

## Chapter - 8

# Magnetism and Properties of Magnetic Substances

We have studied about magnets in earlier classes. The property of attracting iron, cobalt, nickel is called magnetism and the material that shows this property is called magnet. In this chapter we will study about different physical quantities related to magnetism. The earth also behaves like a magnet, so we will study about elements of its magnetism. Every material shows some magnetic property, so we will classify materials on this basis.

### 8.1 Natural Magnets

In ancient times in Greece, some deposits were found in island magnesia, which showed the property of attracting iron, cobalt and nickel. This material was named magnet after the place, and the property as magnetism. It was magnetite, an ore of iron ( $\text{Fe}_3\text{O}_4$ ). Normally natural magnets are not used because of their irregular shape and weak strength.

### 8.2 Artificial Magnets

Artificial magnets are prepared either by rubbing a ferromagnetic material by a strong magnet, keeping in long contact with pole of a magnet or by keeping in magnetic field of a solenoid. They are of two types (i) permanent (ii) temporary.

**(i) Permanent magnet** - Their magnetism stays for a long time. They are prepared by hard steel, cobalt steel, tungsten or an alloy *ALNICO* (*Al Ni Co*) or other alloys. Their magnetism can't be controlled.

**(ii) Temporary Magnet** - These magnets show the property as long as magnetizing field exists. Their shape and strength can be manipulated. They normally are of soft iron, and used in motor, generator, electric bell and electromagnetic relay.

#### 8.2.1 Properties of Bar Magnet

Normally magnets are used in the form of a bar. They have following basic properties -

**(i) Attraction property** - These magnets attract iron, nickel and cobalt like ferromagnetic materials. The strength is maximum at ends (called Pole) and zero at mid point.

**(ii) Directional Property** - When suspended freely from centre of gravity, the bar magnet, in equilibrium, always stays in N-S direction. The end which stays in north direction is marked as north pole, the end which stays in south direction as south pole.

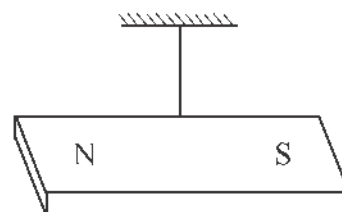


Fig 8.1 Directional property of a bar magnet

**(iii) Existence as dipole** - Magnets always exist as dipole. North pole and south pole are equal in magnitude (strength). Existence of monopole is not possible.

**(iv) Attraction and repulsion** - Same poles repel each other, while opposite poles attract.

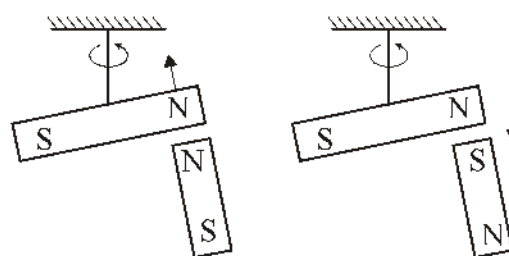


Fig 8.2 Attraction and repulsion

**(v) Equality of pole strength** - The pole strength of both the poles is always the same. As shown in the figure 8.3 (A) and (B). If divided transversely, the two pieces behave like two separate magnets of same pole strength. And if divided longitudinally into two parts, their pole strength will be halved. Here  $m$  is taken as symbol of pole strength.

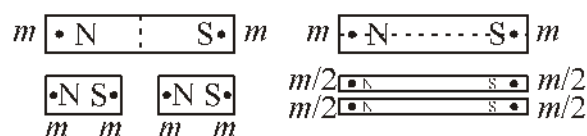


Fig 8.3 Division of pole strength of a magnet

**(vi) Repulsion is a sure test to differentiate between a magnet and an iron bar-** If you have two bars, one is certainly magnet, but the other you don't know. To test, bring one end of the second bar towards a magnet; if it gets attracted - other may be magnet or iron bar. If the second end is brought near the magnet -

- (1) If it is attracted - the other bar is iron bar and
- (2) If it gets repelled - the other bar is a magnet hence repulsion is sure test in this case.

**(vii) Magnetic induction** - When a magnetic material is kept near in contact with a bar magnet it acquires magnetic property. This phenomenon is called magnetic induction. The other pole will be of opposite polarity.

**(viii) Demagnetization** - A magnet will lose its property by heating, beating by a hammer, kept under influence of AC current or by keeping dumped in earth for a long time.

**(ix) Repulsion of some material** - Some materials get repelled by a magnet these materials are called diamagnetic materials, water, gold and silver are some examples. This repulsion is extremely weak and can only be observed by sensitive devices or arrangement.

## 8.2.2 Some Definitions Related to Magnet

**(i) Magnetic Poles and Magnetic Axis** - At the point, very near to the end of a bar magnet magnetism (field) is strongest. These points are called poles. All the field lines (lines of action of magnetic force) pass through these points.

The imaginary line passing through the poles and extending up to infinity is called axis of a bar magnet.

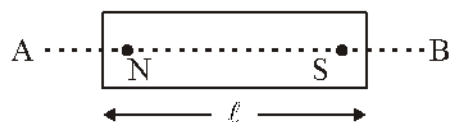


Fig 8.4 Magnetic axis and effective length

**(ii) Effective length of a bar magnet** - The distance between the two poles is called effective length of a bar magnet. It is approximately  $5/6$  of the physical length. (Since poles are situated slightly inside and not exactly at ends). It is a vector quantity  $\vec{l}$  and its direction is from S pole to N pole.

**(iii) Magnetic Meridian** - The imaginary vertical plane passing through the axis of a bar magnet, when it is freely suspended and is in equilibrium is called magnetic meridian. Any other plane which is parallel to the above mentioned will also be magnetic meridian.

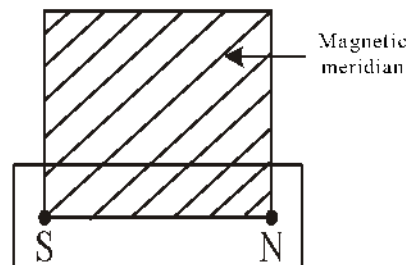


Fig 8.5 Magnetic meridian

**(iv) Pole Strength** - The attraction power of a magnet is expressed by a physical quantity called pole strength its symbol is  $m$  and unit  $A\ m$ .

**(v) Coulomb's Law for the force between magnetic poles** - Just as gravitational force between two masses and electrostatic force between two electric charges, we have inverse square law for magnetism.

The Coulomb force is inversely proportional to the squared distance between the magnetic poles and directly proportional to the product of poles' strengths.

Let two poles of strength  $m_1$  and  $m_2$  are at a distance from each other in air/vacuum. (Situation is imaginary since magnetic monopole does not exist). The attractive or repulsive force between them is

$$F \propto \frac{m_1 m_2}{r^2}$$

$$F = k \frac{m_1 m_2}{r^2}$$

$$F = \frac{\mu_0}{4\pi} \frac{m_1 m_2}{r^2} \quad \dots (8.1) \text{ is given by}$$

here  $k = \frac{\mu_0}{4\pi} = 10^{-7} \text{ Web/Am}$  is a constant

and  $\mu_0$  = magnetic permeability of air/vacuum.

$$F = \frac{\mu_0}{4\pi} = 10^{-7} \text{ N}$$

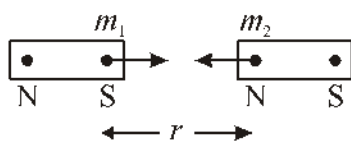


Fig 8.6 Force between magnetic poles

### Definition of unit pole

If  $m_1 = m_2 = 1 \text{ A m}$ ,  $r = 1 \text{ m}$  and

$$F = \frac{\mu_0}{4\pi} = 10^{-7} \text{ N. Then using equation (8.1) we}$$

get  $m_1 = m_2 = 1 \text{ A m}$  (i.e. unit pole)

If two equal poles separated by 1m in air/vacuum experience a force of  $10^{-7} \text{ N}$ , then both poles have unit pole strength.

### 8.3 Magnetic Field Lines (Magnetic Lines of Forces)

If a small magnetic compass needle is moved in a magnetic field, and path of one pole is traced using dots, joining these dots gives curves which are called magnetic field lines. (Earlier it was defined as the locus of a free north pole in a magnetic field).

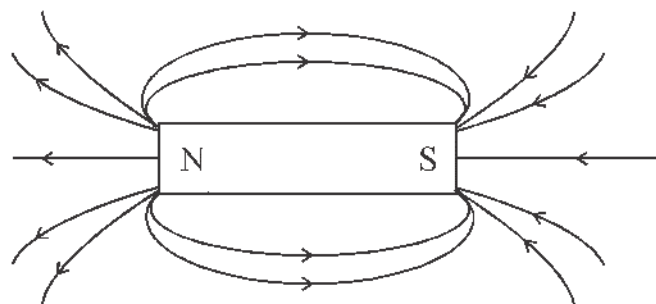


Fig 8.7 Magnetic field lines

Fig 8.7 show the magnetic field lines of a bar magnet. Place a paper or a glass sheet on a bar magnet. Sprinkle some iron filings on the glass sheet. The pattern of the iron filings will give you an idea of the field lines.

