as -1645 keV. If your answer is N fill value } \frac{N}{235} \, . \\ \end{array}$
- In an  $\alpha-decay$  the KE of  $\alpha$  particle in 48 MeV and Q-value of the reaction is 50 MeV. If the mass number of the mother nucleus is x. Then the value of  $\left\{\frac{2x}{100}\right\}$  will be (Assume that daughter nucleus is in ground state)
- 17. In a fission reaction  ${}^{236}_{92}U \rightarrow {}^{117}X + {}^{117}Y + n + n$ , the binding energy per nucleon of X and Y is 8.5 MeV whereas of  ${}^{236}U$  is 7.58 MeV. The total energy liberated is 25N MeV. Fill the value of N in OMR sheet.
- The radio nuclide decays according to  $^{11}C \rightarrow ^{11}B + e^+ + \upsilon$ . Find the disintegration energy Q of this process (in MeV). Given that atomic masses  $m_C = 11.011433 \, u$ ,  $m_e = 0.0005486 \, u$ ,  $m_B = 11.009305 \, u$ , 1 amu = 931 MeV. Fill  $\frac{100Q}{19}$  in OMR sheet.

				Ans	wers	S			
1.	(B)	2.	(B)	3.	(B)	4.	(B)	5.	(A,C)
6.	(A,C)	7.	(A,B,D)	8.	(A,D)	9.	(B,C)	10.	(A,C)
11.	(A,B,C)	12.	(A,B,C)	13.	125	14.	1	15.	8
16.	2	17.	8	18.	5				