

## PART : MATHEMATICS

1. If  $f(x) = \begin{cases} -2 & ; -2 \leq x < 0 \\ x-2 & ; 0 \leq x \leq 2 \end{cases}$  and  $h(x) = f(|x|) + |f(x)|$  then  $\int_0^k h(x)dx$  is equal to (where  $0 < k \leq 2$ )  
 (1)  $k$       (2)  $\frac{k}{2}$       (3)  $\frac{2k}{3}$       (4)  $0$

**Ans.** (4)

**Sol.**  $f(|x|) = \begin{cases} -x-2 & ; -2 \leq x < 0 \\ x-2 & ; 0 \leq x \leq 2 \end{cases}$

And  $|f(x)| = \begin{cases} 2 & ; -2 \leq x < 0 \\ -(x-2) & ; 0 \leq x \leq 2 \end{cases}$

So  $h(x) = \begin{cases} (-x-2) + 2 = -x & ; -2 \leq x < 0 \\ x-2 - x + 2 = 0 & ; 0 \leq x \leq 2 \end{cases}$

Hence  $\int_0^k h(x)dx = \int_0^k 0 dx = 0$

2. Let ABC be a triangle . If  $P_1, P_2, P_3, P_4, P_5$  are five points on side AB,  $P_6, P_7, \dots, P_{11}$ , are 6 points on side BC and  $P_{12}, P_{13}, \dots, P_{18}$ , are 7 points on side AC then find the number of triangles formed by these 18 points taking as vertices .

**Ans.** 751

**Sol.** Number of triangles =  ${}^{18}C_3 - ({}^5C_3 + {}^6C_3 + {}^7C_3) = \frac{18 \times 17 \times 16}{6} - (10 + 20 + 35) = 816 - 65 = 751$

3. Let  $y(x)$  be a curve given by differential equation  $\frac{dy}{dx} - y = 1 + 4\sin x$ . If  $y(0) = 1$  then value of  $y(\pi/2)$  is equal to

(1)  $-3 + 4e^{\pi/2}$       (2)  $3 - 4e^{\pi/2}$       (3)  $3 + 4e^{-\pi/2}$       (4)  $3 + 4e^{\pi/2}$

**Ans.** (1)

**Sol.**  $\frac{dy}{dx} - y = 1 + 4\sin x$  linear differential equation

I.F. =  $e^{\int -dx} = e^{-x}$

So solution of linear differential equation is

$ye^{-x} = \int e^{-x}(1 + 4\sin x)dx$

$ye^{-x} = -e^{-x} + 4 \int e^{-x} \sin x dx$

$ye^{-x} = -e^{-x} + 4 \frac{e^{-x}}{2} [-\sin x - \cos x] + C$

$y = -1 - 2(\sin x + \cos x) + C e^x$

Now  $y(0) = 1 \Rightarrow 1 = -1 - 2(0+1) + C \Rightarrow 2 = -2 + C \Rightarrow C = 4 \Rightarrow y = -1 - 2(\sin x + \cos x) + 4e^x$

$\Rightarrow y\left(\frac{\pi}{2}\right) = -1 - 2(1+0) + 4e^{\frac{\pi}{2}} \Rightarrow y\left(\frac{\pi}{2}\right) = -3 + 4e^{\frac{\pi}{2}}$

4. Let there are 3 bags A, B and C. Bag A contains 5 black balls and 7 red balls, bag B contains 5 red and 7 black balls and bag C contains 7 red and 7 black balls. A ball is drawn and found to be black, then the probability that it is drawn from bag A, is

(1)  $\frac{7}{18}$       (2)  $\frac{5}{42}$       (3)  $\frac{5}{18}$       (4)  $\frac{1}{3}$

**Ans.** (3)

**Sol.** prob. that ball drawn from bag is black

$$= \frac{1}{3} \times \frac{5}{12} + \frac{1}{3} \times \frac{7}{12} + \frac{1}{3} \times \frac{7}{14}$$

Prob. that black ball drawn from bag A is

$$\begin{aligned}&= \frac{\frac{1}{3} \times \frac{5}{12}}{\frac{1}{3} \times \frac{5}{12} + \frac{1}{3} \times \frac{7}{12} + \frac{1}{3} \times \frac{7}{14}} \\&= \frac{5}{5+7+6} \\&= \frac{5}{18}\end{aligned}$$