### Properties of Field Lines

- They are imaginary and are in the form of closed loops.
- Outside the magnet their direction is from N to S, while inside they are from S to N.
- The tangent drawn at any point on the field line, gives the direction of magnetic field at that point.
- They never intersect each other. If they do, two

tangents can be drawn on the point of intersection which gives two directions of the field, which is not possible.

- The area where field lines are close, the field is strong and vice-versa. The field is strong near the poles.
- The parallel field lines represent uniform magnetic field.

### 8.4 Neutral Point

The earth has its own magnetic field. So when we place a bar magnet on a paper placed on wooden table, there will be super position of two fields (i.e. of earth and bar magnet). The pattern of field lines drawn, show some (one/two) points where the net magnetic field is zero. These points are called null points. At these points, the horizontal component of earth's magnetic field exactly cancels the magnet field of bar magnet i.e.  $B - B_H = 0$ . The location of null points depends on the orientation of the bar magnet.

**(i) When S pole of bar magnet is in Geographical North Direction** - In this position/orientation as shown in fig (8.8A). The field on equator (i.e.  $\perp$  line to axis) is strong near the magnet because both fields are in the same direction. We get null points on axis as  $N_1$  and  $N_2$ .

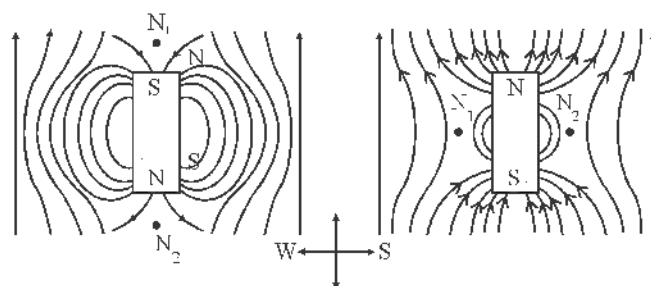


Fig 8.8 Neutral Point (A) When S pole of the magnet is towards geographical north. (B) When N pole of magnet is towards geographical north.

**(ii) When North Pole of Bar Magnet is towards geographical North** - In this case the null points  $N_1$  and  $N_2$  are obtained on equatorial line, as shown in fig 8.8 (B).

**(iii)** If the bar magnet is kept vertical and its north pole is downwards on the paper, the field lines will be as shown in fig 8.9. We get only one null point in south direction. If south pole is kept downwards the position of null point is reversed, i.e. in north.

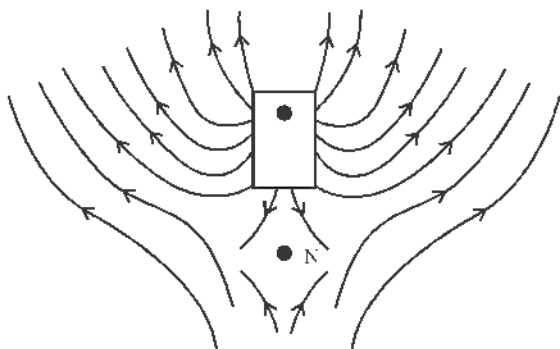


Fig 8.9 : Field lines when magnet is kept vertically

## 8.5 Magnetic Dipole and Magnetic Dipole Moment

### 8.5.1 Magnetic Dipole

In a bar magnet, both north pole and south pole exist. In a current carrying solenoid, one end behaves like north pole and the other as south pole. In a current loop, one face behaves like north pole and other face as south pole. In nut shell magnetism exist as dipole and it is the elementary entity of magnetism. Mono pole is not possible. Even if we go on dividing a magnet into two, each piece has dipole.

### 8.5.2 Magnetic Dipole Moment

It is the physical quantity which gives the strength of a magnet.

We have learnt that a coil having  $N$  turns, area  $A$ , current  $I$ , experiences a torque in external uniform magnetic field  $B$ ;

$$\tau = NIAB \sin \theta \quad \dots (8.2)$$

Comparing it with the torque experienced by an electric dipole in external electrical field  $E$ ,

$$\tau = pE \sin \theta \quad \dots (8.3)$$

We get an equivalent quantity to  $p$  as  $NIA$ , this quantity is similarly named as magnetic dipole moment  $M$ . Just as in electrostatics, we can write where  $m$  is pole strength and is a vector distance between two poles, which is from  $S$  to  $N$ .

$$M = NIA \quad \dots (8.4)$$

the direction of  $\vec{A}$  is  $\perp$  to the plane of current loop.

The unit of  $\vec{M}$  is  $A m^2$ .

It can be defined using relation

$\tau = MB \sin \theta \quad \dots (8.5)$  for a dipole. If  $B = 1$ ,  $\theta = 90^\circ$ , then  $\tau = M$ . Hence the magnetic moment is equal to the torque experienced by a dipole in unit magnetic field, when it is placed perpendicular to the field.

### 8.5.3 Magnetic Moment of a Bar Magnet

$$\text{It is given by } M = m \times \ell \quad \dots (8.6)$$

where  $m$  = pole strength and  $\ell$  is effective length of a bar magnet.

(A) If we bisect a bar magnet of dipole moment  $M$  into two, perpendicular to its length. The dipole moment of each part is

$$M_1 = m \times \frac{\ell}{2} = \frac{m\ell}{2} = \frac{M}{2}$$

(B) If a bar magnet is divided into two, by dividing along its length, again

$$M_2 = \frac{m}{2} \times \ell = \frac{m\ell}{2} = \frac{M}{2}$$

(C) If a bar magnet of length  $2\ell$  and magnetic moment  $M$  is bent into a semi circle of radius  $r$ . Circumference of semi circle  $\pi r = \ell$ . Then  $M_3 = m \times 2r$ ;

$$M_3 = m \times \frac{2\ell}{\pi} = \frac{2M}{\pi}$$

(D) If two bar magnets are kept at an angle  $\theta$  between their axis, the net magnetic moment will be vector sum of individual  $M$ .

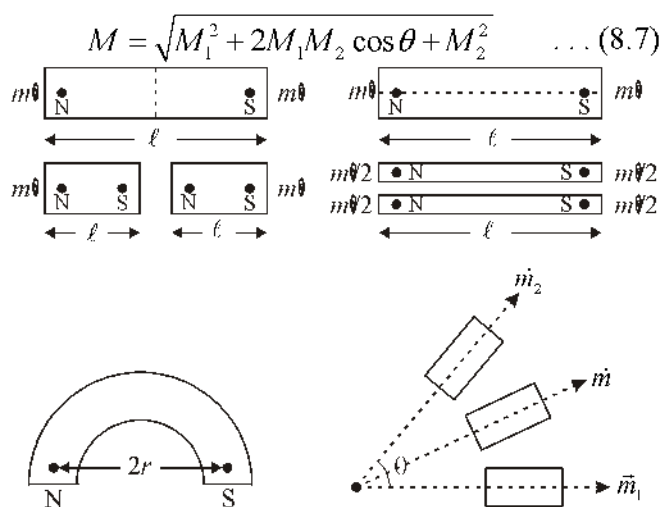


Fig 8.10 Magnetic moment of a bar magnet

### 8.5.2.2 Magnetic Moment of a Revolving Electron

In an atom, electrons revolve round the nucleus, which is equivalent to current loop. Hence every orbit (having one electron) has a magnetic moment  $M = NI A$ . For an revolution ( $N=1$ ), charge =  $e$ , and time  $t=T$  hence

$$I = \frac{e}{T} \text{ but } M = \frac{e}{T} \times \pi r^2 \text{ or } I = \frac{2\pi}{\omega}$$

where  $r$  = radius of orbit,  $v$  = linear velocity of electron and  $\omega$  = angular velocity.

$$\text{So } M = \frac{e}{2\pi / \omega} \times \pi r^2 = \frac{1}{2} e \omega r^2 \quad \dots (8.8)$$

$$\text{and } M = \frac{1}{2} e v r \quad \dots (8.9)$$

since  $v = r\omega$

**Example 8.1 :** Find the magnetic moment of a bar magnet with pole strength 40 Am and effective length 5 cm.

**Solution :**  $M = m \times \ell$

$$m = 40 \text{ Am}, \ell = 5 \text{ cm} = 0.05 \text{ m}$$

$$M = 0.05 \times 40 = 2 \text{ Am}^2$$

**Example 8.2 :** A current carrying coil has magnetic moment  $5 \text{ Am}^2$ . If its radius is halved and the current is doubled, what will be new magnetic moment compared to previous one.

