

Chapter : 9. PERCENTAGE

Exercise : 9A

Question: 1

Express each of t

Solution:

(i) 48% means, 48 divided by 100.

$$\text{So, } 48\% = 48 / 100$$

$$= 12 / 25$$

(ii) 220% means, 220 divided by 100.

$$\text{So, } 220\% = 220 / 100$$

$$= 11 / 5$$

(ii) 2.5% means, 2.5 divided by 100.

$$\text{So, } 2.5\% = 2.5 / 100$$

$$= 1 / 40$$

Question: 2

Express each of t

Solution:

(i) 6% means, 6 divided by 100.

$$\text{So, } 6\% = 6 / 100$$

$$= 3 / 50 = 0.06$$

(ii) 72% means, 72 divided by 100.

$$\text{So, } 72\% = 72 / 100$$

$$= 18 / 25 = 0.72$$

(iii) 125% means, 125 divided by 100.

$$\text{So, } 125\% = 125 / 100$$

$$= 5 / 4 = 1.25$$

Question: 3

Express each of t

Solution:

$$(i) \frac{9}{25} = \left(\frac{9}{25} \times 100 \right) \%$$

$$= (9 \times 4) \%$$

$$= 36\%$$

$$(ii) \frac{3}{125} = \left(\frac{3}{125} \times 100 \right) \%$$

$$= 2.4\%$$

$$(iii) \frac{12}{5} = \left(\frac{12}{5} \times 100 \right) \%$$

$$= (12 \times 20) \%$$

$$= 240\%$$

Question: 4

Convert the ratio

Solution:

$$4 : 5 = \frac{4}{5}$$

$$= \left(\frac{4}{5} \times 100\right) \% \text{ [Because } 100\% = 1]$$

$$= 80\%$$

Question: 5

Express 125% as a

Solution:

$$125\% = 125/100$$

$$= 5/4 \text{ [Divided by 25]}$$

$$= 5 : 4$$

Question: 6

Which is largest

Solution:

$$6\frac{2}{3}\%$$

$$= (20/3) \%$$

$$= (20/3 \times 1/100)$$

$$= 1/15$$

$$= 0.06 \text{ ____ (i)}$$

$$\frac{3}{20} = 0.15 \text{ ____ (ii)}$$

$$0.14 \text{ ____ (iii)}$$

From equation (i), (ii) and (iii),

$$0.15 > 0.14 > 0.06$$

Question: 7 A

What per cent of

Solution:

$$\text{Percentage} = (96/150 \times 100) \%$$

$$= (96/3 \times 2) \% \text{ [Divided by 50]}$$

$$= (32 \times 2) \%$$

$$= 64\%$$

Question: 7 B

What per cent of

Solution:

$$5 \text{ kg} = 5 \times 1000$$

$$= 5000 \text{ g}$$

Now,

$$\text{Percentage} = (200 / 5000 \times 100) \%$$

$$= (200 / 50) \% \text{ [Divided by 100]}$$

$$= 4 \%$$

Question: 7 C

What per cent of

Solution:

$$2 \text{ liters} = 2 \times 1000$$

$$= 2000 \text{ mL}$$

Now,

$$\text{Percentage} = (250 / 2000 \times 100) \%$$

$$= (250 / 20) \% \text{ [Divided by 100]}$$

$$= 12.5 \%$$

Question: 8

Find

Solution:

$$4\frac{1}{2}\% = (9 / 2) \times 100$$

$$= 9 / 200$$

Now,

$$9 / 200 \text{ of } 3600 = 9 / 200 \times 3600$$

$$= 9 \times 18 \text{ [Divided by 200]}$$

$$= 162$$

Question: 9

If 16% of number

Solution:

Let the number = Z

\therefore 16% of Z is 72.

$$\Rightarrow 16 / 100 \times Z = 72$$

$$\Rightarrow 16 Z = 7200$$

$$\Rightarrow Z = 7200 / 16$$

$$\Rightarrow Z = 450$$

Question: 10

A man saves 18% o

Solution:

Let Rs. Z his monthly income.