5. The number of rational terms in the expansion of  $\left(2^{\frac{1}{5}} + 3^{\frac{1}{3}}\right)^{15}$

**Ans.** (2)

**Sol.**  $T_{r+1} = {}^{15}C_r 2^{\frac{15-r}{5}} \times 3^{\frac{r}{3}}$

for rational numbers  $\frac{15-r}{5}$  &  $\frac{r}{3}$

should be integers

so  $r = 0, 5, 10, 15$  for  $\frac{15-r}{5}$

&  $r = 0, 3, 6, 9, 12, 15$  for  $\frac{r}{3}$

common values 0, 15

So only 2 terms are rational

6. 2 and 6 are roots of the equation  $ax^2 + bx + 1 = 0$  then the quadratic equation whose roots are

$\frac{1}{a+3b}$  and  $\frac{1}{a+6b}$  is

(1)  $1081x^2 + 840x - 144 = 0$

(2)  $1081x^2 + 840x + 144 = 0$

(3)  $1081x^2 - 840x + 144 = 0$

(4)  $1081x^2 - 840x - 144 = 0$

**Ans.** (2)

**Sol.** Sum of roots  $-\frac{b}{a} = 2 + 6 = 8 \Rightarrow b = -8a$

Product of roots  $\frac{1}{a} = 12 \Rightarrow a = \frac{1}{12} \quad b = -\frac{2}{3}$

Hence new roots  $\frac{1}{a+3b} = \frac{1}{\frac{1}{12} - 2} = \frac{12}{-23}$

and  $\frac{1}{a+6b} = \frac{1}{\frac{1}{12} - 4} = -\frac{12}{47}$

so other quadratic equation is

$$x^2 + \left(\frac{12}{23} + \frac{12}{47}\right)x + \frac{144}{23 \times 47} = 0$$

$$\Rightarrow 1081x^2 + 840x + 144 = 0$$

7. Let  $f(x) = \begin{cases} \frac{1-\cos 2x}{x^2} & x < 0 \\ \alpha & x = 0 \\ \beta \left( \frac{\sqrt{1-\cos x}}{x} \right) & x > 0 \end{cases}$

If  $f(x)$  is continuous at  $x = 0$  then value of  $4|\alpha^2 + \beta^2|$  is

- (1) 48      (2) 36      (3) 28      (4) 16

**Ans.** (1)

**Sol.**  $f(x)$  is continuous at  $x = 0$

$$\Rightarrow f(0) = \lim_{x \rightarrow 0^-} f(x) = \lim_{x \rightarrow 0^+} f(x) \quad \Rightarrow \quad \alpha = \lim_{x \rightarrow 0} \frac{1-\cos 2x}{x^2} = \lim_{x \rightarrow 0} \frac{\beta \sqrt{1-\cos x}}{x}$$

$$\Rightarrow \alpha = \lim_{x \rightarrow 0^-} \frac{2\sin^2 x}{x^2} = \lim_{x \rightarrow 0} \frac{\sqrt{2} \beta \sin \frac{x}{2}}{x} \Rightarrow \alpha = 2 = \frac{\beta}{\sqrt{2}}$$

$$\Rightarrow \alpha = 2 \text{ & } \beta = 2\sqrt{2} \quad \text{So} \quad 4|\alpha^2 + \beta^2| = 4|4 + 8| = 48$$

8. One points of intersection of curves  $y = 1 + 3x - 2x^2$  and  $y = \frac{1}{x}$  is  $\left(\frac{1}{2}, 2\right)$  and area of region bounded by

both curves is  $\frac{1}{24}(\ell\sqrt{5} + m) - n\ln(1+\sqrt{5})$  then value of  $(\ell + m + n)$  is

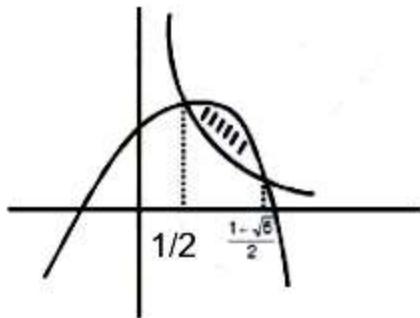
**Ans.** (30)