**Solution :**  $M = NI\pi r^2$  The new magnetic moment will be  $M' = NI'\pi r'^2$

$$r' = \frac{r}{2} \quad I' = 2I$$

$$\frac{M'}{M} = \frac{N \times 2I \times (r/2)^2}{N \times I \times r^2} = \frac{1}{2},$$

dividing we get  $M' = \frac{M}{2}$

**Example 8.3 :** Find the magnetic moment of the electron in first orbit of hydrogen atom.

$$(r = 0.53 \text{ \AA}, v = 2.2 \times 10^6 \text{ ms}^{-1}).$$

**Solution :**  $M = \frac{1}{2} e v r$

$$r = 0.53 \text{ \AA}$$

$$r = 0.53 \times 10^{-10} \text{ m}$$

$$v = 2.2 \times 10^6 \text{ m s}^{-1}$$

$$M = \frac{1}{2} \times 1.6 \times 10^{-19} \times 2.2 \times 10^6 \times 0.53 \times 10^{-10}$$

$$M = 0.93 \times 10^{-23} \text{ Am}^2$$

**Note :** It is called Bohr Magneton and is a fundamental constant in physics.

### 8.6 Intensity of Magnetic Field

Earlier it was defined as  $\vec{B}$  (force on unit N pole). In analogy to (force per unit positive charge).

But now we define it using the relation  $\vec{\tau} = \vec{M} \times \vec{B}$  (since  $M$  is the most basic quantity in magnetism and magnetic monopole does not exist).

$B$  is equal to the torque experienced by a magnet of unit magnetic moment placed perpendicular to it.

Its SI unit is  $\text{N/A m}$ , or Tesla.

#### 8.6.1 Magnetic Field at an Axial Point of a Bar Magnet

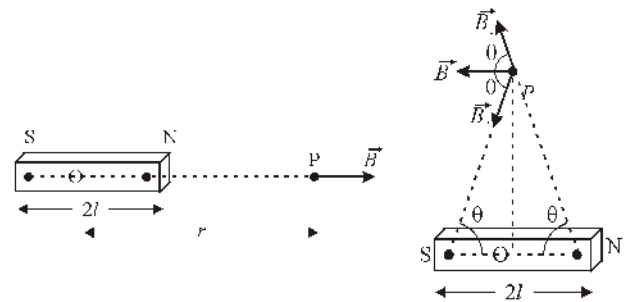


Fig 8.11 : Intensity at an equatorial point

As shown in fig 8.11, pole strength of a bar magnet is  $m$ , its effective length is  $2l$ . The magnetic field at an axial point at a distance  $r$  from the center  $O$ , of the bar magnet is  $\vec{B} = \vec{B}_1 + \vec{B}_2$ , where  $\vec{B}_1$  and  $\vec{B}_2$  are the field due to north and south pole at  $p$ . Using Coulomb's law, and definition of  $B$  we get ; hence

$$B_1 = \frac{\mu_0}{4\pi} \frac{m}{(r-l)^2}$$

$$\text{and } B_2 = \frac{\mu_0}{4\pi} \frac{(m)}{(r+l)^2} \dots (8.9b)$$

By convention, taking pole strength of north pole is (+m) and for that of south pole as (-m).

$$\begin{aligned} \text{We get } B &= \frac{\mu_0}{4\pi} \frac{m}{(r-l)^2} + \frac{\mu_0(-m)}{4\pi(r+l)^2} \\ &= \frac{\mu_0 m}{4\pi} \left[ \frac{1}{(r-l)^2} - \frac{1}{(r+l)^2} \right] \\ &= \frac{\mu_0 m}{4\pi} \times \frac{m4rl}{(r^2 - l^2)^2} \\ B &= \frac{\mu_0}{4\pi} \frac{2Mr}{(r^2 - l^2)^2} [\because M = m \times 2l] \dots (8.10) \end{aligned}$$

For Special Condition of  $l \ll r$  (for a very small magnet) we modify equ. 8.10 by taking common from denominator-

$$B = \frac{\mu_0}{4\pi} \frac{2Mr}{(r^2 - l^2)^2}$$

here  $l^2/r^2$  is a negligible quantity

$$\text{hence } B = \frac{\mu_0}{4\pi} \times \frac{2M}{r^3} \dots (8.11)$$

### 8.6.2 Magnetic Field due to Bar Magnet at its Equatorial Point

As clear from fig 8.11, the magnetic field at P, due to north pole is  $B_1 = \frac{\mu_0}{4\pi} \times \frac{m}{(r^2 + l^2)}$  along line NP and away from N. Similarly field due to south pole is

$$B_2 = \frac{\mu_0}{4\pi} \times \frac{m}{(r^2 + l^2)} \text{ (a long Ps, towards S).}$$

Resolving  $\vec{B}_1$  and  $\vec{B}_2$  into components along axis and equator. We see that the sine components get cancelled being equal and opposite; and only cosine components contribute to  $\vec{B}$  at equator. We get

$$\vec{B} = \vec{B}_1 + \vec{B}_2 \text{ (only cosine components of } \vec{B}_1 \text{ \& } \vec{B}_2 \text{)}$$

$$\therefore B = B_1 \cos \theta + B_2 \cos \theta$$

$$B = 2B_1 \cos \theta \quad [\because B_1 = B_2]$$

$$\therefore B = \frac{\mu_0 \times 2m}{4\pi(r^2 + l^2)} \times \cos \theta$$

$$\text{(but } \cos \theta = \frac{l}{(r^2 + l^2)^{1/2}})$$

$$\therefore B = \frac{\mu_0}{4\pi} \frac{2ml}{(r^2 + l^2)^{3/2}} \dots (8.12a)$$

Again for special condition for a small bar magnet  $l \ll r$ ,  $l^2/r^2$  being negligible, we get

$$B = \frac{\mu_0}{4\pi} \frac{M}{r^3} [\because M = m \times 2l] \dots (8.12b)$$

The direction of  $\vec{B}$  here is opposite to that of  $\vec{M}$ .

We appreciate the similarity to that of the electric field due to an electric dipole at axis and equator

$$\vec{E} = \frac{1}{4\pi \epsilon_0} \frac{2\vec{p}}{r^3} \dots (8.13a)$$

$$\vec{E} = \frac{1}{4\pi \epsilon_0} \frac{\vec{P}}{r^3} \dots (8.13b)$$

here  $M$  is replaced by  $P$  and  $\mu_0$  by  $\frac{1}{\epsilon_0}$ .

### 8.7 The Torque on a Bar Magnet in Uniform External Magnetic Field

As in fig 8.12 a bar magnet of pole strength  $m$  and effective length  $2l$  is placed in external uniform magnetic field  $\vec{B}$ , such that it is parallel to  $\vec{B}$ . The net force on the magnet is  $F = F_N + F_S = mB + (-mB) = 0$ . Also the torque is zero.

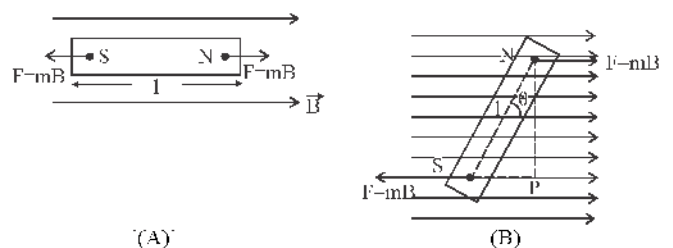


Fig 8.12 (A) and (B) Force on poles of a bar magnet in external magnetic field



If the bar magnet is slightly rotated by an angle  $\theta$  from equilibrium ( $\theta$  is angle between  $\vec{B}$  and  $2\ell$ ), The net force on the magnet is again zero; but the magnet experiences a torque which is  $\tau = mB \times NP$  (distance between forces).

$$\tau = mB \times NP$$

$$\tau = mB \times \ell \sin \theta$$

$$\tau = (m \times \ell) B \sin \theta$$

$$\tau = MB \sin \theta \quad \dots (8.14a)$$

$$(M = m \times \ell)$$

$$\vec{\tau} = \vec{M} \times \vec{B} \quad \dots (8.14b)$$

### Special Conditions

(i) When ( $\theta = 0$ ) magnet being parallel to  $B$

$$\tau = MB \sin 0 = 0$$

(ii) When magnet is perpendicular to  $\vec{B}$ , then ( $\theta = 90^\circ$ ) and  $\tau_{\max} = MB \sin 90 = MB$ . The torque will be maximum.

The potential energy of a bar magnet (magnetic dipole) in external magnetic field.

$U/m$  = work done in rotating the magnet by angle  $\theta$ .

$U_m = \int \tau(\theta) d\theta$  here shows that  $\tau$  is a function of  $\theta$ .

$$U_m = \int \tau(\theta) d\theta$$

$$= \int MB \sin \theta d\theta = -MB \cos \theta$$

$$U_M = -\vec{M} \cdot \vec{B} \quad \dots (8.15)$$

for position  $\theta = 0^\circ$ ;  $(U_M)_{\min} = -MB$  (most stable condition for (ii)  $\theta = \pi$ ,  $(U_M)_{\max} = MB$ ) (most unstable)

If we rotate the magnet by an angle to  $\theta$ . then the definite integral will give you -

$$W = \int_0^\theta MB \sin \theta d\theta$$

$$W = MB [-\cos \theta]_0^\theta$$

$$= MB(\cos 0 - \cos \theta)$$

$$W = MB(1 - \cos \theta) \quad \dots (8.16)$$

**Example 8.4 :** Find the torque on a bar magnet of pole strength 25 Am and effective length 10 cm, which is at an angle  $\theta = 30^\circ$  from  $B_H$  (earth magnetic field)

$$(B_H = 0.4 \times 10^{-4} \text{ T}).$$

**Solution :**  $\tau = MB_H \sin \theta$

$$m = 25 \text{ Am}, \ell = 0.1 \text{ m}, \theta = 30^\circ$$

$$\tau = m\ell B_H \sin \theta$$

$$= 25 \times 0.1 \times 0.4 \times 10^{-4} \times 0.5$$

$$= 0.5 \times 10^{-4} \text{ N m}$$

**Example 8.5 :** A magnet of magnetic moment 5  $\text{Am}^2$  is placed in magnetic field 0.2 T. Find the work done in rotating it, from parallel to antiparallel position. Also find the potential energy at the two positions.

