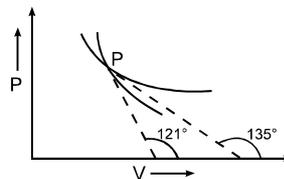


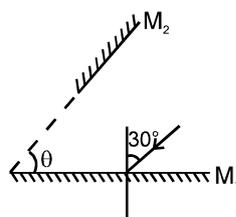
Topics : Kinetic Theory of Gases ,Thermodynamics, Projectile Motion, Friction, Geometrical Optics, String Waves

Type of Questions		M.M., Min.
Single choice Objective ('-1' negative marking) Q.1 to Q.3	(3 marks 3 min.)	[9, 9]
Multiple choice Objective ('-1' negative marking) Q.4	(4 marks 4 min.)	[4, 4]
Subjective Question ('-1' negative marking) Q.5	(4 marks 5 min.)	[4, 5]
Comprehension ('-1' negative marking) Q.6 to Q.8	(3 marks 3 min.)	[9, 9]

1. A gas undergoes an adiabatic process and an isothermal process. The two processes are plotted on a P-V diagram. The resulting curves intersect at a point P. Tangents are drawn to the two curves at P. These make angles of 135° & 121° with the positive V-axis. If $\tan 59^\circ = 5/3$, the gas is likely to be:



- (A) monoatomic
(B) diatomic
(C) triatomic
(D) a mixture of monoatomic & diatomic gases
2. A particle is projected from a point P (2, 0, 0)m with a velocity 10 m/s making an angle 45° with the horizontal. The plane of projectile motion passes through a horizontal line PQ which makes an angle of 37° with positive x-axis, xy plane is horizontal. The coordinates of the point where the particle will strike the line PQ is: (Take $g = 10 \text{ m/s}^2$)
(A) (10, 6, 0)m (B) (8, 6, 0)m (C) (10, 8, 0)m (D) (6, 10, 0)m
3. A ray of light is incident at an \angle of 30° on a plane mirror M_1 . Another plane mirror M_2 is inclined at angle θ to M_1 . What is the value of angle θ so that light reflected from M_2 is parallel to M_1 .



- (A) 60° (B) 75° (C) 67.5° (D) none of these
4. A variable force $F = 10t$ is applied to block B placed on a smooth surface. The coefficient of friction between A & B is 0.5. (t is time in seconds. Initial velocities are zero, A is always on B)



- (A) block A starts sliding on B at $t = 5$ seconds
(B) the heat produced due to friction in first 5 seconds is 312.5J
(C) the heat produced due to friction in first 5 seconds is $(625/8)$ J
(D) acceleration of A at 10 seconds is 5 m/s^2 .

5. A point source S is centered in front of a 70 cm wide plane mirror. A man starts walking from the source along a line parallel to the mirror in a single direction. Maximum distance that can be walked by man without losing sight of the image of the source is _____.

COMPREHENSION

A sinusoidal wave is propagating in negative x-direction in a string stretched along x-axis. A particle of string at $x = 2\text{ m}$ is found at its mean position and it is moving in positive y direction at $t = 1$ sec. If the amplitude of the wave, the wavelength and the angular frequency of the wave are 0.1 meter, $\pi/4$ meter and 4π rad/sec respectively.

6. The equation of the wave is
(A) $y = 0.1 \sin (4\pi(t - 1) + 8(x - 2))$ (B) $y = 0.1 \sin ((t-1) - (x - 2))$
(C) $y = 0.1 \sin (4\pi(t - 1) - 8(x - 2))$ (D) none of these
7. The speed of particle at $x = 2$ m and $t = 1$ sec is
(A) 0.2π m/s (B) 0.6π m/s
(C) 0.4π m/s (D) 0
8. The instantaneous power transfer through $x=2$ m and $t= 1.125$ sec, is
(A) 10 J/s (B) $\frac{4\pi}{3}$ J/s (C) $\frac{2\pi}{3}$ J/s (D) zero

Answers Key

1. (A)
2. (A)
3. (A)
4. (A,D)
5. 70 cm
6. (A)
7. (C)
8. (D)

Hints & Solutions

1. (A)

