

Coordinate Geometry

1. The distance between the point $(a, b), (-a, -b)$ is

(a) $2\sqrt{a^2 + b^2}$

(b) $2\sqrt{a^2 - b^2}$

(c) $\sqrt{a^2 + b^2}$

(d) $\sqrt{a + b}$

Ans. $2\sqrt{a^2 + b^2}$

2. The area of triangle whose vertices are $(1, -1), (-4, 6)$ and $(-3, -5)$ is

(a) 21

(b) 32

(c) 24

(d) 25

Ans. (c) 24

3. The point $(5, -3)$ lies in

(a) 1st quadrant

(b) 2nd quadrant

(c) 3rd quadrant

(d) 4th quadrant

Ans. d) 4th quadrant

4. The distance between the points $(\cos\theta, \sin\theta)$ and $(\sin\theta, -\cos\theta)$ is

(a) $\sqrt{3}$

(b) 2

(c) 1

(d) $\sqrt{2}$

Ans. (d) $\sqrt{2}$

5. If $(1, 2)$, $(4, y)$, $(x, 6)$ and $(3, 5)$ are the vertices of a parallelogram taken in order.
 (x, y)

Then is

- (a) $(6, 2)$
- (b) $(6, 3)$
- (c) $(6, 4)$
- (d) $(3, 4)$

Ans.(b) $(6, 3)$

6. The coordinates of the point which divides the join of $(-1, 7)$ and $(4, -3)$ in the ratio 2:3 is

- (a) $(1, 3)$
- (b) $(2, 3)$
- (c) $(3, 1)$
- (d) $(1, 1)$

Ans. (a) $(1, 3)$

7. The coordinates of a point A, where AB is the diameters of a circle whose centre $(2, -3)$ and B is $(1, 4)$ is

- (a) $(3, -9)$
- (b) $(2, 9)$
- (c) $(3, -10)$
- (d) $(4, 5)$

Ans. (c) $(3, -10)$

8. If the area of a quadrilateral ABCD is zero, then the four points A, B, C, D are

- (a) Collinear
- (b) Not collinear
- (c) Nothing can be said
- (d) None of these

Ans. (a) Collinear

9. The value of K if the points $A(2, 3)$, $B(4, K)$ and $C(6, -3)$ are collinear is

- (a) (1)
- (b) (-1)
- (c) (2)
- (d) (0)

Ans. (d) (0)

10. The mid-point of the line segment joining $(2a, 4)$ and $(-2, 3b)$ is $(1, 2a+1)$. The values of a and b is

- (a) $a=2, b=2$
- (b) $a=1, b=3$
- (c) $a=2, b=3$
- (d) $a=1, b=1$

Ans. (a) $a=2, b=2$

11. Coordinate of A and B are $(-3, \alpha)$ and $(1, \alpha+4)$. The mid-point of AB is $(-1, 1)$. The value of α is

- (a) (-1)
- (b) (2)
- (c) (3)
- (d) (1)

Ans. (a) (-1)

12. The distance between $P(a, 7)$ and Q $(1, 3)$ is 5. The value of a is

- (a) (4, 2)
- (b) (-4, -2)
- (c) (4, -2)
- (d) (4, 1)

Ans. (c) (4, -2)

13. On which axis point $(-4, 0)$ lie

- (a) x-axis
- (b) y-axis
- (c) both
- (d) none of these

Ans. (a) x-axis

14. The distance of the point $(-4, -6)$ from the origin is

- (a) $\sqrt{53}$
- (b) $2\sqrt{13}$
- (c) $2\sqrt{12}$
- (d) $\sqrt{13}$

Ans. (b) $2\sqrt{13}$

15. The coordinates of the mid-point of the line segment joining $(-5, 4)$ and $(7, -8)$ is

- (a) $(1, -2)$
- (b) $(1, 2)$
- (c) $(1, 3)$
- (d) $(-1, -2)$

Ans. (a) $(1, -2)$

16. Two vertices of a $\triangle ABC$ are $A(1, -1)$ and $B(5, 1)$. If the coordinates of its centroid be $\left(\frac{5}{3}, 1\right)$, then the coordinates of the third vertex C is

- (a) $(-1, -3)$
- (b) $(1, 3)$
- (c) $(-1, 3)$
- (d) $(1, 2)$

Ans. (c) $(-1, 3)$

17. The abscissa of every point on y-axis is

- (a) 0
- (b) 1
- (c) 2
- (d) -1

Ans. (a) 0

18. The ordinate of every point on x-axis is

- (a) 1
- (b) 2
- (c) 0

(d) -1

Ans. (c) 0

19. Find the distance between the following pairs of points:

(i) (2, 3), (4, 1)

(ii) (-5, 7), (-1, 3)

(iii) (a, b), (-a, -b)

Ans. (i) Applying Distance Formula to find distance between points (2, 3) and (4, 1), we get

$$\begin{aligned}d &= \sqrt{(4-2)^2 + (1-3)^2} \\&= \sqrt{(2)^2 + (-2)^2} \\&= \sqrt{4+4} = \sqrt{8} = 2\sqrt{2} \text{ units}\end{aligned}$$

(ii) Applying Distance Formula to find distance between points (-5, 7) and (-1, 3), we get

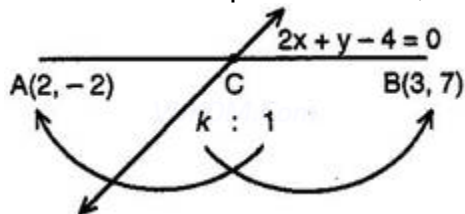
$$\begin{aligned}d &= \sqrt{[-1-(-5)]^2 + (3-7)^2} \\&= \sqrt{(4)^2 + (-4)^2} \\&= \sqrt{16+16} = \sqrt{32} = 4\sqrt{2} \text{ units}\end{aligned}$$

(iii) Applying Distance Formula to find distance between points (a, b) and (-a, -b), we get

$$\begin{aligned}d &= \sqrt{(-a-a)^2 + (-b-b)^2} \\&= \sqrt{(-2a)^2 + (-2b)^2} = \sqrt{4a^2 + 4b^2} \\&= \sqrt{4(a^2 + b^2)} = 2\sqrt{a^2 + b^2}\end{aligned}$$

20. Determine the ratio in which the line $2x+y-4=0$ divides the line segment joining the points A(2,-2) and B(3,7).

Ans. Let the line $2x+y-4=0$ divides the line segment joining A(2,-2) and B(3,7) in the ratio $k:1$ at point C. Then, the coordinates of C are $\left(\frac{3k+2}{k+1}, \frac{7k-2}{k+1}\right)$.



But C lies on $2x+y-4=0$, therefore

$$2\left(\frac{3k+2}{k+1}\right) + \left(\frac{7k-2}{k+1}\right) - 4 = 0$$

$$\Rightarrow 6k+4+7k-2-4k-4=0$$

$$\Rightarrow 9k-2=0$$

$$\Rightarrow k = \frac{2}{9}$$

Hence, the required ratio is 2 : 9 internally.

21. Find a relation between x and y if the points (x, y) , $(1, 2)$ and $(7, 0)$ are collinear.

Ans. The points A (x, y) , B $(1, 2)$ and C $(7, 0)$ will be collinear if
Area of triangle = 0

$$\Rightarrow \frac{1}{2}[x(2-0)+1(0-y)+7(y-2)]=0$$

$$\Rightarrow 2x-y+7y-14=0$$

$$\Rightarrow 2x+6y-14=0$$

$$\Rightarrow x+3y-7=0$$