**Solution :** The work done in rotating the magnet is

$$W = MB(\cos \theta_1 - \cos \theta_2)$$

$$W = 5 \times 0.2(\cos 0 - \cos 180)$$

$$= 1.0 (1 + 1) = 2 \text{ J}$$

Similarly the energy in position 1 i.e.  $\theta = 0$

$$U_1 = -MB \cos \theta_1 = -MB \cos 0 = -MB$$

$$= -5 \times 0.2 = -1 \text{ J}$$

$$U_2 = -MB \cos 180 = MB = 5 \times 0.2 = 1 \text{ J}$$

## 8.8 Earth's Magnetism

The earth behaves like a bar magnet, it has its own magnetic field. It is called geomagnetism. The following facts confirm it -

- (i) A bar magnet freely suspended from its C G always stays in NS direction in equilibrium.
- (ii) An iron piece kept buried in earth for a long time acquires magnetism.
- (iii) We get null points while plotting field lines of a bar magnet.

The magnetic field on the surface varies from place to place and is of the order  $10^{-5} \text{ T}$ .

### 8.8.1 Cause of Earth's Magnetism

The origin of geomagnetism is not well understood. There are certain explanations, the simplest one of existence of a giant magnet at the center of earth was rejected due to hot conditions inside earth where such magnet can't exist. The other one is "dynamo effect", given by Elsasser is most accepted. According to it certain metals like iron and nickel exist in the outer core of earth in molten and ionic form. They rotate with earth and causes convection current which in turn produces magnetic field.

Magnetic field lines of earth are mapped, and their simplest version resembles to the field lines of an imaginary bar magnet placed inside the earth such that its axis makes an angle  $11.3^\circ$  to earth's axis and its north pole is towards south pole and south pole towards north pole of the earth. The location of these pole on earth surface are at latitude  $79.74^\circ N$  and longitude  $71.8^\circ W$  a place in north Canada. And  $79.74^\circ S$  and  $108.22^\circ E$  which is in Antarctica.

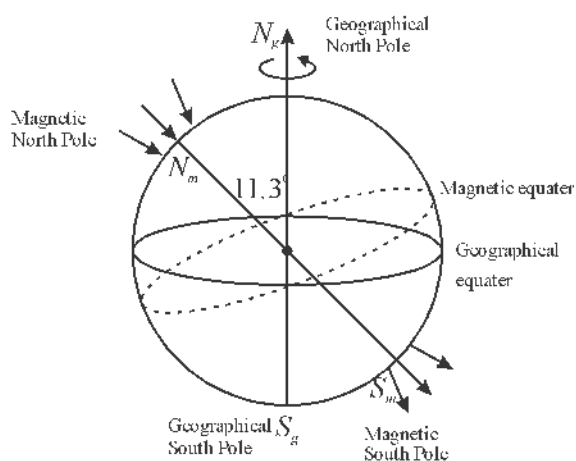


Fig 8.13 : Geomagnetism

### 8.8.2 Elements of Earth's Magnetism

To know about earth's magnetic field at certain place, need to know about three physical quantities about it. These are called elements of earth's magnetism. They are -

- (1) Angle of declination (or simply declination).
- (2) Dip angle.
- (3) Intensity of earth's magnetism (or simply

horizontal component of it). First two give the direction of earth's magnetic field in horizontal and vertical plane respectively, and third gives its magnitude (or magnitude in horizontal direction).

#### (i) Angle of declination

Magnetic meridian is a vertical plane passing through the axis of a freely suspended bar magnet from its CG and is in equilibrium.

Geographical meridian is a vertical plane passing through the axis of rotation of earth. It also contains longitude circle.

The angle of declination is the acute angle between magnetic meridian and geographical meridian. It is different at different places of earth. At Delhi it is  $0^\circ 41' E$  and at Mumbai it is  $0^\circ 58' W$ . These small values show that at these places, the direction shown by a compass needle is true north-south.

#### (ii) Dip angle or angle of dip

If we take a compass needle, which is free to rotate about a horizontal axis, in a vertical plane, then in equilibrium, the angle between its axis with horizontal is called angle of dip. It gives the direction of earth's magnetic field in a vertical plane. Again the dip angle varies from place to place on the surface of the earth. It is  $0^\circ$  at the equator and  $90^\circ$  at the poles.

#### (iii) Horizontal component of earth's magnetic field

At a place other than the equator or pole, the direction of magnetic field makes a certain angle with the horizontal. We can resolve this magnetic field  $B$  into two components, as  $B_v$  and  $B_H$ , i.e. vertical component and horizontal component.

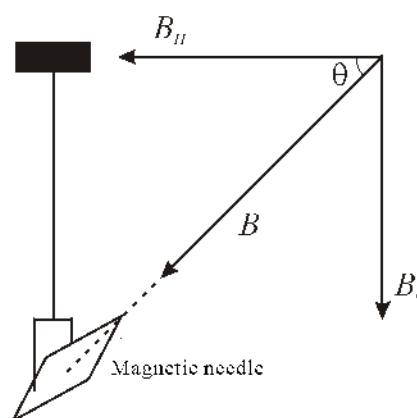


Fig 8.16 Components of earth's magnetic field



$$B_v = B \sin \theta \quad \dots (8.17)$$

$$B_H = B \cos \theta \quad \dots (8.18)$$

Such that  $\vec{B} = \vec{B}_H + \vec{B}_v$

$$B = \sqrt{B_H^2 + B_v^2 + 2B_H B_v \cos 90^\circ}$$

$$B = \sqrt{B_H^2 + B_v^2}$$

$$\tan \theta = \frac{B_v}{B_H}$$

$$B_v = B_H \tan \theta \quad \dots (8.19)$$

**Example 8.6 :** At certain point on earth surface dip angle is  $60^\circ$  and horizontal component of earth's magnetic field is 0.25 G. Find vertical component of earth's magnetic field at this place. Also find the resultant magnetic field at that point.

**Solution :**  $B_v = B_H \tan \theta$

$$B_v = 0.25 \tan 60^\circ$$

$$= 0.25 \times \sqrt{3} = 0.25 \times 1.732 = 0.433 \text{ G}$$

$$B_H = B \cos \theta$$

$$B = \frac{B_H}{\cos \theta} = \frac{0.25}{\cos 60} = \frac{0.25}{0.5}$$

$$B = 0.50 \text{ G}$$

## 8.9 Magnetism and Gauss's Law

According Gauss's law in electrostatics i.e for a closed surface integral of electric field is proportional to the algebraic sum of charges enclosed by the surface.

If a surface encloses electric dipole. The incoming electric flux is equal to outgoing electric flux. Exactly in the

same way for magnetic field  $\phi_B = \oint_S \vec{B} \cdot d\vec{S}$  because magnet always exist as dipole. The incoming magnetic flux through a closed surface is exactly equal to the outgoing flux, and net flux = 0. Hence Gauss's law for magnetism is

$$\phi_B = \oint_S \vec{B} \cdot d\vec{S} = 0 \quad \dots (8.20)$$

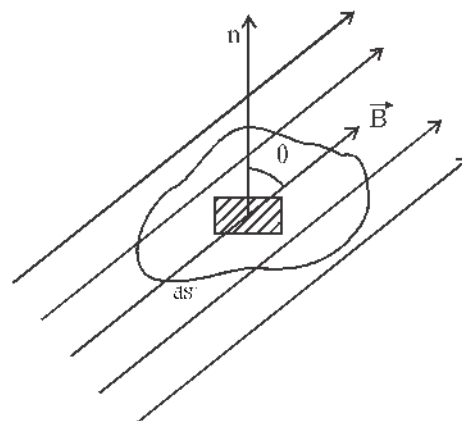


Fig 8.17: Magnetic flux

## 8.10 Behaviour of Substances/Materials in External Magnetic Field

Faraday found that all materials are affected by magnetic field or react to external magnetic field. However they interact with the field differently.

To investigate the behaviour of different materials following experimental set up is suggested -

A current carrying solenoid produces magnetic field, strong inside and weak near its ends. A test tube with sample to be tested is attached to a very sensitive spring balance near the end, as shown in fig 8.18.

