

Electrostatic Potential and Capacitance

Numerical

Q.1 The electric field in an electromagnetic wave is given by $E = (50 \text{ NC}^{-1}) \sin \omega (t - x/c)$

The energy contained in a cylinder of volume V is 5.5×10^{-12} J. The value of V is

 $_ \text{cm}^3$. (given $\in \in_0 = 8.8 \times 10^{-12} \text{C}^2 \text{N}^{-1} \text{m}^{-2}$)

31st Aug Morning Shift 2021

Q.2 Consider an electrical circuit containing a two way switch 'S'. Initially S is open and then T_1 is connected to T_2 . As the current in $R = 6\Omega$ attains a maximum value of steady state level, T_1 is disconnected from T_2 and immediately connected to T_3 . Potential drop across $r = 3\Omega$ resistor immediately after T_1 is connected to T_3 is

_____V. (Round off to the Nearest Integer)



27th July Morning Shift 2021

Q.3 A particle of mass 1 mg and charge q is lying at the mid-point of two stationary

particles kept at a distance '2 m' when each is carrying same charge 'q'. If the free charged particle is displaced from its equilibrium position through distance 'x' (x < 1 m). The particle executes SHM. Its angular frequency of oscillation will be ______ × 10⁵ rad/s if q² = 10 C².

25th July Morning Shift 2021

Q.4 A body having specific charge 8 μ C/g is resting on a frictionless plane at a distance 10 cm from the wall (as shown in the figure). It starts moving towards the wall when a uniform electric field of 100 V/m is applied horizontally towards the wall. If the collision of the body with the wall is perfectly elastic, then the time period of the motion will be ______ s.



20th July Morning Shift 2021

Q.5 An infinite number of point charges, each carrying 1 μ C charge, are placed along the y-axis at y = 1 m, 2 m, 4 m, 8 m

The total force on a 1C point charge, placed at the origin, is $x \times 10^3$ N.

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The value of x, to the nearest integer, is _____. [Take rac{1}{4\piarepsilon_0}=9	imes10^9 Nm²/C²]
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18th Mar Evening Shift 2021

Q.6 27 similar drops of mercury are maintained at 10V each. All these spherical drops combine into a single big drop. The potential energy of the bigger drop is ______ times that of a smaller drop.

26th Feb Evening Shift 2021

Q.7 Two small spheres each of mass 10 mg are suspended from a point by threads 0.5 m long. They are equally charged and repel each other to a distance of 0.20 m.

The charge on each of the sphere is $\frac{a}{21}$ × 10⁻⁸C. The value of 'a' will be _____. [Given g = 10 ms⁻²]

25th Feb Evening Shift 2021

Q.8 In the given circuit of potentiometer, the potential difference E across AB (10 m length) is larger than E_1 and E_2 as well. For key K_1 (closed), the jockey is adjusted to touch the wire at point J_1 so that there is no deflection in the galvanometer. Now the first battery (E_1) is replaced by second battery (E_2) for working by making K_1 open and K_2 closed. The galvanometer gives then null deflection at J_2 . The value of



Numerical Answer Key

- 1. Ans. (500)
- 2. Ans. (3)
- 3. Ans. (6)
- 4. Ans. (1)
- 5. Ans. (12)
- 6. Ans. (243)
- 7. Ans. (20)
- 8. Ans. (1)

Numerical Explanation

Ans 1.

 $E = 50 \sin\left(\omega t - \frac{\omega}{c}. x\right)$

Energy density = $\frac{1}{2} \in_0 E_0^2$

Energy of volume $V=rac{1}{2}{\in}_0 E_0^2.~V=5.5 imes10^{-12}$

$$\frac{1}{2}8.8 \times 10^{-12} \times 2500V = 5.5 \times 10^{-12}$$

$$V = \frac{5.5 \times 2}{2500 \times 8.8} = .0005m^3$$

$$= .0005 \times 10^{6} (c.m)^{3}$$

 $= 500 (c.m)^3$

Ans 2. What T_1 and T_2 are connected, then the steady state current in the

$$I=rac{6}{6}=1A$$
 inductor

When T_1 and T_3 are connected then current through inductor remains same. So potential difference across 3Ω

 $V = Ir = 1 \times 3 = 3$ Volt

Ans 3.



