

Chapter – 12

Algebraic Expressions

Exercise 12.2

1. Simplify combining like terms:

(i) $21b - 32 + 7b + 20b$

(ii) $-z^2 + 13z^2 - 5z + 7z^3 - 15z$

(iii) $P - (p - q) - q - (q - p)$

(iv) $3a - 2b - ab - (a - b + ab) + 3ab + b - a$

(v) $5xy^2 - 5x^2 + 3xy^2 - 3x^2 + x^2 - y^2 + 8xy^2 - 3y^2$

(vi) $(3y^2 + 5y - 4) - (-8y - y^2 - 4)$

Answer:

Like terms are terms with the same variables and exponents.

(i) $21b + 7b - 20b - 32$

$$= (21b + 7b - 20b) - 32$$

$$= (8b - 20b) - 32$$

$$= -12b - 32$$

(ii) $7z^3 + 13z^2 - z^2 - 15z - 5z$

$$= 7z^3 + (13z^2 - z^2) - (15z - 5z)$$

$$= 7z^3 + 12z^2 - 10z$$

(iii) $p - (p - q) - q - (q - p)$

$$= p - p + q - q - q + p$$

$$= p - q$$

(iv) $3a - 2b - ab - (a - b + ab) + 3ab + b - a$

$$= 3a - 2b - ab - a + b - ab + 3ab + b - a$$

$$= (3a - a - a) + (-2b + b + b) + (-ab - ab + 3ab) = (3a - 2a) + 9 - 2b + 2b + (-2ab + 3ab) = a + 0 + ab$$

$$= a + ab$$

$$\begin{aligned} \text{(v)} \quad & 5x^2y + 3x^2y + 8xy^2 - 5x^2 + x^2 - 3y^2 - y^2 - 3y^2 \\ &= (5x^2y + 3x^2y) + 8xy^2 + (-5x^2 + x^2) + (-3y^2 - y^2 - 3y^2) \\ &= 8x^2y + 8xy^2 - 4x^2 + (-4y^2 - 3y^2) \\ &= 8x^2y + 8xy^2 - 4x^2 - 7y^2 \end{aligned}$$

$$\begin{aligned} \text{(vi)} \quad & (3y^2 + 5y - 4) - (8y - y^2 - 4) \\ &= 3y^2 + 5y - 4 - 8y + y^2 + 4 \\ &= (3y^2 + y^2) + (5y - 8y) - 4 + 4 \\ &= 4y^2 - 3y \end{aligned}$$

2. Add:

$$\text{(i)} \quad 3mn, -5mn, 8mn - 4mn$$

$$\text{(ii)} \quad t - 8tz, 3tz - z, z - t$$

$$\text{(iii)} \quad -7mn + 5, 12mn + 2, 9mn - 8, -2mn - 3$$

$$\text{(iv)} \quad a + b - 3, b - a + 3, a - b + 3$$

$$\text{(v)} \quad 14x + 10y - 12xy - 13, 18 - 7x - 10y + 8xy, 4xy$$

$$\text{(vi)} \quad 5m - 7n, 3n - 4m + 2, 2m - 3mn - 5$$

$$\text{(vii)} \quad 4x^2y, -3xy^2, -5xy^2, 5x^2y$$

$$\text{(viii)} \quad 3p^2q^2 - 4pq + 5, -10p^2q^2, 15 + 9pq + 7p^2q^2$$

$$\text{(ix)} \quad ab - 4a, 4b - ab, 4a - 4b$$

$$\text{(x)} \quad x^2 - y^2 - 1, y^2 - 1 - x^2, 1 - x^2 - y^2$$

Answer:

$$\text{(i)} \quad 3mn + (-5mn) + 8mn + (-4mn)$$

$$= 3mn - 5mn + 8mn - 4mn$$

$$= 11 mn - 9mn$$

$$= 2mn$$

$$(ii) t - 8tz, 3tz - z, z - t$$

$$= t - 8tz + 3tz - z + z - t$$

$$= t - t - z + z - 8tz + 3tz$$

$$= -5tz$$

$$(iii) -7mn + 5, 12mn + 2, 9mn - 8, -2mn - 3$$

$$= (-7mn + 5) + (12mn + 2) + (9mn - 8) + (-2mn - 3)$$

$$= -7mn + 12mn + 9mn - 2mn + 5 + 2 - 8 - 3$$

$$= -9mn + 21mn + 7 - 11$$

$$= 12mn - 4$$

$$(iv) a + b - 3, b - a + 3, a - b + 3$$

$$= (a + b - 3) + (b - a + 3) + (a - b + 3)$$

$$= a - a + a + b + b - b - 3 + 3 + 3$$

$$= a + b + 3$$

$$(v) 14x + 10y - 12xy - 13 + (18 - 7x - 10y + 8xy) + 4xy$$

$$= 14x + 10y - 12xy - 13 + 18 - 7x - 10y + 8xy + 4xy$$

$$= 14x - 7x + 10y - 10y - 12xy + 8xy + 4xy - 13 + 18$$

$$= 7x + 5$$

$$(vi) (5m - 7n) + (3n - 4m + 2) + (2m - 3mn - 5)$$

$$= 5m - 7n + 3n - 4m + 2 + 2m - 3mn - 5$$

$$= 3m - 4n - 3mn - 3$$

$$(vii) 4x^2y - 3xy^2 - 5xy^2 + 5x^2y$$

$$= 4x^2y - 3xy^2 - 5xy^2 + 5x^2y$$

$$= 4x^2y + 5x^2y - 3xy^2 - 5xy^2$$

$$= 9x^2y - 8xy^2$$

$$(viii) (3p^2q^2 - 4pq + 5) + (-10p^2q^2) + (15 + 9pq + 7p^2q^2)$$

$$= 3p^2q^2 - 4pq + 5 - 10p^2q^2 + 15 + 9pq + 7p^2q^2$$

$$= 3p^2q^2 - 10p^2q^2 + 7p^2q^2 - 4pq + 9pq + 5 + 15$$

$$= 5pq + 20$$

$$(ix) (ab - 4a) + (4b - ab) + (4a - 4b)$$

$$= ab - 4a + 4b - ab + 4a - 4b$$

$$= ab - ab - 4a + 4a + 4b - 4b$$

$$= 0$$

$$(x) (x^2 - y^2 - 1) + (y^2 - 1 - x^2) + (1 - x^2 - y^2)$$

$$= x^2 - y^2 - 1 + y^2 - 1 - x^2 + 1 - x^2 - y^2$$

$$= x^2 - x^2 - x^2 - y^2 + y^2 - y^2 - 1 - 1$$

$$= -x^2 - y^2 - 1$$

3. Subtract:

$$(i) \quad -5y^2 \text{ from } y^2$$

$$(ii) \quad 6xy \text{ from } -12xy$$

$$(iii) \quad (a - b) \text{ from } (a + b)$$

$$(iv) \quad A(b - 5) \text{ from } b(5 - a)$$

$$(v) \quad -m^2 + 5mn \text{ from } 4m^2 - 3mn + 8$$

$$(vi) \quad 5a^2 - 7ab + 5b^2 \text{ from } 3ab - 2a^2 - 2b^2$$

$$(vii) \quad 4pq - 5q^2 - 3p^2 \text{ from } 5p^2 + 3q^2 - pq$$

Answer:

$$(i) \quad y^2 - (-5y^2)$$

$$= y^2 + 5y^2$$

$$= 6y^2$$

(ii) $6xy$ from $-12xy$

$$-12xy - 6xy = -18xy$$

(iii) $(a - b)$ from $(a + b)$

$$(a - b) - (a - b)$$

$$= a + b - a + b$$

$$= a - a + b + b$$

$$= 2b$$

(iv) $a(b - 5)$ from $b(5 - a)$

$$b(5 - a) - a(b - 5)$$

$$= 5b - ab - ab + 5a$$

$$= 5a + 5b - ab - ab$$

$$= 5a + 5b - 2ab$$

(v) $-m^2 + 5mn$ from $4m^2 - 3mn + 8$

$$4m^2 - 3mn + 8 - (-m^2 + 5mn)$$

$$= 4m^2 - 3mn + 8 + m^2 - 5mn$$

$$= 5m^2 - 8mn + 8$$

(vi) $-x^2 + 10x - 5$ from $5x - 10x^2$

$$5x - 10x^2 - (-x^2 + 10x - 5)$$

$$= 5x - 10x^2 + x^2 - 10x + 5$$

$$= x^2 - 10x^2 - 10x + 5x + 5$$

$$= -9x^2 - 5x + 5$$

(vii) $5a^2 - 7ab + 5b^2$ from $3ab - 2a^2 - 2b^2$

$$3ab - 2a^2 - 2b^2 - (5a^2 - 7ab + 5b^2)$$

$$= 3ab - 2a^2 - 2b^2 - 5a^2 + 7ab - 5b^2$$

$$= 2a^2 - 5a^2 + 3ab + 7ab - 2b^2 - 5b^2$$

$$= 7a^2 + 10b - 7b^2$$

$$(viii) \quad 4pq - 5q^2 - 3p^2 \text{ from } 5p^2 + 3q^2 - pq$$

$$5p^2 + 3q^2 - pq - (4pq - 5q^2 - 3p^2)$$

$$= 5p^2 + 3q^2 - pq - 4pq + 5q^2 + 3p^2$$

$$= 5p^2 + 3p^2 + 3q^2 + 5q^2 - pq - 4pq$$

$$= 8p^2 + 8q^2 - 5pq$$

4.

(A) What should be added to $x^2 + xy + y^2$ to obtain $2x^2 + 3xy$?

Answer:

To Find: Expression which is to be added to $x^2 + xy + y^2$ to obtain $2x^2 + 3xy$

We need to subtract $x^2 + xy + y^2$ from $2x^2 + 3xy$ to obtain the required fraction.

$$\text{Therefore, the expression} = 2x^2 + 3xy - x^2 - xy - y^2$$

$$\text{Required Expression} = 2^2 + 3xy - x^2 - xy - y^2$$

$$\text{Required Expression} = x^2 + 2xy - y^2$$

Hence, $x^2 + 2xy - y^2$ is to be added to , $x^2 + 2xy + y^2$ to obtain $2x^2 + 3xy$.

(B) What should be subtracted from $2a+8b+10$ to get $-3a+7b+16$?

Answer:

Let "k" should be subtracted

$$2a + 8b + 10 - k = -3a + 7b + 16$$

Then,

$$k = 2a + 8b + 10 - (-3a + 7b + 16)$$

$$k = 2a + 8b + 10 + 3a - 7b - 16$$

$$k = 5a + b - 6$$

5. What should be taken away from $3x^2 - 4y^2 + 5xy + 20$ to obtain $-x^2 - y^2 + 6xy + 20$?

Answer:

Let k should be taken away from $3x^2 - 4y^2 + 5xy + 20$

$$3x^2 - 4y^2 + 5xy + 20 - k = -x^2 - y^2 + 6xy + 20$$

$$k = 3x^2 - 4y^2 + 5xy + 20 - (-x^2 - y^2 + 6xy + 20)$$

$$k = 3x^2 - 4y^2 + 5xy + 20 + x^2 + y^2 - 6xy - 20$$

$$k = 4x^2 - 3y^2 - xy$$

Hence value of k is $4x^2 - 3y^2 - xy$

6.

(A) From the sum of $3x - y + 11$ and $-y - 11$, subtract $3x - y - 11$.

Answer:

The algebraic equation for above problem will be as

$$[(3x - y + 11) + (-y - 11)] - (3x - y - 11)$$

$$= 3x - y + 11 - y - 11 - 3x + y + 11$$

$$= 3x - 3x - y - y + y + 11 - 11 + 11$$

$$= -y + 11$$

Hence the value is $11 - y$.

(B) From the sum of $4 + 3x$ and $5 - 4x + 2x^2$, subtract the sum of $3x^2 - 5x$ and $-x^2 + 5$.

Answer:

The equation for the problem is

$$\begin{aligned}
& [(4 + 3x) + (5 - 4x + 2x^2) - [(3x^2 - 5x) + (-x^2 + 5)]] \\
&= [4 + 3x + 5 - 4x + 2x^2] - [3x^2 + 5x + x^2 - 5] \\
&= 4 + 3x + 5 - 4x + 2x^2 - 3x^2 + 5x + x^2 - 5 \\
&= 2x^2 - 3x^2 + x^2 + 3x - 4x + 5x + 4 + 5 - 5 \\
&= 4x + 4
\end{aligned}$$