When a current is set in the solenoid -

- (i) Some materials like, iron, nickel and cobalt are strongly pulled inside the solenoid, these materials move from weak field to strong field.
- (ii) Some other materials like aluminium,  $\text{CuCl}_2$  etc are weakly attracted inside, i.e. with very weak force.
- (iii) Majority of the materials like  $\text{Zn}$ ,  $\text{B}_2$ , gold etc are weakly repelled out in above experiment i.e they go from strong magnetic field to weak magnetic field.

There are many more types of materials, which you will know in chemistry or in higher classes. Here we restrict ourselves to only three types mentioned above.

- (i) The first type strongly attracted by magnetic field are called Ferromagnetic materials.
- (ii) The second type which are very weakly attracted by magnetic field are called paramagnetic materials.
- (iii) The third type which is very weakly repelled by magnetic field is called diamagnetic material.

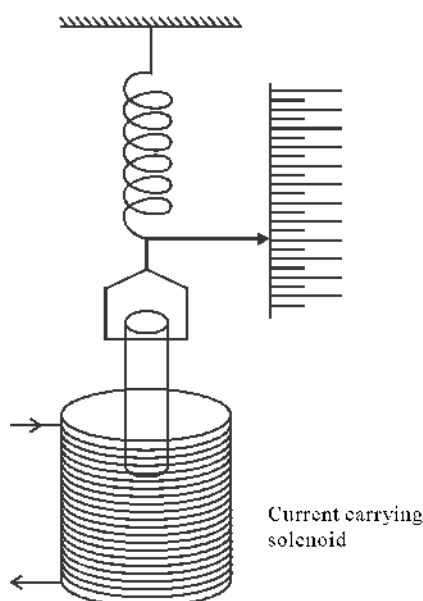


Fig 8.18 Behaviour of materials in a solenoid

## 8.11 Important Physical Quantities Related to Magnetism

### 8.11.1 Intensity of magnetisation $I$

We know that the circulating electron has a magnetic moment; when material is not magnetized, the magnetic dipole sum up to zero. When an external magnetic field is applied the magnetic moments are aligned in a particular direction, and the material gets a net non-zero dipole moment. The net dipole moment per unit volume is defined as magnetization or intensity of magnetisation. Its symbol is  $I$ , and its unit is  $\text{Am}^{-1}$ . It is a vector quantity. Its dimensional formula is  $[\text{M}^1\text{L}^{-1}\text{T}^0\text{A}^1]$ .

### 8.11.2 Magnetizing Field $H$

The magnetic field produced only by electric current (without any contribution of medium) in solenoid,

it is  $nI$  or  $H = \frac{B_0}{\mu_0}$ . It is also called magnetic

intensity. It is the external field that induce magnetic property in material. Its unit is also  $\text{Am}^{-1}$ .

### 8.11.3 Magnetic Susceptibility

When a material is placed in external magnetizing field  $H$ , the material gets magnetized. For small magnetizing field, the  $I$  acquired by the material is proportional to  $H$ , i.e.  $I \propto H$  or  $I = \chi_m H$  here  $\chi_m$  is a constant for a particular material called the magnetic susceptibility of that material. It is defined as, if  $H = 1$ , then  $\chi_m = I$  in words we say the magnetization  $I$  acquired

by the material in unit magnetizing field is equal to its magnetic susceptibility.

### 8.11.4 Magnetic permeability $\mu$

It is a measure of ability of the medium to allow magnetic field to set in the medium.  $\mu_0$  is magnetic permeability of vacuum/air.  $\mu$  is magnetic permeability of medium. And  $\mu_r = \frac{\mu}{\mu_0}$  is relative magnetic permeability of the medium.

## 8.12 Relation between different Magnetic Quantities

Imagine a core of a material is placed inside the solenoid. The net magnetic field produced by the system is

$$B = B_0 + B_1 \quad \dots (8.25)$$

$B_0$  is contribution of current  $B_1$  is contribution of material of core.

here  $B_1 \propto I$

$$\Rightarrow B_1 = \mu_0 I$$

$$\text{again } B = \mu_0 H + \mu_0 I$$

Substituting in equation 8.25

$$B = \mu_0 (H + I) \quad \dots (8.26)$$

$$B = \mu_0 (H + \chi_m H) \quad [\because I = \chi_m H]$$

$$\frac{B}{H} = \mu_0 (1 + \chi_m)$$

$$\mu = \mu_0 (1 + \chi_m) \quad \because \frac{\mu}{\mu_0} = \mu_r$$

$$\mu_r = (1 + \chi_m) \quad \dots (8.27)$$

$$\text{Or } \frac{B}{\mu_0} - I = H \quad \dots (8.28)$$

**Example 8.7 :** The paramagnetic material chromium has magnetic susceptibility as  $2.7 \times 10^{-4}$ . Find its magnetic permeability and relative magnetic permeability.

**Solution :**  $\mu = \mu_0 (1 + \chi_m)$

$$\chi_m = 2.7 \times 10^{-4}$$

$$\mu = 4\pi \times 10^{-7} (1 + 2.7 \times 10^{-4})$$

$$\mu = 12.56 \times 1.00027 \times 10^{-7}$$

$$\mu = 12.5634 \times 10^{-7} \text{ H/m}$$

Relative permeability

$$\mu_r = 1 + \chi_m$$

$$= 1 + 2.7 \times 10^{-4} = 1.00027$$

**Example 8.8 :** Paramagnetic material Aluminium has magnetic susceptibility  $2.3 \times 10^{-5}$ . It is placed in a magnetizing field  $4 \times 10^5 \text{ A/m}$ . Find the magnetization of the material.

**Solution :**  $I = \chi_m H$

$$\chi_m = 2.3 \times 10^{-5} \text{ and } H = 4 \times 10^5 \text{ A/m}$$

$$I = 2.3 \times 10^{-5} \times 4 \times 10^5 = 9.2 \text{ A/m}$$

**Example 8.9 :** An iron wire of length  $l = 1 \text{ m}$  and cross section  $1 \text{ mm}^2$  is placed inside a solenoid, which produced a magnetizing field  $4 \times 10^3 \text{ A/m}$ . Find the magnetic moment of the wire. ( $16\pi \times 10^{-5} \text{ H/m}$ )

**Solution :**  $\chi_m = \frac{I}{H} = \frac{M}{HV}$

$$M = \chi_m HV$$

$$l = 1 \text{ m},$$

$$A = 1 \text{ mm}^2 = 10^{-6} \text{ m}^2$$

$$H = 4 \times 10^3 \text{ A/m}, \mu = 16\pi \times 10^{-5} \text{ H/m}$$

$$V = A l = 10^{-6} \times 1 = 10^{-6} \text{ m}^3$$

$$\chi_m = \frac{\mu}{\mu_0} - 1 = \frac{16\pi \times 10^{-5}}{4\pi \times 10^{-7}} - 1 = 400 - 1 = 399$$

$$M = \chi_m HV$$

$$= 399 \times 4 \times 10^3 \times 10^{-6} = 1.596 \text{ A m}^2$$

**Example 8.10 :** A rod of cross section  $0.40 \text{ cm}^2$  is placed in magnetizing field  $4000 \text{ A/m}$ . If the magnetic flux passing the rod is  $5 \times 10^{-5} \text{ Wb}$ , then find magnetic induction, magnetic susceptibility and magnetization of the material of rod.

**Solution :**  $B = \frac{\phi_B}{A}$

given  $\phi_B = 5 \times 10^{-5} \text{ Wb}$ ,

$$A = 4 \times 10^{-5} \text{ m}^2, H = 4000 \text{ A/m}$$

$$B = \frac{5 \times 10^{-5}}{4 \times 10^{-5}} = 1.25 \text{ Wb/m}^2$$

Magnetic permeability

$$\mu = \frac{B}{H} = \frac{1.25}{4000} = 0.3125 \times 10^{-3}$$

$$= 3.125 \times 10^{-4} \text{ H/m}$$

Magnetic susceptibility

$$\chi_m = \mu_r - 1 = \frac{\mu}{\mu_0} - 1 = \frac{3.125 \times 10^{-4}}{4 \times 3.14 \times 10^{-7}} - 1$$

$$\chi_m = 248.8 - 1 = 247.8$$

$$I = \chi_m H = 247.8 \times 4000 = 9.90 \times 10^5 \text{ A/m given}$$

**Example 8.11 :** An iron rod of dimensions  $5 \text{ cm} \times 1 \text{ cm} \times 0.5 \text{ cm}$  is placed in magnetizing field  $10^4 \text{ A/m}$ . If a magnetic moment of  $10 \text{ A/m}^2$  is induced in it. Find magnetic induction.