Net force on free charged particle

$$egin{aligned} F &= rac{kq^2}{\left(d+x
ight)^2} - rac{kq^2}{\left(d-x
ight)^2} \ F &= -kq^2 \left[rac{4dx}{\left(d^2-x^2
ight)^2}
ight] \ a &= -rac{4kq^2d}{m} \left(rac{x}{d^4}
ight) \ a &= -\left(rac{4kq^2}{md^3}
ight) x \end{aligned}$$

So, angular frequency

$$\omega = \sqrt{rac{4kq^2}{md^3}}$$

$$\omega = \sqrt{\frac{4 \times 9 \times 10^9 \times 10}{1 \times 10^{-6} \times 1^3}}$$

 $\omega = 6 \times 10^8 \text{ rad/sec}$

Ans 4. Given,

 $q = 8\mu C/g = 8 \times 10^{-6} C/g = 8 \times 10^{-3} C/kg$

 $s = 10 \text{ cm} = 0.1 \text{ m} \Rightarrow \text{E} = 100 \text{ V/m}$

We know that, acceleration, $a = \frac{force(F)}{mass(m)}$

$$\Rightarrow a = \frac{qE}{m} [:: F = qE]$$

$$= \frac{8 \times 10^{-6} \times 100}{10^{-3}} = 0.8 \text{ ms}^{-2}$$

As per question, when electric field is switched on, the body strikes to the wall and then returns back.

For one oscillation,

$$s = ut + \frac{1}{2} at^{2}$$

$$\Rightarrow 0.1 = \frac{1}{2} \times 0.8 t^{2} [\because u = 0]$$

$$\Rightarrow 0.2 = 0.8 t^{2}$$

$$\Rightarrow \frac{2}{8} = t^{2} \Rightarrow t^{2} = \frac{1}{4} \Rightarrow t = \frac{1}{2}$$

 \therefore Time period = 2 $\times \frac{1}{2}$ = 1 s

Therefore, if the collision of the body is perfectly elastic, the time period of motion will be 1s.

Ans 5.

$$\begin{split} F_{total} &= \frac{kq_1q_2}{r_1^2} + \frac{kq_1q_3}{r_2^2} + \frac{kq_1q_4}{r_3^2} + \dots \\ &= 9 \times 10^9 \times 10^{-6} \left[1 + \left(\frac{1}{2}\right)^2 + \left(\frac{1}{2^2}\right)^2 + \left(\frac{1}{2^3}\right)^2 + \left(\frac{1}{2^{\infty}}\right)^2 \right] \\ &= 9 \times 10^9 \times 10^{-6} \left[\frac{1}{1 - \frac{1}{4}} \right] \\ &\because \left[S_{\infty} &= \frac{a}{1 - r} \right] \text{ for G.P.} \\ &= 9 \times 10^3 \times \frac{4}{3} = 12 \times 10^3 \text{ N} \end{split}$$

Ans 6.

$$(27)\left(rac{4}{3}\pi r^3
ight)=rac{4}{3}\pi R^3$$

R = 3r

Potential energy of smaller drop :

$$U_1=rac{3}{5}rac{kq^2}{r}$$

Potential energy of bigger drop

$$egin{aligned} U &= rac{3}{5} rac{kQ^2}{R} \ U &= rac{3}{5} rac{k(27q)^2}{R} \ U &= rac{3}{5} k rac{(27)(27)q^2}{3r} \end{aligned}$$

$$U=rac{(27)(27)}{3}\left(rac{3}{5}rac{kq^2}{r}
ight)$$

 $U=243\,U_1$





For battery E_1 , balancing length is l_1

 $l_1 = 380 \text{ cm} [\text{from end } A]$

For battery E_2 , balancing length is l_2

 l_2 = 760 cm [from end A] Now, we know that $rac{E_1}{E_2}=rac{l_1}{l_2}$

$$\Rightarrow \frac{E_1}{E_2} = \frac{380}{760} = \frac{1}{2} = \frac{a}{b}$$

∴a = 1 & b = 2

∴a = 1

MCQ (Single Correct Answer)

