# **MODERN PHYSICS**

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# JEE (Advance) Syllabus

Photoelectric effect; Bohr's theory of hydrogen-like atoms; characteristic and continuous X-rays, Moseley's law; de Broglie wavelength of matter waves.

# JEE (Main) Syllabus

Photoelectric effect, Hertz and Lenard's observations; Einstein's photoelectric equation – particle nature of light. Matter waves – wave nature of particles, de Broglie relation. Davisson-Germer experiment(experimental details should be omitted; only conclusion should be explained.)

Note: Marked Questions can be used for Revision.

# **MODERN PHYSICS**

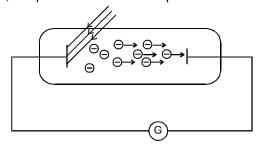


### 1 PHOTOELECTRIC EFFECT :

It was discovered by Hertz in 1887. He found that when the negative plate of an electric discharge tube was illuminated with ultraviolet light, the electric discharge took place more readily. Further experiments carried out by Hallwachs confirmed that certain negatively charged particles are emitted, when a Zn plate is illuminated with ultraviolet light. These particles were identified as electrons.

The phenomenon of emission of electrons from the surface of certain substances, when suitable radiations of certain frequency or wavelength are incident upon it is called photoelectric effect.

When electromagnetic radiations of suitable wavelength are incident on a metallic surface then electrons are emitted, this phenomenon is called photo electric effect.



**Photoelectron:** The electron emitted in photoelectric effect is called photoelectron.

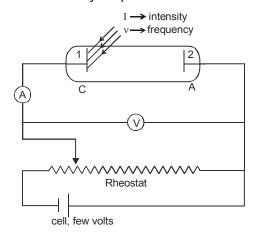
**Photoelectric current**: If current passes through the circuit in photoelectric effect then the current is called photoelectric current.

**Work function**: The minimum energy required to make an electron free from the metal is called work function. It is constant for a metal and denoted by  $\phi$  or W. It is the minimum for Cesium. It is relatively less for alkali metals.

### Work functions of some photosensitive metals

Metal	Work function (ev) Metal		Work function (eV)	
Cesium	1.9	Calcium	3.2	
Potassium	2.2	Copper	4.5	
Sodium	2.3	Silver	4.7	
Lithium	2.5	Platinum	5.6	

To produce photo electric effect only metal and light is necessary but for observing it, the circuit is completed. Figure shows an arrangement used to study the photoelectric effect.



Here the plate (1) is called emitter or cathode and other plate (2) is called collector or anode.

**Saturation current**: When all the photo electrons emitted by cathode reach the anode then current flowing in the circuit at that instant is known as saturated current, this is the maximum value of photoelectric current.

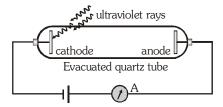
**Stopping potential**: Minimum magnitude of negative potential of anode with respect to cathode for which current is zero is called stopping potential. This is also known as cutoff voltage. This voltage is independent of intensity.

**Retarding potential**: Negative potential of anode with respect to cathode which is less than stopping potential is called retarding potential.

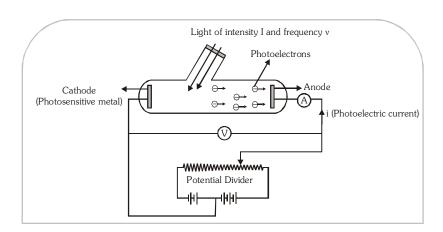
### **EXPERIMENTS**

Hertz Experiment

Hertz observed that when ultraviolet rays are incident on negative plate of electric discharge tube then conduction takes place easily in the tube.

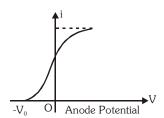


- Hallwach experiment: Hallwach observed that if negatively charged Zn plate is illuminated by U.V. light, its
  negative charge decreases and it becomes neutral and after some time it gains positive charge. It means in
  the effect of light, some negative charged particles are emitted from the metal.
- Lenard Explanation: He told that when ultraviolet rays are incident on cathode, electrons are ejected.
  These electrons are attracted by anode and circuit is completed due to flow of electrons and current flows.
  When U.V. rays incident on anode, electrons are ejected but current does not flow.
  For the photo electric effect the light of short wavelength (or high frequency) is more effective than the light of long wavelength (or low frequency)
- Experimental study of photoelectric Effect: When light of frequency v and intensity I falls on the cathode, electrons are emitted from it. The electrons are collected by the anode and a current flows in the circuit. This current is called photoelectric current. This experiment is used to study the variation of photoelectric current with different factors like intensity, frequency and the potential difference between the anode and cathode.



(i) Variation of photoelectric current with potential difference

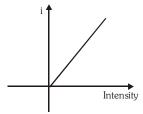
With the help of the above experimental setup, a graph is obtained between current and potential difference. The potential difference is varied with the help of a potential divider. The graph obtained is shown below. The main points of observation are:



- (a) At zero anode potential, a current exists. It means that electrons are emitted from cathode with some kinetic energy.
- (b) As anode potential is increased, current increases. This implies that different electrons are emitted with different kinetic energies.
- (c) After a certain anode potential, current acquires a constant value called saturation current. Current acquires a saturation value because the number of electrons emitted7 per second from the cathode are fixed.
- (d) At a certain negative potential, the photoelectric current becomes zero. This is called stopping potential  $(V_0)$ . Stopping potential is a measure of maximum kinetic energy of the emitted electrons. Let  $KE_{max}$  be the maximum kinetic energy of an emitted electron, then  $KE_{max} = eV_0$ .

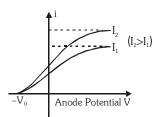
## (ii) Variation of current with intensity

The photoelectric current is found to be directly proportional to intensity of incident radiation.



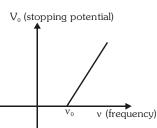
## (iii) Effect of intensity on saturation current and stopping potential

- (a) Saturation current increases with increase in intensity.
- (b) Stopping potential (and therefore maximum kinetic energy) is independent of intensity.



## (iv) Effect of frequency

- (a) Stopping potential is found to vary with frequency of incident light linearly. Greater the frequency of incident light, greater the stopping potential.
- (b) There exists a certain minimum frequency  $\nu_{_0}$  below which no stopping potential is required as no emission of electrons takes place. This frequency is called threshold frequency. For photoelectric emission to take place,  $\nu > \nu_{_0}$ .



#### **IMPORTANT POINTS**

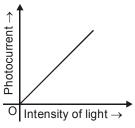
- Photo electric effect is an instantaneous process, as soon as light is incident on the metal, photo electrons are emitted.
- Stopping potential does not depend on the distance between cathode and anode.
- The work function represented the energy needed to remove the least tightly bounded electrons from the surface. It depends only on nature of the metal and independent of any other factors.

## Failure of wave theory of light

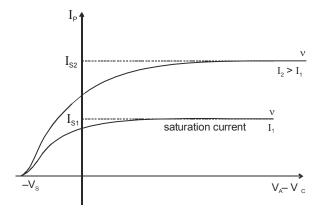
- (i) According to wave theory when light incident on a surface, energy is distributed continuously over the surface. So that electron has to wait to gain sufficient energy to come out. But in experiment there is no time lag. Emission of electrons takes place in less than 10<sup>-9</sup> s. This means, electron does not absorb energy. They get all the energy once.
- (ii) When intensity is increased, more energetic electrons should be emitted. So that stopping potential should be intensity dependent. But it is not observed.
- (iii) According to wave theory, if intensity is sufficient then, at each frequency, electron emission is possible. It means there should not be existence of threshold frequency.

# **OBSERVATIONS: (MADE BY EINSTEIN)**

A graph between intensity of light and photoelectric current is found to be a straight line as shown in figure. Photoelectric current is directly proportional to the intensity of incident radiation. In this experiment the frequency and retarding potential are kept constant.



A graph between photoelectric current and potential diffrence between cathode and anode is found as shown in figure.



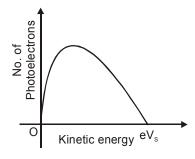
In case of saturation current,

rate of emission of photoelectrons = rate of flow of photoelectrons, here,  $v_s \rightarrow$  stopping potential and it is a positive quantity Electrons emitted from surface of metal have different energies. Maximum kinetic energy of photoelectron on the cathode = eV<sub>s</sub>

 $KE_{max} = eV_s$ Whenever photoelectric effect takes place, electrons are ejected out with kinetic energies ranging from

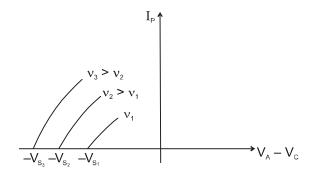
0 to K.E<sub>max</sub> i.e.  $0 \le KE_C \le eV_s$ 

The energy distribution of photoelectron is shown in figure.



If intensity is increased (keeping the frequency constant) then saturation current is increased by same factor by which intensity increases. Stopping potential is same, so maximum value of kinetic energy is not effected.

If light of different frequencies is used then obtained plots are shown in figure.

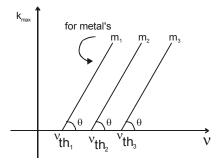


It is clear from graph, as v increases, stopping potential increases, it means maximum value of kinetic energy increases.

Graphs between maximum kinetic energy of electrons ejected from different metals and frequency of light used are found to be straight lines of same slope as shown in flugre

Graph between  $K_{max}$  and v

m<sub>1</sub>, m<sub>2</sub>, m<sub>3</sub>: Three different metals.



It is clear from graph that there is a minimum frequency of electromagnetic radiation which can produce photoelectric effect, which is called threshold frequency.

$$v_{th}$$
 = Threshold frequency

$$v \ge v_{th}$$
 $v < v_{th}$ 

for no photoelectric effect 
$$\nu$$

Minimum frequency for photoelectric effect =  $v_{th}$ 

$$v_{min} = v_{th}$$

**Threshold wavelength**  $(\lambda_{in}) \rightarrow$  The maximum wavelength of radiation which can produce photoelectric effect.

$$\lambda \leq \lambda_{th}$$
 for photo electric effect

Maximum wavelength for photoelectric effect

$$\lambda_{\text{max}} = \lambda_{\text{th}}$$

Now writing equation of straight line from graph.

We have 
$$K_{max} = A_V + B$$

When 
$$v = v_{th}$$
,  $K_{max} = 0$ 

and 
$$B = -A_1$$

Hence 
$$[K_{max} = A(v - v_{th})]$$

and 
$$A = \tan \theta = 6.63 \times 10^{-34} \text{ J-s}$$
 (from experimental data)

It is also observed that photoelectric effect is an instantaneous process. When light falls on surface electrons start ejecting without taking any time.

### 3. THREE MAJOR FEATURES OF THE PHOTOELECTRIC EFFECT CANNOT BE EXPLAINED IN TERMS OF THE CLASSICAL WAVE THEORY OF LIGHT.

Intensity: The energy crossing per unit area per unit time perpendicular to the direction of propagation is called the intensity of a wave.

Consider a cylindrical volume with area of cross-section A and length c ∆t along the X-axis. The energy contained in this cylinder crosses the area A in time ∆t as the wave propagates at speed c. The energy contained.



$$U = u_{av}(c. \Delta t)A$$

$$I = \frac{U}{A \wedge t} = u_{av} c.$$

In the terms of maximum electric field,

$$I = \frac{1}{2} \epsilon_0 E_0^2 c.$$

If we consider light as a wave then the intensity depends upon electric field.

If we take work function  $W = I \cdot A \cdot t$ ,

then

$$t = \frac{W}{IA}$$

so for photoelectric effect there should be time lag because the metal has work function.

But it is observed that photoelectric effect is an instantaneous process.

Hence, light is not of wave nature.

**The intensity problem:** Wave theory requires that the oscillating electric field vector **E** of the light wave increases in amplitude as the intensity of the light beam is increased. Since the force applied to the electron is e**E**, this suggests that the kinetic energy of the photoelectrons should also increased as the light beam is made more intense. However observation shows that maximum kinetic energy is independent of the light intensity.

The frequency problem: According to the wave theory, the photoelectric effect should occur for any frequency of the light, provided only that the light is intense enough to supply the energy needed to eject the photoelectrons. However observations shows that there exists for each surface a characteristic cutoff frequency  $\nu_{th}$ , for frequencies less than  $\nu_{th}$ , the photoelectric effect does not occur, no matter how intense is light beam.

The time delay problem: If the energy acquired by a photoelectron is absorbed directly from the wave incident on the metal plate, the "effective target area" for an electron in the metal is limited and probably not much more than that of a circle of diameter roughly equal to that of an atom. In the classical theory, the light energy is uniformly distributed over the wavefront. Thus, if the light is feeble enough, there should be a measurable time lag, between the impinging of the light on the surface and the ejection of the photoelectron. During this interval the electron should be absorbing energy from the beam until it had accumulated enough to escape. However, no detectable time lag has ever been measured.

Now, quantum theory solves these problems in providing the correct interpretation of the photoelectric effect.

# 4 PLANCK'S QUANTUM THEORY:

The light energy from any source is always an integral multiple of a smaller energy value called quantum of light.hence energy Q = NE,

where

E = hv

N (number of photons) = 1,2,3,...

Here energy is quantized. hv is the quantum of energy, it is a packet of energy called as **photon**.

$$E = h_V = \frac{hc}{\lambda}$$

and

hc = 12400 eV Å

## 5. EINSTEIN'S PHOTON THEORY

In 1905 Einstein made a remarkable assumption about the nature of light; namely, that, under some circumstances, it behaves as if its energy is concentrated into localized bundles, later called photons. The energy E of a single photon is given by

$$E = hv$$
,

If we apply Einstein's photon concept to the photoelectric effect, we can write

and

$$h_V = W + K_{max}$$
, (energy conservation)

Equation says that a single photon carries an energy  $h\nu$  into the surface where it is absorbed by a single electron. Part of this energy W (called the work function of the emitting surface) is used in causing the electron to escape from the metal surface. The excess energy  $(h\nu - W)$  becomes the electron's kinetic energy; if the electron does not lose energy by internal collisions as it escapes from the metal, it will still have this much kinetic energy after it emerges. Thus  $K_{max}$  represents the maximum kinetic energy that the photoelectron can have outside the surface. There is complete agreement of the photon theory with experiment.

Now IA = Nhv

 $\Rightarrow$ 

 $N = \frac{IA}{hv}$  = no. of photons incident per unit time on an area 'A' when light of

intensity 'I' is incident normally.

If we double the light intensity, we double the number of photons and thus double the photoelectric current; we do not change the energy of the individual photons or the nature of the individual photoelectric processes.

The second objection (the frequency problem) is met if  $K_{max}$  equals zero, we have  $h_{V_{th}} = W$ ,

Which asserts that the photon has just enough energy to eject the photoelectrons and none extra to appear as kinetic energy. If  $\nu$  is reduced below  $\nu_{th}$ ,  $h\nu$  will be smaller than W and the individual photons, no matter how many of them there are (that is, no matter how intense the illumination), will not have enough energy to eject photoelectrons.

The third objection (the time delay problem) follows from the photon theory because the required energy is supplied in a concentrated bundle. It is not spread uniformly over the beam cross section as in the wave

Hence Einstein's equation for photoelectric effect is given by

$$h_V = h_{V_{th}} + K_{max}$$
  $K_{max} = \frac{hc}{\lambda} - \frac{hc}{\lambda_{th}}$ 

# SOLVED EXAMPLE \_

- In an experiment on photo electric emission, following observations were made; Ex. 1
  - Wavelength of the incident light =  $1.98 \times 10^{-7}$  m; (i)
  - Stopping potential = 2.5 volt. (ii)

Find: (a) Kinetic energy of photoelectrons with maximum speed.

- (b) Work function and
- (c) Threshold frequency;

Since  $\dot{v}_s = 2.5 \text{ V}$ ,  $K_{max} = eV_s$ Energy of incident photon  $K_{max} = 2.5 \text{ eV}$ Sol. SO, (a)

(b)

$$E = \frac{12400}{1980} \text{ eV} = 6.26 \text{ eV}$$
  $W = E - K_{\text{max}} = 3.76 \text{ eV}$ 

(c) 
$$h_{V_{th}} = W = 3.76 \times 1.6 \times 10^{-19} \,\text{J}$$
  $\therefore$   $v_{th} = \frac{3.76 \times 1.6 \times 10^{-19}}{6.6 \times 10^{-34}} \approx 9.1 \times 10^{14} \,\text{Hz}$ 

A beam of light consists of four wavelength 4000 Å, 4800 Å, 6000 Å and 7000 Å, each of intensity Ex.2 1.5 × 10<sup>-3</sup> Wm<sup>-2</sup>. The beam falls normally on an area 10<sup>-4</sup> m<sup>2</sup> of a clean metallic surface of work function 1.9 eV. Assuming no loss of light energy (i.e. each capable photon emits one electron) calculate the number of photoelectrons liberated per second.

**Sol.** 
$$E_1 = \frac{12400}{4000} = 3.1 \text{ eV}, \quad E_2 = \frac{12400}{4800} = 2.58 \text{ eV}$$
  $E_3 = \frac{12400}{6000} = 2.06 \text{ eV}$  and  $E_4 = \frac{12400}{7000} = 1.77 \text{ eV}$ 

Therefore, light of wavelengths 4000 Å, 4800 Å and 6000 Å can only emit photoelectrons.

Number of photoelectrons emitted per second = No. of photons incident per second)

$$= \frac{I_1 A_1}{E_1} + \frac{I_2 A_2}{E_2} + \frac{I_3 A_3}{E_3} = IA \left( \frac{1}{E_1} + \frac{1}{E_2} + \frac{1}{E_3} \right)$$

$$= \frac{(1.5 \times 10^{-3})(10^{-4})}{1.6 \times 10^{-19}} \left( \frac{1}{3.1} + \frac{1}{2.58} + \frac{1}{2.06} \right)$$

$$= 1.12 \times 10^{12} \quad \text{Ans.}$$

- **Ex. 3** A small potassium foil is placed (perpendicular to the direciton of incidence of light) a distance r = 0.5 m from a point light source whose output power  $P_0$  is 1.0W. Assuming wave nature of light how long would it take for the foil to soak up enough energy (= 1.8 eV) from the beam to eject an electron? Assume that the ejected photoelectron collected its energy from a circular area of the foil whose radius equals the radius of a potassium atom (1.3 ×  $10^{-10}$  m).
- **Sol.** If the source radiates uniformly in all directions, the intensity I of the light at a distance r is given by

$$I = \frac{P_0}{4\pi r^2} = \frac{1.0 \text{ W}}{4\pi (0.5 \text{ m})^2} = 0.32 \text{ W/m}^2.$$

The target area A is  $\pi(1.3 \times 10^{-10} \text{ m})^2$  or  $5.3 \times 10^{-20} \text{ m}^2$ , so that the rate at which energy falls on the target is given by

$$P = IA = (0.32 \text{ W/m}^2) (5.3 \times 10^{-20} \text{ m}^2)$$

$$= 1.7 \times 10^{-20} \text{ J/s}.$$

If all this incoming energy is absorbed, the time required to accumulate enough energy for the electron to escape is

$$t = \left(\frac{1.8 \text{ eV}}{1.7 \times 10^{-20} \text{ J/s}}\right) \left(\frac{1.6 \times 10^{-19} \text{ J}}{1 \text{ eV}}\right) = 17 \text{ s.}$$

Our selection of a radius for the effective target area was some-what arbitrary, but no matter what reasonable area we choose, we should still calculate a "soak-up time" within the range of easy measurement. However, no time delay has ever been observed under any circumstances, the early experiments setting an upper limit of about 10<sup>-9</sup> s for such delays.

- **Ex. 4** A metallic surface is irradiated with monochromatic light of variable wavelength. Above a wavelength of 5000 Å, no photoelectrons are emitted from the surface. With an unknown wavelength, stopping potential is 3 V. Find the unknown wavelength.
- **Sol.** Using equation of photoelectric effect

$$Kmax = E - W (Kmax = eVs)$$
∴  $3 eV = \frac{12400}{\lambda} - \frac{12400}{5000} = \frac{12400}{\lambda} - 2.48 eV$ 
or  $\lambda = 2262 \text{ Å}$ 

- **Ex. 5** Illuminating the surface of a certain metal alternately with light of wavelengths  $\lambda_1$  = 0.35  $\mu$ m and  $\lambda_2$  = 0.54  $\mu$ m, it was found that the corresponding maximum velocities of photo electrons have a ratio  $\eta$  = 2. Find the work function of that metal.
- Sol. Using equation for two wavelengths

$$\frac{1}{2}mv_1^2 = \frac{hc}{\lambda_1} - W \qquad ....(i)$$

$$\frac{1}{2}mv_2^2 = \frac{hc}{\lambda_2} - W \qquad \qquad ....(ii)$$

Dividing Eq. (i) with Eq. (ii), with  $v_1 = 2v_2$ , we have  $4 = \frac{\frac{hc}{\lambda_1} - W}{\frac{hc}{\lambda_2} - W}$ 

$$3W = 4\left(\frac{hc}{\lambda_2}\right) - \left(\frac{hc}{\lambda_1}\right) = \frac{4 \times 12400}{5400} - \frac{12400}{3500} = 5.64 \text{ eV}$$

$$W = \frac{5.64}{3} \text{ eV} = 1.88 \text{ eV}$$
 Ans.

- Ex. 6 A photocell is operating in saturation mode with a photocurrent 4.8 μA when a monochromatic radiation of wavelength 3000 Å and power 1 mW is incident. When another monochromatic radiation of wavelength 1650 Å and power 5 mW is incident, it is observed that maximum velocity of photoelectron increases to two times. Assuming efficiency of photoelectron generation per incident to be same for both the cases, calculate,
  - (a) threshold wavelength for the cell
  - (b) efficiency of photoelectron generation. [(No. of photoelectrons emitted per incident photon) × 100]
  - (c) saturation current in second case

**Sol.** (a) 
$$K_1 = \frac{12400}{3000} - W = 4.13 - W$$
 ...(i)

$$K_2 = \frac{12400}{1650} - W = 7.51 - W$$
 ....(ii)

Since

or

$$v_2 = 2v_1$$
 so,  $K_2 = 4K_1$  ...(iiii)

Solving above equations, we get

$$W = 3 eV$$

$$\therefore \qquad \text{Threshold wavelegth} \qquad \qquad \lambda_0 = \frac{12400}{3} = 4133 \, \text{Å} \qquad \qquad \text{Ans.}$$

(b) Energy of a photon in first case = 
$$\frac{12400}{3000}$$
 = 4.13 eV

$$E_{1} = 6.6 \times 10^{-19} \text{ J}$$

Rate of incident photons (number of photons per second)

$$= \frac{P_1}{E_1} = \frac{10^{-3}}{6.6 \times 10^{-19}} = 1.5 \times 10^{15} \text{ per second}$$

Number of electrons ejected =  $\frac{4.8 \times 10^{-6}}{1.6 \times 10^{-19}}$  per second =  $3.0 \times 10^{13}$  per second

: Efficiency of photoelectron generation

$$(\eta) = \frac{3.0 \times 10^{13}}{1.5 \times 10^{15}} \times 100 = 2\%$$
 Ans.

(c) Energy of photon in second case

$$E_2 = \frac{12400}{1650} = 7.51 \text{ eV} = 12 \times 10^{-19} \text{ J}$$

Therefore, number of photons incident per second

$$n_2 = \frac{P_2}{E_2} = \frac{5.0 \times 10^{-3}}{12 \times 10^{-19}} = 4.17 \times 10^{15} \text{ per second}$$

Number of electrons emitted per second =  $\frac{2}{100} \times 4.7 \times 10^{15}$ 

= 
$$9.4 \times 10^{13}$$
 per second

∴ Saturation current in second case 
$$i = (9.4 \times 10^{13}) (1.6 \times 10^{-19})$$
 amp  $= 15 \mu A$  Ans.

**Ex. 7** Light described at a place by the equation  $E = (100 \text{ V/m}) [\sin (5 \times 10^{15} \text{ s}^{-1}) \text{ t} + \sin (8 \times 10^{15} \text{ s}^{-1}) \text{ t}]$  falls on a metal surface having work function 2.0 eV. Calculate the maximum kinetic energy of the photoelectrons.

**Sol.** The light contains two different frequencies. The one with larger frequency will cause photoelectrons with largest kinetic energy. This larger frequency is

$$v = \frac{\omega}{2\pi} = \frac{8 \times 10^{15} \, \text{s}^{-1}}{2\pi}$$

The maximum kinetic energy of the photoelectrons is

$$K_{\text{max}} = h_{\text{U}} - W$$
  
= (4.14 × 10<sup>-15</sup> eV/s) ×

= 
$$(4.14 \times 10^{-15} \text{ eV-s}) \times \left(\frac{8 \times 10^{15}}{2\pi} \text{ s}^{-1}\right) - 2.0 \text{ eV}$$
  
=  $5.27 \text{ eV} - 2.0 \text{ eV} = 3.27 \text{ eV}.$ 

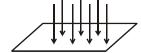


# 6 FORCE DUE TO RADIATION (PHOTON)

Each photon has a definite energy and a definite linear momentum. All photons of light of a particular wavelength  $\lambda$  have the same energy  $E = hc/\lambda$  and the same magnitude of momentum  $p = h/\lambda$ .

When light of intensity I falls on a surface, it exerts force on that surface. Assume absorption and reflection coefficient of surface be 'a' and 'r' and assuming no transmission.

Assume light beam falls on surface of surface area 'A' perpendicularly as shown in figure.



For calculating the force exerted by beam on surface, we consider following cases.

Case: (I)

$$a = 1, r = 0$$

initial momentum of the photon =  $\frac{h}{\lambda}$ 

final momentum of photon = 0

change in momentum of photon =  $\frac{h}{\lambda}$  (upward)

$$\Delta P = \frac{h}{\lambda}$$

energy incident per unit time = IA

no. of photons incident per unit time  $=\frac{IA}{hv}=\frac{IA\lambda}{hc}$ 

: total change in momentum per unit time =  $n \Delta P$ 

$$= \frac{IA\lambda}{hc} \times \frac{h}{\lambda}$$
$$= \frac{IA}{c} \quad \text{(upward)}$$

force on photons = total change in momentum per unit time

$$=\frac{IA}{c}$$
 (upward)

 $\therefore \qquad \text{force on plate due to photons}(F) = \frac{IA}{C} \qquad (downward)$ 

pressure = 
$$\frac{F}{A} = \frac{IA}{cA} = \frac{I}{c}$$

Case: (II)

when 
$$r = 1$$
,  $a = 0$ 

intial momentum of the photon 
$$=\frac{h}{\lambda}$$
 (downward)

final momentum of photon 
$$=\frac{h}{\lambda}$$
 (upward)

change in momentum 
$$= \frac{h}{\lambda} + \frac{h}{\lambda} = \frac{2h}{\lambda}$$

∴ energy incident per unit time = IA

no. of photons incident per unit time =  $\frac{IA\lambda}{hc}$ 

$$=\frac{IA\lambda}{hc}\cdot\frac{2h}{\lambda}=\frac{2IA}{C}$$

 $= n \cdot \Delta P$ 

force = total change in momentum per unit time

$$F = \frac{2IA}{c}$$
 (upward on photons and downward on the plate)

pressure

$$P = \frac{F}{A} = \frac{2IA}{cA} = \frac{2I}{c}$$

Case: (III)

When 
$$o < r < 1$$

$$a + r = r$$

change in momentum of photon when it is reflected = 
$$\frac{2h}{\lambda}$$
 (upward)

change in momentum of photon when it is absorbed = 
$$\frac{h}{\lambda}$$
 (upward)

no. of photons incident per unit time = 
$$\frac{IA\lambda}{hc}$$

No. of photons reflected per unit time 
$$=\frac{IA\lambda}{hc}$$
. r

No. of photon absorbed per unit time = 
$$\frac{IA\lambda}{hc}$$
 (1 – r)

force due to absorbed photon (F<sub>a</sub>) = 
$$\frac{IA\lambda}{hc}$$
 (1 - r) .  $\frac{h}{\lambda}$  =  $\frac{IA}{c}$  (1 - r) (downward)

Force due to reflected photon (F<sub>r</sub>) 
$$= \frac{IA\lambda}{hc} . r \frac{2h}{\lambda} = \frac{2IA\lambda}{c}$$
 (downward)

total force 
$$= F_a + F_r$$
 (downward) 
$$= \frac{IA}{c} (1 - r) + \frac{2IAr}{c}$$
 
$$= \frac{IA}{c} (1 + r)$$

Now pressure P = 
$$\frac{IA}{C}$$
 (1 + r) ×  $\frac{1}{A}$  =  $\frac{I}{C}$  (1 + r)

# SOLVED EXAMPLE.

A plate of mass 10 gm is in equilibrium in air due to the force exerted by light beam on plate. Ex. 8

Calculate power of beam. Assume plate is perfectly absorbing.