**Solution :**  $B = \mu_0 \left( \frac{M}{V} + H \right)$

$$M = 10 \text{ A/m}^2,$$

$$V = 5 \times 1 \times 0.5 \times 10^{-6} = 2.5 \times 10^{-6} \text{ m}^3$$

$$H = 10^4 \text{ A/m}$$

$$B = 4\pi \times 10^{-7} \left( \frac{10}{2.5 \times 10^{-6}} + 10^4 \right)$$

$$= 12.56 \times 10^{-7} (4 \times 10^6 + 10^4) = 5.036 \text{ Wb/m}^2$$

### 8.13 Classification of magnetic materials

According to the behaviour of materials in external magnetic field, the materials are of mainly three types - (i) Diamagnetic (ii) Paramagnetic (iii) Ferromagnetic

#### 8.13.1 Diamagnetic Substances

If placed in non uniform external magnetic field, the materials moves from strong field to weak field, or

they outstead by the field. Actually they aquire a small, net non-zero magnetization opposite to the applied field. These materials are called diamagnetic and the property, diamagnetism. examples- Cu, Zn, Sb, Bi, Hg, H<sub>2</sub>, N<sub>2</sub>, Au, Ag, air water diamond etc.

### Explanation of Diamagnetism

Such materials have pairedelectron in their atoms, which revole in opposite direction. In the absence external magnetic field, the magnetic moment of those electron get cancelled being equal and opposite. In the presence of external magnetic field, the magnetic force on moving electron is opposite in both pairing electrons, on one electron, it is towards the nucleus, increasing its velocity, hence increasing magnetic moment;  $m = I/2evr$ . One other it is away from nucleus, thus decreasing  $v$  and magnetic moment.

The magnetic moment in the direction of applied field get decreased, and that which is opposite, get increased. Hence the net magnetization induced in the material is opposite to the applied field.

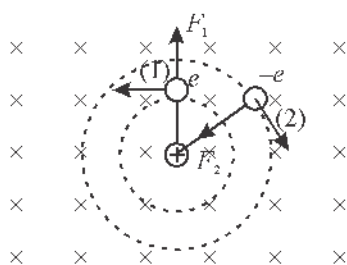


Fig 8.19 Explanation of diamagnetism

Diamagnetism is present in all substances in some it is not observed due to other dominet properties present. Super conductors are ideal diamagnetic substances. For them  $\chi_m = -1$  ;  $\mu_0 = 0$  this effect is called Meisner effect. Magnetic field lines of external field are completly expelled by them. Aliquid diamagnetic substance placed in watch glass over magentic poles, behaves as shown in the figure 8.20.

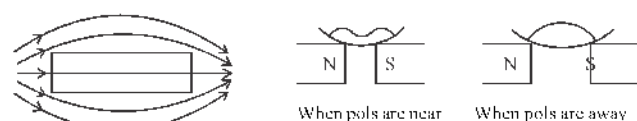


Fig 8.20 : Behaviour of diamagnetic materials

### 8.13.2 Paramagnetic Substances

These substances, when placed in external

magnetic field move slightly from weak field to strong field or they are slightly, attracted by manetic field. We say that they aquire small net magnetic moment in the direction of applied field. These substances are called paramagnetic substances. Example - Na, Ca, Al, CuCl<sub>2</sub> etc.

### Explanation of Paramagnetism-

This type of materials have unpaired electron in their atom. So every atom is a magnetic moment. The net magnetic moment, in the absence of external field is zero because of random orientations due to thermal agitation.

When external field is applied, the torque acting on them, align some of these atomic magnetic dipoles in the direction of applied field. All magnetic dipoles do not get aligned due to thermal effect. Hence the material gets some net non-zero magnetic moment in the direction of applied field.

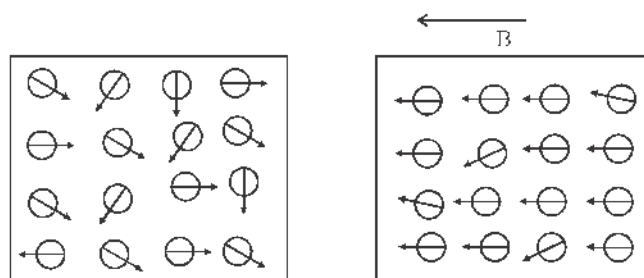


Fig 8.21 : Explanation of paramagnetism

Such materials allow. Some of the field lines of external field to pass through them. IF placed in watch glass over the poles of a magnet, shows the behaviour as shown in fig 8.22.

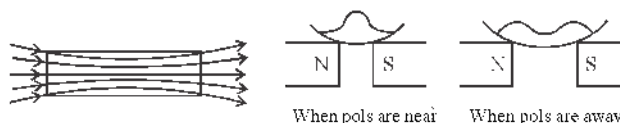


Fig 8.22 : Behaviour of paramagnetic materials

### Temperature Dependance

Practically the magnetic intensity of a paramagnetic substance is proportional to the imposed magnetic field and inversly proportional to the absolute temperature

$$I \propto \frac{B_0}{T}$$

$$\text{or } I = C \frac{B_0}{T} \quad \dots (8.29)$$

here C = Curie Constant

But  $B_0 = \mu_0 H$

$$I = C \frac{\mu_0 H}{T}$$

or  $\frac{I}{H} = C \frac{\mu_0}{T}$

which gives  $\chi_m = \frac{C \mu_0}{T} \dots (8.30)$

called curie law.

### 8.13.3 Ferromagnetic Substances

When placed in non uniform magnetic field, these materials rapidly move towards strong field or they are strongly attracted by a magnetic field. Also they get magnetized in the direction of applied magnetic field.

Example - Fe, Co, Ni,  $\text{Fe}_2\text{O}_3$ , gadolinium and magnetite ( $\text{Fe}_3\text{O}_4$ ).

### Explanation of Ferromagnetism

As in paramagnetism, the ferromagnetic materials also have permanent dipole moment (of a group of atoms, oriented in same direction). The difference is of intensity. The orientation of these groups of atom is random, which make for whole sample.

Due to complex interaction between the atoms, one dipole, compels the other, to orient in the same direction. In this process, small colony of dipoles having same orientation is formed. This colony is called "domain". Whole sample is divided into domains having different orientations, making for whole sample. Size of one domain is of the order of few mm and it contains atoms of the order of  $10^{11}$ .

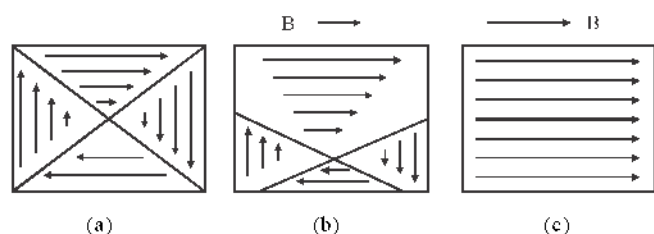


Fig 8.23 : Ferromagnetic materials

When a sample of ferromagnetic material is kept in an external magnetic field; if the applied field is weak, then the area or size of the domain having same orientation as that of applied field, increases and vice-versa. If the external magnetic field is removed; the

phenomenon is reversed due to thermal effect. Hence the process is reversible.

If the applied magnetic field is strong. The whole domain rotates in the direction of applied field. The first to rotate is that which makes minimum angle with applied field. If kept in the field for a long time, the whole sample becomes one domain.

If the external field is removed, the sample does not return to original state, but some residual magnetism remains.

### 8.14 Curie Law and Curie Temperature

Pierre Curie studied the effect of temperature on magnetic materials and found that the magnetic susceptibility of diamagnetic materials does not depend on temperature, whereas the magnetic susceptibility of paramagnetic substance/material is inversely proportional to its absolute temperature i.e.

$$\chi_m \propto \frac{1}{T} \text{ Or } \chi_m = \frac{C}{T}$$

where C = Curie constant

T = Absolute Temperature of the material

Temperature dependence of a ferromagnetic material obeys Curie - Weiss law. According to this law the magnetic susceptibility of a ferromagnetic material is given

$$\text{by } \chi_m = \frac{C}{T - T_c} \dots (8.31)$$

where C = Curie constant; T is the temperature of the material and  $T_c$  is Curie temperature for that material. Below  $T_c$  the material behaves like a ferromagnetic material and above  $T_c$  the material behaves like a paramagnetic material. Above  $T_c$  all materials are paramagnetic.  $T_c$  is different for different materials. The Curie temperature for some materials are given as -

Materials	Curie temperature
Iron	$T_c = 1043 \text{ K}$
Cobalt	$T_c = 1394 \text{ K}$
Nickel	$T_c = 631 \text{ K}$
Gadolinium	$T_c = 317 \text{ K}$

**Example 8.12 :** The Curie temperature for some material is 300 K. If its magnetic susceptibility at 420 K is 0.4, then find Curie constant.

**Solution :** magnetic susceptibility  $\chi = \frac{C}{T - T_c}$

$$\chi = 0.4, \quad T_c = 300 \text{ K} \quad \text{तथा} \quad T = 420 \text{ K}$$

$$C = \chi(T - T_c)$$

$$= 0.4 (420 - 300) = 0.4 \times 120 = 48 \text{ K}$$

### 8.15 Magnetic Hysteresis Curve (B - H Curve)

When a ferromagnetic material is placed in magnetic field  $H$  (magnetizing field), magnetization of material takes place which produces magnetic field  $B$ . The curve showing of  $B$  and  $H$  is known as Hysteresis curve or B-H curve.