Q.1 Two particles A and B having charges $20\mu\mu$ C and $--5\mu\mu$ C respectively are held fixed with a separation of 5 cm. At what position a third charged particle should be placed so that it does not experience a net electric force?

 $20 \ \mu C \qquad -5 \ \mu C$ A 5 cm from 20 \ \mu C on the left side of system A At 5 cm from 20 \ \mu C on the right side B At 5 cm from -5 \ \mu C on the right side C At 1.25 cm from -5 \ \mu C between two charges

D At midpoint between two charges

31st Aug Morning Shift 2021

Q.2 For full scale deflection of total 50 divisions, 50 mV voltage is required in galvanometer. The resistance of galvanometer if its current sensitivity is 2 div/mA will be :



27th Aug Evening Shift 2021

Q.3 The Colour coding on a carbon resistor is shown in the given figure. The resistance value of the given resistor is:



27th Aug Evening Shift 2021

Q.4 If you are provided a set of resistances 2Ω , 4Ω , 6Ω and 8Ω . Connect these resistances so as to obtain an equivalent resistance of $\frac{46}{3}\Omega$

A 4Ω and 6Ω are in parallel with 2Ω and 8Ω in series

B 6 Ω and 8 Ω are in parallel with 2 Ω and 4 Ω in series

 \bigcirc 2 Ω and 6 Ω are in parallel with 4 Ω and 8 Ω in series

D 2 Ω and 4 Ω are in parallel with 6 Ω and 8 Ω in series

26th Aug Evening Shift 2021

Q.5 A solid metal sphere of radius R having charge q is enclosed inside the concentric spherical shell of inner radius a and outer radius b as shown in the figure.

The approximate variation electric field \vec{E} as a function of distance r from centre 0 is given by





26th Aug Morning Shift 2021

Q.6 The resistance of a conductor at 15° C is 16Ω and at 100° C is 20Ω . What will be the temperature coefficient of resistance of the conductor?



D 0.042°C^{−1}

27th July Evening Shift 2021

Q.7 What will be the magnitude of electric field at point O as shown in the figure? Each side of the figure is l and perpendicular to each other?



27th July Evening Shift 2021

Q.8 Two identical tennis balls each having mass 'm' and charge 'q' are suspended from a fixed point by threads of length 'l'. What is the equilibrium separation when each thread makes a small angle ' θ ' with the vertical?

A
$$x = \left(rac{q^2 l}{2\pi arepsilon_0 mg}
ight)^{rac{1}{2}}$$

B $x = \left(rac{q^2 l}{2\pi arepsilon_0 mg}
ight)^{rac{1}{3}}$

$$\begin{array}{c} \bullet \quad x = \left(\frac{q^2l^2}{2\pi\varepsilon_0m^2g}\right)^{\frac{1}{3}} \\ \hline \\ \bullet \quad x = \left(\frac{q^2l^2}{2\pi\varepsilon_0m^2g^2}\right)^{\frac{1}{3}} \end{array} \end{array}$$

27th July Morning Shift 2021

Q.9 In the given potentiometer circuit arrangement, the balancing length AC is measured to be 250 cm. When the galvanometer connection is shifted from point (1) to point (2) in the given diagram, the balancing length becomes 400 cm. The ratio of

the emf of two cells $\frac{\epsilon_1}{\epsilon_2}$ is :



25th July Evening Shift 2021

Q.10 An electric dipole is placed on x-axis in proximity to a line charge of linear charge density 3.0×10^{-6} C/m. Line charge is placed on z-axis and positive and negative charge of dipole is at a distance of 10 mm and 12 mm from the origin respectively. If total force of 4N is exerted on the dipole, find out the amount of positive or negative charge of the dipole.