Sol. Since plate is in air, so gravitational force will act on this

$$F_{\text{gravitational}} = \text{mg} \qquad \text{(downward)}$$
$$= 10 \times 10^{-3} \times 10$$

for equilibrium force exerted by light beam should be equal to F<sub>gravitational</sub>

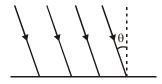
 $F_{photon} = F_{gravitational}$ Let power of light beam be P

$$\therefore \qquad \qquad \mathsf{F}_{\mathsf{photon}} = \frac{\mathsf{P}}{\mathsf{c}}$$

$$\frac{P}{c} = 10^{-1} \qquad P = 3.0 \times 10^{8} \times 10^{-1}$$

$$P = 3 \times 10^{7} \text{ W}$$

Ex. 9 Calculate force exerted by light beam if light is incident on surface at an angle  $\theta$  as shown in figure. Consider all cases.



a = 1, r = 0Sol. Case - I

initial momentum of photon (in downward direction at an angle  $\theta$  with vertical) =  $\frac{h}{\lambda}$  [  $\frac{h}{\theta}$  ]

final momentum of photon = 0

change in momentum (in upward direction at an angle  $\theta$  with vertical) =  $\frac{h}{\lambda}$ 



energy incident per unit time = IA  $\cos \theta$ Intensity = power per unit normal area

$$I = \frac{P}{A\cos\theta} \qquad P = IA\cos\theta$$

No. of photons incident per unit time =  $\frac{IA\cos\theta}{hc}$ . $\lambda$ 

total change in momentum per unit time (in upward direction at an angle  $\theta$  with vertical)

$$= \frac{IA\cos\theta.\lambda}{hc} \ . \ \frac{h}{\lambda} = \frac{IA\cos\theta}{c}$$



Force (F) = total change in momentum per unit time

$$F = \frac{IA\cos\theta}{c} \text{ (direction } \begin{array}{c} \bullet \\ \bullet \end{array} \text{ on photon and } \begin{array}{c} \bullet \\ \bullet \end{array} \text{ on the plate)}$$

Pressure = normal force per unit Area

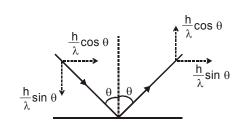
Pressure = 
$$\frac{F\cos\theta}{A}$$
  $P = \frac{IA\cos^2\theta}{cA} = \frac{I}{c}\cos^2\theta$ 

When r = 1, a = 0Case II

change in momentum of one photon

$$= \frac{2h}{\lambda} \cos \theta \qquad \text{(upward)}$$

No. of photons incident per unit time



$$= \frac{IA\cos\theta \cdot \lambda}{hc}$$

: total change in momentum per unit time

$$= \frac{IA\cos\theta \cdot \lambda}{hc} \times \frac{2h}{\lambda} \cos\theta \qquad \qquad = \frac{2IA\cos^2\theta}{c} \quad \text{(upward)}$$

 $\therefore \qquad \text{force on the plate} = \frac{2IA\cos^2\theta}{c} \quad \text{(downward)}$ 

Pressure = 
$$\frac{2IA\cos^2\theta}{cA}$$
 P =  $\frac{2I\cos^2\theta}{c}$ 

**Case III** 0 < r < 1, a + r = 1

change in momentum of photon when it is reflected =  $\frac{2h}{\lambda} \cos \theta$  (downward)

change in momentum of photon when it is absorbed =  $\frac{h}{\lambda}$  (in the opposite direction of incident beam) energy incident per unit time = IA cos  $\theta$ 

no. of photons incident per unit time =  $\frac{IA\cos\theta \cdot \lambda}{hc}$ 

no. of reflected photon (
$$n_r$$
) =  $\frac{IA\cos\theta.\lambda r}{hc}$ 

no. of absorbed photon  $(n_a) = \frac{IA \cos \theta . \lambda}{hc} (1 - r)$ 

force on plate due to absorbed photons  $F_a = n_a \cdot \Delta P_a$ 

$$= \frac{IA\cos\theta.\lambda}{hc} (1-r) \frac{h}{\lambda}$$

$$= \frac{IA\cos\theta}{c} (1-r) \qquad \text{(at an angle } \theta \text{ with vertical}$$

force on plate due to reflected photons  $F_r = n_r \Delta P_r$ 

$$= \frac{IA\cos\theta \cdot \lambda}{hc} \times \frac{2h}{\lambda}\cos\theta \text{ (vertically downward)}$$

$$= \frac{IA\cos^2\theta}{c} \cdot 2r$$

now resultant force is given by  $F_R = \sqrt{F_r^2 + F_a^2 + 2F_aF_r\cos\theta}$ 

$$= \frac{IA\cos\theta}{c} \sqrt{(1-r)^2 + (2r)^2\cos^2\theta + 4r(r-1)\cos^2\theta}$$

and, pressure

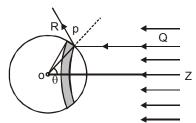
$$P = \frac{F_a \cos \theta + F_r}{A}$$

$$= \frac{IA \cos \theta (1 - r) \cos \theta}{cA} + \frac{IA \cos^2 \theta \cdot 2r}{cA}$$

$$= \frac{I \cos^2 \theta}{cA} (1 - r) + \frac{I \cos^2 \theta}{cA} 2r = \frac{I \cos^2 \theta}{cA} (1 + r)$$

# SOLVED EXAMPLE.

- **Ex. 10** A perfectly reflecting solid sphere of radius r is kept in the path of a parallel beam of light of large aperture. If the beam carries an intensity I, find the force exerted by the beam on the sphere.
- **Sol.** Let O be the centre of the sphere and OZ be the line opposite to the incident beam (figure). Consider a radius OP of the sphere making an angle  $\theta$  with OZ. Rotate this radius about OZ to get a circle on the sphere. Change  $\theta$  to  $\theta$  +  $d\theta$  and rotate the radius about OZ to get another circle on the sphere. The part of the sphere between these circles is a ring of area  $2\pi r^2 \sin\theta \ d\theta$ . Consider a small part  $\Delta A$  of this ring at P. Energy of the light falling on this part in time  $\Delta t$  is



....(ii)

$$\Delta U = I\Delta t(\Delta A \cos \theta)$$

The momentum of this light falling on  $\Delta A$  is  $\Delta U/c$  along QP. The light is reflected by the sphere along PR. The change in momentum is

$$\Delta p = 2 \frac{\Delta U}{c} \cos \theta = \frac{2}{c} I \Delta t (\Delta A \cos^2 \theta)$$
 (direction along  $\overrightarrow{OP}$ )

The force on  $\triangle A$  due to the light faling on it, is

$$\frac{\Delta p}{\Delta t} = \frac{2}{c} I \Delta A \cos^2 \theta.$$
 (direction along  $\overrightarrow{PO}$ )

The resultant force on the ring as well as on the sphere is along ZO by symmetry. The component of the force on  $\Delta A$  along ZO

$$\frac{\Delta p}{\Delta t} \cos \theta = \frac{2}{c} I\Delta A \cos^3 \theta.$$
 (along  $\overrightarrow{ZO}$ )

The force acting on the ring is  $dF = \frac{2}{c} \, I(2\pi r^2 \sin\theta \, d\theta) cos^3 \, \theta.$ 

The force on the entire sphere is  $F = \int_{0}^{\pi/2} \frac{4\pi r^2 I}{c} \cos^3 \theta \sin \theta \ d\theta$ 

$$= -\int_{0}^{\pi/2} \frac{4\pi r^{2}I}{c} \cos^{3}\theta \ d(\cos\theta) \qquad = -\int_{\theta=0}^{\pi/2} \frac{4\pi r^{2}I}{c} \left[ \frac{\cos^{4}\theta}{4} \right]_{0}^{\pi/2} = \frac{\pi r^{2}I}{c}$$

Note that integration is done only for the hemisphere that faces the incident beam.

## $\square$

# 7. de-BROGLIE WAVELENGTH OF MATTER WAVE

A photon of frequency v and wavelength  $\lambda$  has energy.

$$E = hv = \frac{hc}{\lambda}$$

By Einstein's energy mass relation,  $E = mc^2$  the equivalent mass m of the photon is given by,

$$m = \frac{E}{c^2} = \frac{hv}{c^2} = \frac{h}{\lambda c} \qquad ....(i)$$

or 
$$\lambda = \frac{h}{mc}$$
 or  $\lambda = \frac{h}{p}$ 

Here p is the momentum of photon. By analogy de-Broglie suggested that a particle of mass m moving with speed v behaves in some ways like waves of wavelength  $\lambda$  (called de-Broglie wavelength and the wave is called matter wave) given by,

$$\lambda = \frac{h}{mv} = \frac{h}{p} \qquad \dots (iii)$$

where p is the momentum of the particle. Momentum is related to the kinetic energy by the equation,

$$p = \sqrt{2Km}$$

and a charge q when accelerated by a potential difference V gains a kinetic energy K = qV. Combining all these relations Eq. (iii), can be written as,

$$\lambda = \frac{h}{mv} = \frac{h}{p} = \frac{h}{\sqrt{2Km}} = \frac{h}{\sqrt{2qVm}}$$
 (de-Broglie wavelength) ....(iv)

## de-Broglie wavelength for an electron

If an electron (charge = e) is accelerated by a potential of V volts, it acquires a kinetic energy,

$$K = eV$$

Substituting the values of h, m and q in Eq. (iv), we get a simple formula for calculating de-Broglie wavelength of an electron.

$$\lambda(\text{in Å}) = \sqrt{\frac{150}{\text{V(involts)}}} \qquad \dots (\text{v})$$

## de-Broglie wavelength of a gas molecule:

Let us consider a gas molecule at absolute temperature T. Kinetic energy of gas molecule is given by

K.E. = 
$$\frac{3}{2}$$
 kT; k = Boltzman constant

$$\lambda_{\text{gas molecule}} = \frac{h}{\sqrt{3mkT}}$$

# SOLVED EXAMPLE \_\_\_\_

- **Ex. 11** An electron is accelerated by a potential difference of 50 volt. Find the de-Broglie wavelength associated with it.
- **Sol.** For an electron, de-Broglie wavelength is given by,

$$\lambda = \sqrt{\frac{150}{V}} = \sqrt{\frac{150}{50}} = \sqrt{3}$$
  
= 1.73 Å Ans.

- **Ex. 12** Find the ratio of De-Broglie wavelength of molecules of hydrogen and helium which are at temperatures 27°C and 127°C respectively.
- Sol. de-Broglie wavelength is given by

$$\therefore \frac{\lambda_{H_2}}{\lambda_{H_2}} = \sqrt{\frac{m_{He}T_{He}}{m_{H_2}T_{H_2}}} = \sqrt{\frac{4}{2} \cdot \frac{(127 + 273)}{(27 + 273)}} = \sqrt{\frac{8}{3}}$$

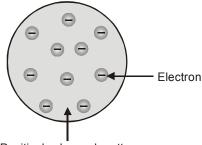


## 8. THOMSON'S ATOMIC MODEL:

J.J. Thomson suggested that atoms are just positively charge lumps of matter with electrons embedded in them like raisins in a fruit cake. Thomson's model called the 'plum pudding' model is illustrated in figure.

Thomson played an important role in discovering the electron, through gas discharge tube by discovering cathode rays. His idea was taken seriously.

But the real atom turned out to be guite different.



Positively charged matter

# 9. RUTHERFORD'S NUCLEAR ATOM:

Rutherford suggested that; "All the positive charge and nearly all the mass were concentrated in a very small volume of nucleus at the centre of the atom. The electrons were supposed to move in circular orbits round the nucleus (like planets round the sun). The electronstatic attraction between the two opposite charges being the required centripetal force for such motion.

Hence

$$\frac{mv^2}{r} = \frac{kZe^2}{r^2}$$

and total energy = potential energy + kinetic energy

$$= \frac{-kZe^2}{2r}$$

Rutherford's model of the atom, although strongly supported by evidence for the nucleus, is inconsistent with classical physics. This model suffer's from two defects

**Regarding stability of atom:** An electron moving in a circular orbit round a nucleus is accelerating and according to electromagnetic theory it should therefore, emit radiation continuously and thereby lose energy. If total energy decreases then radius increases as given by above formula. If this happened the radius of the orbit would decrease and the electron would spiral into the nucleus in a fraction of second. But atoms do not collapse. In 1913 an effort was made by Neil Bohr to overcome this paradox.

**Regarding explanation of line spectrum:** In Rutherford's model, due to continuously changing radii of the circular orbits of electrons, the frequency of revolution of the electrons must be changing. As a result, electrons will radiate electromagnetic waves of all frequencies, i.e., the spectrum of these waves will be 'continuous' in nature. But experimentally the atomic spectra are not continuous. Instead they are line spectra.

### 10. THE BOHR'S ATOMIC MODEL

In 1913, Prof. Niel Bohr removed the difficulties of Rutherford's atomic model by the application of Planck's quantum theory. For this he proposed the following postulates

- (a) An electron moves only in certain circular orbits, called stationary orbits. In stationary orbits electron does not emit radiation, contrary to the predictions of classical electromagnetic theory.
- (b) According to Bohr, there is a definite energy associated with each stable orbit and an atom radiaties energy only when it makes a transition from one of these orbits to another. If the energy of electron in the higher orbit be E<sub>2</sub> and that in the lower orbit be E<sub>1</sub>, then the frequency v of the radiated waves is given by

$$hv = E_2 - E_1$$
$$v = \frac{E_2 - E_1}{h}$$

or

Bohr found that the magnitude of the electron's angular momentum is quantized, and this magnitude

for the electron must be integral multiple of  $\frac{h}{2\pi}$ . The magnitude of the angular momentum is L = mvr for a particle with mass m moving with speed v in a circle of radius r. So, according to Bohr's postulate,

$$mvr = \frac{nh}{2\pi}$$
 (n = 1, 2, 3....)

Each value of n corresponds to a permitted value of the orbit radius, which we will denote by r<sub>a</sub>. The value of n for each orbit is called **principal quantum number** for the orbit. Thus,

$$mv_n r_n = mvr = \frac{nh}{2\pi}$$
 ...(ii)

According to Newton's second law a radially inward centripetal force of magnitude  $F = \frac{mv^2}{r}$  is

needed by the electron which is being provided by the electrical attraction between the positive proton and the negative electron.

Thus.

$$\frac{mv_n^2}{r_n} = \frac{1}{4\pi\epsilon_0} \frac{e^2}{r_n^2} \qquad ....(iii)$$

Solving Eqs. (ii) and (iii), we get

$$r_n = \frac{\epsilon_0 n^2 h^2}{\pi m e^2} \qquad ...(iv)$$

and

$$v_n = \frac{e^2}{2\epsilon_0 nh} \qquad ...(v)$$

The smallest orbit radius corresponds to n = 1. We'll denote this minimum radius, called the **Bohr radius** as a<sub>0</sub>. Thus,

$$a_0 = \frac{\epsilon_0 h^2}{\pi m e^2}$$

Substituting values of  $\epsilon_{_0}$ , h, p, m and e, we get  $a_{_0}$  = 0.529 × 10<sup>-10</sup> m = 0.529 Å

$$a_0 = 0.529 \times 10^{-10} \text{ m} = 0.529 \text{ Å}$$
 ....(vi)

Eq. (iv), in terms of 
$$a_{_0}$$
 can be written as, 
$$r_{_n} = n^2 \, a_{_0} \qquad \text{or} \qquad r_{_n} \propto n^2 \qquad \qquad .... \text{(vii)}$$

Similarly, substituting values of e,  $\epsilon_0$  and h with n = 1 in Eq. (v), we get  $v_1$  = 2.19 × 10<sup>6</sup> m/s

$$v_1 = 2.19 \times 10^6 \text{ m/s}$$
 ....(viii)

This is the greatest possible speed of the electron in the hydrogen atom. Which is approximately equal to c/137 where c is the speed of light in vacuum.

Eq. (v), in terms of v<sub>1</sub> can be written as,

$$v_n = \frac{v_1}{n}$$
 or  $v_n \propto \frac{1}{n}$ 

**Energy levels**: Kinetic and potential energies  $K_n$  and  $U_n$  in nth orbit are given by

$$K_n = \frac{1}{2} m v_n^2 = \frac{me^4}{8 \epsilon_0^2 n^2 h^2}$$

and

$$U_n = -\frac{1}{4\pi\epsilon_0} \frac{e^2}{r_n} = -\frac{me^4}{4{\epsilon_0}^2 n^2 h^2}$$

(assuming infinity as a zero potential energy level)

The total energy E<sub>n</sub> is the sum of the kinetic and potential energies.

so, 
$$E_n = K_n + U_n = -\frac{me^4}{8{\epsilon_0}^2 n^2 h^2}$$
 Substituting values of m, e,  ${\epsilon_0}$  and h with n = 1, we get the least energy of the atom in first orbit, which

is -13.6 eV. Hence,

$$E_1 = -13.6 \text{ eV}$$
 ....(x)

and

$$E_n = \frac{E_1}{n^2} = -\frac{13.6}{n^2} \text{ eV}$$
 ....(xi)

Substituting n = 2, 3, 4, ...., etc., we get energies of atom in different orbits.

$$E_2 = -3.40 \text{ eV}, E_3 = -1.51 \text{ eV}, \dots E_{\infty} = 0$$

#### (i) **Hydrogen Like Atoms**

The Bohr model of hydrogen can be extended to hydrogen like atoms, i.e., one electron atoms, the nuclear charge is +ze, where z is the atomic number, equal to the number of protons in the nucleus. The effect in the previous analysis is to replace e<sup>2</sup> every where by ze<sup>2</sup>. Thus, the equations for, r<sub>n</sub>, v<sub>n</sub> and E<sub>n</sub> are altered as under:

$$r_n = \frac{\varepsilon_0 n^2 h^2}{nmze^2} = \frac{n^2}{z} a_0$$
 or  $r_n \propto \frac{n^2}{z}$  ....(i)

where

$$a_0 = 0.529 \text{ Å}$$

(radius of first orbit of H)

$$v_n = \frac{ze^2}{2\epsilon_0 nh} = \frac{z}{n} v_1$$
 or  $v_n \propto \frac{z}{n}$  ....(ii)

where

$$v_1 = 2.19 \times 10^6 \,\mathrm{m/s}$$

 $v_1 = 2.19 \times 10^6 \text{ m/s}$  (speed of electron in first orbit of H)

$$E_n = -\frac{mz^2e^4}{8\epsilon_0^2n^2h^2} = \frac{z^2}{n^2} E_1 \text{ or } E_n \propto \frac{z^2}{n^2}$$
 ....(iii)

where

$$E_1 = -13.60 \text{ eV}$$

(energy of atom in first orbit of H)

#### (ii) Definations valid for single electron system

(a) **Ground state:** Lowest energy state of any atom or ion is called ground state of the atom.

Ground state energy of H atom = -13.6 eV

Ground state energy of He<sup>+</sup> Ion = -54.4 eV

Ground state energy of Li<sup>++</sup> Ion = -122.4 eV

Excited State: State of atom other than the ground state are called its excited states. (b)

> first excited state n = 2n = 3second excited state third excited state noth excited state  $n = n_0 + 1$

**Ionisation energy (I.E.)**: Minimum energy required to move an electron from ground state to  $n = \infty$ (c) is called ionisation energy of the atom or ion

Ionisation energy of H atom = 13.6 eV

Ionisation energy of He<sup>+</sup> Ion = 54.4 eV

Ionisation energy of Li<sup>++</sup> Ion = 122.4 eV

Ionisation potential (I.P.): Potential difference through which a free electron must be accelerated (d) from rest such that its kinetic energy becomes equal to ionisation energy of the atom is called ionisation potential of the atom.

I.P of H atom = 13.6 V

I.P. of He+ Ion = 54.4 V

Excitation energy: Energy required to move an electron from ground state of the atom to any other (5) exited state of the atom is called excitation energy of that state.

Energy in ground state of H atom = -13.6 eV

Energy in first excited state of H-atom = -3.4 eV

Ist excitation energy = 10.2 eV.

Excitation Potential: Potential difference through which an electron must be accelerated from rest so that its kinetic energy becomes equal to excitation energy of any state is called excitation potential of that state.

Ist excitation energy = 10.2 eV.

Ist excitation potential = 10.2 V.

Binding energy or Seperation energy: Energy required to move an electron from any state to n **(f)**  $=\infty$  is called binding energy of that state. or energy released during formation of an H-like atom/ion from  $n = \infty$  to some particular n is called binding energy of that state.

Binding energy of ground state of H-atom = 13.6 eV

# SOLVED EXAMPLE

- Ex. 13 First excitation potential of a hypothetical hydrogen like atom is 15 volt. Find third excitation potential of the atom.
- Sol. Let energy of ground state =  $E_0$

$$E_0 = -13.6 \, Z^2 \, \text{eV}$$
 and

$$E_n = \frac{E_0}{n^2}$$

$$n = 2, E_2 = \frac{E_0}{4}$$

given 
$$\frac{\mathsf{E}_0}{4} - \mathsf{E}_0 = 15$$

$$-\frac{3E_0}{4} = 15$$

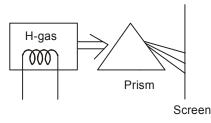
$$n = 4$$
,  $E_4 = \frac{E_0}{16}$ 

third exicitation energy = 
$$\frac{E_0}{16} - E_0 = -\frac{15}{16}E_0 = -\frac{15}{16}\cdot\left(\frac{-4\times15}{3}\right) = \frac{75}{4}$$
 eV

third excitation potential is  $\frac{75}{4}$  V



#### Emission spectrum of hydrogen atom: (iii)



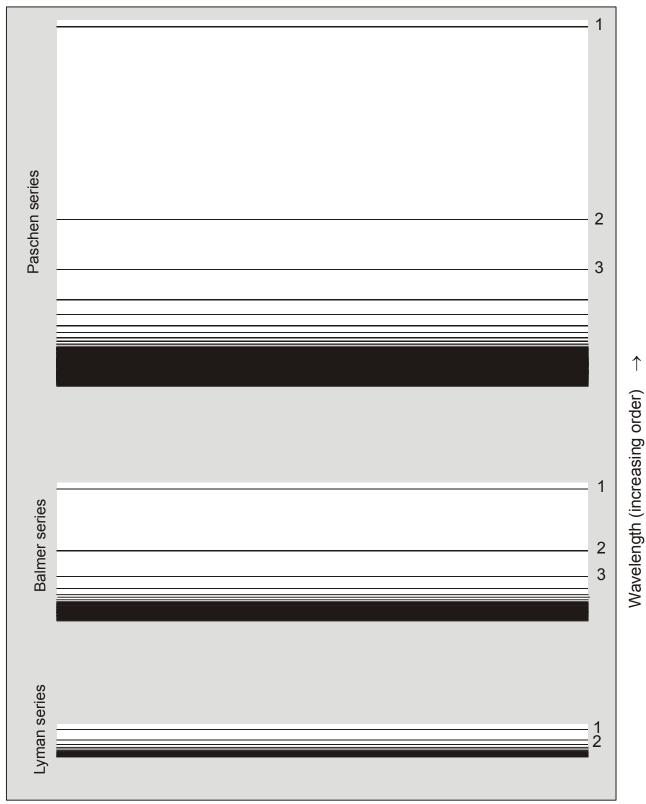
Under normal conditions the single electron in hydrogen atom stays in ground state (n = 1). It is excited to some higher energy state when it acquires some energy from external source. But it hardaly stays there for more than 10<sup>-8</sup> second.

A photon corresponding to a particular spectrum line is emitted when an atom makes a transition from a state in an excited level to a state in a lower excited level or the ground level.

Let n, be the initial and n, the final energy state, then depending on the final energy state following series are observed in the emission spectrum of hydrogen atom.

On Screen:

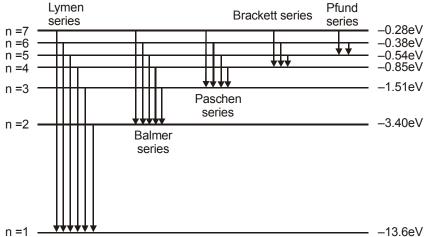
A photograph of spectral lines of the Lymen, Balmer, Paschen series of atomic hydrogen.



1, 2, 3..... represents the I, II & III line of Lymen, Balmer, Paschen series.

Name of series	Number of Line	Quantum Number			
		n <sub>i</sub> (Lower State	n <sub>f</sub> (Upper State)	Wavelength (nm)	Energy
Lymen	I	1	2	121.6	10.2 eV
	II	1	3	102.6	12.09 eV
	III	1	4	97	12.78 eV
	series limit	1	∞ (series limit)	91.2	13.6 eV
Balmer	I	2	3	656.3	1.89 eV
	II	2	4	486.1	2.55 eV
	III	2	5	434.1	2.86 eV
	series limit	2	∞ (series limit)	364.6	3.41 eV
Paschen	I	3	4	1875.1	0.66 eV
	II	3	5	1281.8	0.97 eV
	III	3	6	1093.8	1.13 eV
	series limit	3	∞ (series limit)	822	1.51 eV

**Series limit**: Line of any group having maximum energy of photon and minimum wavelength of that group is called series limit.



## For the Lymen series $n_r = 1$ , for Balmer series $n_r = 2$ and so on.

## (iv) Wavelength of Photon Emitted in De-excitation

According to Bohr when an atom makes a transition from higher energy level to a lower level it emits a photon with energy equal to the energy difference between the initial and final levels. If  $E_i$  is the initial energy of the atom before such a transition,  $E_f$  is its final energy after the transition, and the

photon's energy is  $h_V = \frac{hc}{\lambda}$ , then conservation of energy gives,

$$hv = \frac{hc}{\lambda} = E_i - E_f$$
 (energy of emitted photon) ....(i)

By 1913, the spectrum of hydrogen had been studied intensively. The visible line with longest wavelength, or lowest frequency is in the red and is called  $H_{\alpha}$ , the next line, in the blue-green is called  $H_{\beta}$  and so on.

In 1885, Johann Balmer, a Swiss teacher found a formula that gives the wave lengths of these lines. This is now called the Balmer series. The Balmer's formula is,

$$\frac{1}{\lambda} = R\left(\frac{1}{2^2} - \frac{1}{n^2}\right)$$
 ....(ii)

Here, n = 3, 4, 5 ...., etc.

R = Rydberg constant =  $1.097 \times 10^7 \,\mathrm{m}^{-1}$ 

and  $\lambda$  is the wavelength of light/photon emitted during transition,

For n = 3, we obtain the wavelength of  $H_{\alpha}$  line.