To find B-H curve of a ferromagnetic material we take its demagnetized form in the shape of a rod. We place this rod in a current carrying solenoid. The current in the solenoid produces  $H$  ( $H = ni$ ). This  $H$  magnetises the material which in turn produces  $B$ . We can change  $H$  by changing current, and we have a device to measure  $B$ .

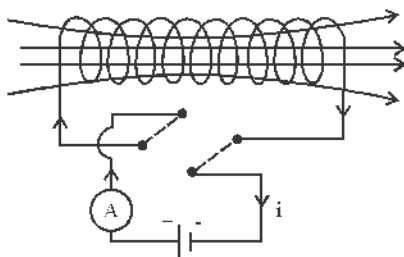


Fig 8.24 : Magnetic material inside a solenoid

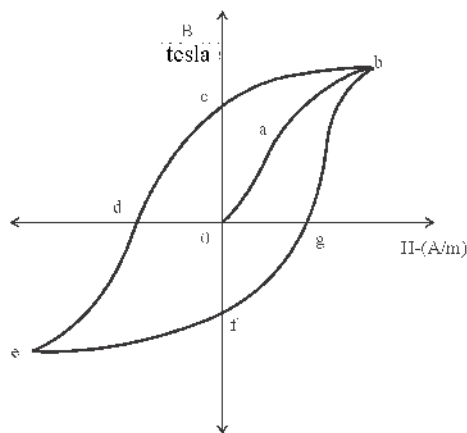


Fig 8.25 : Hysteresis loop

We start our experiment with  $i=0, H=0, B$  will be zero i.e the origin  $O$ . Increasing  $H, B$  will increase but the relation is not linear, it goes as per curve  $Oab$  in the

diagram. After the point  $b$ , increasing  $H$  does increase  $B$  (the material is saturated and all the domains are aligned in one direction). The value of  $H$  after which  $B$  does not increase, but become constant, is called magnetic saturation.

Now if we reduce  $H$  to zero, the curve does not retrace the path  $b \rightarrow a \rightarrow O$ ; but it goes from  $b$  to  $c$ . At point  $c, H=0$  but  $B \neq 0$  i.e some magnetization remains in the material. This remanent magnetism is called residual magnetism. The value of  $B$  at  $H=0$  is called retentivity or remanence,  $B_r$ . The domains are not completely randomised although external field  $H=0$ .

Now if we reverse the direction of current in the solenoid, and increase it slowly,  $B$  decreases as curve  $cd$  and  $B$  becomes zero at certain value of  $H$ , which is called coercivity of the material. If we go on increasing  $H$  beyond  $d$ , the material is magnetized in opposite direction and get saturated at  $e$  (i.e all the domains are aligned in opposite direction). If we reduce  $H$  to zero again  $B$  will not be zero but have a value of the remanent value in opposite direction. This is shown as  $of$  in the curve. Again if we increase  $i$  in the original direction, the curve goes as  $fgb$ , and completes a cycle. Again the value of  $H, O_g$  is coercivity of the material. We can know about the behaviour of material and its magnetic properties from its B-H loop  $bedefgb$ . Fig 8.26 shows B-H curves of soft iron and steel.

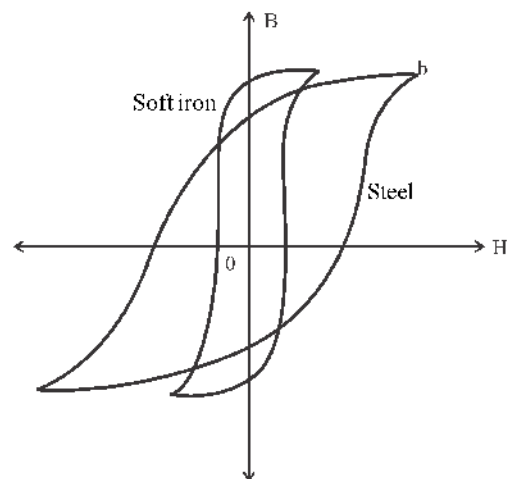


Fig 8.26 : Hysteresis loop for soft iron & steel

From this diagram it is evident that -

- (1) For any value of  $H$ , the value of  $B$  for soft iron is more than that for steel, hence magnetic permeability  $\mu$ , of soft iron is more than that of steel.



- (2) Retentivity of soft iron is more than of steel.
- (3) Steel has more coercivity than soft iron.
- (4) For any value of  $H$ , the value of magnetization  $I$  is more for soft iron than steel; i.e.  $\chi_m = I/H$  is more for iron which shows that the value of magnetic susceptibility of soft iron is more than that of steel.
- (5) The area of B-H loop for soft iron is less than that for steel which shows that hysteresis loss is less in soft iron compared to steel. The area of B-H loop represents the energy loss per cycle per unit volume.
- (6)  $B$  always lags behind  $H$ , this property is called hysteresis.

To select a material for core of electromagnet soft iron is suitable for its high permeability  $\mu$ , less coercivity and less hysteresis loss.

#### 8.15.1 Hysteresis Loss

Energy is given to the material during magnetization. But during demagnetization the material does not release the whole energy it received. Some energy gets lost (work done in rotating the domains). This loss of energy per cycle is called Hysteresis loss. This energy is converted to heat energy.

Area of B-H loop represents energy loss per cycle

per unit volume. Hence the loss of energy per second is  $Q = VAn$ ;  $V$  = Volume of sample;  $A$  = Area of B-H loop and  $n$  is the frequency (number of cycles/s).

Electromagnet consists of insulated copper wire wound over a soft iron core. It is used in telephone electric bell, electric motor, dynamo, telegraphy and separation of magnetic materials from a mixture. It is also used in medical sciences.

For a permanent magnet the material chosen, should have high retentivity and high coercivity. It should also have high Curie temperature and high saturation magnetism, so that it does not get demagnetized due to temperature, stray magnetic field and mechanical impulses. Hysteresis is meaningless for permanent magnet. For permanent magnet the suitable materials are steel and alnico (Al + Ni + Co). In these materials, the domains once get oriented remain as such and the external demagnetizing effects are minimum. Permanent magnets are used in galvanometers, ammeter, voltmeter and loudspeaker.

The material for a transformer core, should also have the properties that are required for electromagnet i.e. high  $\mu$ , high  $\chi_m$ , high retentivity. An extra quality of low hysteresis is required. For transformer core the suitable materials are, superalloy, transformer steel (soft iron 4% silicon) and  $\mu$ -metal (Cu+Fe+Ni+Mn).

### Important Points

1. Magnets show directional and attractive properties. Both the poles can not be separated.
2. Magnetic field lines are imaginary close loops. The tangent drawn at any point gives the direction of magnetic field at that point.
3. Superposition of magnetic fields of two magnets gives two points, where magnetic field is zero, these points are called null points.
4. The magnetic moment of following dipoles is as given -
  - (i) For bar magnet  $M = \text{pole strength} \times \text{effective length}$
  - (ii) For a revolving electron
 
$$M = \frac{1}{2}evr = \frac{1}{2}e\omega r^2$$
5. When a magnet of magnetic moment  $M$  is placed in uniform magnetic field  $B$ 
  - (i) net force on it is zero.
  - (ii) Torque  $\vec{\tau} = \vec{M} \times \vec{B}$
  - (iii) Potential energy  $U = -\vec{M} \cdot \vec{B}$

(iv) work done in rotating the magnet is

$$W = MB(1 - \cos \theta)$$

6. Magnetic axis does not coincide with axis of rotation of earth, but it makes an angle  $11.3^\circ$ .
7. The quantities that give complete information about earth's magnetic field are called elements of earth's magnetism, they are (i) angle of declination (ii) dip angle (iii) Horizontal component of earth's magnetic field.
8. The Gauss's law for magnetism is

$$\phi_B = \oint_S \vec{B} \cdot d\vec{s} = 0$$

9. If a material is kept in magnetic field  $B_0$  then magnetizing field or magnetic intensity  $\vec{H} = \vec{B}_0 / \mu_0$ .  
Magnetic intensity  $I = M / V$  i.e magnetic moment per unit volume.