22th July Evening Shift 2021

Q.11 A Copper (Cu) rod of length 25 cm and cross-sectional area 3 mm² is joined with a similar Aluminium (Al) rod as shown in figure. Find the resistance of the combination between the ends A and B.

(Take Resistivity of Copper = $1.7 \times 10^{-8} \Omega m$ and Resistivity of Aluminium = $2.6 \times 10^{--8} \Omega m$)



22th July Evening Shift 2021

Q.12 A certain charge Q is divided into two parts q and (Q - q). How should the charges Q and q be divided so that q and (Q - q) placed at a certain distance apart experience maximum electrostatic repulsion?

A Q = 2q **B** Q = 4q **C** Q = 3q **D** Q = $\frac{q}{2}$

20th July Morning Shift 2021

Q.13 A current of 5 A is passing through a non-linear magnesium wire of crosssection 0.04 m². At every point the direction of current density is at an angle of 60° with the unit vector of area of cross-section. The magnitude of electric field at every point of the conductor is:

(Resistivity of magnesium $\rho = 44 \times 10^{-8} \Omega m$)



20th July Morning Shift 2021

Q.14 An oil drop of radius 2 mm with a density 3g cm⁻³ is held stationary under a constant electric field 3.55×10^5 V m⁻¹ in the Millikan's oil drop experiment. What is the number of excess electrons that the oil drop will possess? (consider g = 9.81 m/s²)



18th Mar Morning Shift 2021

Q.15 A current of 10A exists in a wire of cross-sectional area of 5 mm² with a drift velocity of 2×10^{-3} ms⁻¹. The number of free electrons in each cubic meter of the wire is ______.



17th Mar Morning Shift 2021

Q.16 Find out the surface charge density at the intersection of point x = 3 m plane and x-axis, in the region of uniform line charge of 8 nC/m lying along the z-axis in free space.



16th Mar Evening Shift 2021

Q.17 A conducting wire of length 'l', area of cross-section A and electric resistivity $\rho\rho$ is connected between the terminals of a battery. A potential difference V is developed between its ends, causing an electric current.

If the length of the wire of the same material is doubled and the area of cross-section is halved, the resultant current would be:



16th Mar Morning Shift 2021

Q.18 Two electrons each are fixed at a distance '2d'. A third charge proton placed at the midpoint is displaced slightly by a distance x (x << d) perpendicular to the line joining the two fixed charges. Proton will execute simple harmonic motion having angular frequency: (m = mass of charged particle)



24th Feb Evening Shift 2021

Q.19 A cube of side 'a' has point charges +Q located at each of its vertices except at the origin where the charge is -Q. The electric field at the centre of cube is :





24th Feb Morning Shift 2021

MCQ Answer Key

1. Ans. (b)	10. Ans. (d)	19. Ans. (d)
2. Ans. (d)	11. Ans. (c)	
3. Ans. (d)	12. Ans. (a)	
4. Ans. (d)	13. Ans. (a)	
5. Ans. (a)	14. Ans. (b)	
6. Ans. (c)	15. Ans. (a)	
7. Ans. (b)	16. Ans. (a)	
8. Ans. (b)	17. Ans. (c)	
9. Ans. (a)	18. Ans. (b)	

Ans 1. Null point is possible only right side of –5 μC

$$\frac{20\mu C}{x} - 5\mu C}{x}$$

$$E_N = +\frac{k(-5\mu C)}{x^2} + \frac{k(20\mu C)}{(5+x)^2} = 0$$

x = 5 cm

Ans 2.

$$I_{\mathrm{max}} = rac{50}{2} = 25 \,\mathrm{mA}$$

$$R = \frac{V}{I} = \frac{50mV}{25mA} = 2\Omega$$

Ans 3.

$$R = 75 \times 10^2 \pm 5\%$$
 of 7500

R = (7500
$$\pm$$
 375) Ω

Ans 4.