Similarly, for n = 4, we obtain the wavelength of  $H_g$  line. For n =  $\infty$ , the smallest wavelength (= 3646

Å) of this series is obtained. Using the relation, E =  $\frac{hc}{\lambda}$  we can find the photon energies correspond-

ing to the wavelength of the Balmar series.

$$E = \frac{hc}{\lambda} = hcR\left(\frac{1}{2^2} - \frac{1}{n^2}\right) = \frac{Rhc}{2^2} - \frac{Rhc}{n^2}$$

This formula suggests that,

$$E_n = -\frac{Rhc}{n^2}$$
, n = 1, 2, 3..... ....(iii)

The wavelengths corresponding to other spectral series (Lymen, Paschen, (etc.) can be represented by formula similar to Balmer's formula.

Lymen Series : 
$$\frac{1}{\lambda} = R\left(\frac{1}{1^2} - \frac{1}{n^2}\right)$$
, n = 2, 3, 4.....

Paschen Series : 
$$\frac{1}{\lambda} = R \left( \frac{1}{3^2} - \frac{1}{n^2} \right)$$
, n = 4, 5, 6.....

Brackett Series : 
$$\frac{1}{\lambda} = R\left(\frac{1}{4^2} - \frac{1}{n^2}\right)$$
, n = 5, 6, 7.....

Pfund Series : 
$$\frac{1}{\lambda} = R\left(\frac{1}{5^2} - \frac{1}{n^2}\right)$$
, n = 6, 7, 8

The Lymen series is in the ultraviolet, and the Paschen. Brackett and Pfund series are in the infrared region.

# SOLVED EXAMPLE

**Ex. 14** Calculate (a) the wavelength and (b) the frequency of the H<sub>B</sub> line of the Balmer series for hydrogen.

**Sol.** (a)  $H_{\beta}$  line of Balmer series corresponds to the transition from n = 4 to n = 2 level. The corresponding wavelength for  $H_{\beta}$  line is,

$$\frac{1}{\lambda} = (1.097 \times 10^7) \left( \frac{1}{2^2} - \frac{1}{4^2} \right)$$

$$= 0.2056 \times 10^7$$

∴ 
$$\lambda = 4.9 \times 10^{-7} \,\text{m}$$
 Ans.

(b) 
$$v = \frac{c}{\lambda} = \frac{3.0 \times 10^8}{4.9 \times 10^{-7}}$$

$$= 6.12 \times 10^{14} \text{ Hz}$$

Ans.

**Ex. 15** Find the largest and shortest wavelengths in the Lymen series for hydrogen. In what region of the electromagnetic spectrum does each series lie?

**Sol.** The transition equation for Lymen series is given by,

$$\frac{1}{\lambda} = R \left[ \frac{1}{(1)^2} - \frac{1}{n^2} \right]$$
  $n = 2, 3, \dots$ 

for largest wavelength, n = 2

$$\frac{1}{\lambda_{\text{max}}} = 1.097 \times 10^{7} \left( \frac{1}{1} - \frac{1}{4} \right) = 0.823 \times 10^{7}$$

$$\lambda_{\text{max}} = 1.2154 \times 10^{-7} \text{ m} = 1215 \text{ Å}$$
 Ans.

The shortest wavelength corresponds to  $n = \infty$ 

$$\frac{1}{\lambda_{max}} = 1.097 \times 10^7 \left( \frac{1}{1} - \frac{1}{\infty} \right)$$

or  $\lambda_{min} = 0.911 \times 10^{-7} \text{ m} = 911 \text{ Å}$  Ans.

Both of these wavelengths lie in ultraviolet (UV) region of electromagnetic spectrum.

**Ex. 16** How may different wavelengths may be observed in the spectrum from a hydrogen sample if the atoms are excited to states with principal quantum number n?

**Sol.** From the nth state, the atom may go to (n - 1)th state, ...., 2nd state or 1st state. So there are (n - 1) possible transitions starting from the nth state. The atoms reaching (n - 1)th state may make (n - 2) different transitions. Similarly for other lower states. The total number of possible transitions is

$$(n-1) + (n-2) + (n-3) + \dots + 2 + 1$$

$$= \frac{n(n-1)}{2}$$
 (Remember)

- **Ex. 17** (a) Find the wavelength of the radiation required to excite the electron in Li<sup>++</sup> from the first to the third Bohr orbit.
  - (b) How many spectral linea are observed in the emission spectrum of the above excited system?
- **Sol.** (a) The energy in the first orbit =  $E_1 = Z^2 E_0$  where  $E_0 = -13.6$  eV is the energy of a hydrogen atom in ground state thus for Li<sup>++</sup>,

$$E_1 = 9E_0 = 9 \times (-13.6 \text{ eV})$$
 = -122.4 eV

The energy in the third orbit is

$$E_3 = \frac{E_1}{n^2} = \frac{E_1}{9} = -13.6 \text{ eV}$$

Thus, 
$$E_3 - E_1 = 8 \times 13.6 \text{ eV} = 108.8 \text{ eV}.$$

Energy required to excite Li\*\* from the first orbit to the third orbit is given by

$$E_3 - E_1 = 8 \times 13.6 \text{ eV} = 108.8 \text{ eV}.$$

The wavelength of radiation required to excite Li\*\* from the first orbit to the third orbit is given by

$$\frac{hc}{\lambda} = E_3 - E_1$$

or, 
$$\lambda = \frac{hc}{E_3 - E_1}$$

$$= \frac{1240 \, eV - nm}{108.8 \, eV} \approx 11.4 \, nm$$

- (b) The spectral lines emitted are due to the transitions  $n = 3 \rightarrow n = 2$ ,  $n = 3 \rightarrow n = 1$  $n = 2 \rightarrow n = 1$ . Thus, there will be three spectral lines in the spectrum. and
- Ex. 18 Find the kinetic energy potential energy and total energy in first and second orbit of hydrogen atom if potential energy in first orbit is taken to be zero.

**Sol.** 
$$E_1 = -13.60 \text{ eV}$$

$$K_1 = -E_1 = 13.60 \text{ eV}$$

$$U_1 = 2E_1 = -27.20 \text{ eV}$$

$$E_2 = \frac{E_1}{(2)^2} = -3.40 \text{ eV}$$
  $K_2 = 3.40 \text{ eV}$  and  $U_2 = -6.80 \text{ eV}$ 

$$\zeta_2 = 3.40 \text{ eV}$$

$$U_{3} = -6.80 e^{-1}$$

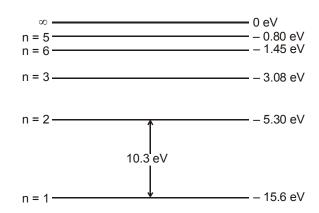
Now U<sub>1</sub> = 0, i.e., potential energy has been increased by 27.20 eV while kinetic energy will remain unchanged. So values of kinetic energy, potential energy and total energy in first orbit are 13.60 eV, 0, 13.60 respectively and for second orbit these values are 3.40 eV, 20.40 eV and 23.80 eV.

- Ex. 19 A lithium atom has three electrons, Assume the following simple picture of the atom. Two electrons move close to the nucleus making up a spherical cloud around it and the third moves outside this cloud in a circular orbit. Bohr's model can be used for the motion of this third electron but n = 1 states are not available to it. Calculate the ionization energy of lithium in ground state using the above picture.
- Sol. In this picture, the third electron moves in the field of a total charge + 3e - 2e = + e. Thus, the energies are the same as that of hydrogen atoms. The lowest energy is:

$$E_2 = \frac{E_1}{4} = \frac{-13.6 \text{ eV}}{4} = -3.4 \text{ eV}$$

Thus, the ionization energy of the atom in this picture is 3.4 eV.

- **Ex. 20** The energy levels of a hypothetical one electron atom are shown in the figure.
  - (a) Find the ionization potential of this atom.
  - Find the short wavelength limit of the se-(b) ries terminating at n = 2
  - Find the excitation potential for the state (c) n = 3.
  - Find wave number of the photon emitted (d) for the transition n = 3 to n = 1.
  - What is the minimum energy that an elec-(e) tron will have after interacting with this atom in the ground state if the initial kinetic energy of the electron is
    - 6 eV (i)
- (ii) 11 eV



**Sol.** (a) Ionization potential = 15.6 V

(b) 
$$\lambda_{min} = \frac{12400}{5.3} = 2340 \text{ Å}$$

(c) 
$$\Delta E_{31} = -3.08 - (-15.6) = 12.52 \text{ eV}$$

Therefore, excitation potential for state n = 3 is 12.52 volt.

(d) 
$$\frac{1}{\lambda_{31}} = \frac{\Delta E_{31}}{12400} \quad \mathring{A}^{-1} = \frac{12.52}{12400} \mathring{A}^{-1}$$

$$\approx 1.01 \times 10^7 \, m^{-1}$$

(e) (i) 
$$E_2 - E_1 = 10.3 \text{ eV} > 6 \text{ eV}.$$

Hence electron cannot excite the atoms. So,  $K_{min} = 6$  eV.

(ii) 
$$E_2 - E_1 = 10.3 \text{ eV} < 11 \text{ eV}.$$

Hence electron can excite the atoms. So,  $K_{min} = (11 - 10.3) = 0.7 \text{ eV}$ .

- **Ex. 21** A small particle of mass m moves in such a way that the potential energy U = ar<sup>2</sup> where a is a constant and r is the distance of the particle from the origin. Assuming Bohr's model of quantization of angular momentum and circular orbits, find the radius of n<sup>th</sup> allowed orbit.
- **Sol.** The force at a distance r is,

$$F = -\frac{dU}{dr} = -2ar$$

Suppose r be the radius of nth orbit. The necessary centripetal force is provided by the above force. Thus,

$$\frac{mv^2}{r}$$
 = 2ar

Further, the quantization of angular momentum gives,

$$mvr = \frac{nh}{2\pi}$$

Solving Eqs. (i) and (ii) for r, we get

$$r = \left(\frac{n^2h^2}{8am\pi^2}\right)^{1/4}$$
 Ans.

- Ex. 22 An imaginary particle has a charge equal to that of an electron and mass 100 times the mass of the electron. It moves in a circular orbit around a nucleus of charge + 4e. Take the mass of the nucleus to be infinite. Assuming that the Bohr's model is applicable to the system.
  - (a) Derive and expression for the radius of n<sup>th</sup> Bohr orbit.
  - (b) Find the wavelength of the radiation emitted when the particle jumps from fourth orbit to the second.

$$\frac{m_p v^2}{r_n} = \frac{1}{4\pi\epsilon_0} \frac{ze^2}{r_n^2} \qquad \qquad .....(i)$$

The quantization of angular momentum gives,

$$m_p vr_n = \frac{nh}{2\pi}$$
 .....(ii)

Solving Eqs. (i) and (ii), we get

$$r = \frac{n^2 h^2 \varepsilon_0}{z \pi m_p e^2}$$

Substituting  $m_p = 100 \text{ m}$ where m = mass of electron and z = 4

we get,  $r_n = \frac{n^2 h^2 \epsilon_0}{400 \, \pi m e^2} \quad \text{Ans.}$ 

(b) As we know, Energy of hydrogen atom in ground state = - 13.60 eV

and  $E_{_{n}} \propto \left(\frac{z^{2}}{n^{2}}\right)\!m$ 

For the given particle,  $E_4 = \frac{(-13.60)(4)^2}{(4)^2} \times 100 = -1360 \text{ eV}$ 

and  $E_2 = \frac{(-13.60)(4)^2}{(2)^2} \times 100 = -5440 \text{ eV}$   $\Delta E = E_4 - E_2 = 4080 \text{ eV}$ 

 $\lambda (in \, \text{Å}) = \frac{12400}{4080} = 3.0 \, \text{Å}$  Ans.

Ex. 23 A particle known as  $\mu$ -meason, has a charge equal to that of an electron and mass 208 times the mass of the electron. It moves in a circular orbit around a nucleus of charge +3e. Take the mass of the nucleus to be infinite. Assuming that the Bohr's model is applicable to this system, (a) derive an expression for the radius of the nth Bohr orbit, (b) find the value of n for which the radius of the orbit is approximately the same as that of the first Bohr orbit for a hydrogen atom and (c) find the wavelength of the radiation emitted when the  $\mu$ -meson jumps from the third orbit to the first orbit.

Sol. (a) We have,

or,

$$\frac{mv^2}{r} = \frac{Ze^2}{4\pi\epsilon_0 r^2}$$
 
$$v^2 r == \frac{Ze^2}{4\pi\epsilon_0 m} \qquad ...(i)$$

The quantization rule is  $vr = \frac{nh}{2\pi m}$ 

The radius is  $r = \frac{(vr)^2}{v^2r} = \frac{4\pi\epsilon_0 m}{Ze^2}$   $= \frac{n^2h^2\epsilon_0}{Z\pi me^2} \qquad ....(ii)$ 

For the given system, Z = 3 and  $m = 208 m_a$ .

Thus  $r_{\mu} = \frac{n^2 h^2 \epsilon_0}{624 \pi m_e e^2} \label{eq:rmu}$ 

(b) From (ii), the radius of the first Bohr orbit for the hydrogen atom is

$$r_h = \frac{h^2 \epsilon_0}{\pi m_e e^2}$$

For 
$$r_{\mu} = r_{h}$$
, 
$$\frac{n^{2}h^{2}\epsilon_{0}}{624\pi m_{e}e^{2}} = \frac{h^{2}\epsilon_{0}}{\pi m_{e}e^{2}}$$

or, 
$$n^2 = 624$$
  
or,  $n = 25$ 

(c) From (i), the kinetic energy of the atom is

$$\frac{mv^2}{2} = \frac{Ze^2}{8\pi\epsilon_0 r}$$

and the potential energy is –  $\frac{Ze^2}{4\pi\epsilon_0 r}$ 

The total energy is  $E_n = \frac{Ze^2}{8\pi\epsilon_0 r}$ 

$$\text{Using (ii)}, \qquad \quad \mathsf{E}_{_{n}} = - \; \frac{\mathsf{Z}^{2} \pi m e^{4}}{8 \pi \epsilon_{0}^{2} n^{2} h^{2}} \; = - \; \frac{9 \times 208 m_{_{e}}^{\; \; 4}}{8 \epsilon_{0}^{2} n^{2} h^{2}} \; = \; \frac{1872}{n^{2}} \; \left( - \frac{m_{_{e}} e^{4}}{8 \epsilon_{0}^{2} \, h^{2}} \right)$$

But  $\left(-\frac{m_e e^4}{8\epsilon_0^2 h^2}\right)$  is the ground state energy of hydrogen atom and hence is equal to - 13.6 eV.

From (iii), 
$$E_n = -\frac{1872}{n^2} \times 13.6 \text{ eV} = \frac{-25459.2 \text{ eV}}{n^2}$$

Thus,  $E_1 = -25459.2$  eV and  $E_3 = \frac{E_1}{Q} = -2828.8$  eV. The energy difference is  $E_3 - E_1 = 22630.4$ eV.

The wavelength emitted is

$$\lambda = \frac{hc}{\Delta E} = \frac{1240 \,\text{eV} - \text{nm}}{22630.4 \,\text{eV}} = 55 \,\text{pm}.$$

- **Ex. 24** A gas of hydrogen like atoms can absorb radiations of 68 eV. Consequently, the atoms emit radiations of only three different wavelength. All the wavelengths are equal or smaller than that of the absorbed photon.
  - (a) Determine the initial state of the gas atoms.
  - (b) Identify the gas atoms.
  - (c) Find the minimum wavelength of the emitted radiations.
  - (d) Find the ionization energy and the respective wavelength for the gas atoms.

**Sol.** (a) 
$$\frac{n(n-1)}{2} = 3$$

i.e., after excitation atom jumps to second excited state.

Hence 
$$n_r = 3$$
. So  $n_i$  can be 1 or 2

If  $n_i = 1$  then energy emitted is either equal to, greater than or less than the energy absorbed.

Hence the emitted wavelength is either equal to, less than or greater than the absorbed wavelength.

Hence  $n_i \neq 1$ .

If 
$$n_i = 2$$
, then  $E_e \ge E_a$ . Hence  $\lambda_e \le \lambda_0$ 

(b) 
$$E_3 - E_2 = 68 \text{ eV}$$

$$\therefore (13.6) (Z^2) \left( \frac{1}{4} - \frac{1}{9} \right) = 68$$

$$\therefore$$
 Z = 6

(c) 
$$\lambda_{\min} = \frac{12400}{E_3 - E_1} = \frac{12400}{(13.6)(6)^2 \left(1 - \frac{1}{9}\right)} = \frac{12400}{435.2} = 28.49$$
 Ans.

(d) Ionization energy = 
$$(13.6)(6)^2 = 489.6 \text{ eV}$$
 Ans.

$$\lambda = \frac{12400}{489.6}$$
 = 25.33 Å **Ans.**

- Ex. 25 An electron is orbiting in a circular orbit of radius r under the influence of a constant magnetic field of strength B. Assuming that Bohr's postulate regarding the quantisation of angular momentum holds good for this electron, find
  - the allowed values of the radius 'r' of the orbit. (a)
  - (b) the kinetic energy of the electron in orbit
  - (c) The potential energy of interaction between the magnetic moment of the orbital current due to the electron moving in its orbit and the magnetic field B.
  - The total energy of the allowed energy levels. (d)
- Sol. (a) radius of circular path

$$r = \frac{mv}{Be} \qquad \qquad ....(i)$$

$$mvr = \frac{nh}{2\pi} \qquad ....(ii)$$

Solving these two equations, we get

$$r = \sqrt{\frac{nh}{2\pi Be}}$$
 and  $v = \sqrt{\frac{nhBe}{2\pi m^2}}$ 

(b) 
$$K = \frac{1}{2} mv^2 = \frac{nhBe}{4\pi m}$$
 Ans.

(c) 
$$M = iA = \left(\frac{e}{T}\right) (\pi r^2) = \frac{evr}{2}$$

$$= \frac{e}{2} \sqrt{\frac{nh}{2\pi Be}} \sqrt{\frac{nhBe}{2\pi m^2}} = \frac{nhe}{4\pi m}$$

Now potential energy U = -M.B

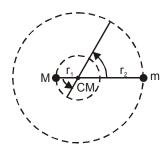
$$= \frac{\text{nheB}}{4\pi \text{m}}$$

(d) 
$$E = U + K = \frac{\text{nheB}}{2\pi m}$$



# 11. EFFECT OF NUCLEUS MOTION ON ENERGY OF ATOM

Let both the nucleus of mass M, charge Ze and electron of mass m, and charge e revolve about their centre of mass (CM) with same angular velocity  $(\omega)$  but different linear speeds. Let  $r_{_1}$  and  $r_{_2}$  be the distance of CM from nucleus and electron. Their angular velocity should be same then only their separation will remain unchanged in an energy level.



Let r be the distance between the nucleus and the electron. Then

$$Mr_1 = mr_2$$
$$r_1 + r_2 = r$$

$$\therefore \qquad \qquad r_{_{1}} = \frac{mr}{M+m} \qquad \text{ and } \qquad$$

$$r_2 = \frac{Mr}{M+m}$$

Centripetal force to the electron is provided by the electrostatic force. So,

$$mr_2\omega^2 = \frac{1}{4\pi\epsilon_0} \frac{Ze^2}{r^2}$$

or 
$$m \left( \frac{Mr}{M+m} \right) \, \omega^2 = \, \frac{1}{4\pi\epsilon_0} \; . \; \frac{Ze^2}{r^2} \label{eq:mass}$$

or 
$$\left( \frac{Mm}{M+m} \right) \, r^3 \, \omega^2 = \, \frac{Ze^2}{4\pi\epsilon_0}$$

or 
$$\mu r^3 \omega^2 = \frac{e^2}{4\pi\epsilon_0}$$

where 
$$\frac{Mm}{M+m} = \mu$$

Moment of inertia of atom about CM,

$$I = Mr_{_{1}}{}^{2} + mr_{_{2}}{}^{2} = \left(\frac{Mm}{M+m}\right) \, r^{2} = \mu r^{2}$$

According to Bohr's theory,  $\frac{\text{nh}}{2\pi} = I \omega$ 

or 
$$\mu r^2 \omega = \frac{nh}{2\pi}$$

Solving above equations for r, we get

$$r = \frac{\varepsilon_0 n^2 h^2}{\pi \mu e^2 Z}$$
 and  $r = (0.529 \text{ Å}) \frac{n^2}{Z} \cdot \frac{m}{\mu}$ 

Further electrical potential energy of the system,

$$U=\frac{-Ze^2}{4\pi\epsilon_0 r} \qquad \qquad U=\frac{-Z^2e^4\mu}{4\epsilon_0^2n^2h^2} \label{eq:U}$$

and kinetic energy, 
$$K = \frac{1}{2} \ \mathrm{I} \omega^2 = \frac{1}{2} \ \mu r^2 \ \omega^2 \quad \text{ and } \quad K = \frac{1}{2} \ \mu v^2$$

v-speed of electron with respect to nucleus. ( $v = r\omega$ )

here 
$$\omega^2 = \frac{Ze^2}{4\pi\epsilon_0~\mu r^3}$$

$$\label{eq:K} \text{K} = \frac{Ze^2}{8\pi\epsilon_0 r} \qquad = \qquad \frac{Z^2e^4\mu}{8\pi\epsilon_0^2n^2h^2}$$

 $\therefore$  Total energy of the system  $E_n = K + U$ 

$$E_n = -\frac{\mu e^4}{8\epsilon_0^2 n^2 h^2}$$

this expression can also be written as

$$E_n = - (13.6 \text{ eV}) \frac{Z^2}{n^2} \cdot \left(\frac{\mu}{m}\right)$$

The expression for  $E_n$  without considering the motion of proton is  $E_n = -\frac{me^4}{8{\epsilon_0}^2 n^2 h^2}$ , i.e., m is replaced by  $\mu$  while considering the motion of nucleus.

# SOLVED EXAMPLE \_

- **Ex. 26** A positronium 'atom' is a system that consists of a positron and an electron that orbit each other. Compare the wavelength of the spectral lines of positronium with those of ordinary hydrogen.
- **Sol.** Here the two particle have the same mass m, so the reduced mass is

$$\mu = \frac{mM}{m+M} = \frac{m^2}{2m} = \frac{m}{2}$$

where m is the electron mass. We know that  $E_n \propto m$ 

$$\therefore \qquad \frac{E'_n}{E_n} = \frac{\mu}{m} = \frac{1}{2} \qquad \text{energy of each level is halved.} \ \therefore \ \text{Their difference will also be halved.}$$

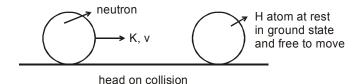
Hence  $\lambda'_n = 2\lambda_n$ 

#### 12. ATOMIC COLLISION

In such collisions assume that the loss in the kinetic energy of system is possible only if it can excite or ionise.

# SOLVED EXAMPLE

Ex. 27



What will be the type of collision, if K = 14eV, 20.4 eV, 22 eV, 24.18 eV

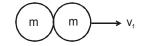
(elastic/inelastic/perectly inelastic)

**Sol.** Loss in energy ( $\Delta E$ ) during the collision will be used to excite the atom or electron from one level to another. According to quantum Mechanics, for hydrogen atom.

$$\Delta E = \{0, 10.2 \text{ eV}, 12.09 \text{ eV}, \dots, 13.6 \text{ eV}\}$$

According to Newtonion mechanics

for maximum loss collision will be perfectly inelastic



if neutron collides perfectly inelastically

then, Applying momentum conservation

$$mv_0 = 2mv_f$$

$$v_f = \frac{v_0}{2}$$

final K.E. = 
$$\frac{1}{2} \times 2m \times \frac{v_0^2}{4}$$

$$= \frac{\frac{1}{2}mv_0^2}{2} = \frac{K}{2}$$

maximum loss =  $\frac{K}{2}$ 

According to classical mechanics ( $\Delta E$ ) = [0,  $\frac{K}{2}$ ]

(a) If K = 14 eV, According to quantum mechanics

$$(\Delta E) = \{0, 10.2eV, 12.09 eV\}$$

According to classical mechanics

$$\Delta E = [0, 7 \text{ eV}]$$

loss = 0, hence it is elastic collision speed of particle changes.

4m He<sup>+</sup>

(b) If 
$$K = 20.4 \text{ eV}$$

According to classical mechanics

$$loss = [0, 10.2 eV]$$

According to quantum mechanics

(c) If 
$$K = 22 \text{ eV}$$

Classical mechanics  $\Delta E = [0, 11]$ 

Quantum mechanics  $\Delta E = \{0, 10.2eV, 12.09eV, \dots \}$ 

loss = 0 elastic collision loss = 10.2 eV inelastic collsion

(d) If K = 24.18 eV

According to classical mechanics  $\Delta E = [0, 12.09eV]$ 

According to quantum mechanics  $\Delta E = \{0, 10.2eV, 12.09eV, \dots 13.6eV\}$ 

loss = 0 elastic collision loss = 10.2 eV inelastic collision

loss = 12.09 eV perfectly inelastic collision

- **Ex. 28** A He<sup>+</sup> ion is at rest and is in ground state. A neutron with initial kinetic energy K collides head on with the He<sup>+</sup> ion. Find minimum value of K so that there can be an inelastic collision between these two particle.
- **Sol.** Here the loss during the collision can only be used to excite the atoms or electrons.

So according to quantum mechanics

$$E_n = -13.6 \frac{Z^2}{n^2} \text{ eV}$$

Now according to newtonion mechanics

Minimum loss = 0

maximum loss will be for perfectly inelastic collision.

let  $v_0$  be the initial speed of neutron and  $v_1$  be the final common speed.

so by momentum conservation  $mv_0 = mv_f + 4mv_f$ 

$$v_f = \frac{v_0}{5}$$

where m = mass of Neutron

∴ mass of He<sup>+</sup> ion = 4m

so final kinetic energy of system

K.E. = 
$$\frac{1}{2}$$
 m  $v_f^2 + \frac{1}{2}$  4m  $v_f^2$  =  $\frac{1}{2}$ .(5m). $\frac{v_0^2}{25}$  =  $\frac{1}{5}$ .( $\frac{1}{2}$ m $v_0^2$ ) =  $\frac{K}{5}$ 

$$\text{maximum loss} = K - \frac{K}{5} = \frac{4K}{5}$$

so loss will be 
$$\left[0, \frac{4K}{5}\right]$$
 ....(2)

or

For inelastic collision there should be at least one common value other than zero in set (1) and (2)

$$\therefore \frac{4K}{5} > 40.8 \text{ eV}$$

minimum value of K = 51 eV.

- Ex. 29 A moving hydrogen atom makes a head on collision with a stationary hydrogen atom. Before collision both atoms are in ground state and after collision they move together. What is the minimum value of the kinetic energy of the moving hydrogen atom, such that one of the atoms reaches one of the excitation state.
- Let K be the kinetic energy of the moving hydrogen atom and K', the kinetic energy of combined mass after Sol. collision.

From conservation of linear momentum,

 $p = p' \text{ or } \sqrt{2Km} = \sqrt{2K'(2m)}$ K = 2K' ....(i)  $K = K' + \Delta E$  ....(ii) ....(i)  $\Delta E = 10.2 \text{ eV}$ From conservation of energy,

Solving Eqs. (i) and (ii), we get  $\Delta E = \frac{K}{2}$ 

Now minimum value of  $\Delta E$  for hydrogen atom is 10.2 eV.