The slope of isothermal curve at point of intersection

$$\text{is } \frac{dP}{dV} = -\frac{P}{V} = \tan 135^\circ \quad \dots(1)$$

The slope of adiabatic curve at point of intersection is

$$\frac{dP}{dV} = -\frac{\gamma P}{V} = \tan 121^\circ \quad \dots(2)$$

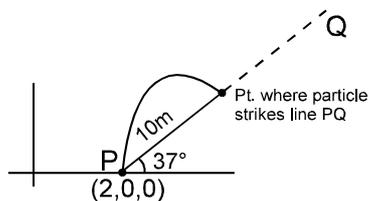
from (1) and (2)

$$\gamma = \tan 59^\circ = 1.66 = 5/3$$

\therefore gas is monoatomic

2. Range = 10 m.

For point where particle strikes line PQ



$$\therefore x \text{ coordinate} = 10 \cos 37^\circ + 2 = 10\text{m}$$

$$y \text{ coordinate} = 10 \sin 37^\circ = 6\text{m}$$

$$z \text{ coordinate} = 0\text{m}$$

4.



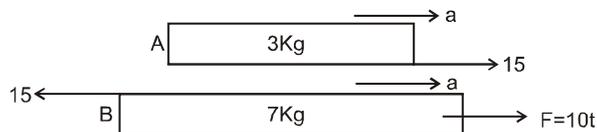
$$f_{\max} = \mu \times 3g$$

$$= 0.5 \times 30 = 15 \text{ N}$$

block A starts sliding when friction force becomes

max. i.e. $f_{\max} = 15$

at that instant (F.B. D.)



both will move with same acceleration

$$\text{So } 15 = 3a \Rightarrow a = 5\text{m/s}^2$$

$$F - 15 = 7a$$

$$10t - 15 = 7 \times 5$$

$$10t = 50$$

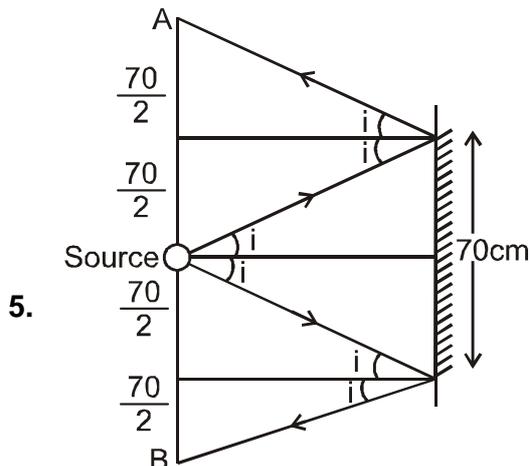
$$\Rightarrow t = 5 \text{ sec}$$

Work done by friction in 5 seconds

$$W = \int F.ds$$

$$= \int 10t.ds \quad (a = \frac{F}{m} = \frac{10t}{10} = t)$$

$$\begin{aligned}
&= \int_0^5 10t \cdot V dt \quad (ds = v dt) \\
&= \int_0^5 10t \cdot \frac{t^2}{2} dt \quad (V = \int a dt = \int t dt = \frac{t^2}{2}) \\
&= \int_0^5 5t^3 dt \\
&= 5 \left[\frac{t^4}{4} \right]_0^5 = \frac{5}{4} [625 - 0] = \frac{625 \times 5}{4}
\end{aligned}$$



From figure if man moves from source to point A

$\left(\frac{70}{2} + \frac{70}{2} = 70 \text{cm} \right)$. Then he can see image

If man moves from source to point B

$\left(\frac{70}{2} + \frac{70}{2} = 70 \text{cm} \right)$. then he can not loose sight of image.

6. The equation of wave moving in negative x-direction, assuming origin of position at $x = 2$ and origin of time (i.e. initial time) at $t = 1$ sec.

$$y = 0.1 \sin (4\pi t + 8x)$$

Shifting the origin of position to left by 2m, that is, to $x = 0$. Also shifting the origin of time backwards by 1 sec, that is to $t = 0$ sec.

$$y = 0.1 \sin [(4\pi t + 8(x - 2))]$$

7. As given the particle at $x = 2$ is at mean position at $t = 1$ sec.

$$\therefore \text{its velocity } v = \omega A = 4\pi \times 0.1 = 0.4 \pi \text{ m/s.}$$

8. Time period of oscillation $T = \frac{2\pi}{\omega} = \frac{2\pi}{4\pi} = \frac{1}{2}$ sec.

Hence at $t = 1.125$ sec, that is, at $\frac{T}{4}$ seconds after

$t = 1$ second, the particle is at rest at extreme position. Hence instantaneous power at $x = 2$ at $t = 1.125$ sec is zero.