Ans 5. Considering outer spherical shell is non-conducting.

Electric field inside a metal sphere is zero.

 $r < R \Rightarrow E = 0$



Option (b)



r < R, E = 0

 $R \le r < a$

 $E = \frac{kQ}{r^2}$

a≤ r < b,

E = 0

 $r\geq b,$

 $\mathsf{E} = \frac{kQ}{r^2}$



Ans 6.

 $16 = R_0 [1 + \alpha (15 - T_0)]$ $20 = R_0 [1 + \alpha (100 - T_0)]$

Assuming $T_0 = 0$ °C, as a general convention.

$$\Rightarrow \frac{16}{20} = \frac{1 + \alpha \times 15}{1 + \alpha \times 100}$$
$$\Rightarrow \alpha = 0.003^{\circ} \mathrm{C}^{-1}$$

Ans 7.



Ans 8.



 $T\cos\theta = mg$

 $T\sin\theta = rac{kq^2}{x^2}$ $an heta = rac{kq^2}{x^2mq}$

$$an heta pprox \sin heta pprox rac{x}{2L}$$
 $rac{x}{2L} = rac{Kq^2}{x^2mg}$ $x = \left(rac{q^2L}{2\piarepsilon_0mg}
ight)^{1/3}$

 $E_{1} = kl_{1} \dots (i)$ $E_{1} + E_{2} = kl_{2} \dots (ii)$ $\frac{E_{1}}{E_{1} + E_{2}} = \frac{l_{1}}{l_{2}} = \frac{250}{400} = \frac{5}{8}$ $8E_{1} = 5E_{1} + 5E_{2}$ $3E_{1} = 5E_{2}$ $\frac{E_{1}}{E_{2}} = \frac{5}{3}$





Ans 11.

$$R_{Cu} = \frac{\rho_{Cu} \times l}{A}$$

$$R_{Al} = \frac{\rho_{Al} \times l}{A}$$

$$R_{Eq} = \frac{\rho_{Cu} \times \rho_{Al}}{\rho_{Cu} + \rho_{Al}} \times \left(\frac{l}{A}\right)$$

$$= \frac{1.7 \times 10^{-8} \times 2.6 \times 10^{-8}}{(1.7 + 2.6) \times 10^{-8}} \times \frac{0.25}{3 \times 10^{-6}}$$

$$= 0.856 \text{ m}\Omega$$

Ans 12. Let's say the charge q and (Q - q) are at r distance from each other. This can be shown as



According to Coulomb's law, force between both the parts can be given as

$$F = rac{kq(Q-q)}{r^2}$$

$$F = \frac{k}{r^2}(qQ - q^2)$$

As we know that $\frac{dF}{dq} = 0$, for maximum force.

$$\Rightarrow rac{dF}{dq} = rac{d}{dq} \left[rac{k}{r^2} (qQ - q^2)
ight] = 0$$

$$\Rightarrow \frac{k}{r^2}(Q-2q) = 0 \Rightarrow Q = 2q$$

Ans 13. Given, current, I = 5A

Area of cross-section of wire, $A = 0.04 \text{ m}^2$

We know that, $J = \frac{I}{A}$

or
$$I = J$$
. A or $I = JA\cos\theta$

where, J = current density.

$$\Rightarrow 5 = J\left(\frac{4}{100}\right) \times \cos(60^\circ)$$
 [:: Given, $\theta = 60^\circ$]

$$J = 500 \times \frac{1}{2} [\because \cos 60^\circ = \frac{1}{2}]$$

 \Rightarrow J = 250 Am⁻²

The relation between electric field, current density and resistivity can be given as,