**Sol.** Solving curves  $y = 1 + 3x - 2x^2$  and  $y = \frac{1}{x}$

$$2x^3 - 3x^2 - x + 1 = 0$$

$$(2x-1)(x^2-x-1) = 0$$

$$x = \frac{1}{2}, \quad x = \frac{1 \pm \sqrt{5}}{2}$$



$$\text{Area} = \int_{\frac{1}{2}}^{\frac{\sqrt{5}+1}{2}} \left( 1 + 3x - 2x^2 - \frac{1}{x} \right) dx$$

$$= \left( x + \frac{3x^2}{2} - \frac{2x^3}{3} - \ln x \right) \Big|_{1/2}^{\sqrt{5}+1/2}$$

$$= \frac{\sqrt{5}+1}{2} + \frac{3}{8}(\sqrt{5}+1)^2 - \frac{1}{12}(\sqrt{5}+1)^3 - \ln\left(\frac{\sqrt{5}+1}{2}\right) - \left( \frac{1}{2} + \frac{3}{8} - \frac{1}{12} - \ln\frac{1}{2} \right)$$

$$\begin{aligned}
 &= \frac{1}{24} \left[ 12(\sqrt{5} + 1) + 9(\sqrt{5} + 1)^2 - 2(\sqrt{5} + 1)^3 - 12 - 9 + 2 \right] - \ell n \left( \frac{\sqrt{5} + 1}{2} \times 2 \right) \\
 &= \frac{1}{24} \left[ 12(\sqrt{5} + 1) + 9(6 + 2\sqrt{5}) - 2(5\sqrt{5} + 1 + 3\sqrt{5}(\sqrt{5} + 1)) - 19 \right] - \ell n(\sqrt{5} + 1) \\
 &= \frac{1}{24} [14\sqrt{5} + 15] - \ell n(\sqrt{5} + 1)
 \end{aligned}$$

Now,  $\ell = 14$ ,  $m = 15$ ,  $n = 1$

$$\text{then } \ell + m + n = 30$$



(3)

**Sol.**      $\bar{z}^2 + |z| = 0 \dots\dots\dots(1)$

$$z^2 + |\bar{z}| = 0 \dots\dots\dots(2)$$

By (1) and (2) as  $|z| \neq |\bar{z}|$

$$\Rightarrow \bar{z}^2 = z^2$$

$$\Rightarrow z = \bar{z} \text{ or } z = -\bar{z}$$

$$\Rightarrow I(z) = 0 \quad \text{or} \quad R(z) = 0$$

Case-I Let  $I(z) = 0 \Rightarrow z$

By (1)  $x^2 \neq |x| \Rightarrow x \neq 0$  only rejected.

Case-II Let  $R(z) = 0 \Rightarrow z = iy$ ,  $y \in R -$

$$\text{By (1)} - y^2 + |y| = 0$$

$$y^2 = |y|$$

$$y = \pm 1,$$

$$z = \pm i$$

$$\Rightarrow \text{sum } \alpha = + i -$$

And product  $\beta = (i) +$

$$\Rightarrow 4(\alpha^2 + \beta^2) = 4$$

$$\Rightarrow 4(\alpha + \beta) = 4$$

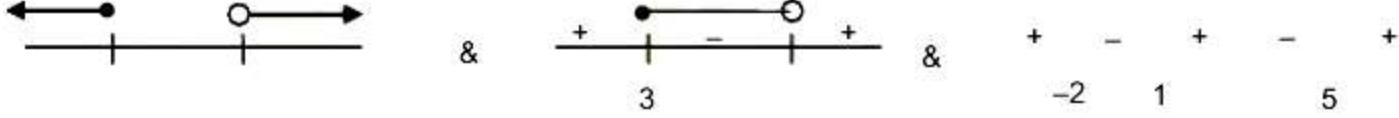
10. If domain of the function  $f(x) = \sin^{-1}\left(\frac{3x-22}{2x-19}\right) + \ln\left(\frac{3x^2+8x+5}{x^2-3x-10}\right)$  is  $(\alpha, \beta]$  then value of  $(3\alpha + 10\beta)$  is

**Ans. (97)**

$$\text{Sol. } -1 \leq \frac{3x-22}{2x-19} \leq 1 \text{ & } \frac{3x^2-8x+5}{x^2-3x-10} > 0$$

$$\frac{3x-22}{2x-19} \geq -1 \quad \text{and} \quad \frac{3x-22}{2x-19} \leq 1 \quad \& \quad \frac{(x-1)(3x-5)}{(x-5)(x+2)} > 0$$

$$\Rightarrow \frac{5x - 41}{2x - 19} \geq 0 \quad \text{and} \quad \frac{x - 3}{2x - 19} \leq 0 \quad \text{and} \quad \frac{(x-1)(3x-5)}{(x-5)(x+2)} > 0$$



$$\Rightarrow x \in \left(5, \frac{41}{5}\right]$$

$$\text{Hence } 3\alpha + 10\beta = 15 + 82 = 97$$

11. The value of  $\lim_{x \rightarrow 4} \frac{(5+x)^{\frac{1}{3}} - (1+2x)^{\frac{1}{3}}}{(5+x)^{\frac{1}{2}} - (1+2x)^{\frac{1}{2}}}$  is