 $\Delta E \geq 10.2 \text{ eV}$ or

$$\therefore \qquad \qquad \frac{K}{2} \geq 10.2$$

Therefore, the minimum kinetic energy of moving hydrogen is 20.4 eV Ans.

- Ex. 30 A neutron moving with speed v makes a head-on collision with a hydrogen atom in ground state kept at rest. Find the minimum kinetic energy of the neutron for which inelastic (completely or partially) collision may take place. The mass of neutron = mass of hydrogen =  $1.67 \times 10^{-27}$  kg.
- Suppose the neutron and the hydrogen atom move at speed v<sub>1</sub> and v<sub>2</sub> after the collision. The collision will be Sol. inelastic if a part of the kinetic energy is used to excite the atom. Suppose an energy  $\Delta E$  is used in this way. Using conservation of linear momentum and energy.

$$mv = mv_1 + mv_2$$
 ....(i)

and 
$$\frac{1}{2} \text{ mv}^2 = \frac{1}{2} \text{ mv}_1^2 + \frac{1}{2} \text{ mv}_2^2 + \Delta E$$
 ....(ii)

From (i), 
$$v^2 = v_1^2 + v_2^2 + 2v_1v_2^2$$
,

From (ii), 
$$V^2 = V_1^2 + V_2^2 + \frac{2\Delta E}{m}$$

Thus, 
$$2v_1v_2 = \frac{2\Delta E}{m}$$

Hence, 
$$(v_1 - v_2)^2 - 4v_1v_2 = v^2 - \frac{4\Delta E}{m}$$

As 
$$v_1 - v_2$$
 must be real,  $v^2 - \frac{4\Delta E}{m} \ge 0$ 

or, 
$$\frac{1}{2} \text{ mv}^2 > 2\Delta \text{E}.$$

The minimum energy that can be absorbed by the hydrogen atom in ground state to go in an excited state is 10.2 eV. Thus, the minimum kinetic energy of the neutron needed for an inelastic collision is

$$\frac{1}{2}mv_{min}^2 = 2 \times 10.2 \, eV = 20.4 \, eV$$

- Ex. 31 How many head-on, elastic collisions must a neutron have with deuterium nucleus to reduce its energy from 1 MeV to 0.025 eV.
- **Sol.** Let mass of neutron = m and mass of deuterium = 2m

initial kinetic energy of neutron = K<sub>o</sub>

Let after first collision kinetic energy of neutron and deuterium be K<sub>1</sub> and K<sub>2</sub>.

Using C.O.L.M. along direction of motion

$$\sqrt{2mK_0} = \sqrt{2mK_1} + \sqrt{4mK_2}$$

velocity of seperation = velocity of approach

$$\frac{\sqrt{4mK_2}}{2m} - \frac{\sqrt{2mK_1}}{m} = \frac{\sqrt{2mK_0}}{m}$$

Solving equaiton (i) and (ii) we get

$$K_1 = \frac{K_0}{9}$$

Loss in kinetic energy after first collision

$$\Delta K_1 = K_0 - K_1$$

$$\Delta K_1 = \frac{8}{9} K_0$$
 ..... (1)

After second collision

$$\Delta K_2 = \frac{8}{9} K_1 = \frac{8}{9} \cdot \frac{K_0}{9}$$

:. Total energy loss

$$\Delta K = \Delta K_1 + \Delta K_2 + \dots + \Delta K_n$$

As, 
$$\Delta K = \frac{8}{9} K_0 + \frac{8}{9^2} K_0 + \dots + \frac{8}{9^n} K_0$$

$$\Delta K = \frac{8}{9} K_0 (1 + \frac{1}{9} + \dots + \frac{1}{9^{n-1}})$$

$$\frac{\Delta K}{K_0} = \frac{8}{9} \left[ \frac{1 - \frac{1}{9^n}}{1 - \frac{1}{9}} \right] = 1 - \frac{1}{9^n}$$

$$\Delta K = (10^6 - 0.025) \text{ eV}$$

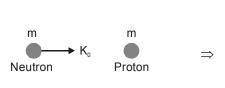
$$\frac{1}{9^{n}} = \frac{K_{0} - \Delta K}{K_{0}} = \frac{0.025}{10^{6}} \qquad \text{or} \qquad 9^{n} = 4 \times 10^{7}$$

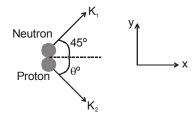
or 
$$9^n = 4 \times 10^7$$

Taking log both sides and solving, we get

$$n = 8$$

- Ex. 32 A neutron with an energy of 4.6 MeV collides with protons and is retarded. Assuming that upon each collision neutron is deflected by 45° find the number of collisions which will reduce its energy to 0.23 eV.
- Sol. Mass of neutron ≈ mass of proton = m





From conservation of momentum in y-direction

$$\sqrt{2mK_1} \sin 45^\circ = \sqrt{2mK_2} \sin \theta$$
 ....(i)

In x-direction

$$\sqrt{2mK_0} - \sqrt{2mK_1} \cos 45^\circ = \sqrt{2mK_2} \cos \theta$$
 ....(ii

Squaring and adding equation (i) and (ii), we have

$$K_2 = K_1 + K_0 - \sqrt{2K_0K_1}$$
 ....(iii)

From conservation of energy

$$K_2 = K_0 - K_1 \qquad \dots (iv)$$

Solving equations (iii) and (iv), we get

$$K_1 = \frac{K_0}{2}$$

i.e., after each collision energy remains half. Therefore, after n collisions,

$$K_n = K_0 \left(\frac{1}{2}\right)^n$$

$$0.23 = (4.6 \times 10^6) \left(\frac{1}{2}\right)^n$$

$$2^n = \frac{4.6 \times 10^6}{0.23}$$

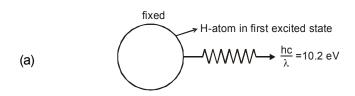
Taking log and solving, we get

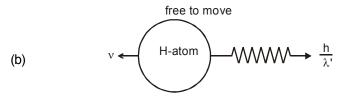
Ans.



### Calculation of recoil speed of atom on emission of a photon

momentum of photon =  $mc = \frac{h}{\lambda}$ 





m - mass of atom

According to momentum conservation

$$mv = \frac{h}{\lambda'}$$
 .... (i)

According to energy conservation

$$\frac{1}{2}mv^2 + \frac{hc}{\lambda'} = 10.2 \text{ eV}$$

Since mass of atom is very large than photon

hence  $\frac{1}{2}mv^2$  can be neglected

$$\frac{hc}{\lambda'} = 10.2 \text{ eV}$$

$$\frac{h}{\lambda} = \frac{10.2}{c} \text{ eV}$$

$$mv = \frac{10.2}{c} \text{ eV}$$

$$v = \frac{10.2}{cm}$$

recoil speed of atom =  $\frac{10.2}{\text{cm}}$ 

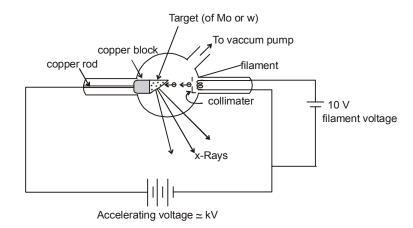


#### 13. X-RAYS

It was discovered by **ROENTGEN**. The wavelength of x-rays is found between 0.1 Å to 10 Å. These rays are invisible to eye. They are electromagnetic waves and have speed  $c = 3 \times 10^8$  m/s in vacuum. Its photons have energy around 1000 times more than the visible light.

When fast moving electrons having energy of order of several KeV strike the metallic target then x-rays are produced.

### Production of x-rays by coolidge tube :



The melting point, specific heat capacity and atomic number of target should be high. When voltage is applied across the filament then filament on being heated emits electrons from it. Now for giving the beam shape of electrons, collimator is used. Now when electron strikes the target then x-rays are produced.

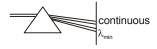
When electrons strike with the target, some part of energy is lost and converted into heat. Since, target should not melt or it can absorb heat so that the melting point, specific heat of target should be high.

Here copper rod is attached so that heat produced can go behind and it can absorb heat and target does not get heated very high.

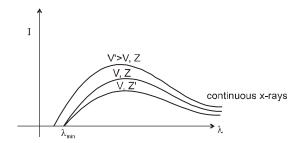
For more energetic electron, accelerating voltage is increased.

For more no. of photons voltage across filament is increased.

The x-ray were analysed by mostly taking their spectrum



## Variation of Intensity of x-rays with $\lambda$ is plotted as shown in figure :



The minimum wavelength corresponds to the maximum energy of the x-rays which in turn is equal to the maximum kinetic energy eV of the striking electrons thus

$$eV = hv_{max} = \frac{hc}{\lambda_{min}}$$

$$\lambda_{min} = \frac{hc}{eV} = \frac{12400}{V(involts)} \text{ Å}.$$

We see that cutoff wavelength  $\lambda_{min}$  depends only on accelerating voltage applied between target and filament. It does not depend upon material of target, it is same for two different metals (Z and Z')

# SOLVED EXAMPLE

- **Ex. 33** An X-ray tube operates at 20 kV. A particular electron loses 5% of its kinetic energy to emit an X-ray photon at the first collision. Find the wavelength corresponding to this photon.
- **Sol.** Kinetic energy acquired by the electron is

$$K = eV = 20 \times 10^3 eV$$
.

The energy of the photon

$$= 0.05 \times 20 = 10^{3} \text{ eV} = 10^{3} \text{ eV}.$$

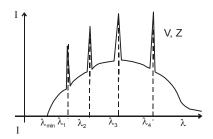
Thus, 
$$\frac{h\nu}{\lambda} = 10^3 \, eV \qquad = \frac{(4.14 \times 10^{-15} \, eV - s) \times (3 \times 10^8 \, m/s)}{10^3 \, eV} \qquad = \frac{1242 \, eV - nm}{10^3 \, eV} = 1.24 \, nm$$



### **Charactristic X-rays**

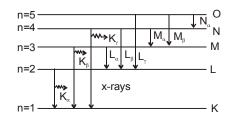
The sharp peaks obtained in graph are known as characteristic x-rays because they are characteristic of target material.

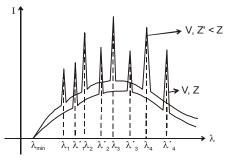
 $\lambda_1$ ,  $\lambda_2$ ,  $\lambda_3$ ,  $\lambda_4$ , ...... = charecteristic wavelength of material having atomic number Z are called **characteristic x-rays** and the spectrum obtained is called **characteristic spectrum**. If target of atomic number Z' is used then peaks are shifted.



Characteristic x-ray emission occurs when an energetic electron collides with target and remove an inner shell electron from atom, the vacancy created in the shell is filled when an electron from higher level drops into it. Suppose vacancy created in innermost K-shell is filled by an electron droping from next higher level L-shell then  $K_{\alpha}$  characteristic x-ray is obtained. If vaccany in K-shell is filled by an electron from M-shell,  $K_{\beta}$  line is produced and so on

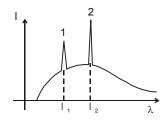
similarly  $L_{\alpha}$ ,  $L_{\beta}$ ,.... $M_{\alpha}$ ,  $M_{\beta}$  lines are produced.





# \_Solved Example\_

**Ex. 34** Find which is  $K_{\alpha}$  and  $K_{\alpha}$ 



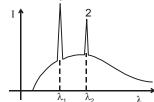
**Sol.** 
$$\Delta E = \frac{hc}{\lambda}, \qquad \lambda = \frac{hc}{\Delta E}$$

$$\lambda = \frac{hc}{\lambda F}$$

since energy difference of  $K_{\alpha}$  is less than  $K_{\alpha}$ 

$$\begin{array}{c} \Delta E_{k\alpha} < \Delta E_{k\beta} \\ \lambda_{k\beta} < \lambda_{k\alpha} \end{array}$$
 1 is  $K_{\beta}$  and 2 is  $K_{\alpha}$ 

Ex. 35



Sol

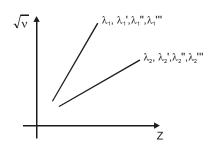
Find which is 
$$K_{\alpha}$$
 and  $L_{\alpha}$   
 $\therefore \Lambda E > \Lambda E$ 

 $\therefore \qquad \Delta E_{\kappa_{\alpha}} > \overset{\circ}{\Delta} E_{L_{\alpha}}$ 1 is  $K_{\alpha}$  and 2 is  $L_{\alpha}$ 



#### 14. **MOSELEY'S LAW:**

Moseley measured the frequencies of characteristic x-rays for a large number of elements and plotted the sqaure root of frequency against position number in periodic table. He discovered that plot is very closed to a straight line not passing through origin.



Wavelength of charactristic wavelengths.

Moseley's observations can be mathematically expressed as

$$\sqrt{v} = a(Z - b)$$

a and b are positive constants for one type of x-rays & for all elements (independent of Z). Moseley's Law can be derived on the basis of Bohr's theory of atom, frequency of x-rays is given by

$$\sqrt{v} = \sqrt{CR\left(\frac{1}{n_1^2} - \frac{1}{n_2^2}\right)} \cdot (Z - b)$$

by using the formula  $\frac{1}{\lambda} = R z^2 \left( \frac{1}{n_1^2} - \frac{1}{n_2^2} \right)$  with modification for multi electron system.

 $b \to known$  as screening constant or shielding effect, and (Z – b) is effective nuclear charge.

$$n_1 = 1$$
,  $n_2 = 2$ 

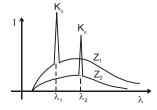
$$\therefore \sqrt{v} = \sqrt{\frac{3RC}{4}} (Z - b)$$

$$\sqrt{v} = a(Z - b)$$

Here  $a = \sqrt{\frac{3RC}{4}}$ , [b = 1 for  $K_{\alpha}$  lines]

# SOLVED EXAMPLE \_\_\_\_

Ex. 36



Find in  $Z_1$  and  $Z_2$  which one is greater.

Sol.

$$\because \sqrt{v} \equiv \sqrt{cR\left(\frac{1}{n_1^2} - \frac{1}{n_2^2}\right)} \cdot (Z - b)$$

If Z is greater then  $\nu$  will be greater,  $\lambda$  will be less

$$\begin{array}{ccc} \therefore & \lambda_1 < \lambda_2 \\ \therefore & Z_1 > Z_2. \end{array}$$

- Ex. 37 A cobalt target is bombarded with electrons and the wavelength of its characteristic spectrum are measured. A second, fainter, characteristic spectrum is also found because of an impurity in the target. The wavelength of the K<sub>g</sub> lines are 178.9 pm (cobalt) and 143.5 pm (impurity). What is the impurity?
- **Sol.** Using Moseley's law and putting  $c/\lambda$  for v (and assuming b = 1), we obtain

$$\sqrt{\frac{c}{\lambda_{c_0}}} = aZ_{c_0} - a$$

and

$$\sqrt{\frac{c}{\lambda_x}} = aZ_x - a$$

Dividing yields

$$\sqrt{\frac{\lambda_{c_0}}{\lambda_x}} = \frac{Z_x - 1}{Z_{c_0} - 1}$$

Substituting gives us

$$\sqrt{\frac{178.9\,\mathrm{pm}}{143.5\,\mathrm{pm}}} = \frac{Z_{\mathrm{x}} - 1}{27 - 1} \,.$$

Solving for the unknown, we find  $Z_x = 30.0$ ; the impurity is zinc.

**Ex. 38** Find the constants a and b in Moseley's equation  $\sqrt{v} = a(Z - b)$  from the following data.

Element	Z	Wavelength of $K_{\alpha}$ X-ray
Мо	42	71 pm
Co	27	178.5 pm

### Sol. Moseley's equation is

$$\sqrt{v} = a(Z - b)$$

Thus, 
$$\sqrt{\frac{c}{\lambda_1}} = a(Z_1 - b) \qquad \qquad ....(i)$$

and 
$$\sqrt{\frac{c}{\lambda_2}} = a(Z_2 - b) \qquad \qquad ....(ii)$$

From (i) and (ii) 
$$\sqrt{c} \left( \frac{1}{\sqrt{\lambda_1}} - \frac{1}{\sqrt{\lambda_2}} \right) = a(Z_1 - Z_2)$$

or, 
$$a = \frac{\sqrt{c}}{(Z_1 - Z_2)} \left( \frac{1}{\sqrt{\lambda_1}} - \frac{1}{\sqrt{\lambda_2}} \right)$$

$$= \frac{(3 \times 10^8 \text{m/s})^{1/2}}{42 - 27} \left[ \frac{1}{(71 \times 10^{-12} \text{m})^{1/2}} - \frac{1}{(178.5 \times 10^{-12} \text{m})^{1/2}} \right]$$
$$= 5.0 \times 10^7 \text{ (Hz)}^{1/2}$$

Dividing (i) by (ii),

$$\sqrt{\frac{\lambda_2}{\lambda_1}} = \frac{Z_1 - b}{Z_2 - b}$$

or, 
$$\sqrt{\frac{178.5}{71}} = \frac{42 - b}{27 - b}$$

or, 
$$b = 1.37$$

# MISCELLANEOUS SOLVED EXAMPLE....

**Problem 1.** Find the momentum of a 12.0 MeV photon.

**Solution :**  $p = \frac{E}{c} = 12 \text{ MeV/c}.$ 

**Problem 2.** Monochromatic light of wavelength 3000 Å is incident nornally on a surface of area 4 cm<sup>2</sup>. If the intensity of the light is  $15 \times 10^{-2}$  W/m<sup>2</sup>, determine the rate at which photons strike the surface.

**Solution :** Rate at which photons strike the surface

$$= \frac{IA}{hc/\lambda} = \frac{6 \times 10^{-5} \text{ J/s}}{6.63 \times 10^{-19} \text{ J/photon}} = 9.05 \times 10^{13} \text{ photon/s}.$$

**Problem 3.** The kinetic energies of photoelectrons range from zero to  $4.0 \times 10^{-19}$  J when light of wavelength 3000 Å falls on a surface. What is the stopping potential for this light?

**Solution :**  $K_{max} = 4.0 \times 10^{-19} \text{ J} \times \frac{1 \text{eV}}{1.6 \times 10^{-19} \text{ J}} = 2.5 \text{ eV}.$ 

Then, from  $eV_s = K_{max}$ ,  $V_s = 2.5 \text{ V}$ .

**Problem 4.** What is the threshold wavelength for the material in above problem?

**Solution :** 2.5 eV =  $\frac{12.4 \times 10^3 \text{ eV.Å}}{3000 \text{ Å}} - \frac{12.4 \times 10^3 \text{ eV.Å}}{\lambda_{th}}$ 

Solving,  $\lambda_{in} = 7590 \text{ Å}.$ 

**Problem 5.** Find the de Broglie wavelength of a 0.01 kg pellet having a velocity of 10 m/s.

**Solution:**  $\lambda = h/p = \frac{6.63 \times 10^{-34} \text{ J.s}}{0.01 \text{kg} \times 10 \text{ m/s}} = 6.63 \times 10^{-23} \text{ Å}.$ 

**Problem 6.** Determine the accelerating potential necessary to give an electron a de Broglie wavelength of 1 Å, which is the size of the interatomic spacing of atoms in a crystal.

**Solution :**  $V = \frac{h^2}{2m_0 e \lambda^2} = 151 \text{ V}.$ 

**Problem 7.** Determine the wavelength of the second line of the Paschen series for hydrogen.

**Solution**.  $\frac{1}{\lambda} = (1.097 \times 10^{-3} \, \text{Å}^{-1}) \, \left( \frac{1}{3^2} - \frac{1}{5^2} \right)$  or  $\lambda = 12,820 \, \text{Å}$ .

**Problem 8.** How many different photons can be emitted by hydrogen atoms that undergo transitions to the ground state from the n = 5 state?

**Solution**: No of possible transition from n = 5 are  ${}^{5}C_{2} = 10$ 

**Ans.** 10 photons.

**Problem 9.** An electron rotates in a circle around a nucleus with positive charge Ze. How is the electrons' velocity releated to the radius of its orbit?

**Solution**: The force on the electron due to the nuclear provides the required centripetal force

$$\frac{1}{4\pi\epsilon_0} \ \frac{Ze.e}{r^2} = \frac{mv^2}{r}$$

$$\Rightarrow v = \sqrt{\frac{Ze^2}{4\pi\epsilon_0.rm}} \qquad \qquad \text{Ans.} \qquad v = \sqrt{\frac{Ze^2}{4\pi\epsilon_0.rm}} \ .$$

**Problem 10.** (i) Calculate the first three energy levels for positronium.

(ii) Find the wavelength of the  $H_a$  line (3  $\rightarrow$  2 transition) of positronium.

**Solution:** In positronium electron and positron revolve around their centre of mass

$$\frac{1}{4p\epsilon_0} \frac{e^2}{r^2} = \frac{mv^2}{r/2}$$
 ———(1)

$$\frac{\mathsf{nh}}{\mathsf{2}\pi} = 2 \times \mathsf{mv}_{\mathsf{k}/2} \tag{2}$$

From (1) & (2)

$$V = \frac{1}{2} \cdot \frac{1}{4\pi\epsilon_0} \cdot \frac{e^2}{nh} \times 2p = \frac{e^2}{4\epsilon_0 nh}$$

TE = 
$$-\frac{1}{2}$$
 mv<sup>2</sup> × 2 = -m.  $\frac{e^4}{16\epsilon_0^2 n^2 h^2}$ 

$$=-6.8 \frac{1}{n^2} \text{ eV}$$

(i) 
$$E_1 = -6.8 \text{ eV}$$

$$E_2 = -6.8 \times \frac{1}{2^2} \text{ eV} = -1.70 \text{ eV}$$

$$E_3 = -6.8 \times \frac{1}{3^2} \text{ eV} = -0.76 \text{ eV}$$

(ii) 
$$\Delta E (3 \rightarrow 2) = E_3 - E_2 = -0.76 - (-1.70) \text{ eV}$$
  
= 0.94 eV

The corresponding wave length

$$\lambda = \frac{1.24 \times 10^4}{0.94} \text{ Å} = 1313 \text{ Å}$$

**Ans.** (i) -6.8 eV, -1.7 eV, -0.76 eV; (ii) 1313 Å.

Problem 11. A H-atom in ground state is moving with intial kinetic energy K. It collides head on with a He<sup>+</sup> ion in ground state kept at rest but free to move. Find minimum value of K so that both the particles can excite to their first excited state.

**Solution :** Energy available for excitation =  $\frac{4K}{5}$ 

Total energy required for excitation

$$\therefore \frac{4k}{5} = 51 \implies k = 63.75 \text{ eV}$$

**Problem 12.** A TV tube operates with a 20 kV accelerating potential. What are the maximum–energy X–rays from the TV set ?

**Solution :** The electrons in the TV tube have an energy of 20 keV, and if these electrons are brought to rest by a collision in which one X–ray photon is emitted, the photon energy is 20 keV.

**Problem 13.** In the Moseley relation,  $\sqrt{v}=a(Z-b)$  which will have the greater value for the constant a for  $K_{\alpha}$  or  $K_{\beta}$  transition ?

**Solution :** A is larger for the  $K_{R}$  transitions than for the  $K_{R}$  transitions.

# **Exercise #1**

### **PART - I: SUBJECTIVE QUESTIONS**

#### **SECTION (A): PHOTOELECTRIC EFFECT**

- **A 1.** The electric field associated with a monochromatic light to given by  $E = E_0 \sin (1.2 \times 10^{15} \pi t kx)$  Find the maximum kinetic energy of the photoelectrons when this light falls on a metal surface whose work function is 2.0 eV
- **A 2.** When a light of wavelength 400 nm falls on a metal of workfunction 2.5 eV, what will be the maximum magnitude of linear momentum of emitted photoelectron?
- **A 3.** One milliwatt of light of wavelength  $\lambda$  = 4560 Å is incident on a cesium metal surface. Calculate the electron current liberated. Assume a quantum efficiency of  $\eta$  = 0.5 %. [work function for cesium = 1.89 eV] Take hc = 12400 eV-Å.
- **A 4.** The magnetic field at a point associated with a light wave is  $B = 2 \times 10^{-6}$  Tesla sin [(3.0 × 10<sup>15</sup> s<sup>-1</sup>)t] sin [(6.0 × 10<sup>15</sup> s<sup>-1</sup>)t]. If this light falls on a metal surface having a work function of 2.0 eV, what will be the maximum kinetic energy of the photoelectrons?
- **A 5.** Suppose the wavelength of the incident light is increased from 3000 A° to 3040 A°. Find the corresponding change in the stopping potential. [Take the product  $hc = 12.4 \times 10^{-7} \text{ eV m}$ ]
- A 6. In an experiment on photoelectric effect, light of wavelength 800 nm (less than threshold wavelength) is incident on a cesium plate at the rate of 5.0 W .The potential of the collector plate is made sufficiently positive with respect to the emitter so that the current reaches its saturation value .Assuming that on the average one of every 10<sup>6</sup> photons is able to eject a photoelectron, find the photo current in the circuit.
- A 7. In a photoelectric effect experiment, photons of energy 5 eV are incident on the photocathode of work function 3 eV. For photon intensity  $I_A = 10^{15}$  m<sup>-2</sup> s<sup>-1</sup>, saturation current of 4.0  $\mu$  A is obtained. Sketch the variation of photocurrent  $i_p$  against the anode voltage  $V_a$  in the figure below for photon intensity  $I_A$  (curve A) and  $I_B = 2 \times 10^{15}$  m<sup>-2</sup> s<sup>-1</sup> (curve B) (in JEE graph was to be drawn in the answer sheet itself.)

[JEE '2003, Mains 2/60]

#### SECTION (B): PHOTON EMISSION FROM A SOURCE AND RADIATION PRESSURE

- **B 1.** A parallel beam of monochromatic light of wavelength 663 nm is incident on a totally reflecting plane mirror. The angle of incidence is  $60^{\circ}$  and the number of photons striking the mirror per second is  $5 \times 10^{19}$ . Calculate the force exerted by the light beam on the mirror. (h =  $6.63 \times 10^{-34}$  J.s.)
- **B 2.** Intensity of sunlight falling normally on the earth surface is  $1.4 \times 10^3 \text{W/m}^2$ . Assume that the light is monochromatic with average wavelength 5000Å and that no light is absorbed in between the sun and the earth's surface. The distance between the sun and the earth is  $1.5 \times 10^{11} \text{m}$ .
  - (a) Calculate the number of the photons falling per second on each square meter of earth's surface directly below the sun.
  - (b) How many photons are there in each cubic meter near the earth's surface at any instant?
  - (c) How many photons does the sun emits per second?

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**B 3.** A sodium lamp of power 10 W is emitting photons of wavelength 590 nm. Assuming that 60% of the consumed energy is converted into light, find the number of photons emitted per second by the lamp.

**B 4.** A beam of white light is incident normally on a plane surface absorbing 70% of the light and reflecting the rest. If the incident beam carries 30 W of power, find the force exerted by it on the surface.

#### SECTION (C): DE-BROGLIE WAVE LENGTH

- **C-1.** Two identical nonrelativistic particles move at right angles to each other, possessing De Broglie wavelengths,  $\lambda_1$  &  $\lambda_2$ . Find the De Broglie wavelength of each particle in the frame of their centre of mass.
- **C 2.** Photo electrons are liberated by ultraviolet light of wavelength 3000 Å from a metallic surface for which the photoelectric threshold wavelength is 4000 Å. Calculate the de Broglie wavelength of electrons emitted with maximum kinetic energy.