E =
$$\rho$$
 . J
= 44 × 10⁻⁸ × 250 [:: Resistivity, ρ = 44 × 10⁻⁸ Ω-m]
= 11 × 10⁻⁵ V/m





 $F_e = qE = (ne)E$

F_e = mg

(ne)E = mg

$$n = \frac{mg}{eE} = \frac{\rho \frac{4}{3}\pi R^3 \times g}{eE}$$

$$n = \frac{3000 \times \frac{4}{3} \times 3.14 \times 8 \times 10^{-9} \times 9.8}{1.6 \times 10^{-19} \times 3.55 \times 10^5}$$
$$n = \frac{984704 \times 10^5}{5.68} = 1.73 \times 10^{10}$$

$$n=1.73 imes10^{10}$$

Ans 15.

 $I = neAV_d$

$$n = rac{I}{eAV_d}$$

$$=\frac{10}{1.6\times10^{-9}\times5\times10^{-6}\times2\times10^{-3}}$$

$$=rac{10^{25}}{16}=6.25 imes10^{27}=625 imes10^{25}$$

Ans 16.

Electric field due to wire is given by $E = rac{2k\lambda}{r}$

Electric field with surface charge density $E=\frac{\sigma}{\in_0}$

$$\frac{2k\lambda}{r} = \frac{\sigma}{\epsilon_0}$$

$$\Rightarrow 2rac{1}{4\pi \in_0}rac{\lambda}{r} = rac{\sigma}{\in_0}$$

$$\Rightarrow \frac{8}{2 \times 3.14 \times 3} = \sigma$$

 $\Rightarrow \sigma = 0.424 ~ \mathrm{n} ~ \mathrm{Cm}^{-2}$

Ans 17. We know that

$$R = \rho \frac{l}{A}$$

- Now, new length : l' = 2lnew area of cross section : A' = A/2 \therefore New resistance : $R' = \rho \cdot \frac{2l}{A/2}$
- : New resistance : $R' = \rho \cdot \frac{2l}{A/2}$
- $\Rightarrow R' = 4 \frac{\rho l}{A}$
- $\Rightarrow R' = 4R$
- \therefore Resultant current : $I = \frac{V}{4R}$
- $\Rightarrow I = \frac{1}{4} \frac{VA}{\rho l}$

Ans 18. The arrangement of charges is shown below



As we know that,

Coulomb's force between two charges. i.e., q_1 and q_2 ,

$$F = rac{1}{4\pi arepsilon_0} rac{q_1 q_2}{r^2} = rac{1}{4\pi arepsilon_0} rac{q_1 q_2}{(d^2 + x^2)}$$
 (i)

Here, $q_1 = q_2 = q$

Force in SHM, $F = m\omega^2 x$ (ii)

Since, in order to have SHM +q should move downwards and force responsible for this will be only

$$F' = F\sin\theta + F\sin\theta = 2F\sin\theta$$
 (iii)

Using Eqs. (ii) and (iii), we get

 $\begin{aligned} 2F\sin\theta &= m\omega^2 x\\ \Rightarrow \frac{2}{4\pi\varepsilon_0} \frac{q^2}{(d^2 + x^2)} \sin\theta &= m\omega^2 x\\ \Rightarrow \frac{2}{4\pi\varepsilon_0} \frac{q^2}{(d^2 + x^2)} \cdot \frac{x}{(d^2 + x^2)^{1/2}} &= m\omega^2 x\\ \Rightarrow \omega &= \left(\frac{1}{2\pi\varepsilon_0} \frac{q^2}{(d^2 + x^2)^{3/2}m}\right)^{1/2}\\ \text{As, } x << d \end{aligned}$

$$\therefore \omega = \left(\frac{1}{2\pi \varepsilon_0} \frac{q^2}{m d^3} \right)^{1/2}$$