\therefore Saving = 18% of Rs. Z

$$\Rightarrow 3780 = 18 / 100 \times Z$$

$$\Rightarrow 3780 = 9 / 50 \times Z$$

$$\Rightarrow Z = 3780 \times 50 / 9$$

$$\Rightarrow Z = 420 \times 50$$

[Because $420 \times 9 = 3780$]

$$\Rightarrow Z = 21000$$

Therefore, his monthly income is Rs 21000/-

Question: 11

A football team w

Solution:

Let, total games played = Z

\therefore percentage of games won = 35% of Z

$$\Rightarrow 7 = 35 / 100 \times Z$$

$$\Rightarrow 7 = 7 / 20 \times Z \text{ [Divided by 5]}$$

$$\Rightarrow Z = 7 \times 20 / 7$$

$$\Rightarrow Z = 20$$

Question: 12

Amit was given an

Solution:

Let Amit's old salary = Z

\therefore Salary after increment = $(Z + 20Z / 100)$

Now,

$$\Rightarrow (Z + 20 Z / 100) = 30600$$

$$\Rightarrow (100 Z + 20 Z) / 100 = 30600$$

$$\Rightarrow 120 Z = 30600 \times 100$$

$$\Rightarrow Z = 25500$$

Question: 13

Sonal attended he

Solution:

Let the number of days the school was opened = Z

\therefore Percentage of attendance = 85% of Z

Now,

$$85\% \text{ of } Z = 204$$

$$\Rightarrow 85 / 100 \times Z = 204$$

$$\Rightarrow Z = 204 \times 100 / 85$$

$$\Rightarrow Z = 204 \times 20 / 17 \text{ [Divided by 5]}$$

$$\Rightarrow Z = 12 \times 20$$

$$\Rightarrow Z = 240$$

Question: 14

A's income

Solution:

Let B's income = 100

Then, A's income = $(100 - 20) = 80$

\therefore B's income more than A's income = $(100 - 80)/80 \times 100$

= $20/80 \times 100$

= $1/4 \times 100$

= 25

Question: 15

The price of petr

Solution:

Let the consumption of petrol = 1 unit and its cost = Rs.100

\therefore New cost of 1 unit of petrol = Rs.110

Now,

Rs.110 will yield 1 unit of petrol.

\therefore Rs.100 will yield $(1/110 \times 100)$

= $10/11$ unit of petrol

Now,

Reduction of consumption = $1 - (10/11)$

= $1/11$

Percentage of reduction = $(1/11 \times 100) \%$

= $9\frac{1}{11} \%$

Question: 16

The population of

Solution:

Let population of the town a year ago = Z

\therefore Present population = 108% of Z

$\Rightarrow 54000 = Z \times 108/100$

$\Rightarrow 54000 = Z \times 27/25$

$\Rightarrow Z = 54000 \times 25/27$

$\Rightarrow Z = 2000 \times 25$

$\Rightarrow Z = 50000$

Question: 17

The value of a ma

Solution:

Let the value of machine last year = Z

\therefore Present value = $(100 - 20) \%$ of Z

$\Rightarrow 160000 = 80\%$ of Z

$$\Rightarrow 160000 = Z \times 80/100$$

$$\Rightarrow Z = 160000 \times 100/80$$

$$\Rightarrow Z = 2000 \times 100$$

$$\Rightarrow Z = 200000$$

Question: 18

An alloy contains

Solution:

Given,

Percentage of copper = 40%

Percentage of nickel = 32%

\therefore Percentage of zinc = $\{100 - (40 + 32)\}$ %

$$= 28 \%$$

Now,

Mass of zinc in 1 kg of the alloy = $(28 \times 1/100)$ kg

$$= 0.28 \text{ kg}$$

$$= 0.28 \times 1000 \text{ g}$$

$$= 280 \text{ g}$$

Question: 19

Balanced diet sho

Solution:

Amount of proteins = 12% of 2600

$$= 2600 \times \frac{12}{100}$$

$$= 26 \times 12$$

= 312 calories

Amount of fats = 25% of 2600

$$= 2600 \times \frac{25}{100}$$

$$= 26 \times 25$$

= 650 calories

Amount of carbohydrates = 63% of 2600

$$= 2600 \times \frac{63}{100}$$

$$= 26 \times 63$$

= 1638 calories

Question: 20

Gunpowder contain

Solution:

Let the amount of gunpowder which carries 9 kg nitre = Z

$$\therefore 75\% \text{ of } Z = 9 \text{ kg}$$

$$\Rightarrow Z \times 75/100 = 9$$

$$\Rightarrow Z = 9 \times 100/75$$

$$\Rightarrow Z = 9 \times 4/3$$

$$\Rightarrow Z = 12 \text{ kg}$$

Now,

Let the amount of gunpowder which carries 2.5 kg sulphur = K

$$\therefore 10\% \text{ of } K = 2.5 \text{ kg}$$

$$\Rightarrow K \times 10/100 = 2.5$$

$$\Rightarrow K = 2.5 \times 100/10$$

$$\Rightarrow K = 2.5 \times 10$$

$$\Rightarrow K = 25 \text{ kg}$$

Question: 21

Divide Rs. 7000 a

Solution:

Let the amount of money gets by C = Rs. Z

$$\therefore \text{Amount of money B gets} = (50\% \text{ of Rs. } Z)$$

$$\therefore \text{Amount of money A gets} = (50\% \text{ of B})$$

$$= (25\% \text{ of Rs. } Z)$$

Now,

$$Z + (50\% \text{ of Rs. } Z) + (25\% \text{ of Rs. } Z) = \text{RS. } 7000$$

$$\Rightarrow Z + (Z \times 50/100) + (Z \times 25/100) = 7000$$

$$\Rightarrow Z + 50 Z/100 + 25 Z/100 = 7000$$

$$\Rightarrow 175 Z/100 = 7000$$

$$\Rightarrow Z = 7000 \times 100/175$$

$$\Rightarrow Z = 7000 \times 4/7$$

$$\Rightarrow Z = 4000$$

$$\therefore \text{C gets} = \text{Rs. } 4000$$

$$\therefore \text{Amount of money B gets} = (50\% \text{ of Rs. } Z)$$

$$= (50\% \text{ of Rs. } 4000)$$

$$= (\text{Rs. } 4000 \times 50/100)$$

$$= \text{Rs. } 2000$$

$$\therefore \text{Amount of money A gets} = (25\% \text{ of Rs. } Z)$$

$$= (25\% \text{ of Rs. } 4000)$$

$$= (\text{Rs. } 4000 \times 25/100)$$

$$= \text{Rs. } 1000$$

Question: 22

Find the percenta

Solution:

22-carat gold contains 22 parts out of 24 parts.

$$\therefore \text{Percentage of pure gold in 22-carat gold} = \left(\frac{22}{24} \times 100\right)\% = 91\frac{2}{3}\%.$$

Hence, 22-carat gold contains $91\frac{2}{3}\%$ of pure gold.

Question: 23

The salary of an

Solution:

Let the original salary = Rs.100

Then,

After increment of 25% = $100(1 + 25/100)$

$$= 100(125/100)$$

$$= \text{Rs.125}$$

Now,

To restore the original salary,

Let the new salary decreased by Z%

$$\therefore 125(1 - Z/100) = 100$$

$$\Rightarrow (1 - Z/100) = 100/125$$

$$\Rightarrow (1 - Z/100) = 4/5$$

$$\Rightarrow Z/100 = 1/5 [1 - 4/5 = 1/5]$$

$$\Rightarrow Z = 100/5$$

$$\Rightarrow Z = 20\%$$

Exercise : 9B

Question: 1

Choose the

Solution:

$$3/5 = (3/5 \times 100)\%$$

$$= (3 \times 20)\%$$

$$= 60\%$$

Question: 2

Solution:

$$0.8\% = 0.8/100$$

$$= 0.008$$

Question: 3

Solution:

$$6 : 5 = 6/5$$

$$= (6/5 \times 100)\% [100\% = 1]$$

$$= (6 \times 20)\%$$

$$= 120 \%$$

Question: 4**Solution:**

Let number = Z

Then,

$$5\% \text{ of } Z = 9$$

$$\Rightarrow \frac{5}{100} \times Z = 9$$

$$\Rightarrow 5 Z = 900$$

$$\Rightarrow Z = 180$$

Question: 5

What per cent of

Solution:

Let Z% of 90 is 120

$$\therefore \frac{Z}{100} \times 90 = 120$$

$$\Rightarrow 90 Z = 120 \times 100$$

$$\Rightarrow Z = \frac{12000}{90}$$

$$\Rightarrow Z = \frac{400}{3}$$

$$\Rightarrow Z = 133\frac{1}{3}\%$$

Question: 6

What per cent of

Solution:

$$10 \text{ kg} = 10 \times 1000$$

$$= 10000 \text{ g}$$

Let Z% of 1000 is 250

$$\therefore \frac{Z}{100} \times 10000 = 250$$

$$\Rightarrow 100 Z = 250$$

$$\Rightarrow Z = \frac{250}{100}$$

$$\Rightarrow Z = 2.5\%$$

Question: 7**Solution:**

Let, 40% of Z = 240

$$\Rightarrow \frac{40}{100} \times Z = 240$$

$$\Rightarrow Z = 240 \times \frac{100}{40}$$

$$\Rightarrow Z = 6 \times 100 [40 \times 6 = 240]$$

$$\Rightarrow Z = 600$$

Question: 8

$$?\% \text{ of } 400 = 60$$

Solution:

$$\text{Let, } Z\% \text{ of } 400 = 600$$

$$\Rightarrow Z/100 \times 400 = 600$$

$$\Rightarrow 4Z = 600$$

$$\Rightarrow Z = 600/4$$

$$\Rightarrow Z = 150$$

Question: 9

(180% of ?)

Solution:

$$\text{Let } (180\% \text{ of } Z) + 2 = 504$$

$$\therefore (180/100 \times Z) + 2 = 504$$

$$\Rightarrow (18/10 \times Z) = 504 - 2$$

$$\Rightarrow Z = (504 - 2) \times 10/18$$

$$\Rightarrow Z = 502 \times 10/9$$

$$\Rightarrow Z = 557.78$$

Question: 10

20% of Rs. 800 =

Solution:

$$20\% \text{ of Rs. } 800 = 20/100 \times 800$$

$$= 20 \times 8$$

$$= 160$$

Question: 11

In an examination

Solution:

$$\text{Let the maximum marks} = Z$$

$$\therefore 56\% \text{ of } Z = 98$$

$$\Rightarrow Z \times 56/100 = 98$$

$$\Rightarrow Z = 98 \times 100/56$$

$$\Rightarrow Z = 7 \times 100/4$$

$$\Rightarrow Z = 175$$

Question: 12

A number is first

Solution:

$$\text{Let the number} = Z$$

$$10\% \text{ increased by number} = Z (1 + 10/100)$$

$$= 11Z/10$$

Now,

$$10\% \text{ decreased by number} = 11Z/10 (1 - 10/100)$$

$$= (11Z/10) (90/100)$$

$$= 99Z/100$$

$$\therefore \text{difference} = Z - 99Z/100$$

$$= Z/100$$

$$\text{Percentage of decreases} = Z/100 \times 1/Z \times 100$$

$$= 1\%$$

Question: 13

A period of 4 hou

Solution:

$$4 \text{ hours } 30 \text{ min} = (4 \times 60) + 30$$

$$= 240 + 30$$

$$= 270 \text{ min}$$

$$24 \text{ hours} = 24 \times 60$$

$$= 1440 \text{ min}$$

Now,

$$\text{Percentage} = (270/1440 \times 100) \%$$

$$= (3/16 \times 100) \%$$

$$= (3/4 \times 25) \%$$

$$= (75/4) \%$$

$$= 18\frac{3}{4} \%$$

Question: 14

In an examination

Solution:

Let the total number of examines = Z

$$\text{Percentage of examines failed} = (100 - 65) \% = 35\%$$

$$\therefore 35\% \text{ of } Z = 420$$

$$\Rightarrow Z \times 35/100 = 420$$

$$\Rightarrow Z = 420 \times 100/35$$

$$\Rightarrow Z = 12 \times 100$$

$$\Rightarrow Z = 1200$$

Question: 15

A number exceeds

Solution:

Let the number = Z

$$\therefore 20\% \text{ of } Z + 40 = Z$$

$$\Rightarrow (Z \times 20/100) + 40 = Z$$

$$\Rightarrow Z/5 + 40 = Z$$

$$\Rightarrow Z - Z/5 = 40$$

$$\Rightarrow 4Z/5 = 40$$

$$\Rightarrow Z = 40 \times 5/4$$

$$\Rightarrow Z = 50$$

Question: 16

A number decrease

Solution:

Let the number = Z

$$\therefore Z - (27\frac{1}{2}\% \text{ of } Z) = 87$$

$$\Rightarrow Z - (Z \times 55/2 \times 1/100) = 87$$

$$\Rightarrow Z - (Z \times 11/2 \times 1/20) = 87$$

$$\Rightarrow Z - (11Z/40) = 87$$

$$\Rightarrow 29Z/40 = 87$$

$$\Rightarrow 29Z/40 = 87$$

$$\Rightarrow Z = 87 \times 40/29$$

$$\Rightarrow Z = 120$$

Question: 17

Solution:

$$\text{Percentage} = (0.05/20 \times 100) \%$$

$$= (0.05 \times 5) \%$$

$$= 0.25\%$$

Question: 18

One-third of 1206

Solution:

$$\text{Percentage} = \{(1/3 \times 1206) \times (1/134) \times 100\} \%$$

$$= \{402 \times 1/134 \times 100\} \%$$

$$= \{3 \times 100\} \%$$

$$= 300\%$$

Question: 19

x% of y is y% of <

Solution:

Let x% of y is y% of Z

$$\therefore x/100 \times y = y/100 \times Z$$

$$\Rightarrow x y/100 = y/100 \times Z$$

$$\Rightarrow Z = x y/100 \times 100/y$$

$$\Rightarrow Z = x$$

Question: 20

What per cent of <

Solution:

$$\text{Percentage} = \{(1/35)/(2/7) \times 100\} \%$$

$$\begin{aligned} &= \{1/35 \times 7/2 \times 100\} \% \\ &= \{1/5 \times 1/2 \times 100\} \% \\ &= \{1/5 \times 50\} \% \\ &= 10\% \end{aligned}$$

Exercise : CCE TEST PAPER-9

Question: 1 A

Express:

<

Solution:

24% means, 24 divided by 100.

$$\begin{aligned} \text{So, } 24\% &= 24/100 \\ &= 6/25 \end{aligned}$$

Question: 1 B

Express:

<

Solution:

105% means, 105 divided by 100.

$$\begin{aligned} \text{So, } 105\% &= 105/100 \\ &= 1.05 \end{aligned}$$

Question: 1 C

Express:

<

Solution:

$$\begin{aligned} 4 : 5 &= 4/5 \\ &= (4/5 \times 100) \% \text{ [Because } 100\% = 1] \\ &= 80\% \end{aligned}$$

Question: 1 D

Express:

<

Solution:

56% means, 56 divided by 100.

$$\begin{aligned} \text{So, } 56\% &= 56/100 \\ &= 14/25 \\ &= 14:25 \end{aligned}$$

Question: 2

If 34% of a number

Solution:

$$\begin{aligned} \text{Let the number} &= Z \\ \therefore 34\% \text{ of } Z &= 85 \end{aligned}$$

$$\Rightarrow 34/100 \times Z = 85$$

$$\Rightarrow Z = 85 \times 100/34$$

$$\Rightarrow Z = 5 \times 100/2$$

$$\Rightarrow Z = 250$$

Question: 3

The value of a ma

Solution:

Let the value of the machine last year = Z

\therefore Present value of the machine = (100 - 10) % of Rs.Z

$$\Rightarrow 54000 = 90\% \text{ of } Z$$

$$\Rightarrow 54000 = Z \times 90/100$$

$$\Rightarrow Z = 54000 \times 100/90$$

$$\Rightarrow Z = 600 \times 100$$

$$\Rightarrow Z = 60000$$

Question: 4

An alloy contains

Solution:

Given,

Percentage of copper = 30%

Percentage of nickel = 42%

\therefore Percentage of zinc = {100 - (30 + 42)} %

$$= 28 \%$$

Now,

Mass of zinc in 1 kg of the alloy = (28 \times 1/100) kg

$$= 0.28 \text{ kg}$$

$$= 0.28 \times 1000 \text{ g}$$

$$= 280 \text{ g}$$

Question: 5

In a class, 60% o

Solution:

Let the total number of students = Z

Percentage of girls = (100 - 60) % = 40%

Now,

Number of girls = 40% of Z

$$\Rightarrow 14 = Z \times 40/100$$

$$\Rightarrow Z = 14 \times 100/40$$

$$\Rightarrow Z = 14 \times 5/2$$

$$\Rightarrow Z = 35$$

Question: 6

Solution:

$$\begin{aligned}\text{Percentage} &= (54/45 \times 100) \% \\ &= (54/9 \times 20) \% \\ &= (6 \times 20) \% \\ &= 120\%\end{aligned}$$

Question: 11

A number exceeds

Solution:

$$\begin{aligned}\text{Let the number} &= Z \\ \therefore 25\% \text{ of } Z + 60 &= Z \\ \Rightarrow (Z \times 25/100) + 60 &= Z \\ \Rightarrow Z/4 + 60 &= Z \\ \Rightarrow Z - Z/4 &= 60 \\ \Rightarrow 3Z/4 &= 60 \\ \Rightarrow Z &= 60 \times 4/3 \\ \Rightarrow Z &= 80\end{aligned}$$

Question: 12

5% of which numbe

Solution:

$$\begin{aligned}\text{Let the number} &= Z \\ \therefore 5\% \text{ of } Z &= 12 \\ \Rightarrow Z \times 5/100 &= 12 \\ \Rightarrow Z &= 12 \times 100/5 \\ \Rightarrow Z &= 12 \times 20 \\ \Rightarrow Z &= 240\end{aligned}$$

Question: 13

Fill in the blank

Solution:

(i) 90

$$\begin{aligned}7\frac{1}{2}\% \text{ of Rs.1200} &= (15/2) \% \text{ of Rs.1200} \\ &= 15/2 \times 1/100 \times 1200 \\ &= 15/2 \times 12 \\ &= 90\end{aligned}$$

\therefore Rs.90

(ii) 8

$$240 \text{ mL} = (240/1000) \text{ L}$$

Now,

$$\text{Percentage} = (240/1000 \times 1/3 \times 100) \%$$

$$= (240/10 \times 1/3) \%$$

$$= (80/10) \%$$

$$= 8\%$$

(iii) 120

$$X\% \text{ of } 35 = 42$$

$$\Rightarrow 35 \times X/100 = 42$$

$$\Rightarrow 35X/100 = 42$$

$$\Rightarrow X = 42 \times 100/35$$

$$\Rightarrow X = 6 \times 100/5$$

$$\Rightarrow X = 120$$

(iv) 240

$$12/5 = (12/5 \times 100) \%$$

$$= (12 \times 20) \%$$

$$= 240\%$$

(v) 150

Let the number = Z

$$\therefore 120 = Z\% \text{ of } 80$$

$$\Rightarrow 120 = 80 \times Z/100$$

$$\Rightarrow Z = 120 \times 100/80$$

$$\Rightarrow Z = 120 \times 5/4$$

$$\Rightarrow Z = 150$$

Question: 14

Write 'T' & '#'

Solution:

(i) False

$$6\% \text{ of } 8 = 8 \times 6/100$$

$$= 48/100$$

$$= 0.48$$

(ii) False

$$6:5 = 6/5$$

$$= (6/5 \times 100) \%$$

$$= (6 \times 20) \%$$

$$= 120\%$$

(iii) True

$$3/5 = 3/5$$

$$= (3/5 \times 100) \%$$

$$= (3 \times 20) \%$$

$$= 60\%$$

(iv) True

1 day = 24 hours

6 hours = $(6/24 \times 100) \%$

= $(1/4 \times 100) \%$

= 25%