#### SECTION (D): BOHR'S THEORY FOR HYDROGEN, HYDROGEN LIKE ATOMS (PROPERTIES)

- **D 1.** Find the numerical value of DeBroglie wavelength of an electron in the 1<sup>st</sup> orbit of hydrogen atom assuming Bohr's atomic model. You can use standard values of the constants. Leave your answer in terms of  $\pi$ .
- **D 2.** Find the radius and energy of a  $He^+$  ion in the states (a) n = 2, (b) n = 3.
- **D 3.** Find the temperature at which the average kinetic energy of the molecules of hydrogen equals the binding energy of its electron in ground state, assuming average kinetic energy of hydrogen gas molecule =  $\frac{3}{2}$ kT.
- **D 4.** A positive hydrogen like ion having electron at its ground state ejects it, if a photon of wavelength 228 Å or less is absorbed by it. Identify the ion.
- **D 5.** A monochromatic light source of frequency  $\nu$  illuminates a metallic surface and ejects photoelectrons. The photoelectrons having maximum energy are just able to ionize the hydrogen atoms in ground state. When the whole experiment is repeated with an incident radiation of frequency  $\left(\frac{5}{6}\right)\nu$  the photoelectrons so emitted are able to excite the hydrogen atom beam which then emits a radiation of wavelength of 1215 Å. Find the frequency  $\nu$ .

# SECTION (E): ELECTRONIC TRANSITION IN THE H/H-LIKE ATOM/SPECIES & EFFECT OF MOTION OF NUCLEUS

- **E 1.** Find the smallest wavelength in emission spectra of (a) hydrogen, (b) He <sup>+</sup>
- **E 2.** Find the quantum number n corresponding to the excited state of He<sup>+</sup> ion, if on transition to the ground state that ion emits two photons in succession with wave lengths 108.5 and 30.4 nm.
- **E 3.** Calculate the angular frequency of revolution of an electron occupying the second Bohr orbit of He<sup>+</sup> ion.
- **E 4.** A stationary hydrogen atom emits a photon corresponding to first line of the Lyman series. What velocity does the atom acquire?
- **E 5.** Consider a gas of hydrogen like ions in a excited state A. It emits photons having wavelength equal to the wavelength of the first line of the lyman series together with photons of five other wavelengths. Identify the gas and find the principal quantum number of the state A.

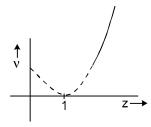
- **E 6.** From the condition of the foregoing problem, find how much (in %) the energy of the emitted photon differs from the energy of the corresponding transition in a hydrogen atom.
- **E 7.** A free atom of iron emits a photon of energy 6.4 keV. Then find the recoil kinetic energy of the atom. (Take mass of iron atom =  $9.3 \times 10^{-26}$  kg).
- **E 8.** Consider a gas consisting Li<sup>+2</sup> (which is hydrogen like ion).
  - (a) Find the wavelength of radiation required to excite the electron in  $Li^{++}$  from n = 1 and n = 3. (Ionisation energy of the hydrogen atom equals 13.6 eV).
  - (b) How many spectral lines are observed in the emission spectrum of the above excited system?

#### **SECTION (F): ATOMIC COLLISIONS**

**F 1.** At what minimum kinetic energy must a hydrogen atom move for it's inelastic headon collision with another stationary hydrogen atom so that one of them emits a photon? Both atoms are supposed to be in the ground state prior to the collision.

#### **SECTION (G): X-RAYS**

- **G 1.** Find the cutoff wavelength for the continuous X-rays coming from an X-ray tube operating at 40 kV.
- **G 2.** On increasing the operating voltage in a x-ray tube by 1.5 times, the shortest wavelength decreases by 26 pm. Find the original value of operating voltage.
- **G 3.** If the operating potential in an X -ray tube is increased by 0.1%, by what percentage does the cutoff wavelength decrease?
- **G 4.** An X-ray tube operates at 20 kV. Suppose the electron converts 70% of its energy into a photon at each collision. Find the lowest three wavelength emitted from the tube. Neglect the energy imparted to the atom with which the electron collides.
- **G 5.** Find the wavelength of the  $K_{\alpha}$  line in copper (Z = 29 ), if the wave length of the  $K_{\alpha}$  line in iron (Z = 26) is known to be equal to 193 pm. (Take b = 1)
- **G 6.** Figure shows the variation of frequency of a characteristic x-ray and atomic number.



- (i) Name the characteristic x-ray
- (ii) Find the energy of photon emitted when this x-ray is emitted by a metal having z = 101.
- **G 7.** A hydrogen like atom (atomic number Z) is in a higher excited state of quantum number n. This excited atom can make a transition to the first excited state by successively emitting two photons of energies 10.20 eV & 17.00 eV respectively. Alternatively, the atom from the same excited state can make a transition to the second excited state by successively emitting two photons of energies 4.25 eV and 5.95 eV respectively. Determine the values of n & Z. (Ionization energy of hydrogen atom = 13.6 eV)

[JEE'94, 6]

G 8. Characteristic X-rays of frequency 4.2 × 10<sup>18</sup> Hz are emitted from a metal due to transition from L- to K-shell. Find the atomic number of the metal using Moseley's law. Take Rydberg constant  $R = 1.1 \times 10^7 \,\mathrm{m}^{-1}$ . [JEE '2003, Mains 2/60]

#### **SECTION (H): FOR JEE MAIN**

An electron beam of energy 10 KeV is incident on metallic foil. If the interatomic distance is 0.55Å. Find the H1. angle of diffraction.

### **PART - II: OBJECTIVE QUESTIONS**

### **SECTION (A): PHOTOELECTRIC EFFECTS**

- A 1. If the frequency of light in a photoelectric experiment is doubled then maximum kinetic energy of photoelec-
  - (A) be doubled (B) be halved
  - (C) become more than double (D) become less than double
- A 2. In a photoelectric experiment, if stopping potential is applied, then photocurrent becomes zero. This means that:
  - (A) the emission of photoelectrons is stopped
  - (B) the photoelectrons are emitted but are reabsorbed by the emitter metal
  - (C) the photoelectrons are accumulated near the collector plate
  - (D) the photoelectrons are dispersed from the sides of the apparatus.
- A 3. Two separate monochromatic light beams A and B of the same intensity (energy per unit area per unit time) are falling normally on a unit area of a metallic surface. Their wavelength are  $\lambda_{\Delta}$  and  $\lambda_{R}$  respectively. Assuming that all the incident light is used in ejecting the photoelectrons, the ratio of the number of photoelectrons from beam A to that from B is

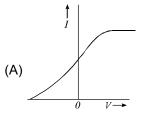
(A) 
$$\left(\frac{\lambda_A}{\lambda_B}\right)$$

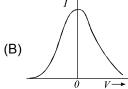
(B) 
$$\left(\frac{\lambda_{\rm B}}{\lambda_{\rm A}}\right)$$

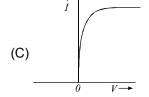
(B) 
$$\left(\frac{\lambda_{\rm B}}{\lambda_{\rm A}}\right)$$
 (C)  $\left(\frac{\lambda_{\rm A}}{\lambda_{\rm B}}\right)^2$ 

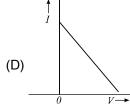
(D) 
$$\left(\frac{\lambda_{\rm B}}{\lambda_{\rm A}}\right)^2$$

- A 4. When a centimetre thick surface is illuminated with light of wavelength  $\lambda$ , the stopping potential is V. When the same surface is illuminated by light of wavelength  $2\lambda$ , the stopping potential is V/3. The threshold wavelength for the surface is:
  - (A)  $\frac{4\lambda}{3}$
- (B) 4 λ
- (C) 6 λ
- A 5. Which one of the following graphs in figure shows the variation of photoelectric current (I) with voltage (V) between the electrodes in a photoelectric cell?









<sup>\*</sup> Marked Questions may have more than one correct option.

(A) 2V

is 4 eV. The stopping potential is:

(B) 4V

A-6.\_

(D) 10V

A 7.	-	saturation photocurrent is	-	ly above the cathode plate. Light ld is switched on which has verti-	
	(A) The photocurrent w	ill increase	(B) The kinetic energy of	of the electrons will increase	
	(C) The stopping poten	tial will decrease	(D) The threshold wave	length will increase	
A 8.	In a photoelectric effect experiment the threshold wavelength of the light is 380 nm. If the wavelentgh of incident light is 260 nm, the maximum kinetic energy of emitted electrons will be:MP			<del>_</del>	
	Given E (in eV) = $\frac{123}{\lambda(in)}$	nm)		[JEE Main 2019, April; 4/120, –1]	
	(A) 1.5 eV	(B) 4.5 eV	(C) 15.1 eV	(D) 3.0 eV	
SEC	TION (B): PHOTON	EMISSION FROM A	SOURCE AND RAD	ATION PRESSURE	
B 1.	A photon of light enters the glass block	a block of glass after trave	elling through vacuum. Th	e energy of the photon on entering	
	(A) increases because	its associated wavelengtl	n decreases		
	(B) Decreases because	e the speed of the radiatio	on decreases		
	(C) Stays the same bed	cause the speed of the rac	diation and the associated	d wavelength do not change	
	(D) Stays the same bed	cause the frequency of the	e radiation does not chan	ge	
B 2.	= -	d from the surface and th		solar panel. Some part of incident orce exerted on 1m² surface area [JEE Main-2019, April; 4/120, -1]	
	(A) 15 × 10 <sup>-8</sup> N	(B) 35 × 10 <sup>-8</sup> N	(C) 10 × 10 <sup>-8</sup> N	(D) 20 × 10 <sup>-8</sup> N	
SECTION (C): DE-BROGLIE WAVES					
C 1.	The de Broglie wavelength of an electron moving with a velocity $1.5 \times 10^8  \text{ms}^{-1}$ is equal to that of a photon. The ratio of the kinetic energy of the electron to that of the energy of photon is :				
	(A) 2	(B) 4	(C) $\frac{1}{2}$	(D) $\frac{1}{4}$	
C 2.	The energy of a photon of frequency $v$ is $E = hv$ and the momentum of a photon of wavelength $\lambda$ is $p = h/\lambda$ From this statement one may conclude that the wave velocity of light is equal to :				
	(A) $3 \times 10^8  \text{ms}^{-1}$	(B) $\frac{E}{p}$	(C) <i>E p</i>	(D) $\left(\frac{E}{p}\right)^2$	

The maximum kinetic energy of photoelectrons emitted from a surface when photons of energy 6 eV fall on it

(C) 6V

C 3.

	(in same medium)						
	(A) both p and E increa	se	(B) p ir	ncreases and E dec	creases		
	(C) p decreases and E	increases	(D) bot	h p and E decreas	es		
C 4.	A particle of mass <i>M</i> at ratio of the de Broglie w				and $m_{_{2}}^{},$	having non zero ve	elocities. The
	(A) $\frac{m_1}{m_2}$	(B) $\frac{m_2}{m_1}$		(C) 1:1		(D) $\sqrt{\frac{m_2}{m_1}}$	
C 5.–	The wavelength $\lambda$ of depotential difference of	_			nass <i>m</i> ,	charge e) accelera	ted through a
	(A) $\lambda = h/mV$	(B) $\lambda = h/2 \text{ me} \lambda$	/	(C) $\lambda = h/\sqrt{\text{meV}}$		(D) $\lambda = h/\sqrt{2\text{meV}}$	
C 6.	The de Broglie waveler the de Broglie wavelen	•	•	•	•	•	. What will be
	(A) $\frac{\lambda}{2}$	<b>(</b> Β <b>)</b> λ		(C) 2 \(\lambda\)		(D) 4 λ	
C 7.	The total energy of the of the electron in this s		st excite	ed state of hydroge	n is – 3.	4 eV. What is the k	inetic energy
	(A) + 1.7 eV	(B) + 3.4 eV		(C) + 6.8 eV		(D) – 13.4 eV	
C 8.	The orbital speed of the excited to the energy s	_	round sta	ate of hydrogen is v	∕. What	will be its orbital spe	eed when it is
	(A) 2 <i>v</i>	(B) $\frac{v}{2}$		(C) $\frac{v}{4}$		(D) $\frac{v}{8}$	
C 9.	In above Q., the poten	tial energy of the	electron	is:			
	(A) – 1.7 eV	(B) - 3.4  eV		(C) - 6.8  eV		(D) – 13.4 eV	
	An electron of mass m a field E. The rate of chang						
						[JEE Main 2020, Jan	.; 4/120, –1]
	(A) $\frac{-h}{ e Et^2}$	(B) $\frac{ e Et}{h}$		$(C) - \frac{h}{ e  E\sqrt{t}}$		(D) $-\frac{h}{ e Et}$	

Let p and E denote the linear momentum and the energy of a photon. For another photon of smaller wavelength

D 2.

(A) Energy of a state is double

(C) Velocity of electrons in an orbit is doubled.

#### SECTION (D): BOHR'S ATOMIC MODEL OF H-ATOM & H-LIKE SPECIES (PROPERTIES)

If  $a_0$  is the Bohr radius, the radius of the n = 2 electronic orbit in triply ionized beryllium is -

When Z is doubled in an atom, which of the following statements are consistent with Bohr's theory?

(B) Radius of an orbit is doubled.

(D) Radius of an orbit is halved.

	(A) 4a <sub>0</sub>	$(B) a_0$	(C) $a_0/4$	(D) $a_0/16$	
D 3*.	Let $A_n$ be the area enclosed by the $n^{th}$ orbit in a hydrogen atom. The graph of $\ell n$ ( $A_n$ / $A_1$ ) against In(n)				
	(A) will pass through the	e origin			
	(B) will have certain points lying on a straight line with slope 4				
	(C) will be a monotonic	ally increasing nonlinear o	curve		
	(D) will be a circle				
D 4.	Which energy state of hydrogen? Given Z for	•	Li <sup>++</sup> ) has the same energ	gy as that of the ground state of	
	(A) $n = 1$	(B) $n = 2$	(C) $n = 3$	(D) $n = 4$	
D 5.		he orbit, speed of the elec		than that of B. Let r, u, E and L and orbital angular momentum of	
	(A) $r_A > r_B$	(B) $u_A > u_B$	(C) $E_A > E_B$	(D) $L_A > L_B$	
D 6.	proton and the electron	•	ground state orbit, m is	Coulomb attraction between the the mass and e the charge of an	
	(A) zero	(B) $\frac{e}{\sqrt{\epsilon_0 a_0 m}}$	(C) $\frac{e}{\sqrt{4\pi\epsilon_0 a_0 m}}$	(D) $\frac{\sqrt{4\pi\varepsilon_0 a_0 m}}{e}$	
D 7.	In the Bohr model of the quantum state <i>n</i> is:			ne total energy of the electron in a	
	(A) – 1	(B) + 1	(C) $\frac{1}{n}$	(D) $\frac{1}{n^2}$	
D 8.		s initial value. If the radius	•	a higher energy state, its orbital e ground state is $r$ , then the radius	
	(A) 2 <i>r</i>	(B) 4 <i>r</i>	(C) 8r	(D) 16 <i>r</i>	
D 9.	The innermost orbit of the	ne hydrogen atom has a c	liameter of 1.06 Å. What i	s the diameter of the tenth orbit?	
	(A) 5.3 Å	(B) 10.6 Å	(C) 53 Å	(D) 106 Å	
	<b>0.</b> The energy required to ionise a hydrogen like ion in its ground state is 9 Rydbergs. What is the wavelength of the radiation emitted when the electron in this ion jumps from the second excited state to the ground state?				
	(A) 35.8 nm	(B) 24.2 nm	(C) 8.6 nm	[JEE Main 2020, Jan.; 4/120, -1] (D) 11.4 nm	

# SECTION (E): ELECTRONIC TRANSITION IN THE H/H-LIKE ATOM/SPECIES OF EFFECT OF MOTION OF NUCL FUS

	OF MOTION OF	NUCLEUS			
E 1.	In a hypothetical ato obtain infrared radiat		to n = 3 produces visible	e light then the possible transition to	
	(A) $n = 5$ to $n = 3$	(B) n = 4 to n = 2	(C) $n = 3$ to $n = 1$	(D) none of these	
E 2.	•	ng from emission spectra hese photons must come		icked up. Their energies are 12.1eV,	
	(A) a single atom	(B)	two atoms		
	(C) three atom	(D)	either two atoms or three	atoms	
E 3.		-		in the ground state are excited by I be emitted by the hydrogen atoms?	
	(A) one	(B) two	(C) three	(D) four	
E 4.	The wavelength of the second line:	e first line in balmer serie	s in the hydrogen spectru	m is $\lambda$ . What is the wavelength of the	
	(A) $\frac{20\lambda}{27}$	(B) $\frac{3\lambda}{16}$	(C) $\frac{5\lambda}{36}$	(D) $\frac{3\lambda}{4}$	
E 5.	$\lambda_2$ and $\lambda_3$ are the wav	nd C of a certain atom correlengths of radiations correct?	respond to increasing values of the seconding to transitions (	ues of energy, i.e. $E_A < E_B < E_C$ . If $\lambda_1$ , C to $B$ , $B$ to $A$ and $C$ to $A$ respectively,	
	(A) $\lambda_3 = \lambda_1 + \lambda_2$	(B) $\lambda_3 = \frac{\lambda_1 \lambda_2}{\lambda_1 + \lambda_2}$ (C) $\lambda_3 = \frac{\lambda_1 \lambda_2}{\lambda_1 + \lambda_2}$	$\lambda_1 + \lambda_2 + \lambda_3 = 0 \qquad (D)$	$\lambda_3^2 = \lambda_1^2 + \lambda_2^2$	
E 6.	· · · · · · · · · · · · · · · · · · ·	e first line in Lyman series the spectrum of doubly in		m is v. What is the frequency of the	
	(A) v	(B) 3 v	(C) 9 v	(D) 27 v	
E 7.	The first member of the second member of the		gen atom has a waveleng	th of 6561 Å. The wavelength of the [JEE Main-2020, Jan.; 4/120, –1]	
	(A) 486 nm	(B) 586 nm	(C) 386 nm	(D) 686 nm	
E 8.		all possible ways (includ		ength $\lambda$ . when the ion gets deexcited ons), a total of six spectral lines are	
	(Given : $h = 6.63 \times 10^{-1}$	$0^{-34} \text{ Js}$ ; c = 3 × 10 <sup>8</sup> ms <sup>-1</sup>	-1)	[JEE Main-2019, April; 4/120, -1]	
	(A) 9.4 nm	(B) 12.3 nm	(C) 10.8 nm	(D) 11.4 nm	
E 10.	•	rom transitions n = 2 to ssible transition of helium	, ,	ms fall on He+ ions in n = 1 and rgy from the radiation is:	
				[JEE Main-2019, April; 4/120, -1]	
	(A) $n = 1 \rightarrow n = 4$	(B) $n = 2 \rightarrow n = 4$	(C) $n = 2 \rightarrow n = 5$	(D) $n = 2 \rightarrow n = 3$	
SECT	TION (F): ATOMIC	COLLISIONS			
F 1.	An electron with kinetic energy 10 eV is incident on a hydrogen atom in its ground state. The collision				
	(A) must be elastic		(B) may be partially e	(B) may be partially elastic	
	(C) must be completely inelastic		(D) may be complete	(D) may be completely inelastic	

H 2.

In Davisson-Germer experiment, the filament emits

(B) Protons

(A) Photons

## SECTION (G): X-RAYS

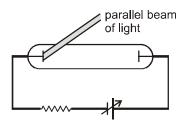
G 1.	If the voltage across the filament is increased, the cutoff wavelength					
	(A) will increase	(B) will decrease	(C) will remain unchanged (D) will change	€		
G 2.	Consider a photon of	continuous X-ray coming f	rom a Coolidge tube. Energy of photon com	es from		
	(A) the kinetic energy of the stricking electron					
	(B) the kinetic energy	(B) the kinetic energy of the free electrons of the target				
	(C) the kinetic energy of the ions of the target					
	(D) an atomic transiti	ion in the target				
*G 3.		d to produced some charal by $\lambda$ . Then which of the fo	ateristic X-rays. Energy of X-rays are given ollowing is true:	by E and wave-		
	(A) $E(K_{\alpha}) > E(K_{\beta}) > E(K_{\beta})$	$(K_{_{\gamma}})$	(B) $E(M_{\alpha}) > E(L_{\alpha}) > E(K_{\alpha})$			
	(C) $\lambda(K_{\alpha}) > \lambda(K_{\beta}) > \lambda(K_{\beta})$	( <sub>y</sub> )	(D) $\lambda(M_{\alpha}) > \lambda(L_{\alpha}) > \lambda(K_{\alpha})$			
*G 4.	X-ray falling on a mate	erial				
	(A) exerts a force on i	it	(B) transfers energy to it			
	(C) transfers moment	um to it	(D) transfers impulse to it			
*G 5.	The potential differen	ce applied to an X-ray tub	e is increased. As a result, in the emitted rac	liation,		
	(A) the intensity incre	ases	(B) the minimum wavelength increases			
	(C) the intensity rema	ains unchanged	(D) the minimum wavelength decreases			
G 6.	The characteristic X-ray spectrum is emitted due to transition of					
	(A) valence electrons of the atom					
	(B) inner electrons of the atom					
	(C) nucleus of the atom					
	(D) both, the inner electrons and the nucleus of the atom					
G 7.	When ultraviolet light is incident on a photocell, its stopping potential is $V_0$ and the maximum kinetic energy of the photoelectrons is $K_{\max}$ . When X-rays are incident on the same cell, then:					
	(A) $V_0$ and $K_{\rm max}$ both i	increase	(B) $V_0$ and $K_{\rm max}$ both decrease			
	(C) $V_0$ increases but $I$	K <sub>max</sub> remains the same	(D) $K_{\rm max}$ increases but $V_0$ remains the sa	ame		
SECT	ION (H) : FOR JEE	MAIN				
H 1.	In the Davisson and (increased by :	Germer experiment, the	velocity of electrons emitted from the elec	tron gun can be [AIPMT-2011]		
	(A) increasing the potential difference between the anode and filament					
	(B) increasing the file	(B) increasing the filament current				
	(C) decreasing the filament current					
	(D) decreasing the potential difference between the anode and filament					

(C) X-rays

(D) Electrons

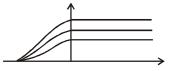
## PART - III: MATCH THE COLUMN

1. In the shown experimental setup to study photoelectric effect, two conducting electrodes are enclosed in an evacuated glass-tube as shown. A parallel beam of monochromatic radiation, falls on photosensitive electrode. Assume that for each photons incident, a photoelectron is ejected if its energy is greater than work function of electrode. Match the statements in column I with corresponding graphs in column II.



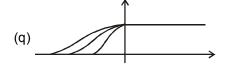
Column-II Column-II

(A) Saturation photocurrent (for same metal) versus intensity (p)

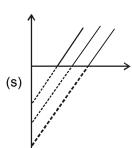


of radiation is represented by

(B) Maximum kinetic energy of ejected photoelectrons versus frequency for electrodes of different work function is represented by



(C) Photo current versus applied (r voltage for different intensity of radiation (for same metal) is represented by



(D) Photo current versus applied voltage at constant intensity of radiation for electrodes of different work function.

2. The energy, the magnitude of linear momentum, magnitude of angular momentum and orbital radius of an electron in a hydrogen atom corresponding to the quantum number n are E, p, L and r respectively. Then according to Bohr's theory of hydrogen atom, match the expressions in column-I with statement in column-II.

Column-II Column-II

(A) Epr (p) is independent of n.

(B)  $\frac{p}{F}$  (q) is directly proportional to n

(C) Er (r) is inversely proportional to n.

(D) pr (s) is directly proportional to L.

3. In each situation of column I a physical quantity related to orbiting electron in a hydrogen like atom is given. The terms 'Z' and 'n' given in column-II have usual meaning in Bohr's theory. Match the quantities in column-I with the terms those depend on quantity given in column-II.

Column I Column II

(A) Frequency of orbiting electron (p) is directly proportional to Z<sup>2</sup>

(B) Angular momentum of orbiting electron (q) is directly proportional to n.

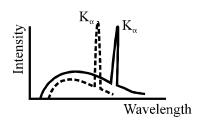
(C) Magnetic moment of orbiting electron (r) is inversely proportional to n<sup>3</sup>

(D) The average current due to orbiting of electron (s) is independent of Z

# **Exercise #2**

#### PART - I: ONLY ONE OPTION CORRECT TYPE

1. Given curve shows the intensity-wavelength relations of X-rays coming from two different Coolidge tubes A and B. The dark curve represents the relation for the tube A in which the potential difference between the target and the filament is  $V_A$  and the atomic number of the target material is  $Z_A$ . Similarly dotted curve is for tube B. These quantities are  $V_B$  and  $Z_B$  for the tube B. Then,



(A)  $V_A > V_B, Z_A > Z_B$  (B)  $V_A > V_B, Z_A < Z_B$ 

 $(C) V_{\Lambda} < V_{D}, Z_{\Lambda} > Z_{D}$   $(D) V_{\Lambda} < V_{D}, Z_{\Lambda} < Z_{D}$ 

- The relation between  $\lambda_1$ : wavelength of series limit of Lyman series,  $\lambda_2$ : the wavelength of the series limit of Balmer series &  $\lambda_3$ : the wavelength of first line of Lyman series is :
  - (A)  $\lambda_1 = \lambda_2 + \lambda_3$

(B)  $\lambda_3 = \lambda_1 + \lambda_2$ 

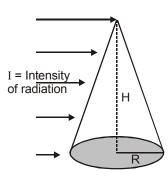
(C)  $\lambda_2 = \lambda_3 - \lambda_1$ 

- (D) none of these
- 3. If  $\lambda_{\min}$  is minimum wavelength produced in X-ray tube and  $\lambda_{k\alpha}$  is the wavelength of  $k_{\alpha}$  line. As the operating tube voltage is increased.
  - (A)  $(\lambda_k \lambda_{min})$  increases

(B)  $(\lambda_k - \lambda_{min})$  decreases

(C)  $\lambda_{k\alpha}$  increases

- (D)  $\lambda_{k\alpha}$  decreases
- **4.** According to Moseley's law the ratio of the slopes of graph between  $\sqrt{V}$  and Z for  $K_B$  and  $K_B$  is:
  - (A)  $\sqrt{\frac{32}{27}}$
- (B)  $\sqrt{\frac{27}{32}}$
- (C)  $\sqrt{\frac{33}{22}}$
- (D)  $\sqrt{\frac{22}{33}}$
- 5. If the frequency of  $K_{\alpha}$  X-ray emitted from element with atomic number 31 is f, then the frequency of  $K_{\alpha}$  X-ray emitted from the element with atomic number 51 would be (assume that screening constant for  $K_{\alpha}$  is 1):
  - (A)  $\frac{5}{3}$  f
- (B)  $\frac{51}{31}$  f
- (C)  $\frac{9}{25}$  f
- (D)  $\frac{25}{9}$  f
- **6.** The radiation force experienced by body exposed to radiation of intensity I, assuming surface of body to be perfectly absorbing is:



- (A)  $\frac{\pi R^2 I}{c}$
- (B)  $\frac{\pi RHI}{c}$
- (C)  $\frac{IRH}{2c}$
- (D)  $\frac{IRH}{c}$
- 7. In a discharge tube when 200 volt potential difference is applied  $6.25 \times 10^{18}$  electrons move from cathode to anode and  $3.125 \times 10^{18}$  singly charged positive ions move from anode to cathode in one second. Then the power of tube is:
  - (A) 100 watt
- (B) 200 watt
- (C) 300 watt
- (D) 400 watt
- **8.** Radiation pressure on any surface (for a given intensity):
  - (A) is dependent on wavelength of the light used
  - (B) is dependent on nature of surface and intensity of light used
  - (C) is dependent on frequency and nature of surface
  - (D) depends on the nature of source from which light is coming and on nature of surface on which it is falling.