Ans 19. We can replace – Q charge at origin by + Q and – 2Q. Now, due to + Q charge at every corner of cube, electric field at centre of cube is zero. So, net electric field at centre is only due to – 2Q charge at origin. Vector form of electric field strength,

$$E = \frac{Kqr}{r^3}$$

Here, position vector, $r=rac{a}{2}(\widehat{x}+\hat{y}+\hat{z})$

$$\Rightarrow |r| = \sqrt{\left(\frac{a}{2}\right)^2 + \left(\frac{a}{2}\right)^2 + \left(\frac{a}{2}\right)^2} = \frac{\sqrt{3}a}{2}$$
$$\Rightarrow E = \frac{1}{4\pi\varepsilon_0} \times \frac{(-2Q)a/2}{\left(\frac{a}{2}\sqrt{3}\right)^3} \cdot (\hat{x} + \hat{y} + \hat{z})$$
$$E = \frac{-2Q(\hat{x} + \hat{y} + \hat{z})}{3\sqrt{3}\pi a^2\varepsilon_0}$$

Electrostatic Potential and Equipotential Surfaces

4.

6.

7.

1. Ten charges are placed on the circumference of a circle of radius R with constant angular separation between successive charges. Alternate charges 1, 3, 5, 7, 9 have charge (+q) each, while 2, 4, 6, 8, 10 have charge (-q)each. The potential V and the electric field E at the centre of the circle are respectively : [Sep. 05, 2020 (II)]

(Take V = 0 at infinity)

- (a) $V = \frac{10q}{4\pi\epsilon_0 R}; E = 0$ (b) $V = 0; E = \frac{10q}{4\pi\varepsilon_0 R^2}$ (c) V = 0; E = 0
- (d) $V = \frac{10q}{4\pi\varepsilon_0 R}; E = \frac{10q}{4\pi\varepsilon_0 R^2}$
- Two isolated conducting spheres S_1 and S_2 of radius $\frac{2}{3}R$ 2.

and $\frac{1}{3}R$ have 12 µC and -3 µC charges, respectively, and are at a large distance from each other. They are now connected by a conducting wire. A long time after this is done the charges on S_1 and S_2 are respectively :

- [Sep. 03, 2020 (I)] (b) $+4.5 \ \mu C$ and $-4.5 \ \mu C$ (a) $4.5 \ \mu C$ on both (c) $3 \mu C$ and $6 \mu C$ (d) $6 \mu C$ and $3 \mu C$
- 3. Concentric metallic hollow spheres of radii R and 4R hold charges Q_1 and Q_2 respectively. Given that surface charge densities of the concentric spheres are equal, the potential difference V(R) - V(4R) is : [Sep. 03, 2020 (II)]

(a)
$$\frac{3Q_1}{16\pi\epsilon_0 R}$$
 (b) $\frac{3Q_2}{4\pi\epsilon_0 R}$

(c)
$$\frac{Q_2}{4\pi\varepsilon_0 R}$$
 (d) $\frac{3Q_1}{4\pi\varepsilon_0 R}$

A charge Q is distributed over two concentric conducting thin spherical shells radii r and R (R > r). If the surface charge densities on the two shells are equal, the electric potential at the common centre is : [Sep. 02, 2020 (II)]

(a)
$$\frac{1}{4\pi\varepsilon_0} \frac{(R+r)}{2(R^2+r^2)} Q$$
 (b) $\frac{1}{4\pi\varepsilon_0} \frac{(2R+r)}{(R^2+r^2)} Q$
(c) $\frac{1}{4\pi\varepsilon_0} \frac{(R+2r)Q}{2(R^2+r^2)}$ (d) $\frac{1}{4\pi\varepsilon_0} \frac{(R+r)}{(R^2+r^2)} Q$

