

Chapter – 2

Fractions and Decimals

Exercise 2.3

1. Find:

(i) $\frac{1}{4}$ of (a) $\frac{1}{4}$ (b) $\frac{3}{5}$ (c) $\frac{4}{5}$

(ii) $\frac{1}{7}$ of (a) $\frac{2}{9}$ (b) $\frac{6}{5}$ (c) $\frac{3}{10}$

Answer:

(i) We have,

(a) $\frac{1}{4}$ of $\frac{1}{4}$

$$= \frac{1}{4} \times \frac{1}{4}$$

$$= \frac{1}{16}$$

(b) $\frac{1}{4}$ of $\frac{3}{5}$

$$= \frac{1}{4} \times \frac{3}{5}$$

$$= \frac{3}{20}$$

(c) Also,

$$\frac{1}{4} \text{ of } \frac{4}{5}$$

$$= \frac{1}{4} \times \frac{4}{5}$$

$$= 5$$

(ii) We have,

(a) $\frac{1}{7}$ of $\frac{2}{9}$

$$= \frac{1}{7} \times \frac{2}{9}$$

$$= \frac{2}{63}$$

$$(b) \frac{1}{7} \text{ of } \frac{6}{5}$$

$$= \frac{1}{7} \times \frac{6}{5}$$

$$= \frac{6}{35}$$

(c) Also,

$$\frac{1}{7} \text{ of } \frac{3}{10}$$

$$\frac{1}{7} \times \frac{3}{10}$$

$$= \frac{3}{70}$$

2. Multiply and reduce to lowest form (if possible):

$$(i) \frac{2}{3} \times 2\frac{2}{3} \quad (ii) \frac{2}{7} \times \frac{7}{9} \quad (iii) \frac{3}{8} \times \frac{6}{4}$$

$$(iv) \frac{9}{5} \times \frac{3}{5} \quad (v) \frac{1}{3} \times \frac{15}{8} \quad (vi) \frac{11}{2} \times \frac{3}{10}$$

$$(vii) \frac{4}{5} \times \frac{12}{7}$$

Answer:

(i) We have,

$$\frac{2}{3} \times 2\frac{2}{3}$$

$$= \frac{2}{3} \times \frac{8}{3}$$

$$= \frac{16}{9}$$

$$= 1\frac{7}{9}$$

(ii) We have,

$$\frac{2}{7} \times \frac{7}{9}$$

$$= \frac{2}{9}$$

(iii) We have,

$$\frac{3}{8} \times \frac{6}{4}$$
$$= \frac{9}{16}$$

(iv) We have,

$$\frac{9}{5} \text{ or } \frac{3}{5}$$
$$= \frac{27}{25}$$
$$= 1\frac{2}{5}$$

(v) We have,

$$\frac{1}{3} \times \frac{15}{8}$$
$$= \frac{5}{8}$$

(vi) We have,

$$\frac{11}{2} \times \frac{3}{10}$$
$$= \frac{33}{20}$$
$$= 1\frac{13}{20}$$

(vii) We have,

$$\frac{4}{5} \times \frac{12}{7}$$
$$= \frac{48}{35}$$
$$1\frac{13}{35}$$

3. Multiply the following fractions:

(i) $\frac{2}{5} \times 5\frac{1}{4}$ (ii) $6 \times \frac{2}{5} \times \frac{7}{9}$ (iii) $\frac{3}{2} \times 5\frac{1}{3}$

$$\begin{array}{lll} \text{(iv)} \frac{5}{6} \times 2\frac{3}{7} & \text{(v)} 3\frac{2}{5} \times \frac{4}{7} & \text{(vi)} 2\frac{3}{5} \times 3 \\ \text{(vii)} 3\frac{4}{7} \times \frac{3}{5} & & \end{array}$$

Answer:

(i) We have,

$$\begin{aligned} & \frac{2}{5} \times 5\frac{1}{4} \\ &= \frac{2}{5} \times \frac{21}{4} \\ &= \frac{21}{10} \end{aligned}$$

We have an improper fraction and now it can be written in terms of the mixed fraction is as follows:

$$\frac{21}{10} = 2\frac{1}{10}$$

(ii) We have,

$$\begin{aligned} & 6\frac{2}{5} \times \frac{7}{9} \\ &= \frac{32}{5} \times \frac{7}{9} \\ &= \frac{224}{45} \end{aligned}$$

We have an improper fraction and now it can be written in terms of mixed fraction is as follows:

$$\frac{224}{45} = 4\frac{44}{45}$$

$$\begin{aligned} \text{(iii)} \quad & \frac{3}{2} \times 5\frac{1}{3} \\ &= \frac{3}{2} \times \frac{16}{3} \\ &= 8 \end{aligned}$$

In this question, we have a whole number

$$\text{(iv)} \quad \frac{5}{6} \times 2\frac{3}{7}$$

$$= \frac{5}{6} \times \frac{17}{7}$$

$$= \frac{85}{42}$$

We have an improper fraction and now it can be written in terms of mixed fraction is as follows:

$$\frac{85}{42} = 2 \frac{1}{42}$$

$$\text{(v)} \quad 3 \frac{2}{5} \times \frac{4}{7}$$

$$= \frac{17}{5} \times \frac{4}{7}$$

$$= \frac{68}{35}$$

We have an improper fraction and now it can be written in terms of the mixed fraction is as follows:

$$\frac{68}{35} = 1 \frac{33}{35}$$

$$\text{(vi)} \quad 2 \frac{3}{5} \times 3$$

$$= \frac{13}{5} \times 3$$

$$= \frac{39}{5}$$

We have an improper fraction and now it can be written in terms of the mixed fraction is as follows:

$$\frac{39}{5} = 7 \frac{4}{5}$$

$$\text{(vii)} \quad 3 \frac{4}{7} \times \frac{3}{5}$$

$$= \frac{25}{7} \times \frac{3}{5}$$

$$= \frac{15}{7}$$

We have an improper fraction and now it can be written in terms of mixed fraction is as follows:

$$\frac{15}{7} = 2\frac{1}{7}$$

4. Which is greater:

(i) $\frac{2}{7}$ of $\frac{3}{4}$ or $\frac{3}{5}$ of $\frac{5}{8}$

(ii) $\frac{1}{2}$ of $\frac{6}{7}$ or $\frac{2}{3}$ of $\frac{3}{7}$

Answer:

(i) We have,

$$\frac{2}{7} \text{ of } \frac{3}{4}$$

$$= \frac{2}{7} \times \frac{3}{4}$$

$$= \frac{3}{14}$$

Also,

$$\frac{3}{5} \text{ of } \frac{5}{8}$$

$$= \frac{3}{5} \times \frac{5}{8}$$

$$= \frac{3}{8}$$

Now converting the above fractions in to like fraction, we get:

$$\frac{3}{14} = \frac{3 \times 40}{14 \times 40}$$

$$= \frac{12}{56}$$

Also,

$$\frac{3}{8} = \frac{3 \times 7}{8 \times 7}$$

$$= \frac{21}{56}$$

Since,

$$\frac{21}{56} > \frac{12}{56}$$

Therefore,

$$\frac{3}{8} > \frac{3}{14}$$

Hence,

$$\frac{3}{5} \text{ is greater than } \frac{5}{8}$$

(ii) We have,

$$\begin{aligned} & \frac{1}{2} \text{ of } \frac{6}{7} \\ &= \frac{1}{2} \times \frac{6}{7} \\ &= \frac{3}{7} \end{aligned}$$

Also,

$$\begin{aligned} & \frac{2}{3} \text{ of } \frac{3}{7} \\ &= \frac{2}{3} \times \frac{3}{7} \\ &= \frac{2}{7} \end{aligned}$$

Since,

$$\frac{3}{7} > \frac{2}{7}$$

Hence,

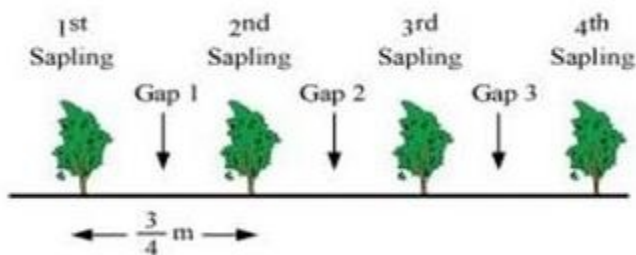
$$\frac{3}{7} \text{ is greater than } \frac{2}{7}.$$

5. Saili plants 4 saplings, in a row, in her garden. The distance between two adjacent saplings is $\frac{3}{4}$ m. Find the distance between the first and the last sapling.

Answer:

It is given in the question that,

$$\text{Length of 1 gap} = \frac{3}{4} \text{ m}$$



Also, from the figure it can be observed that:

Gaps between first and last saplings = 3

Therefore,

Distance between First and last sapling = $3 \times \frac{3}{4}$

$$= \frac{9}{4}$$

$$= 2 \frac{1}{4} \text{ m}$$

6. Lipika reads a book for hours every day. She reads the entire book in 6 days. How many hours in all were required by her to read the book?

Answer:

It is given in the question that,

Number of hours Lipika reads the book = $1 \frac{3}{4}$

$$= \frac{7}{4} \text{ hours}$$

Also,

Total days in which she completes the book = 6

Therefore,

Total number of hours required by her to complete the book = $\frac{7}{4} \times 6$

$$= \frac{21}{2}$$

$$= 10 \frac{1}{2} = 10.5 \text{ hours}$$

7. A car runs 16 km using 1 litre of petrol. How much distance will it cover using $2 \frac{3}{4}$ litres of petrol?

Answer:

It is given in the question that,

Distance travelled by a car in 1 litre of petrol = 16 km

Also,

Total quantity of petrol = $2 \frac{3}{4}$ litre

$$= \frac{11}{4} \text{ litres}$$

Therefore,

Distance travelled by the car in $\frac{11}{4}$ litres of petrol = $\frac{11}{4} \times 16$

$$= 44 \text{ km}$$

Hence,

The car will cover a distance of 44 kms in $2 \frac{3}{4}$ litres of petrol

8.

(A)

(i) Provide the number in the box \square , such that $\frac{2}{3} \times \square = \frac{10}{30}$

(ii) The simplest form of the number obtained in \square Is _____.

Answer:

(i) We have,

$$\frac{2}{3} \times \frac{5}{10} = \frac{10}{30}$$

Hence,

The number in the box will be $\frac{5}{10}$

(ii) We have,

The simplest form of $\frac{5}{10}$:

$$\frac{5}{10} = \frac{1}{2}$$

(B) (i) Provide the number in the box \square , such that $\frac{3}{5} \times \square = \frac{24}{75}$

(ii) The simplest form of the number obtained in \square is _____.

Answer:

(i) We have,

$$\frac{3}{5} \times \frac{8}{15} = \frac{24}{75}$$

Hence,

The number in the box will be $\frac{8}{15}$

(ii) From above,

$\frac{8}{15}$ is itself in a simplest form and it cannot be further simplified