- JEE (Adv.)-Physics Modern Physics The wavelengths of  $K_{\alpha}$  x-rays of two metals 'A' and 'B' are  $\frac{4}{1875 \, R}$  and  $\frac{1}{675 \, R}$  respectively, where 'R' is 9. rydberg constant. The number of elements lying between 'A' and 'B' according to their atomic numbers is (A)3(B)6(C)5An atom consists of three energy levels given by a ground state with energy  $E_0 = 0$ , the first excited 10. state with energy  $E_1 = K$  and the second excited state with energy  $E_2 = 2K$  where K > 0. The atom is initially in the ground state. Light from a laser which emits photons with energy 1.5K is shined on the atom. Which of the following is/are correct? (A) The photons are absorbed, putting one atom in a state  $E_1$  and one atom in a state  $E_2$ . (B) A photon will always be absorbed, but half the time the atom will go into the state with energy K and the other half into the state with energy 2K. In this way, energy will be conserved on the average. (C) The atom absorbs a photon, goes into the first excited state with energy K and emits a photon with energy 0.5 K to conserve energy.
- 11. The work function of a certain metal is  $\frac{hC}{\lambda_0}$ . When a monochromatic light of wavelength  $\lambda < \lambda_0$  is incident such that the plate gains a total power P. If the efficiency of photoelectric emission is  $\eta\%$  and all the emitted photoelectrons are captured by a hollow conducting sphere of radius R already charged to potential V, then neglecting any interaction between plate and the sphere, expression of potential of the sphere at time t is :

$$(A) \ V + \frac{100 \, \eta \, \lambda Pe \, t}{4 \pi \epsilon_0 RhC} \qquad (B) \ V - \frac{\eta \, \lambda Pe \, t}{400 \pi \epsilon_0 RhC} \qquad (C) \ V \qquad \qquad (D) \frac{\lambda Pe \, t}{4 \pi \epsilon_0 RhC}$$

(D) The atom does not absorb any photon and stays in the ground state.

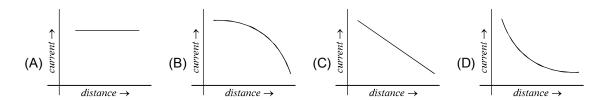
An image of the sun is formed by a lens of focal length 30 cm on the metal surface of a photo-electric cell and it produces a current I. The lens forming the image is then replaced by another lens of the same diameter but of focal length 15 cm. The photoelectric current in this case will be: (In both cases the plate is kept at focal plane and normal to the axis lens). (Assume saturation current only).

(A) I/2 (B) 2 I (C) I (D) 4 I

- 13. When a monochromatic source of light is at a distance of 0.2 m from a photoelectric cell, the cut-off voltage and the saturation current are respectively 0.6 V and 18 mA. If the same source is placed 0.6 m away from the cell, then:
  - (A) the stopping potential will be  $0.2\,\mathrm{V}$  (B) the stopping potential will be  $1.8\,\mathrm{V}$
  - (C) the saturation current will be 6.0 mA (D) the saturation current will be 2.0 mA
- 14. Which one of the following statements is NOT true for de Broglie waves?
  - (A) All atomic particles in motion have waves of a definite wavelength associated with them
  - (B) The higher the momentum, the longer is the wavelength
  - (C) The faster the particle, the shorter is the wavelength
  - (D) For the same velocity, a heavier particle has a shorter wavelength

JEE	(Adv.)-Physics			Modern Physics	
15.	• •		•	tationary electron (but free to move)	
	and bounces off. If $\lambda'$	and v' are respectively the	ne wavelength and freque	ncy of the scattered photon, then:	
	(A) $\lambda' = \lambda$ ; $\nu' = \nu$	(B) $\lambda' < \lambda$ ; $\nu' > \nu$	(C) $\lambda' > \lambda$ ; $\nu' > \nu$	(D) $\lambda' > \lambda$ ; $\nu' < \nu$	
16.	In a photoelectric exp the following stateme	•	and intensity of a light sour	ce are both doubled. Then consider	
	(i) The saturation pho	otocurrent remains almos	st the same.		
	(ii) The maximum kinetic energy of the photoelectrons is doubled.				
	(A) Both (i) and (ii) are	e true	(B) (i) is true but (ii) is	false	
	(C) (i) is false but (ii)	is true	(D) both (i) and (ii) are	false	
17.	placed 50 cm away. V	When the same light is pla		is illuminated by a small bright light photoelectrons emerging from the uce saturation current)	
	(A) each carry one qu	arter of their previous en	ergy		
	(B) each carry one qu	arter of their previous mo	omentum		
	(C) are half as numer	ous			
	(D) are one quarter as	s numerous			
18.	An X-ray tube is oper	ated at 66 kV. Then, in th	ne continuous spectrum of	the emitted X-rays :	
	(A) wavelengths 0.07	1 nm and 0.02 nm will bo	th be present		
	<ul><li>(B) wavelengths 0.01 nm and 0.02 nm will both be absent</li><li>(C) wavelengths 0.01 nm will be present but wavelength 0.02 nm will be absent</li></ul>				
	(D) wavelength 0.01	nm will be absent but wa	velength 0.02 nm will be p	resent	
19.	!		f the Lyman series, $v_2$ be series limited of the Balme	the frequency of the first line of the er series.	
	(A) $v_1 - v_2 = v_3$	(B) $v_2 - v_1 = v_3$	(C) $v_3 = \frac{1}{2} (v_1 + v_3)$	(D) $v_1 + v_2 = v_3$	
20.			eV and that for sodium su o cause photo emission. T	rface is 2.0 ev. The two metals were then:	
	(A) Both aluminium a	nd sodium will have the s	same threshold frequency		
	(B) The threshold frequency of aluminium will be more than that of sodium				
	(C) The threshold free	quency of aluminium will	be less than that of sodiur	n	
	(D) The threshold way	velength of aluminium wi	ll be more than that of sodi	um	
21. A point source of light is used in a photoelectric effect. If the source is moved toward the emitti stopping potential			oved toward the emitting metal, the		
	(A) will increase		(B) will decrease		
	(C) will remain consta	ant	(D) will either increase	e or decrease	

A point source causes photoelectric effect from a small metal plate. Which of the following curves may 22. represent the saturation photocurrent as a function of the distance between the source and the metal?



- 23. The energy difference between the first two levels of hydrogen atom is 10.2 eV. What is the corresponding energy difference for a singly ionized helium atom?
  - (A) 10.2 eV
- (B) 20.4 eV
- (C) 40.8 eV
- (D) 81.6 eV
- 24. In a photoelectric experiment, with light of wavelength  $\lambda$ , the fastest electron has speed v. If the exciting wavelength is changed to  $\frac{3\lambda}{4}$ , the speed of the fastest emitted electron will become
  - (A)  $\sqrt{\frac{3}{4}}$

- (C) less than v  $\sqrt{\frac{3}{4}}$  (D) greater than v  $\sqrt{\frac{4}{3}}$
- 25. For the structural analysis of crystals, X-rays are used because:
  - (A) X-rays have wavelength of the order of the inter-atomic spacing
  - (B) X-rays are highly penetrating radiations
  - (C) Wavelength of X-rays is of the order of nuclear size
  - (D) X-rays are coherent radiations
- 26. An  $\alpha$  particle with a kinetic energy of 2.1 eV makes a head on collision with a hydrogen in ground state atom moving towards it with a kinetic energy of 8.4 eV. The collision.
  - (A) must be perfectly elastic
- (B) may be perfectly inelastic

(C) may be inelastic

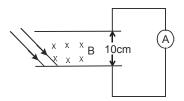
- (D) must be perfectly inelastic
- 27. An energy of 24.6 eV is required to remove one of the electrons from a neutral helium atom. The energy (In eV) required to remove both the electrons from a neutral helium atom is: [JEE 1995, 1]
  - (A) 38.2
- (B) 49.2
- (C)51.8
- (D) 79.0

- 28. The photoelectrons emitted from a metal surface:
  - (A) Are all at rest
  - (B) Have the same kinetic energy
  - (C) Have the same momentum
  - (D) Have speeds varying from zero up to a certain maximum value

- 29. Ultraviolet light of wavelengths  $\lambda_1$  and  $\lambda_2$  when allowed to fall on hydrogen atoms in their ground state is found to liberate electrons with kinetic energy 1.8 eV and 4.0 eV respectively. Find the value of  $\frac{\lambda_1}{\lambda_2}$ .
  - (A)  $\frac{7}{8}$
- (B)  $\frac{8}{7}$
- (C)  $\frac{9}{20}$
- (D)  $\frac{20}{9}$
- **30.** An  $\alpha$ -particle of energy 5 MeV isscattered through 180° by a fixed uranium nucleus. The distance of closest approach is of the order of :
  - (A) 1 Å
- (B) 10<sup>-10</sup> cm
- (C) 10<sup>-12</sup> cm
- (D) 10<sup>-15</sup> cm

## **PART - II: INTEGER TYPE QUESTION**

1. In an experiment on photoelectric effect, the separation between emitter and the collector plates is 10 cm. Plates are connected through an ammeter without any cell. A Magnetic field B exists parallel to the plates. The work function of the emitter is 2.39eV and the light of wavelengths between 400 nm and 600 nm is incident on it. The minimum value of B for which the current registered by the ammeter is (x/10) × 10<sup>-5</sup> T. Evaluate x? zero Neglect any effect of space charge. (asume emission of photo electron to be randomly every possible direction)



- 2. A light beam of wavelength 400 nm is incident on a metal plate of work function 2.2 eV. A particular electron absorbs a photon and makes some collisions before coming out of the metal. Assuming that 10% of the instantaneous energy is lost to the metal in each collision. Find the minimum number of collisions the electron can suffer before it becomes unable to come out of metal. (use hc = 12400 eV Å)
- 3. In the figure shown electromagnetic radiations of wavelength 200nm are incident on the metallic plate A. The photo electrons are accelerated by a potential difference 10V. These electrons strike another metal plate B from which electromagnetic radiations are emitted. The minimum wavelength of the emitted photons is 100nm. Find the work function of the metal 'A'. use hc = 12400 eVÅ,

$$\begin{array}{c|c}
\hline
A & & \\
\hline
& & \\
& & \\
\lambda_{min} = 100 \text{nm}
\end{array}$$

4. Assume that the de Broglie wave associated with an electron can form a standing wave between the atoms arranged in a one dimensional array with nodes at each of the atomic sites. It is found that one such standing wave is formed if the distance 'd' between the atoms of the array is 2 Å. A similar standing wave is again formed if 'd' is increased to 2.5 Å but not for any intermediate value of d. Find the energy of the electrons in electron volts and the least value of d for which the standing wave of the type described above can form.

[JEE 1997, 5]

- **5.** Calculate the magnetic field strength at the centre of a hydrogen atom caused by an electron moving along the first Bohr orbit.
- Suppose the potential energy between electron and proton at a distance r is given by  $U = ke \ell n \frac{r}{a}$ , where r < a and k,e,a are positive constants. Using Bohr's theory the energy of nth energy level for such an atom is

$$\frac{1}{2}$$
ke  $\left(x + y \ln \left(\frac{nh}{2\pi\sqrt{kema^2}}\right)\right)$ . Find x + y.

- 7. Consider Bohr's theory for hydrogen atom. The magnitude of angular momentum, orbit radius and frequency of the electron in  $n^{th}$  energy state in a hydrogen atom are  $\ell$ , r & f respectively. Find out the value of 'x', if  $(fr\ell)$  is directly proportional to  $n^x$ .
- **8.** Radiation from a hydrogen discharge tube (energy of photons ≤ 13.6 eV) goes through a filter which transmits only waves of wavelength greater than 4400 Å and is incident on a metal of work function 2.0 eV. Find the stopping potential which can stop the photoelectrons.
- **9.** The ionization energy of a hydrogen like Bohr atom is 4 Rydberg.
  - (i) What is the wavelength of radiation emitted when the electron jumps from the first excited state to the ground state?
  - (ii) The radius of the first orbit of this atom is  $x \times 10^{-11}$  m. Find x.

(Bohr radius of hydrogen =  $5 \times 10^{-11}$  m; 1 Rydberg =  $2.2 \times 10^{-18}$  J)

10. Consider a hypothetical hydrogen like atom. The wavelength in Å for the spectral lines for transition from n = p to n = 1 are given by -

$$\lambda = \frac{1500 \, p^2}{p^2 - 1}$$

where p = 2, 3, 4, ... (given hc = 12400 eV/Å)

- (a) Find the wavelength of the least energies and the most energetic photons in this series.
- (b) Construct an energy level diagram for this element representing at least three energy levels.
- (c) What is the ionisation potential of this element?
- A sample of hydrogen atom gas contains 100 atoms. All the atoms are excited to the same n<sup>th</sup> excited state. The total energy released by all the atoms is  $\frac{4800}{49}$  Rch (where Rch = 13.6 eV), as they come to the ground state through various types of transitions. then
  - (i) maximum energy of the emitted photon is (x/49)Rch. Find x
  - (ii) Find n.
  - (iii) Find maximum total number of photons that can be emitted by this sample.
- **12.** A positronium consists of an electron and a positron revolving about their common centre of mass. Derive and calculate
  - (i) Separation (in Å) between the electron and positron in their first excited state.
  - (ii) Kinetic energy (in eV) of the electron in ground state.

13. A neutron moving with a speed v strikes a hydrogen atom in ground state moving towards it with the same speed. If the minimum speed of the neutron for which elastic collision dose not take place is  $x \times 10^4$  m/s. Find x. The mass of neutron = mass of hydrogen =  $1.67 \times 10^{-27}$ kg

- A neutron beam, in which each neutron has same kinetic energy, is passed through a sample of hydrogen like gas (but not hydrogen) in ground state. Due to collision of neutrons with the ions of the gas, ions are excited and then they emit photons. Six spectral lines are obtained in which one of the lines is of wavelength (6200/51) nm. What is the minimum possible value of kinetic energy (eV) of the neutrons for this to be possible. The mass of neutron and proton can be assumed to be nearly same. Use hc = 12400 eVÅ.
- In an X-ray tube the accelerating voltage is 20 KV. Two targets A and B are used one by one. For 'A' the wavelength of the  $K_{\alpha}$  line is 62 pm. For 'B' the wavelength of the  $L_{\alpha}$  line is 124 pm. The energy of the 'B' ion with vacancy in 'M' shell is 5.5 KeV higher than the atom of B. [Take hc = 12400 eVÅ]
  - (i) Find  $\lambda_{min}$  in Å.
  - (ii) Can L photons be emitted by 'B'? What is the minimum wavelength (in Å) of the characteristic X-ray that will be emitted by 'B'.
- 16. The  $k_{\beta}$  x-ray of argon has a wavelength of 0.36 nm . The minimum energy (in keV) required to take out the outermost electron from argon atom is 16 eV. Find the energy needed to knock out an electrons from the K shell of an argon.
- In a photo electric effect set up, a point source of light of power  $3.2 \times 10^{-3}$  W emits mono energetic photons of energy 5.0 eV. The source is located at a distance of 0.8 m from the centre of a stationary metallic sphere of work function 3.0 eV & of radius 8.0 x  $10^{-3}$ m. The efficiency of photo electrons emission is one for every  $10^6$  incident photons. Assume that the sphere is isolated and initially neutral, and that photo electrons are instantly swept away after emission. [JEE 1995,10]
  - (a) If the number of photo electrons emitted per second is  $10^x$  s<sup>-1</sup>. Find x.
  - (b) Find the ratio of the wavelength of incident light to the De Broglie wave length of the fastest photo electrons emitted.
  - (c) Evaluate the time t.
- Electrons in hydrogen-like atoms (Z = 3) make transitions from the fifth to the fourth orbit and from the fourth to the third orbit. The resulting radiations are incident normally on a metal plate and eject photoelectrons. The stopping potential for the photoelectrons ejected by the shorter wavelength is 3.95 V. Calculate the work function of the metal, and the stopping potential for the photoelectrons ejected by the longer wavelength (Rydberg constant =  $1.094 \times 10^7 \,\mathrm{m}^{-1}$ )
- Hydrogen atom in its ground state is excited by means of monochromatic radiation of wavelength 975° Å. How many different lines are possible in the resulting spectrum? Calculate the longest wavelength amongst them. You may assume the ionization energy for hydrogen atom is 13.6eV. [JEE'1982; 5M]
- An electron of energy 20 eV collides with a hydrogen atom in the ground state. As a result of the colision, the atom is excited to a higher energy state and the electron is scattered with reduced velocity. The atom subsequently returns to its ground state with emission of radiation of wavelength 1.216 ×  $10^{-7}$  m. If the velocity of the scattered electron is x ×  $10^6$  ms<sup>-1</sup>. Find x.
- 21. A material whose K absorption edge is 0.2 Å is irradiated by X-rays of wavelength 0.15 Å. If the maximum energy of the photoelectrons that are emitted from the K shell is  $3.315 \times 10^{-x}$  J. Find x.

## PART - III: ONE OR MORE THAN ONE CORRECT OPTIONS

**1.** Select the correct alternative(s):

When photons of energy 4.25 eV strike the surface of a metal A, the ejected photo electrons have maximum kinetic energy  $T_A$  eV and de Broglie wave length  $\lambda_A$ . The maximum kinetic energy of photo electrons liberated from another metal B by photons of energy 4.70 eV is  $T_B = (T_A - 1.50)$  eV. If the de-Brogleie wave length of these photo electrons is  $\lambda_B = 2\lambda_A$ , then:

[JEE 1994, 2]

- (A) the work function of A is 2.25 eV
- (B) the work function of B is 4.20 eV

(C) 
$$T_A = 2.00 \text{ eV}$$

(D) 
$$T_{B} = 2.75 \text{ eV}$$

- In an x-ray tube the voltage applied is 20KV. The energy required to remove an electron from L shell is 19.9 KeV. In the x-rays emitted by the tube (hc = 12420 evÅ)
  - (A) minimum wavelength will be 62.1 pm
  - (B) energy of the characterstic x-rays will be equal to or less than 19.9 KeV
  - (C) L<sub>a</sub> x-ray may be emitted
  - (D)  $L_{\alpha}$  x-ray will have energy 19.9 KeV
- 3. Photoelectric effect supports particle nature of light because
  - (A) there is a minimum frequency below which no photoelectrons are emitted
  - (B) the maximum kinetic energy of photoelectrons depends only on the frequency of light and is independent of intensity.
  - (C) even when the metal surface is illuminated with very small intensity the photoelectrons (if  $v \ge v_{th}$ ) leave the surface immediately
  - (D) electric charge of the photoelectrons is quantized
- 4. The collector of the photocell (in photoelectric experiment) is made of tungsten while the emitter is of Platinum having work function of 10 eV. Monochromatic radiation of wavelength 124 Å & power 100 watt is incident on emitter which emits photo electrons with a quantum efficiency of 1%. The accelerating voltage across the photocell is of 10,000 volts (Use: hc = 12400eV Å)
  - (A) The power supplied by the accelerating voltage source is 100 watt
  - (B) The minimum wavelength of radiation coming from the tungsten target (collector) is 1.23 Å
  - (C) The power supplied by the accelerating voltage source is 10 watt
  - (D) The minimum wavelength of radiation coming from the tungsten target (collector) is 2.23 Å
- **5.** For the electron in the n<sup>th</sup> orbit of hydrogen atom. Under the assumption of the Bohr's atomic model choose the **CORRECT** option(s) (Here n is the principal quantum number):-
  - (A) Frequency of the electron is inversely proportional to n<sup>3</sup>
  - (B) The magnitude of potential energy of the electron in an orbit is greater than its kinetic energy
  - (C) Magnetic induction at the nucleus produced due to the motion of electron in the n<sup>th</sup> orbit is proportional to n<sup>5</sup>
  - (D) Magnetic moment produced due to the motion of electron in the n<sup>th</sup> orbit is proportional to n

- In an x-ray tube the voltage applied is 20KV. The energy required to remove an electron from L shell is 19.9 KeV. In the x-rays emitted by the tube (Use hc = 12420 eVÅ)
  - (A) minimum wavelength will be 62.1 pm
  - (B) energy of the characterstic x-rays will be equal to or less than 19.9 KeV
  - (C) L<sub>x</sub> x-ray may be emitted
  - (D) L<sub>a</sub> x-ray will have energy 19.9 KeV

#### **PART - IV: COMPREHENSION**

#### Comprehension - 1

A physicist wishes to eject electrons by shining light on a metal surface. The light source emits light of wavelength of 450 nm. The table lists the only available metals and their work functions.

Metal		$W_0(eV)$
Barium	_	2.5
Lithium	_	2.3
Tantalum	_	4.2
Tungsten	_	4.5

- 1. Which metal(s) can be used to produce electrons by the photoelectric effect from given source of light?
  - (A) Barium only

- (B) Barium or lithium
- (C) Lithium, tantalum or tungsten
- (D) Tungsten or tantalum
- 2. Which option correctly identifies the metal that will produce the most energetic electrons and their energies?
  - (A) Lithium, 0.45 eV

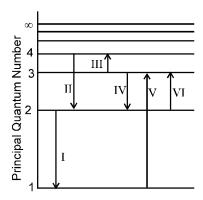
(B) Tungston, 1.75 eV

(C) Lithium, 2.30 eV

- (D) Tungston, 2.75 eV
- 3. Suppose photoelectric experiment is done separately with these metals with light of wavelength 450 nm. The maximum magnitude of stopping potential amongst all the metals is
  - (A) 2.75 volt
- (B) 4.5 volt
- (C) 0.45 volt
- (D) 0.25 volt

#### Comprehension - 2

The figure shows an energy level diagram for the hydrogen atom. Several transitions are marked as I, II, III, . The diagram is only indicative and not to scale.



- In which transition is a Balmer series photon absorbed?
  - (A) II
- (B) III
- (C) IV
- (D) VI
- 5. The wavelength of the radiation involved in transition II is
  - (A) 291 nm
- (B) 364 nm
- (C) 487 nm
- (D) 652 nm
- 6. Which transition will occur when a hydrogen atom is irradiated with radiation of wavelength 103nm?
  - (A)I

- (B) II
- (C) IV
- (D) V

# **Exercise #3**

## PART - I: JEE (ADVANCED) / IIT-JEE PROBLEMS (PREVIOUS YEARS)

- \* Marked Questions may have more than one correct option.
- 1. An α-particle and a proton are accelerated from rest by a potential difference of 100V. After this, their de-Broglie wavelength are  $\lambda_{\alpha}$  and  $\lambda_{p}$  respectively. The ratio  $\frac{\lambda_{p}}{\lambda_{\alpha}}$ , to the nearest integer, is : [JEE 2010, 3/163]

#### PARAGRAPH FOR QUESTIONS 2 TO 4

The key feature of Bohr's theory of spectrum of hydrogen atom is the quantization of angular momentum when an electron is revolving around a proton. We will extend this to a general rotational motion to find quantized rotational energy of a diatomic molecule assuming it to be rigid. The rule to be applied is Bohr's quantization condition. [JEE 2010, 9/163, -1]

- 2. A diatomic molecule has moment of inertia I. By Bohr's quantization condition its rotational energy in the n<sup>th</sup> level (n = 0 is not allowed) is: [JEE 2010, 3/163, -1]

- (A)  $\frac{1}{n^2} \left( \frac{h^2}{8\pi^2 I} \right)$  (B)  $\frac{1}{n} \left( \frac{h^2}{8\pi^2 I} \right)$  (C)  $n \left( \frac{h^2}{8\pi^2 I} \right)$  (D)  $n^2 \left( \frac{h^2}{8\pi^2 I} \right)$
- It is found that the excitation frequency from ground to the first excited state of rotation for the CO molecule 3. is close to  $\frac{4}{\pi} \times 10^{11}$  Hz. Then the moment of inertia of CO molecule about its centre of mass is close to (Take  $h = 2\pi \times 10^{-34} \, J \, s$ [JEE 2010, 3/163, -1]
  - (A)  $2.76 \times 10^{-46} \text{ kg m}^2$  (B)  $1.87 \times 10^{-46} \text{ kg m}^2$  (C)  $4.67 \times 10^{-47} \text{ kg m}^2$  (D)  $1.17 \times 10^{-47} \text{ kg m}^2$
- In a CO molecule, the distance between C (mass = 12 a.m.u.) and O (mass = 16 a.m.u.), where 4. 1 a.m.u. =  $\frac{5}{3} \times 10^{-27}$  kg, is close to : [JEE 2010, 3/163, -1]
- (A)  $2.4 \times 10^{-10}$  m (B)  $1.9 \times 10^{-10}$  m (C)  $1.3 \times 10^{-10}$  m (D)  $4.4 \times 10^{-11}$  m

- The wavelength of the first spectral line in the Balmer series of hydrogen atom is 6561 Å. The wavelength of the second spectral line in the Balmer series of singly ionized helium atom is: [JEE 2010, 3/160, -1]
  - (A) 1215 Å
- (B) 1640 Å
- (C) 2430 Å
- (D) 4687 Å

#### PARAGRAPH FOR QUESTION NOS. 6 AND 7

A dense collection of equal number of electrons and positive ions is called neutral plasma. Certain solids containing fixed positive ions surrounded by free electrons can be treated as neutral plasma. Let 'N' be the number density of free electrons, each of mass 'm'. When the electrons are subjected to an electric field, they are displaced relatively away from the heavy positive ions. If the electric field becomes zero, the electrons begin to oscillate about the positive ions with a natural angular frequency ' $\omega_{_{D}}$ ', which is called the plasma frequency. To sustain the oscillations, a time varying electric field needs to be applied that has an angular frequency  $\omega$ , where a part of the energy is absorbed and a part of it is reflected. As  $\omega$  approaches  $\omega_{\alpha}$  all the free electrons are set to resonance together and all the energy is reflected. This is the explanation of high reflectivity of metals. [JEE 2011, 3×2/160, -1]

- 6. Taking the electronic charge as 'e' and the permitlivity as ' $\epsilon_0$ ', use dimensional analysis to determine the correct expression for  $\omega p$ .
  - (A)  $\sqrt{\frac{Ne}{m\epsilon_0}}$
- (B)  $\sqrt{\frac{m\epsilon_0}{Ne}}$
- (C)  $\sqrt{\frac{Ne^2}{m\epsilon_0}}$  (D)  $\sqrt{\frac{m\epsilon_0}{Ne^2}}$
- 7. Estimate the wavelength at which plasma reflection will occur for a metal having the density of electrons N  $_{lpha}$  4 x 10 $^{27}$  m $^{-3}$ . Take  $\epsilon_{_0}$   $_{lpha}$  10 $^{-11}$  and m  $_{lpha}$  10 $^{-30}$ , where these quantities are in proper SI units.
  - (A) 800 nm
- (B) 600 nm
- (C) 300 nm
- (D) 200 nm
- A silver sphere of radius 1 cm and work function 4.7 eV is suspended from an insulating thread in free-space. 8. It is under continuous illumination of 200 nm wavelength light. As photoelectrons are emitted, the sphere gets charged and acquires a potential. The maximum number of photoelectrons emitted from the sphere is  $A \times 10^{z}$  (where 1 < A < 10). The value of 'Z' is [JEE 2011, 4/160]
- 9. A pulse of light of duration 100 ns is absorbed completely by a small object initially at rest. Power of the pulse is 30mW and the speed of light is 3 × 10 ms<sup>-1</sup>. The final momentum of the object is: [JEE-Advanced-2013]
  - (A)  $0.3 \times 10^{-17} \text{ kg ms}^{-1}$