(1)  $2\left(\frac{1}{9^3}\right)$

(2)  $\frac{2}{\frac{1}{9^3}}$

(3)  $\frac{2\left(\frac{1}{9^3}\right)}{9}$

(4)  $\frac{2}{\frac{1}{3^3}}$

**Ans.** (3)

**Sol.**  $\lim_{x \rightarrow 4} \frac{(5+x)^{\frac{1}{3}} - (1+2x)^{\frac{1}{3}}}{(5+x)^{\frac{1}{2}} - (1+2x)^{\frac{1}{2}}} = \frac{9^{\frac{1}{3}} - 9^{\frac{1}{3}}}{9^{\frac{1}{2}} - 9^{\frac{1}{2}}} = \frac{0}{0}$  form

$$\begin{aligned} &= \lim_{x \rightarrow 4} \frac{[(5+x) - (1+2x)]}{\left\{ (5+x)^{\frac{2}{3}} + (5+x)^{\frac{1}{3}}(1+2x)^{\frac{1}{3}} + (1+2x)^{\frac{2}{3}} \right\}} \cdot \frac{(5+x)^{\frac{1}{2}} + (1+2x)^{\frac{1}{2}}}{(5+x) - (1+2x)} \\ &= \lim_{x \rightarrow 4} \frac{(4-x)\left\{ (5+x)^{\frac{1}{2}} + (1+2x)^{\frac{1}{2}} \right\}}{\left\{ (5+x)^{\frac{2}{3}} + (5+x)^{\frac{1}{3}}(1+2x)^{\frac{1}{3}} + (1+2x)^{\frac{2}{3}} \right\}(4-x)} \\ &= \frac{3+3}{\frac{2}{9^3} + \frac{1}{9^3} \cdot \frac{1}{9^3} + \frac{2}{9^3}} = \frac{6}{3 \cdot \frac{2}{9^3}} = \frac{2}{\frac{2}{9^3}} = \frac{2\left(\frac{1}{9^3}\right)}{9} \end{aligned}$$

12. If the function  $f(x) = \begin{cases} \frac{1}{|x|} & |x| \geq 2 \\ ax^2 + 2b & |x| < 2 \end{cases}$  differentiable on  $\mathbb{R}$  then  $48(a+b)$  is equal to

(1) 19

(2) 16

(3) 15

(4) 20

**Ans.** (3)

**Sol.** Clearly  $f(x)$  must be continuous on  $\mathbb{R}$

$$\Rightarrow f(2) = \lim_{x \rightarrow 2} f(x) \quad \& \quad f(-2) = \lim_{x \rightarrow -2} f(x)$$

$$\Rightarrow \frac{1}{2} = 4a + 2b \quad \& \quad \frac{1}{2} = 4a + 2b$$

$$\Rightarrow 8a + 4b = 1 \dots\dots\dots(1)$$

$$\text{Also differentiable so } Lf'(2) = Rf'(2) \quad \& \quad Lf'(-2) = Rf'(-2)$$

$$\Rightarrow 4a = -\frac{1}{4} \quad \& \quad \frac{1}{4} = -4a$$

$$\text{So } a = \frac{-1}{16} \quad \& \quad b = 3/8$$

$$\text{Hence } 48(a+b) = 48\left(-\frac{1}{16} + \frac{3}{8}\right) = -3 + 18 = 15$$

13. Let  $\alpha, \beta \in \mathbb{R}$ . If the mean and the variance of 6 observation,  $-3, 4, 7, -6, \alpha, \beta$  be 2 and 23 respectively, then mean deviation about the mean of the 6 observation is

(1)  $\frac{11}{3}$

(2)  $\frac{16}{3}$

(3)  $\frac{13}{3}$

(4)  $\frac{14}{3}$

**Ans.** (3)

**Sol.** Mean =  $2 = \frac{-3 + 4 + 7 + (-6) + \alpha + \beta}{6}$

$$12 = 2 + \alpha + \beta$$

$$\alpha + \beta = 10 \quad \text{(1)}$$

again variance

$$23 = \frac{9 + 16 + 49 + 36 + \alpha^2 + \beta^2}{6} - (2)^2$$

$$162 = \alpha^2 + \beta^2 + 110$$

$$\alpha^2 + \beta^2 = 52$$

$$\alpha = 6, \beta = 4 \quad \text{or} \quad \alpha = 4, \beta = 6$$

Now mean deviation about mean.

