Differential Equations

Question 1: Solution of differential equation xdy - ydx = Q represents

- (a) a rectangular hyperbola
- (b) parabola whose vertex is at origin
- (c) straight line passing through origin
- (d) a circle whose centre is at origin

Question 2: The curve for which the slope of the tangent at any point is equal to the ratio of the abscissa to the ordinate of the point is:

- (a) An ellipse
- (b) Parabola
- (c) Circle
- (d) Hyperbola

Question 3: What is the degree of differential equation $(y''')^2 + (y'')^3 + (y')^4 + y^5 = 0$?

- (a) 2
- (b) 3
- (c)4
- (d) 5

Question 4: What is the differential equation of the family of circles touching the y-axis at the origin?

- (a) $2xyy' + x^2 = y^2$
- (b) $2xyy'' + x' = y^2$
- (c) $2xyy' x^2 = y^2$
- (d) $xyy' + x^2 = y^2$

Question 5: The solution of $(x + \log y)dy + ydx = 0$ where y(0) = 1 is

(a)
$$y(x-(A)) + y\log y = 0$$

(b)
$$y(x-1+\log y) + 1 = 0$$

(c)
$$xy + y \log y + 1 = 0$$

(d) None of these

Question 6: The number of arbitrary constants in the particular solution of a differential equation of third order is:

- (a) 3
- (b) 2
- (c) 1
- (d) 0

Question 7:

The solution of $\frac{dy}{dx} = 1 + x + y + xy$ is

(a)
$$x - y = k(1 + xy)$$

(b)
$$\log (1 + y) = x + \frac{x^2}{2} + k$$

(c)
$$\log (1 + x) + y + \frac{y^2}{2} = k$$

(d) None of these

Answer: (b) $\log (1 + y) = x + \frac{x^2}{2} + k$

Question 8:

 $tan^{-1} x + tan^{-1} y = c$ is the general solution of the differential equation

(a)
$$\frac{dy}{dx} = \frac{1+y^2}{1+x^2}$$

(b)
$$\frac{dy}{dx} = \frac{1+x^2}{1+y^2}$$

(c)
$$(1 + x^2)dy + (1 + y^2)dx = 0$$

(d)
$$(1 + x^2 2)dx + (1 + y^2)dy = 0$$

Question 9:

9. The general solution of $rac{dy}{dx}=2xe^{x^{2-y}}$ is

(a)
$$e^{x^2-y}=c$$

(b)
$$e^{-y} + e^{x^2} = c$$

(c)
$$e^y=e^{x^2}+c$$

$$\text{(d) } e^{x^2+y}=c$$

Question 10:

The order and degree of the differential equation

$$(\frac{d^2y}{dx^3})^2 - 3\frac{d^2y}{dx^2} + 2(\frac{dy}{dx})^4 = y^4$$
 are

(a)(1,4)

(b)(3,4)

(c)(2,4)

(d)(3,2)

Question	Answer
1	(c) straight line passing through origin
2	(d) Hyperbola
3	(a) 2
4	(a) $2xyy' + x^2 = y^2$
5	(b) $y(x-1+\log y) + 1 = 0$
6	(d) 0
7	(b)
8	(c) $(1+x^2)dy + (1+y^2)dx = 0$
9	(c)
10	(d) (3,2)