(B)  $1.0 \times 10^{-17} \text{ kg ms}^{-1}$ 

(C)  $3.0 \times 10^{-17} \text{ kg ms}^{-1}$ 

- (D)  $9.0 \times 10^{-17} \text{ kg ms}^{-1}$
- The work functions of Silver and Sodium are 4.6 and 2.3 eV, respectively. The ratio of the slope of the stopping 10. potential versus frequency plot for Silver to that of Sodium is: [JEE-Advanced-2013]
- The radius of the orbit of an electron in a Hydrogen-like atom is 4.5  $a_0$ , where  $a_0$  is the Bohr radius. Its 11. orbital angular momentum is  $\frac{3h}{2\pi}$ . It is given that h is Planck constant and R is Rydberg constant. The [JEE Advanced-2013] possible wavelength(s), when the atom de-excites, is (are):
  - (A)  $\frac{9}{32R}$
- (B)  $\frac{9}{16R}$
- (C)  $\frac{9}{5R}$
- (D)  $\frac{4}{3R}$

12. If  $\lambda_{cu}$  is the wavelength of  $K_{\alpha}$  X-ray line of copper (atomic number 29) and  $\lambda_{mo}$  is the wavelength of the  $K_{\alpha}$  X-ray line of molybdenum (atomic number 42), then the ratio  $\lambda_{cu}/\lambda_{mo}$  is close to **[JEE (Advanced)-2014, 3/60, -1]** 

- (A) 1.99
- (B) 2.14
- (C)0.50
- (D) 0.48

13. A metal surface is illuminated by light of two different wavelengths 248 nm and 310 nm. The maximum speeds of the photoelectrons corresponding to these wavelengths are  $u_1$  and  $u_2$ , respectively. If the ratio  $u_1 : u_2 = 2 : 1$  and  $u_3 : u_4 : u_5 = 2 : 1$  and  $u_5 : u_5 : u_5$ 

[JEE (Advanced)-2014, 3/60, -1]

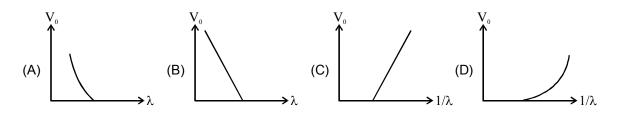
- (A) 3.7 eV
- (B) 3.2 eV
- (C) 2.8 eV
- (D) 2.5 eV

14. Consider a hydrogen atom with its electron in the n<sup>th</sup> orbital. An electromagnetic radiation of wavelength 90 nm is used to ionize the atom. If the kinetic energy of the ejected electron is 10.4 eV, then the value of n is (hc = 1242 eV nm). [JEE Advanced-2015]

**15.** Planck's constant h, speed of light c and gravitational constant G are used to form a unit of length L and a unit of mass M. Then the correct option(s) is(are):- [JEE Advanced-2015]

- (A)  $M \propto \sqrt{c}$
- (B)  $M \propto \sqrt{G}$
- (C)  $L \propto \sqrt{h}$
- (D)  $L \propto \sqrt{G}$

16. For photo-electric effect with incident photon wavelength  $\lambda$ , the stopping potential is  $V_0$ . Identify the correct variation(s) of  $V_0$  with  $\lambda$  and  $1/\lambda$ . [JEE Advanced-2015]



An electron in an excited state of  $Li^{2+}$  ion has angular momentum  $3h/2\pi$ . The de Broglie wavelength of the electron in this state is  $p\pi a_0$  (where  $a_0$  is the Bohr radius). The value of p is **[JEE Advanced-2015]** 

18. In a historical experiment to determine Planck's constant, a metal surface was irradiated with light of different wavelengths. The emitted photoelectron energies were measured by applying a stopping potential. The relevant data for the wavelength  $(\lambda)$  of incident light and the corresponding stopping potential  $(V_0)$  are given below:

[JEE Advanced-2016]

$\overline{\lambda(\mu m)}$	$V_0(Volt)$
0.3	2.0
0.4	1.0
0.5	0.4

Given that  $c = 3 \times 10^8 \text{ ms}^{-1}$  and  $e = 1.6 \times 10^{-19} \text{C}$ , Planck's constant (in units of J s) found from such an experiment is:

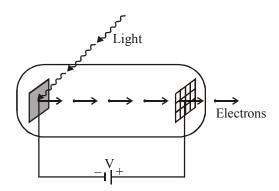
- (A)  $6.0 \times 10^{-34}$
- (B)  $6.4 \times 10^{-34}$
- (C)  $6.6 \times 10^{-34}$
- (D)  $6.8 \times 10^{-34}$

19. Highly excited states for hydrogen like atoms (also called Rydberg states) with nuclear charge Ze are defined by their principal quantum number n, where n >> 1. Which of the following statement(s) is (are) true?

[JEE Advanced-2016]

- (A) Relative change in the radii of two consecutive orbitals does not depend on Z
- (B) Relative change in the radii of two consecutive oribitals varies as 1/n
- (C) Relative change in the energy of two consecutive orbitals varies as  $1/n^3$
- (D) Relative change in the angular momenta of two consecutive orbitals varies as 1/n
- 20. A hydrogen atom in its ground state is irradiated by light of wavelength 970 Å. Taking  $hc/e = 1.237 \times 10^{-6} \text{ eV}$  m and the ground state energy of hydrogen atom as -13.6 eV, the number of lines present in the emission spectrum is [JEE Advanced-2016]
- Light of wavelength  $\lambda_{ph}$  falls on a cathode plate inside a vacuum tube as shown in the figure. The work function of the cathode surface is  $\phi$  and the anode is a wire mesh of conducting material kept at a distance d from the cathode. A potential difference V is maintained between the electrodes. If the minimum de Broglie wavelength of the electrons passing through the anode is  $\lambda_{e}$ , which of the following statement(s) is(are) true?

[JEE Advanced-2016]



- (A) For large potential difference (V >>  $\phi$ /e),  $\lambda_a$  is approximately halved if V is made four times
- (B)  $\lambda_{\rm e}$  increases at the same rate as  $\lambda_{\rm ph}$  for  $\lambda_{\rm ph}$  < hc/ $\phi$
- (C)  $\lambda_a$  is approximately halved, if d is doubled
- (D)  $\lambda_e$  decreases with increase in  $\phi$  and  $\lambda_{nh}$
- 22. An electron in a hydrogen atom undergoes a transition from an orbit with quantum number n, to another with

quantum number  $n_f$ .  $V_i$  and  $V_f$  are respectively the initial and final potential energies of the electron. If  $\frac{V_i}{V_f} = 6.25$ , then the smallest possible  $n_f$  is.

 $\textbf{23.} \qquad \text{A photoelectric material having work-function } \phi_0 \text{ is illuminated with light of wavelength } \lambda \left( \lambda < \frac{hc}{\phi_0} \right). \text{ The fastest } \lambda \left( \lambda < \frac{hc}{\phi_0} \right) = 0.$ 

photoelectron has a de-Broglie wavelength  $\lambda_{\rm d}$ . A change in wavelength of the incident light by  $\Delta\lambda$  results in a change  $\Delta\lambda_{\rm d}$  in  $\lambda_{\rm d}$ . Then the ratio  $\Delta\lambda_{\rm d}/\Delta\lambda$  is proportional to 

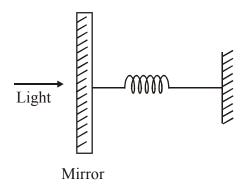
[JEE Advanced-2017]

- (A)  $\lambda_d^3 / \lambda^2$
- (B)  $\lambda_d^3 / \lambda$
- (C)  $\lambda_d^2/\lambda^2$
- (D)  $\lambda_d/\lambda$
- 24. In a photoelectric experiment a parallel beam of monochromatic light with power of 200 W is incident on a perfectly absorbing cathode of work function 6.25 eV. The frequency of light is just above the threshold frequency so that the photoelectrons are emitted with negligible kinetic energy. Assume that the photoelectron emission efficinecy is 100% A potential difference of 500 V is applied between the cathode and the anode. All the emitted electrons are incident normally on the anode and are absorbed. The anode experiences a force  $F = n \times 10^{-4} \text{ N}$  due to the impact of the electrons. The value of n is....... Mass of the electron  $m_e = 9 \times 10^{-31} \text{ kg}$  and  $1.0 \text{ eV} = 1.6 \times 10^{-19} \text{ J}.?$
- 26. A free hydrogen atom after absorbing a photon of wavelength  $\lambda_a$  gets excited from the state n = 1 to the state n = 4. Immediately after that the electron jumps to n = m state by emitting a photon of wavelength  $\lambda_e$ . Let the change in momentum of atom due to the absorption and the emission are  $\Delta p_a$  and  $\Delta p_e$ , respectively. If  $\lambda_a/\lambda_e = \frac{1}{5}$ . Which of the option(s) is/are correct? [Use hc = 1242 eV nm; 1 nm =  $10^{-9}$  m, h and c are

Planck's constant and speed of light, respectively]

[JEE Advanced-2019]

- (A)  $\lambda_{e} = 418 \text{ nm}$
- (B) The ratio of kinetic energy of the electron in the state n = m to the state n = 1 is  $\frac{1}{4}$
- (C) m = 2
- (D)  $\Delta p_a / \Delta p_e = \frac{1}{2}$
- 27. A perfectly reflecting mirror of mass M mounted on a spring constitutes a spring-mass system of angular frequency  $\Omega$  such that  $\frac{4\pi M\Omega}{h} = 10^{24} \text{m}^{-2}$  with h as Planck's constant. N photons of wavelength  $\lambda = 8\pi \times 10^{-6} \text{m}$  strike the mirror simultaneously at normal incidence such that the mirror gets displaced by 1µm. If the value of N is x × 10<sup>12</sup>, then the value of x is \_\_\_\_\_. [JEE Advanced-2019] [Consider the spring as massless]



## PART - II: JEE(MAIN) / AIEEE PROBLEMS (PREVIOUS YEARS)

1. Statement-1: When ultraviolet light is incident on a photocell, its stopping potential is  $V_0$  and the maximum kinetic energy of the photoelectrons is  $K_{max}$ . When the ultraviolet light is replaced by X-rays, both  $V_0$  and  $K_{max}$  increase. [AIEEE 2010, 4/144, -1]

**Statement-2:** Photoelectrons are emitted with speeds ranging from zero to a maximum value because of the range of frequencies present in the incident light.

- (1) Statement-1 is true, Statement-2 is true; Statement-2 is the correct explanation of Statement-1.
- (2) Statement-1 is true, Statement-2 is true; Statement-2 is not the correct explanation of Statement-1
- (3) Statement-1 is false, Statement-2 is true.
- (4) Statement-1 is true, Statement-2 is false.
- 2. If a source of power 4 kW produces 10<sup>20</sup> photons/second, the radiation belongs to a part of the spectrum called:

  [AIEEE 2010, 4/144, -1]
  - (1) X-rays
- (2) ultraviolet rays
- (3) microwaves
- (4) γ-rays
- 3. Energy required for the electron excitation in Li<sup>++</sup> from the first to the thrid Bohr orbit is:

[AIEEE - 2011, 4/120, -1]

(1) 12.1 eV

(2) 36.3 eV

(3) 108.8 eV

(4) 122.4 eV

4. This questions has Statement –1 and statement –2. Of the four choices given after the statements, choose the one that best describes the two statements : [AIEEE - 2011, 1 May; 4/120, –1]

#### Statement -1:

A metallic surface is irradiated by a monochromatic light of frequency  $v > v_0$  (the threshold frequency). The maximum kinetic energy and the stopping potential are  $K_{max}$  and  $V_0$  respectively. If the frequency incident on the surface is doubled, both the  $K_{max}$  and  $V_0$  are also doubled.

#### Statement -2:

The maximum kinetic energy and the stopping potential of photoelectrons emitted from a surface are linearly dependent on the frequency of incident light.

- (1) Statement –1 is true, statement –2 is false.
- (2) Statement –1 is true, Statement –2 is true, Statement –2 is the correct explanation of Statement –1
- (3) Statement –1 is true, Statement –2 is true, Statement –2 is not the correct explanation of Statement–1
- (4) Statement-1 is false, Statement -2 is true
- 5. After absorbring a slowly moving neutron of Mass  $m_N$  (momentum  $\approx 0$ ) a nucleus of mass M breaks into two nuclei of masses  $m_1$  and  $5m_1$  (6  $m_1$  = M +  $m_N$ ) respectively. If the de Broglic wavelength of the nucleus with mass  $m_1$  is  $\lambda$ , the de Broglie wevelength of the nucleus will be: [AIEEE 2011, 11 May; 4/120, -1]
  - $(1)5\lambda$
- (2) λ\5
- $(3) \lambda$

(4)  $25 \lambda$ 

Hydrogen atom is excieted from ground state to another state with principal quantum number equal to 4. 6. Then the number of spectral lines in the emission spectra will be: [AIEEE 2012; 4/120, -1]

(1)2

(2) 3

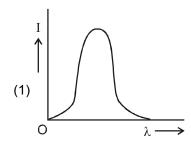
(3) 5

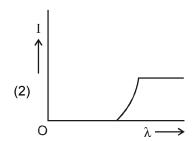
(4)6

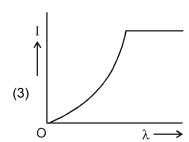
7. A diatomic molecule is made of two masses m<sub>1</sub> and m<sub>2</sub> which are separated by a distance r. If we calculate its rotational energy by applying Bohr's rule of angular momentum quantization, its energy will be given by: (n is an integer) [AIEEE 2012; 4/120, -1]

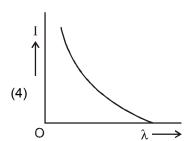
 $(1) \frac{(m_1 + m_2)^2 n^2 h^2}{2 m_1^2 m_2^2 r^2} \qquad (2) \frac{n^2 h^2}{2 (m_1 + m_2) r^2} \qquad (3) \frac{2 n^2 h^2}{(m_1 + m_2) r^2} \qquad (4) \frac{(m_1 + m_2) n^2 h^2}{2 m_1 m_2 r^2}$ 

The anode voltage of a photocellis kept fixed. The wavelength  $\lambda$  of the light falling on the cathode is gradually 8. changed. The plate current I of the photocell varies as follows: [JEE-Main 2013; 4/120, -1]









9. Ina hydrogen like atom electron make transition from an energy level with quantum number n to another with quantum number (n-1). If n>>1, the frequency of radiation emitted is proportional to:

[JEE-Main 2013; 4/120, -1]

 $(1) \frac{1}{n}$ 

(2)  $\frac{1}{n^2}$ 

(3)  $\frac{1}{n^{3/2}}$ 

The radiation corresponding to  $3 \rightarrow 2$  transition of hydrogen atom falls on a metal surface to produce 10. photoelectrons. These electrons are made to enter a magnetic field of 3 × 10<sup>-4</sup> T. If the radius of the largest circular path followed by these electrons is 10.0 mm, the work function of the metal is close to:

[JEE-Main 2014; 4/120, -1]

(1) 1.8 eV

(2) 1.1 eV

(3) 0.8 eV

(4) 1.6 eV

Hydrogen (,H1), Deuterium (,H2), singly ionised Helium (,He4)† and doubly ionised lithium (,Li6)++ all have one 11. electron around the nucleus. Consider an elelctron transition from n = 2 to n = 1. If the wave lengths of emitted radiation are  $\lambda_4$ ,  $\lambda_2$ ,  $\lambda_3$ , and  $\lambda_4$  respectively then approximately which one of the following is correct?

$$(1) 4\lambda_1 = 2\lambda_2 = 2\lambda_3 = \lambda_4$$

$$(2) \lambda_1 = 2\lambda_2 = 2\lambda_3 = \lambda_4$$

(2) 
$$\lambda_1 = 2\lambda_2 = 2\lambda_3 = \lambda_4$$
 [JEE-Main 2014; 4/120, -1]

(3) 
$$\lambda_1 = \lambda_2 = 4\lambda_3 = 9\lambda_4$$

$$(4) \lambda_1 = 2\lambda_2 = 3\lambda_3 = 4 \lambda_4$$

- As an electron makes a transition from an excited state to the ground state of a hydrogen like 12. atom/ion: [JEE Main-2015; 4/120, -1]
  - (1) kinetic energy decreases, potential energy increases but total energy remains same
  - (2) kinetic energy and total energy decrease but potential energy increases
  - (3) its kinetic energy increases but potential energy and total energy decreases
  - (4) kinetic energy, potential energy and total energy decrease
- Match List-I (Fundament Experiment) with List-II (its conclusion) and select the correct option from the 13. choices given below the list: [JEE Main-2015; 4/120. -1]

	List-I		List-II
(A)	Franck-Hertz Experiment.	(i)	Particle nature of light
(B)	Photo-electric experiment	(iii)	Discrete energy levels of atom
(C)	Davison-Germer Experiment	(iiii)	Wave nature of electroc
		(iv)	Structure of atom

Radiation of wavelength  $\lambda$ , is incident on a photocell. The fastest emitted electron has speed  $\nu$ . If the wavelength 14.

of changed to  $\frac{3\lambda}{4}$ , the speed of the fastest emitted electron will be :- [JEE Main-2016; 4/120. -1]

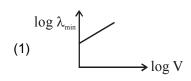
$$(1) = v \left(\frac{3}{5}\right)^{1/2} \qquad (2) > v \left(\frac{4}{3}\right)^{1/2} \qquad (3) < v \left(\frac{4}{3}\right)^{1/2} \qquad (4) = v \left(\frac{4}{3}\right)^{1/2}$$

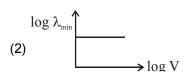
$$(2) > v \left(\frac{4}{3}\right)^{1/3}$$

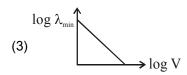
$$(3) < v \left(\frac{4}{3}\right)^{1/2}$$

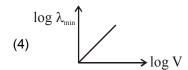
$$(4) = v \left(\frac{4}{3}\right)^{1/2}$$

An electron beam is accelerated by a potential difference V to hit a metallic target to produce 15. X-rays. It produces continuous as well as characteristic X-rays. If  $\lambda_{min}$  is the smallest possible wavelength of X-ray in the spectrum, the variation of log  $\lambda_{min}$  with log V is correctly represented in: [JEE Main-2017; 4/120. –1]

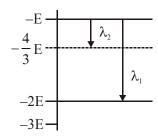








Some energy levels of a molecule are shown in the figure. The ratio of the wavelengths  $r = \lambda_1/\lambda_2$ , is given by : 16. [JEE Main-2017; 4/120. -1]



- (1)  $r = \frac{3}{4}$
- (2)  $r = \frac{1}{2}$
- (3)  $r = \frac{4}{3}$
- (4)  $r = \frac{2}{2}$
- A particle A of mass m and initial velocity v collides with a particle B of mass  $\frac{m}{2}$  which is at rest. The collision 17. is head on, and elastic. The ratio of the de–Broglie wavelengths  $\lambda_{_{A}}$  to  $\lambda_{_{B}}$  after the collision is:

[JEE Main 2017; 4/120, -1]

- $(1) \frac{\lambda_{A}}{\lambda_{B}} = \frac{2}{3} \qquad (2) \frac{\lambda_{A}}{\lambda_{B}} = \frac{1}{2} \qquad (3) \frac{\lambda_{A}}{\lambda_{D}} = \frac{1}{3}$
- (4)  $\frac{\lambda_A}{\lambda} = 2$
- 18. If the series limit frequency of the Lyman series is  $v_L$ , then the series limit frequency of the Pfund series is:

[JEE Main 2018; 4/120, -1]

- $(1) 16 v_1$
- $(2) v_1 / 16$
- $(3) v_1/25$
- $(4) 25 v_1$
- At a given instant, say t = 0, two radioactive substances A and B have equal activities. The ratio  $\frac{R_B}{R_A}$  of their 19. activities after time t itself decays with time t as e<sup>-3t</sup>. If the half-life of A is ℓn2, the half-life of B is: [JEE Main 2019, Jan.; 4/120, -1]
  - (1)  $\frac{ln2}{2}$
- (2) 2In2
- $(3) \frac{l n 2}{4}$
- (4) 4In2
- 20. The magnetic field associated with a light wave is given, at the origin, by

B = B<sub>0</sub> [
$$\sin(3.14 \times 10^7)$$
ct +  $\sin(6.28 \times 10^7)$ ct].

If this light falls on a silver plate having a work function of 4.7 eV, what will be the maximum kinetic energy of the photo electrons ?(c =  $3 \times 10^8 \text{ms}^{-1}$ , h =  $6.6 \times 10^{-34} \text{ J-s}$ ) [JEE Main-2019, Jan.; 4/120, -1]

- (1) 7.72 eV
- (2) 8.52 eV
- (3) 12.5 eV
- (4) 6.82 eV
- A sample of radioactive material A, that has an activity of 10 mCi(I Ci = 3.7 × I010 decays/s), has twice the 21. number of nuclei as another sample of a different radioactive maternal B which has an activity of 20 mCi. The correct choices for hall-lives of A and B would then be respectively: [JEE Main 2019, Jan.; 3/120, -1]
  - (1) 20 days and 5 days

(2) 20 days and 10 days

(3) 5 days and 10 days

(4) 10 days and 40 days

22.

	(Energj	r of photon = $\frac{1}{\lambda t}$	(in nm) eV)		
	(1) 1.8		(2) 1.4	(3) 2.5	(4) 5.6
23.	Condis	er the nuclear fis	ssion		
	$Ne^{20} \rightarrow$	2He <sup>4</sup> + C <sup>12</sup>			
		hat the binding e lentify the corre		•	ively, 8.03 MeV, 7.07 MeV and 7.86 EE Main 2019, Jan.; 4/120, -1]
	(1) 8.3	MeV energy will	be released	(2) energy of	f 12.4 MeV will be supplied
	(3) ene	rgy of 11.9 MeV	has to be supplied	(4) energy of	f 3.6 MeV will be released
24.	the me	tal is 5eV. The er	nergy of the incident phot	ons is 10 eV and only cond and their maxin	ity 16 mW/m <sup>2</sup> .The work function of 10% of it produces photo electrons. num energy, respectively, will be : E Main 2019, Jan.; 4/120, –1]
	(1) 10 <sup>10</sup>	and 5 eV		(2) 10 <sup>14</sup> and 10 eV	
	(3) 1012	and 5 eV		(4) 10 <sup>11</sup> and 5 eV	
25.	was 16	00 counts per se		was 100 counts per se	active source is measured. At t = 0 it econd. The count rate observed, as E Main 2019, Jan.; 4/120, –1]
	(1) 150		(2) 360	(3) 200	(4) 400
26.			pe, the resolution that car n of 7.5 × $10^{-12}$ m, the mini	imum electron energy	order of the wavelength of electrons required is close to :  E Main 2019, Jan.; 4/120, –1]
	(1) 100	keV	(2) 500 keV	(3) 25 keV	(4) 1 keV
27.				o the L-shell, the wave	EL-shell, the wavelength of emitted length of emitted radiation will be:- Main-2019, Jan.; 4/120, –1]
	(1)	$\frac{27}{20}\lambda$	$(2) \frac{16}{25} \lambda$	$(3) \frac{20}{27} \lambda$	$(4) \frac{25}{16} \lambda$
28.	In a ph	otoelectric expe	riment, the wavelength o	f the light incident on a	a metal is changed from 300 nm to
	400 nm	400 nm. The decrease in the stopping potential is close to : $\left(\frac{hc}{e} = 1240  \text{nm} - \text{V}\right)$			
				[JEE	E Main 2019, Jan.; 4/120, −1]
	(1) 0.5	V	(2) 1.0 V	(3) 2.0 V	(4) 1.5 V
29.					oton of wavelength 980Å. The radius IEE Main-2019, Jan.; 4/120, –1]
	$(h_c = 12500 \text{ eV} - \text{Å})$				
	(1) 9a <sub>0</sub>		(2) 25a <sub>0</sub>	$(3) 4a_0$	(4) 16a <sub>0</sub>

Surface of certain metal is first illuminated with light of wavelength  $\lambda_1$  =350 nm and then, by light of wavelength  $\lambda_2$ =540 nm. It is found that the maximum speed of the photo electrons in the two cases differ by a factor of 2. The work function of the metal (in eV) is close to: [JEE Main-2019, Jan.; 4/120, -1]

JEE (Adv.)-Physics Modern Physics If the deBronglie wavelenght of an electron is equal to 10<sup>-3</sup> times the wavelength of a photon of frequency 30.  $6 \times 10^{14}$  Hz, then the speed of electron is equal to : [JEE Main-2019, Jan.; 4/120, -1] (Speed of light =  $3 \times 10^8$  m/s Planck's constant =  $6.63 \times 10^{-34}$  J.s Mass of electron =  $9.1 \times 10^{-31}$  kg)  $(2) 1.7 \times 10^6 \text{ m/s}$  $(3) 1.8 \times 10^6 \text{ m/s}$  $(1) 1.45 \times 10^6 \text{ m/s}$  $(4) 1.1 \times 10^6 \text{ m/s}$ 31. When a certain photosensistive surface is illuminated with monochromatic light of frequency v, the stopping potential for the photo current is  $-V_0/2$ . When the surface is illuminated by monochromatic light of frequency v/2, the stopping potential is  $-V_0$ . The threshold frequency for photoelectric emission is: [JEE Main-2019, Jan.; 4/120, -1] (1)  $\frac{3v}{2}$ (4)  $\frac{5v}{3}$ (3)  $\frac{4}{3}$  V (2) 2vIn a radioactive decay chain, the initial nucleus is  $\frac{232}{90}$ Th . At the end there are 6  $\alpha$ -particles and 4  $\beta$ -particles 32. which are emitted. If the end nucleus, If  ${}_{7}^{A}X$ , A and Z are given by : [JEE Main-2019, Jan.; 3/120, -1] (1) A = 208; Z = 80(2) A = 202; Z = 80(3) A = 200; Z = 81(4) A = 208; Z = 8233. An alpha-particle of mass m suffers 1-dimensional elastic coolision with a nucleus at rest of unknown mass. It is scattered directly backwards losing, 64% of its initial kinetic energy. The mass of the nucleus is :-[JEE Main-2019, Jan.; 4/120, -1] (1) 4 m (2) 3.5 m (3) 2 m(4) 1.5 m In a Frank-Hertz experiment, an electron of energy 5.6 eV passes through mercury vapour and emerges with 34. an energy 0.7 eV. The minimum wavelength of photons emitted by mercury atoms is close to:-[JEE Main-2019, Jan.; 4/120, -1] (1) 2020 nm (2) 220 nm (4) 1700 nm (3) 250 nm A particle of mass m moves in a circular orbit in a central potential field  $U(r) = \frac{1}{2}kr^2$ . If Bohr's quantization 35. conditions are applied, radii of possible orbitals and energy levels vary with quantum number n as: [JEE Main-2019, Jan.; 4/120, -1] (1)  $r_n \propto n^2$ ,  $E_n \propto \frac{1}{n^2}$ (2)  $r_n \propto \sqrt{n}, E_n \propto \frac{1}{n}$ 

A particle A of mass 'm' and charge 'q' is accelerated by a potential difference of 50 V. Another particle B 36. of mass '4 m' and charge 'q' is accelerated by a potential difference of 2500 V. The ratio of de-Broglie wavelengths

 $\frac{\lambda_{\rm A}}{\lambda_{\rm B}}$  is close to :

(3)  $r_n \propto n$ ,  $E_n \propto n$ 

[JEE Main-2019, Jan.; 4/120, -1]