$$= \frac{|-3 - 2| + |4 - 2| + |7 - 2| + |-6 - 2| + |6 - 2| + |4 - 2|}{6}$$

$$= \frac{26}{6} = \frac{13}{3}$$

14. A square is inscribed in the circle  $x^2 + y^2 - 10x - 6y + 30 = 0$  such that one side of the square is parallel to  $y = x + 3$ . If  $(x_i, y_i)$  are the vertices of the square then  $\sum(x_i^2 + y_i^2)$  is equal to

(1) 148

(2) 156

(3) 152

(4) 160

**Ans.** (3)

**Sol.** diagonal of square makes  $45^\circ$  angle with side

Let slope of diagonal = m

$$\text{Then } \tan 45^\circ = \left| \frac{m - 1}{1 + m} \right|$$

So  $m = \text{not defined}$  and  $m = 0$

So diagonals  $x = 5$  and  $y = 3$  are passing through centre

Now solving diagonals with circle we get vertices of square

$$x = 5 \quad \text{and} \quad x^2 + y^2 - 10x - 6y + 30 = 0$$

$$y^2 - 6y + 5 = 0, y = 1, 5$$

two vertices  $(5, 1)$  &  $(5, 5)$

and with  $y = 3$  and

$$x^2 + y^2 - 10x - 6y + 30 = 0$$

$$x^2 - 10x + 21 = 0$$

$$x = 3, 7$$

$$= 25 + 1 + 25 + 25 + 9 + 9 + 49 + 9 = 152$$

15. Let  $f(x) = x^5 + 2e^{x/4} \quad \forall x \in \mathbb{R}$ . Consider a function  $(gof)(x) = x, \forall x \in \mathbb{R}$  then the value of  $g'(2)$  is

(1) 2

(2) 4

(3) 8

(4) 16

**Ans.** (1)

**Sol.**  $g(f(x)) = x$

$$\Rightarrow g'(f(x)) \cdot f'(x) = 1$$

$$\Rightarrow g'(f(x)) = \frac{1}{f'(x)}$$

Now to find  $g'(2)$  let at  $x = a, f(x) = 2$

$$\Rightarrow a^5 + 2e^{a/4} = 2$$

$$\Rightarrow a = 0$$

$$\Rightarrow f(0) = 2$$

$$\text{Hence } g'(f(0)) = \frac{1}{f'(0)}$$

$$\Rightarrow g'(2) = \frac{1}{\left(5x^4 + \frac{1}{2}e^{x/4}\right)_{(x=0)}} = \frac{1}{0 + \frac{1}{2}} = 2$$

16. Let  $f(x) = \frac{2x^2 - 3x + 9}{2x^2 + 3x + 4}$ ,  $x \in \mathbb{R}$ , if maximum and minimum value of  $f(x)$  is  $m$  and  $n$  respectively then  $m+n$  is equal to

(1)  $\frac{60}{23}$

(2)  $\frac{122}{23}$

(3)  $\frac{120}{23}$

(4)  $\frac{5}{23}$

**Ans.** (2)

**Sol.**  $y = \frac{2x^2 - 3x + 9}{2x^2 + 3x + 4}$

$$x^2(2y-2) + x(3y+3) + 4y - 9 = 0$$

as  $x \in \mathbb{R}$  so  $D \geq 0$

$$(3y+3)^2 - 4(2y-2)(4y-9) \geq 0$$

$$9y^2 + 18y + 9 - 8(y-1)(4y-9) \geq 0$$

$$9y^2 + 18y + 9 - 8(4y^2 - 13y + 9) \geq 0$$

$$+ 23y^2 - 122y + 63 \leq 0$$

as  $m \leq y \leq n$

$$\text{by comparing } y^2 - (m+n)y + mn \leq 0$$

$$\text{So } m+n = \frac{122}{23}$$

17.  $\int_0^{\frac{\pi}{4}} \frac{\sin^2 x}{1 + \sin x \cos x} dx =$

(1)  $\frac{\pi}{6\sqrt{3}} - \ln\sqrt{\frac{2}{3}}$

(2)  $\frac{\pi}{6\sqrt{3}} + \ln\sqrt{\frac{2}{3}}$

(3)  $\frac{\pi}{6\sqrt{3}} + \ln\sqrt{\frac{3}{2}}$

(4)  $\frac{\pi}{6\sqrt{2}} + \ln\sqrt{\frac{3}{2}}$

**Ans.** (2)

**Sol.** divide by  $\cos^4 x$  in numerator & denominator

$$\int_0^{\frac{\pi}{4}} \frac{\tan^2 x \sec^2 x dx}{(\tan^2 x + 1 + \tan x)(1 + \tan^2 x)}$$