10. Magnetic susceptibility  $\chi_m = \frac{M}{H}$ .

11. Relation between  $\chi_m$ , and  $\mu_0$  is given as

$$\mu = \mu_0(1 + \chi_m)$$

$$\mu = \mu_0 \mu_r \quad \mu_r = 1 + \chi_m$$

12. Magnetic materials are classified as diamagnetic paramagnetic and ferromagnetic according to their reaction to B.
13. Diamagnetism is due to orbital motion of electrons, paramagnetism is due to orbital and spin motion of electron, ferromagnetism is due to domain property.
14. The hysteresis loop or B-H loop is used to study magnetic properties of materials, and in selecting suitable materials for electric devices.
15. Diamagnetism does not depend on temperature for paramagnetic material  $\chi_m \propto 1/T$  Curie law. For

$$\text{ferromagnetism } \chi_m \propto \frac{1}{T - T_c} \text{ (Curie-Weiss law).}$$

where  $T_c$  = Curie temperature

### Questions for Practice

#### Multiple Choice Questions -

1. If two magnetic poles of unit pole strength are at 1m distance in vacuum. The force between them will be -  
(a)  $4\pi \times 10^{-7} \text{ N}$  (b)  $4\pi \text{ N}$   
(c)  $10^{-7} \text{ N}$  (d)  $\frac{4\pi}{10^{-7}} \text{ N}$
2. For super conductors, magnetic susceptibility is -  
(a) +1 (b) -1  
(c) Zero (d) Infinite
3. Magnetic susceptibility of free space is -  
(a) +1 (b) -1  
(c) Zero (d) Infinite

4. The magnetic susceptibility is negative and very small for -
  - (a) Ferromagnetic materials
  - (b) Paramagnetic materials
  - (c) Diamagnetic materials
  - (d) All of these
5. The relative permeability of a material is 1.0001 the material will be -
  - (a) Ferromagnetic
  - (b) Paramagnetic
  - (c) Diamagnetic
  - (d) Non of above
6. The unit of magnetic moment is -
  - (a) Wb
  - (b) Wb / m<sup>2</sup>
  - (c) A / m
  - (d) Am<sup>2</sup>
7. Wb x A/m is equal to -
  - (a) J
  - (b) N
  - (c) H
  - (d) W
8. Magnetic field does not interact with -
  - (a) Another magnetic field
  - (b) Accelerated magnet
  - (c) A stationary charge
  - (d) Moving electric charge
9. The cause of diamagnetism is -
  - (a) Orbital motion of electron
  - (b) Spin motion of electron
  - (c) Paired electron
  - (d) Non of the above
10. Magnetic moment of diamagnetic substances -
  - (a) Infinite
  - (b) Zero
  - (c) 100 Am<sup>2</sup>
  - (d) Non of the above
11. Relative permeability of ferromagnetic substances is -
  - (a) > 1
  - (b) >> 1
  - (c) = 1
  - (d) = 0
12. The vertical component of earth's magnetic field is zero etc.
  - (a) Magnetic pole
  - (b) Geographical pole
  - (c) Magnetic meridian
  - (d) Non of the above
13. The area of hysteresis loop of a substance represents -
  - (a) Energy loss per cycle to magnetise the material
  - (b) Energy loss per unit volume per cycle in magnetizing the material
  - (c) Energy loss per unit volume in magnetizing
  - (d) Energy loss in magnetizing the material
14. Steel is used to prepare permanent magnet -
  - (a) Less energy loss
  - (b) Density of steel is more
  - (c) The residual magnetism is more
  - (d) Magnetism is not destroyed by ordinary external magnetic field
15. At curie temperature, a ferromagnetic substance becomes -
  - (a) Non-magnetic
  - (b) Diamagnetic
  - (c) Paramagnetic
  - (d) More ferromagnetic

### Very Short Answer Type Questions -

1. A magnetic needle is free to rotate in vertical plane about horizontal axis. What direction it will indicate at magnetic poles?
2. Name the type of magnetic material which does not depend on temperature?
3. How the value of dip angle changes in going from equator to poles?
4. A magnetic material has magnetic susceptibility as -0.085. What type of material it is?
5. What is retentivity or remanence?
6. Name two paramagnetic substances.
7. What is magnetic meridian?
8. Where on earth's surface the dip angle is zero and 90°?
9. Write relation between magnetic permeability and magnetic susceptibility for a medium.
10. Write unit of pole strength.
11. What will be the value of dip angle, where the ratio of vertical and horizontal component of earth's magnetic field is  $\frac{1}{\sqrt{3}}$ .
12. What is magnetic Hysteresis?

- What will be the ratio of magnetic fields at the points on axis and equator, equidistant from center of bar magnet?
- What will be value of dip angle at a place where vertical and horizontal components of earth's magnetic field are equal?
- What will be the change in magnetic moment of a bar magnet if we bisected it along its length?

### Short Answer Type Questions -

- Find the expression for potential energy of a bar magnet placed in uniform magnetic field  $B$ , such that the angle between its dipole moment and  $B$  is  $\theta$ .
- How you will identify rods of paramagnetic and diamagnetic substance?
- Why we get two null points for a bar magnet? Can we get only one null point? How?
- Why soft iron is used for electro magnets.
- A bar magnet of magnetic moment  $M$  is placed parallel to uniform magnetic field  $B$ . What will be the work done in rotating it by  $90^\circ$ ?
- Define angle of declination and dip angle.
- Write down Curie-Weiss law and write the value of Curie temperature for iron.
- Write four properties of magnetic field lines.
- What is the behaviour of diamagnetic, paramagnetic and ferromagnetic substances in non-uniform magnetic field?
- What is Gauss's law for magnetism? What does it indicate?
- Why magnetic field lines are closed loops?
- Compare magnetic fields of a bar magnet and a current carrying solenoid.
- What is cause of earth's magnetism?
- What are uses of hysteresis curve?
- Find the expression for torque on a bar magnet placed at angle with uniform magnetic field. When it will be maximum?

### Essay Type Questions -

- What are elements of earth's magnetism? Define them and show with a labeled diagram.

- What is meant by hysteresis loop? Draw it and define its main physical quantities (specifications).
- Explain diamagnetism, discuss its properties. Write five differences between paramagnetic and diamagnetic substances.
- What is Curie temperature? Explain how the magnetic susceptibility of paramagnetic, diamagnetic and ferromagnetic substances depend on temperature? Also write law regarding it.
- Write specifications of the materials used for (i) Electromagnet (ii) Permanent magnet. Also write their uses.

### Answers (Multiple Choice Questions)

- (A) 2. (B) 3. (C) 4. (C) 5. (B) 6. (D) 7. (B) 8. (C) 9. (A) 10. (B) 11. (B) 12. (D) 13. (B) 14. (D) 15. (C)

### Numerical Questions -

- A bar magnet of magnetic moment  $20 \text{ A m}^2$  is suspended in uniform magnetic field of  $0.86 \text{ T}$ . Find the torque in rotating it by  $60^\circ$ .  
( $86\sqrt{3} \text{ N}\cdot\text{m}$ )
- The horizontal component of earth's magnetic field at certain place is  $B_H = 0.5 \times 10^{-4} \text{ Wb/m}^2$  and dip angle is  $45^\circ$ . Find vertical component of earth's magnetic field.  
( $5 \times 10^{-5} \text{ Wb/m}^2$ )
- An iron rod of cross section  $1 \text{ cm}^2$  is placed in magnetic field of  $200 \text{ oersted}$ . It produces a magnetic field of  $3000 \text{ G}$ . Find magnetic permeability and magnetic susceptibility of the material.  
(15 and 14)
- For a sample of iron the following relation holds -  
$$\mu = \left[ \frac{0.4}{H} + 12 \times 10^{-4} \right] \text{ H/m}$$
  
Find the value of  $H$  which produces a magnetic field of  $1 \text{ T}$ .  
(500 H/m)
- A magnetic field of  $2 \times 10^3 \text{ A/m}$  produces a field

$8\pi$  T in a sample of iron rod. Find relative magnetic permeability of the sample.

( $10^4$ )

6. A sample of volume  $30 \text{ cm}^3$  is placed in magnetic field of  $5 \text{ orested}$ . The magnetic moment induced is  $6 \text{ A/m}^2$ . Find magnetic induction.

( $0.2517 \text{ T}$ )

7. A sample of ferromagnetic material of mass  $0.6 \text{ Kg}$  and density  $7.8 \times 10^3 \text{ kg/m}^3$  is placed in a alternating magnetic field of frequency  $50 \text{ Hz}$ . If the area of hysteresis loop is  $0.722 \text{ m}^2$ . Find hysteresis loss per second.

( $2.777 \times 10^{-4} \text{ J}$ )

8. The curie temperature of ferromagnetic material is  $300 \text{ K}$ . If the magnetic suceptibility at  $450 \text{ K}$  is  $0.6$ . Find curie constant for it.

( $90 \text{ K}$ )

9. Magnetic susceptibility for a paramagnetuic material is  $0.60$  at  $120 \text{ K}$ . Find its magnetic susceptibility at  $27^\circ \text{ C}$ .

( $0.24$ )

10. An iron rod of cross section  $4 \text{ cm}^2$  is placed parallel to a magnetic field of  $10^3 \text{ A/m}$ . If the magnetic flux passing through it is  $4 \times 10^{-4} \text{ Web}$ . Find magnetic permeability, relative magnetic permeability and magnetic susceptibility of iron.

( $10^{-3} \text{ Web/A} \times \text{m}$ ,  $796$ ,  $795$ )

11. A circular coil of  $100$  turns and radius  $0.05 \text{ m}$ , has a current  $0.1 \text{ A}$ . Find the work done in rotating it by  $180^\circ$  in a field of  $1.5 \text{ T}$ .

( $0.236 \text{ J}$ )

12. A coil in the form of unilateral tringle of side  $l$  is suspended in magnetic  $\vec{B}$  which is perpendicular to plane of coil. If the current in the coil is  $I$  and it experience a torque  $\tau$ ; find the expression for length of one side of the tringle.

$$\left[ \left( 2 \frac{\tau}{\sqrt{3} B I} \right)^{1/2} \right]$$