(1) 10.00

(2)14.14

(3)4.47

(4)  $r_n \propto \sqrt{n}$ ,  $E_n \propto n$ 

(4) 0.07

JEE	(Adv.)-Physics			Modern Physics
37.	•	•	_	evelengths are $\lambda_1$ and $\lambda_2$ respectively. The ength $\lambda$ , of the final particle, is given by : [JEE Main-2019, April; 4/120, -1]
	$(1) \lambda = \frac{\lambda_1 + \lambda_2}{2}$	$(2) \frac{2}{\lambda} = \frac{1}{\lambda_1} + \frac{1}{\lambda_2}$	$(3) \ \lambda = \sqrt{\lambda_1 \lambda_2}$	(4) $\frac{1}{\lambda^2} = \frac{1}{\lambda_1^2} + \frac{1}{\lambda_2^2}$
38.				es 'x' and 'y' having de-Broglie wavelengths ons, then the de-Broglie wavelength of 'P' [JEE Main-2019, April; 4/120, –1]
	(1) $\lambda_x + \lambda_y$	$(2) \frac{\lambda_x \lambda_y}{\lambda_x + \lambda_y}$	$(3) \frac{\lambda_x \lambda_y}{ \lambda_x - \lambda_y }$	(4) $\lambda_x - \lambda_y$
39.	A He+ ion is in its firs	t excited state. Its ioniza	ation energy is:	[JEE Main-2019, April; 4/120, –1]
	(1) 6.04 eV	(2) 13.60 eV	(3) 54.40 eV	(4) 48.36 eV
	As total energy of He	+ in 1st excited state is -	–13.6 eV, ionisatio	n energy should be +13.6eV.
40.	_		-	g surface with an energy flux of transferred to the surface in 40 min time  [JEE Main-2019, April; 4/120, -1]
	(1) 5.0 × 10 <sup>-3</sup> Ns	(2) 3.5 × 10 <sup>-6</sup> Ns	(3) 1.4 × 10 <sup>-6</sup> N	Ns (4) 6.3 × 10 <sup>-4</sup> Ns
41.	•	• • •		ed state to the second excited state and vavelengths, $\lambda_1/\lambda_2$ , of the photons emitted [JEE Main-2019, April; 4/120, -1]
	(1) 9/7	(2) 7/5	(3) 27/5	(4) 20/7
42.	Consider an electron i de-Broglie wavelengtl		olving in its second	excited state (having radius 4.65Å). The [JEE Main-2019, April; 4/120, –1]
	(1) 12.9 Å	(2) 3.5 Å	(3) 9.7 Å	(4) 6.6 Å
43.				minutes, respectively. If, initially a sample cayed numbers of nuclei A and B will be : [JEE Main-2019, April; 4/120, -1]
	(1) 9 : 8	(2) 1 : 8	(3) 8 : 1	(4) 3 : 8
44.	·		_	state orbit in a hydrogen atom is rst excited state (in s-1) is:
				[JEE Main-2020, Jan.; 4/120, –1]
	$(1) 6.2 \times 10^{15}$	$(2) 5.6 \times 10^{12}$	$(3) 7.8 \times 10^{14}$	$(4) 1.6 \times 10^{14}$
45.	kinetic energy T <sub>A</sub> eV er from another metal B b	nd de-Broglie wavelength by photon of energy 4.50	$\lambda_A$ . The maximum eV is $T_B = (T_A - 1.5)$	e ejected photoelectrons have maximum kinetic energy of photoelectrons liberated eV. If the de-Broglie wavelength of these [JEE Main-2020, Jan.; 4/120, –1]
	(1) 3eV	(2) 2eV	(3) 4eV	(4) 1.5eV

## **Answers**

## Exercise # 1

## PART - I

#### **SECTION (A):**

**A 1.** 
$$(0.6 \times 10^{15} \text{h} - 2\text{e}) \text{J} = 0.48 \text{ eV}$$

**A 2.** 
$$\frac{P^2}{2m} = \left(\frac{1.24 \times 10^4}{4000} - 2.5\right) eV = 0.6 \, eV \,;$$

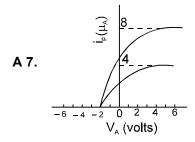
P = 
$$\sqrt{2 \times 9.1 \times 10^{-31} \times 0.6 \times 1.6 \times 10^{-19}}$$
  
= 4.2 ×10<sup>-25</sup> kg.m/s

**A 3.** 
$$I = \eta \cdot \frac{P}{E_{\lambda}} \times \frac{e}{100} = 1.84 \times 10^{-6} \text{ amp}$$

**A 4.** 
$$\left(\frac{9\times10^{15}}{2\pi e}h-2\right)$$
 eV = 3.93 eV

**A 5.** 
$$dV_s = \frac{hc}{e} \cdot \frac{d\lambda}{\lambda^2} = -\frac{hc}{228e} \times 10^7 = -5.5 \times 10^{-2} \text{ volt}$$

**A 6.** 
$$\frac{P\lambda}{hc \times 10^6}$$
 e A = 3.2  $\mu$  A



## **SECTION (B):**

**B 1.** 
$$5 \times 10^{-8} \text{ N}$$

**B 2.** (a) N = 
$$\frac{7 \times 10^{-4}}{\text{hc}}$$
 = 3.5 × 10<sup>21</sup>,

(b) 
$$\frac{7 \times 10^{-4}}{\text{hc}^2}$$
 = 1.2 × 10<sup>13</sup>,

(c) 
$$\frac{7 \times 10^{-4} \times 4\pi (1.5 \times 10^{11})^2}{\text{hc}} = 9.9 \times 10^{44}$$

**B 3.** 
$$\frac{354 \times 10^{-8}}{\text{hc}} = 1.77 \times 10^{19}$$

**B 4.** 
$$\frac{1.3 \times 30}{3 \times 10^8} = 1.3 \times 10^{-7}$$

### SECTION (C):

C-1. 
$$\lambda = \frac{2\lambda_1 \lambda_2}{\sqrt{\lambda_1^2 + \lambda_2^2}}$$

**C 2.** 
$$\lambda_d = \sqrt{\frac{h.\lambda.\lambda_{th}}{2m.c.(\lambda_{th} - \lambda)}} = \sqrt{\frac{6 \times 10^{-7} \, h}{m_e \, c}} \, m = 12.08 \, A^o$$

#### SECTION (D):

**D 1.** 
$$\lambda = 2\pi r = 2\pi \times 0.529 \text{ Å} = 1.058 \pi \text{ Å}$$

**D 2.** (a) 
$$r = 0.529 \times \frac{2^2}{2} = 1.058 \text{ Å}$$

$$E = -13.6 \times \frac{2^2}{2^2} = -13.6 \text{ eV}$$

(b) 
$$r = 0.529 \times \frac{3^2}{2} = 2.38 \text{ Å}$$

E = 
$$-13.6 \times \frac{2^2}{3^2} = -6.04 \text{ eV}.$$

**D 3.** 
$$T = \frac{2E_0}{3K} K = 1.05 \times 10^5 K$$

**D 5.** 
$$v = \frac{6}{h} \left[ 13.6e - \frac{hc \times 10^{10}}{1215} \right] = 5 \times 10^{15} \text{ Hz},$$

#### **SECTION (E):**

- **E 1**. (a) 91 nm (b) 23 nm
- **E 2**. n = 5

**E 3.** 
$$\frac{v_0}{r_0} \cdot \frac{z^2}{n^3} = \frac{2.19 \times 10^6}{0.529 \times 10^{-10}} \times \frac{Z^2}{n^3} = 2.07 \times 10^{16} \text{ s}^{-1}$$

**E 4.** 
$$\frac{E}{c} \cdot \frac{1}{m} = \frac{13.6 \times 3e}{4cm_p} = 3.25 \text{ m/s}$$

**E 5**. He<sup>+</sup> 4,

**E 6.** 
$$\frac{(E-E')}{E} \times 100 = 0.55 \times 10^{-6} \%$$

**E 7.** 
$$K_{\text{recoil}} = \left(\frac{6.4 \times 10^3 \,\text{e}}{\text{c}}\right)^2 \times \frac{1}{2 \times (9.3 \times 10^{26})} \text{J}$$
  
= 3.9 × 10<sup>-4</sup> eV

**E 8.** (a) 
$$\frac{hc}{13.6 \times 8e}$$
 = 113.7 Å (b) 3

### SECTION (F):

**F 1.** 
$$T_{min} = \frac{T}{2} = 10.2 = 20.4 \text{ eV}$$

#### SECTION (G):

**G 1.** 
$$\lambda = \frac{hc}{40 \times 10^3 e} m = 31.05 pm$$

**G 2.** 
$$v_1 = \frac{hc}{1.5e(\lambda_1 + 26 \times 10^{-12})} V = 15.9 \text{ kV}$$

G 3. approximately 0.1%

**G 4.** 
$$\lambda_1 = \frac{hc}{20 \times 10^3 \times (0.7)e} = 88.6 \text{ pm}$$
,

$$\lambda_2 = \frac{hc}{20 \times 10^3 \times (0.7 \times 0.3)e} = 295.6 \text{ pm},$$

$$\lambda_3 = \frac{hc}{20 \times 10^3 \times 0.7 \times (0.3)^2 e} = 985.6 \text{ pm},$$

**G 5.** 
$$\lambda_1 = \left(\frac{26-1}{29-1}\right)^2$$
 193 pm = 154 pm

**G 6.** (i) k<sub>a</sub> (ii) 102 keV.

**G 7.** n = 6, Z = 3

**G 8**. 42

#### SECTION (H):

**H1**. 12.89°

#### PART - II

#### SECTION (A):

**A 1.** (C) **A 2.** (B) **A 3.** (A) **A 4.** (B)

**A 5.** (A) **A-6.** (B) **A 7.** (B) **A 8.** (A)

### SECTION (B):

**B 1.** (D) **B 2.** (D)

#### SECTION (C):

**C 1**. (D) **C 2**. (B) **C 3**. (A) **C 4**. (C)

C 5. (D) C 6. (C) C 7. (B) C 8. (B)

**C 9.** (C) **C 10.** (A)

#### SECTION (D):

**D1** (C,D) **D2**. (B) **D3**. (A, B) **D4**. (C)

**D 5.** (B) **D 6.** (C) **D 7.** (A) **D 8.** (B)

**D 9.** (D) **D 10.** (D)

#### SECTION (E):

**E1.** (D) **E2.** (D) **E3.** (C) **E4.** (A)

**E 5.** (B) **E 6.** (C) **E 7.** (A) **E 8.** (C)

**E 10**. (2)

#### SECTION (F):

**F 1**. (A)

#### SECTION (G):

**G 1.** (C) **G 2.** (A) **G 3.** (C, D) **G 4.** (A,B,C,D)

**G 5.** (A,D) **G 6.** (B) **G 7.** (A)

#### SECTION (H):

**H1.** (A) **H2.** (D)

#### PART - III

1. (A) 
$$\rightarrow$$
 r, (B)  $\rightarrow$  s, (C)  $\rightarrow$  p, (D)  $\rightarrow$  q

2. (A) 
$$\rightarrow$$
 r (B)  $\rightarrow$  q,s (C)  $\rightarrow$  p, (D)  $\rightarrow$  q,s

3. (A)  $\rightarrow$  p,r, (b) q,s, (C) q,s, (D)  $\rightarrow$  p,r

## Exercise # 2

## PART - I

- 2. (D) 4. (A) 1. (B) 3. (A)
- 5. (D) 6. (D) 7. (C) (B) 8.
- 9. (D) 10. (D) (B) 12. (C) 11.
- 13. (D) 14. (B) 15. (D) 16. (B)
- 17. (D) 18. (D) 19. (A) 20. (B)

(D)

- (C) (C) (D) 25. (A) 26. (C) 27. 28. (D) (D)
- 29. (B) 30. (C)

22.

21.

### PART - II

23.

24.

- 1. 57.00 2. 04.00
- 3. 03.80 4. 151.00 and 00.50
- 5. 12.50 6.
- 7. 0.00 8. 00.55
- 9. (i) 300 (ii) 2.50
- 10. (a) 2000, 1500
  - (b) 7.75 eV, 7.35 eV, 6.2 eV, 0 eV
  - (c) 8.27 volt
- 11. (i) 48, (ii) 6, (iii) 600
- (i) 4.23 (ii) 3.4 12.
- 3.13 13.
- 14. 63.75
- (ii) Yes, 0.8 15. (i) 0.62 Å
- 16. 3.47
- 17. (a) 5 (b) 286.18 (c) 111
- 18. 2eV, 0.74V
- 19.  $6, 1.875 \mu m$

03.00

- 20. 1.86
- 21. 15.00

### **PART - III**

- 1. (A,B,C)
- 2. (A,B,C)
- 3. (A,B,C)
- 4. (A,B)
- 5. (A, B, D)
- (A,B,C)6.

## PART - IV

- 1. 2. (A) 3. 4. (D) (B) (C)
- 5. (C) (D) 6.

## Exercise #3

## PART - I:

- 3 2. (B) 4. (C) 1. (D) 3.
- 5. (A) 6. (C) 7. (B) 8. 7
- 9. (B) 10. 1 11. (A,C) 12. (B)
- 13. (A) 14. 2 15. (A,C,D)
- 16. (A,C) 17. 2 18. (B) 19. (A,B,D)
- 20. 21. (A) 5 23. 22. (A)
- 24 [23.60, 24.40] 24. 25. 3 [3,3]
- 26. (B,C) **27**. 1.00

#### PART - II

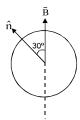
- 1. (4) 2. (2) 3. (3) 4. (4)
- 5. (3)6. (4) 7. (4) 8. (4)
- 9. (4) 10. (2) 11. (3) 12. (3)
- 13. 14. (2) (1) 15. (3) 16. (2)
- 17. (4) 18. (3) 19. (3) 20. (1)
- 21. (1) 22. (1) 23. (3) 24. (4)
- 25. (3)26. (3)27. (3) 28. (2)
- 29. (4) 30. (1) 31. (1) 32. (4)
- 33. (1) 34. (3) 35. (4) 36. (2)
- 37. (4) 38. (3)39. (2) 40. (1)
- 41. (4) 42. (3)43. (1) 44. (3)
- 45. (3)

## **RANKER PROBLEMS**

#### SUBJECTIVE QUESTIONS

- 1. (i) Find the first excitation potential of He<sup>+</sup> ion (ii) Find the ionization potential of Li<sup>++</sup> ion.
- 2. A small particle of mass m moves in such a way that the potential energy  $U = -\frac{1}{2}mb^2r^2$ , where b is a constant and r is the distance of the particle from the origin (Nucleus). Assuming Bohr model of quantization of angular momentum and circular orbits, show that radius of the nth allowed orbit is proportional to  $\sqrt{n}$ .
- 3. Suppose the potential energy between electron & proton at a distance r is given by  $\frac{-ke^2}{3r^3}$ . Use Bohr's theory to obtain energy levels of such a hypothetical hydrogen atom.
- 4. In a transition to a state of excitation energy 10.19 eV a hydrogen atom emits a 4890 A° photon. Determine the binding energy of the initial state. Also find the nature of transition?
- 5. Suppose in certain conditions only those transitions are allowed to hydrogen atoms in which the principal quantum number n change by 2 (i) Find the smallest wavelength emitted by hydrogen (ii) List the wavelengths emitted by hydrogen in the visible range (380 nm to 780 nm)
- **6.** Find the velocity of photoelectrons liberated by electromagnetic radiation of wavelength
  - $\lambda$  = 18.0 nm from stationary He<sup>+</sup> ions in the ground state.
- 7. (I) Find the maximum wavelength  $\lambda$  of light which can ionize a H-atom in ground state.
  - (II) Light of wavelength  $\lambda$  is incident on a H-atom which is in its first excited state. Find the kinetic energy of the electron coming out.
- 8. A beam of monochromatic light of wavelength  $\lambda$  ejects photoelectrons from a cesium surface ( $\Phi$  = 1.9 eV) These photoelectrons are made to collide with hydrogen atoms in ground state .Find the maximum value of  $\lambda$  for which (a) hydrogen atoms may be ionised (b) hydrogen atoms may get excited from the ground state to the first excited state and (c) the excited hydrogen atoms may emit visible light.
- **9.** Hydrogen atom in its ground state is excited by means of monochromatic radiation of wave length 975A°. How many different lines are possible in the resulting spectrum? Calculate the longest wavelength among them. You may assume the ionization energy of hydrogen atom as 13.6 eV.
- **10.** Average life time of a hydrogen atom excited to n = 2 state is  $10^{-8}$  s. Find the number of revolutions made by the electrons on the average before it jumps to ground state.
- In a hydrogen like ionized atom a single electron is orbiting around a stationary positive charge. If a spectral line of  $\lambda$  equal to 4861Å is observed due to transition from n = 12 to n = 6. What is the wavelength of a spectral line due to transition from n = 9 to n = 6 and also identify the element.

- **12.** For atoms of light and heavy hydrogen (H and D) find the difference;
  - (a) between the binding energies of their electrons in the ground state.
  - (b) between the wavelengths of first lines of the Lyman series.
- **13.** An electron in the ground state of hydrogen atoms is revolving in anti clock wise direction in a circular orbit of radius R.



- (i) Obtain an expression for the orbital magnetic dipole moment of the electron.
- (ii) The atom is placed in a uniform magnetic induction, such that the plane normal to the electron orbit make an angle of 30° with the magnetic induction. Find the torque experienced by the orbiting electron.

  [JEE 1996, 5]
- **14.** A proton and an electron, both at rest initially, combine to form a hydrogen atom in ground state. A single photon is emitted in this process. What is the wavelength?
- A neutron of kinetic energy 65 eV collides inelastically with a singly ionized helium atom at rest. It is scattered at an angle of 90° with respect of its original direction. [JEE 1993; 9 + 1M]
  - (a) Find the allowed values of the energy of the neutron and that of the atom after the collision.
  - (b) If the atom gets de-excited subsequently by emitting radiation, find the frequencies of the emitted radiation. [Given: Mass of He atom =  $4 \times (\text{mass of neutrons Ionization energy of H atom} = 13.6 \text{ eV}]$
- Assume that the de Broglie wave associated with an electron can form a standing wave between the atoms arranged in a one dimensional array with nodes at each of the atomic sites. It is found that one such standing wave is formed if the distance 'd' between the atoms of the array is 2 Å. A similar standing wave is again formed if 'd' is increased to 2.5 Å but not for any intermediate value of d. Find the energy of the electrons in electron volts and the least value of d for which the standing wave of the type described above can form.

  [JEE 1997, 5]

## **Answers**

1. (a) 
$$-13.6 \times (2)^2 \left[ \frac{1}{2^2} - \frac{1}{1^2} \right] = 40.8 \text{ V (b) } 13.6 \times \frac{3^2}{1^2} = 122.4 \text{ V}$$

3. 
$$E = \left(\frac{nh}{2\pi}\right)^6 \frac{1}{6 (Ke^2)^2 m^3}$$

4. 
$$\frac{13.6}{(4)^2}$$
 =0.85eV(n = 4 to n= 2)

5. (a) 
$$\frac{9}{8R}$$
 = 103 nm (b)  $\frac{16}{3R}$  = 487 nm

6. 
$$\sqrt{\frac{2}{m_e} \left[ \frac{10^9 \text{hc}}{18} - 54.4 \text{ e} \right]} = 2.2 \times 10^6 \text{ m/s}$$

8. (a) 
$$\lambda = \frac{hc}{(13.6+1.9) \text{ eV}} = 80 \text{ nm}$$
; (b)  $\lambda = \frac{hc}{(10.2+1.9) \text{ eV}} = 102 \text{ nm}$ ; (c)  $\frac{hc}{(12.08+1.9) \text{ eV}} = 89 \text{ nm}$ 

**9.** 
$$6, \ \lambda_{min} = \frac{16 \times 9}{7R} = 18800 \ A^{\circ},$$

**10.** 
$$10^{-8} \times \frac{2.19 \times 10^6}{2\pi (0.529 \times 10^{-10})} \times \frac{(1)^2}{(2)^3} = 8.2 \times 10^6$$

**12.** 
$$E_D - E_H = 3.7 \text{ meV}, \lambda_H - \lambda_D = 33 \text{ pm}$$

13. (i) 
$$\frac{\text{he}}{4\pi\text{m}}$$
 (ii)  $\frac{\text{heB}}{8\pi\text{m}}$ 

14. 
$$\lambda = \frac{12400 \text{ eV}}{13.6 \text{ eV}} = 911.76 \text{ Å} \approx 912 \text{ Å}$$

(b) 
$$1.82 \times 10^{15}$$
 Hz,  $11.67 \times 10^{15}$  Hz,  $9.84 \times 10^{15}$  Hz.

**16.** KE 
$$\cong$$
 151 eV,  $d_{least} = 0.5 A^0$ 

## **SELF ASSESSMENT PAPER**

## JEE (ADVANCED) PAPER - 1

## SECTION-1: ONE OPTION CORRECT TYPE (Maximum Marks - 12)

1.	A polychromatic light is used in an experime	ent on photoelectric effect.	The stopping potential
	, the significant of the side		e etebbilië betermen

(A) is related to the mean wavelength

(B) is related to the longest wavelength

(C) is related to the shortest wavelength (D) is not related to the wavelength.

2. A proton and an electron are accelerated by the same potential difference. Let  $\lambda_e$  and  $\lambda_p$  denote the de Broglie wavelengths of the electron and the proton respectively.

(A)  $\lambda_{e} = \lambda_{p}$  (B)  $\lambda_{e} < \lambda_{p}$  (C)  $\lambda_{e} > \lambda_{p}$ 

(D)  $\lambda_e$  and  $\lambda_p$  depends on the accelerating potential difference.

3. The highest energy state, that unexcited hydrogen atoms can reach when they are bombareded with 12.2 eV electron, is

(A) n = 1 (B) n = 2 (C) n = 3

4. The different lines in the Lyman series have their wavelengths lying between:

(A) zero to infinite (B) 900 Å to 1200 Å

(C) 1000 Å to 1500 Å (D) 500 Å to 1000 Å

## SECTION-2: ONE OR MORE THAN ONE CORRECT TYPE (Maximum Marks - 32)

5. When a hydrogen atom is excited from ground state to first excited state then

(A) its kinetic energy increases by 10.2 eV.

(B) its kinetic energy decreases by 10 .2 eV.

(C) its potential energy increases by 20.4 eV.

(D) its angular momentum increases by  $1.05 \times 10^{-34}$  J-s.

**6.** Two electrons starting from rest are accelerated by equal potential difference.

(A) they will have same kinetic energy

(B) they will have same linear momentum

(C) they will have same de Broglie wave length

(D) they may produce x-rays of same minimum wave length when they strike different targets.

7. A metallic sphere of radius r remote from all other bodies is irradiated with a radiation of wavelength  $\lambda$  which is capable of causing photoelectric effect.

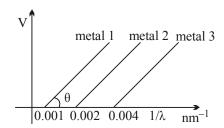
(A) the maximum potential gained by the sphere will be independent of its radius

(B) the net positive charge appearing on the sphere after a long time will depend on the radius of the sphere

(C) the maximum kinetic energy of the electrons emanating from the sphere will keep on declining with time

(D) the kinetic energy of the most energetic electrons emanating from the sphere initially will be independent of the radius of the sphere.

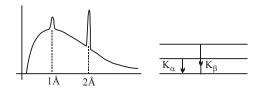
8. The graph between  $1/\lambda$  and stopping potential (V) of three metals having work functions  $\phi_1$ ,  $\phi_2$  and  $\phi_3$  in an experiment of photo-electric effect is plotted as shown in the figure. Which of the following statement(s) is/are correct? [Here  $\lambda$  is the wavelength of the incident ray].



- (A) Ratio of work functions  $\phi_1$ :  $\phi_2$ :  $\phi_3$  = 1 : 2 : 4
- (B) Ratio of work functions  $\phi_1: \phi_2: \phi_3 = 4:2:1$
- (C)  $\tan \theta$  is directly proportional to hc/e, where h is Planck's constant and c is the speed of light
- (D) The violet colour light can eject photoelectrons from metals 2 and 3.
- 9. In an x-ray tube the voltage applied is 20KV. The energy required to remove an electron from L shell is 19.9 KeV. In the x-rays emitted by the tube (Use hc = 12420 eVÅ)
  - (A) minimum wavelength will be 62.1 pm
  - (B) energy of the characterstic x-rays will be equal to or less than 19.9 KeV
  - (C) L<sub>a</sub> x-ray may be emitted
  - (D) L<sub>a</sub> x-ray will have energy 19.9 KeV
- **10.** An electron makes a transition from n = 2 to n = 1 state in a hydrogen like atom.
  - (A) magnetic field at the site of nucleus is decreased by 16 times.
  - (B) magnetic field at the site of nucleus is increased by 32 times
  - (C) angular momentum of electron is changed
  - (D) none of these
- **11.** A particular hydrogen like atom has its ground state Binding Energy =122.4eV.It is in ground state. Then:
  - (A) Its atomic number is 3.
  - (B) An electron of 90 eV can excite it.
  - (C) An electron of kinetic energy 91.8eV can be brought to almost rest by this atom.
  - (D) An electron of KE nearly 2.6 eV may emerge from the atom when electron of KE 125ev collides with this atom
- **12.** When a monochromatic point-source of light is at a distance of 0.2 m from a small photoelectric cell, the stopping potential and the saturation current are respectively 0.6 volt and 18.0 mA. If the same source is placed 0.6 m away from the photoelectric cell, then:
  - (A) The stopping potential will be 0.2 volt
- (B) The stopping potential will be 1.8 volt
- (C) The saturation current will be 6.0 mA
- (D) The saturation current will be 2.0 mA

## SECTION-3: NUMERICAL VALUE TYPE (Maximum Marks - 18)

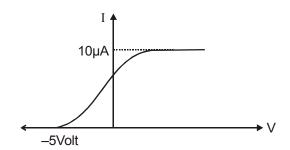
- 13. The wavelength of characteristic  $K_{\alpha}$ -line emitted by a hydrogen like element is 2.5 Å. Find the wavelength of the  $K_{\alpha}$ -line emitted by the same element (in Å). [Assume the shielding effect to be same as of  $K_{\alpha}$ ]
- **14.** Figure shows  $K_{\alpha}$  &  $K_{\beta}$  X-rays along with continuous X-ray. Find the energy of  $L_{\alpha}$  X-ray. (Use hc = 12420 evÅ).



- **15.** Determine the number of lines in Paschen series which have a wavelength greater than 1000 nm.
- **16.** A beam of light has three wavelengths 4144Å, 4972Å & 6216 Å with a total intensity of  $3.6 \times 10^{-3}$  W.m<sup>-2</sup> equally distributed amongst the three wavelengths. The beam falls normally on an area 1.0 cm<sup>2</sup> of a clean metallic surface of work function 2.3 eV. Assume that there is no loss of light by reflection and that each energetically capable photon ejects one electron. If the number of photoelectrons liberated in two seconds  $1.1 \times 10^x$ . Find x.
- 17. A point source of radiation power P is placed on the axis of completely absorbing disc. The distance between the source and the disc is 2 times the radius of the disc. If the force that light exerts on the

disc is 
$$\frac{P}{(x)c}$$
 . Find x?

18. In the photoelectric experiment, if we use a monochromatic light, the I - V curve is as shown. If work function of the metal is 2eV, estimate the power (in w) of light used. (Assume efficiency of photoemission =  $10^{-3}$ %, i.e. number of photoelectrons emitted are  $10^{-3}$ % of number of photons incident on metal.)



# **Answers**

**1.** (C)

**2**. (C)

**3.** (C)

**4.** (B)

**5.** (B,C,D)

**6.** (A,C,D)

**7.** (A,B,D)

**8.** (A, C)

**9.** (A,B,C)

**10.** (B,C)

**11.** (A,C,D)

**12.** (D)

**13.** 2

**14.** 6210

**15.** 4

**16.** 12

**17.** 20

**18.** 7