put  $t = \tan x$

$$dt = \sec^2 x dx$$

$$\begin{aligned}
&= \frac{1}{2} \int_0^1 \frac{2t^2 dt}{(t^2 + t + 1)(t^2 + 1)} = \frac{1}{2} \int_0^1 \frac{t^2 + 1}{(t^2 + 1)(t^2 + t + 1)} + \frac{t^2 - 1}{(t^2 + 1)(t^2 + t + 1)} dt \\
&= \frac{1}{2} \int_0^1 \frac{dt}{t^2 + t + 1} + \frac{1}{2} \int_0^1 \frac{t^2 - 1}{(t^2 + 1)(t^2 + t + 1)} dt = \frac{1}{2} \int_0^1 \frac{dt}{\left(t + \frac{1}{2}\right)^2 + \left(\frac{\sqrt{3}}{2}\right)^2} + \frac{1}{2} \int_0^1 \frac{1 - \frac{1}{t^2}}{\left(t + \frac{1}{t}\right)\left(t + 1 + \frac{1}{t}\right)} dt
\end{aligned}$$

$$\begin{aligned}
&= \left( \frac{1}{2} \frac{2}{\sqrt{3}} \tan^{-1} \left| \frac{t + \frac{1}{2}}{\frac{\sqrt{3}}{2}} \right| \right)_0^1 + I_1 \\
&= \frac{1}{\sqrt{3}} \left( \tan^{-1} \sqrt{3} - \tan^{-1} \frac{1}{\sqrt{3}} \right) + I_1 = \frac{1}{\sqrt{3}} \cdot \frac{\pi}{6} + I_1
\end{aligned}$$

$$\text{Now } I_1 = \frac{1}{2} \int \frac{\left(1 - \frac{1}{t^2}\right) dt}{\left(t + \frac{1}{t}\right)\left(t + 1 + \frac{1}{t}\right)}$$

$$\text{put } t + \frac{1}{t} = u$$

$$\left(1 - \frac{1}{t^2}\right) dt = du$$

$$= \frac{1}{2} \int_{\infty}^2 \frac{du}{u(u+1)}$$

$$= \frac{1}{2} \int_{\infty}^2 \left( \frac{1}{u} - \frac{1}{u+1} \right) du$$

$$= \frac{1}{2} (\ln|u| - \ln|u+1|) \Big|_{\infty}^2$$

$$= \frac{1}{2} \left( \ln \left| \frac{u}{u+1} \right| \right) \Big|_{\infty}^2$$

$$= \frac{1}{2} \left( \ln \left( \frac{2}{3} \right) - 0 \right)$$

$$= \ln \sqrt{\frac{2}{3}}$$

$$\text{So final} = \frac{1}{\sqrt{3}} \left( \frac{\pi}{3} - \frac{\pi}{6} \right) + \ln \sqrt{\frac{2}{3}}$$

$$= \frac{\pi}{6\sqrt{3}} + \ln \sqrt{\frac{2}{3}}$$

**Ans. (1)**

**Sol.** Let  $p = 2r$  and  $q = 2r^2$

Now Let AP be  $a, a + d, a + 2d, \dots$

$$\text{So } a + 2d = 2 \quad \underline{\hspace{2cm}} \quad (1)$$

$$a + 6d = 2r \quad \underline{\hspace{2cm}} \quad (2)$$

$$a + 7d = 2r^2 \quad \underline{\hspace{2cm}} \quad (3)$$

Now from (1) & (2)

$$4d = 2(r-1)$$

$$2d = r - 1 \quad \text{_____} (4)$$

and from (2) & (3)

$$d = 2r(r-1) \quad \dots \quad (5)$$

from (5) & (4)

$$2(2r)(r-1) = r -$$

$$(r - 1)(4r - 1) = 0$$

$$r = \frac{1}{4}, r = 1$$

$$\text{so } r = \frac{1}{4} \text{ as } r \neq 1$$

$$\text{so } p = \frac{1}{2} \text{ & } q = \frac{1}{8} \Rightarrow 64\left(\frac{1}{4} + \frac{1}{64}\right) = 17$$