5. A point dipole = $\vec{p} - p_o \hat{x}$ kept at the origin. The potential and electric field due to this dipole on the y-axis at a distance d are, respectively: (Take V = 0 at infinity)

[12 April 2019 I]

(a)
$$\frac{\left|\vec{p}\right|}{4\pi\varepsilon_{0}d^{2}}, \frac{\vec{p}}{4\pi\varepsilon_{0}d^{3}}$$
 (b) $0, \frac{-\vec{p}}{4\pi\varepsilon_{0}d^{3}}$
(c) $0, \frac{\left|\vec{p}\right|}{4\pi\varepsilon_{0}d^{3}}$ (d) $\frac{\left|\vec{p}\right|}{4\pi\varepsilon_{0}d^{2}}, \frac{-p}{4\pi\varepsilon_{0}d^{3}}$

A uniformly charged ring of radius 3a and total charge q is placed in xy-plane centred at origin. A point charge q is moving towards the ring along the z-axis and has speed v at z = 4a. The minimum value of v such that it crosses the origin is : [10 April 2019 I]

(a)
$$\sqrt{\frac{2}{m}} \left(\frac{4}{15} \frac{q^2}{4\pi\epsilon_0 a}\right)^{1/2}$$
 (b) $\sqrt{\frac{2}{m}} \left(\frac{1}{5} \frac{q^2}{4\pi\epsilon_0 a}\right)^{1/2}$
(c) $\sqrt{\frac{2}{m}} \left(\frac{2}{15} \frac{q^2}{4\pi\epsilon_0 a}\right)^{1/2}$ (d) $\sqrt{\frac{2}{m}} \left(\frac{1}{15} \frac{q^2}{4\pi\epsilon_0 a}\right)^{1/2}$

A solid conducting sphere, having a charge Q, is surrounded by an uncharged conducting hollow spherical shell. Let the potential difference between the surface of the solid sphere and that of the outer surface of the hollow shell be V. If the shell is now given a charge of -4 Q, the new potential difference between the same two surfaces is : [8 April 2019 I]

(a)
$$-2V$$
 (b) $2V$ (c) $4V$ (d) V

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- The electric field in a region is given by $\vec{E} = (Ax + B)\hat{i}$, 8. where E is in NC⁻¹ and x is in metres. The values of constants are A = 20 SI unit and B = 10 SI unit. If the potential at x = 1 is V₁ and that at x = -5 is V₂, then $V_1 - V_2$ is: [8 Jan. 2019 II] (a) 320V (b) -48V (c) 180V(d) -520 V
- 9. The given graph shows variation (with distance r from centre) [11 Jan. 2019 I] of ·



- (a) Electric field of a uniformly charged sphere
- (b) Potential of a uniformly charged spherical shell
- (c) Potential of a uniformly charged sphere
- (d) Electric field of a uniformly charged spherical shell
- **10.** A charge Q is distributed over three concentric spherical shells of radii a, b, c (a < b < c) such that their surface charge densities are equal to one another. The total potential at a point at distance r from their common centre, where r < a, would be:

[10 Jan. 2019 I]

(a)
$$\frac{Q}{12\pi\epsilon_0} \frac{ab+bc+ca}{abc}$$
 (b) $\frac{Q(a^2+b^2+c^2)}{4\pi\epsilon_0(a^3+b^3+c^3)}$
(c) $\frac{Q}{4\pi\epsilon_0(a+b+c)}$ (d) $\frac{Q(a+b+c)}{4\pi\epsilon_0(a^2+b^2+c^2)}$

11. Two electric dipoles, A, B with respective dipole moments $\vec{d}_{A} = -4 \operatorname{qa} \hat{i}$ and $\vec{d}_{B} = -2 \operatorname{qa} \hat{i}$ are placed on the x-axis with a separation R, as shown in the figure

$$\xrightarrow{R \leftarrow A} R \leftarrow B \rightarrow X$$

The distance from A at which both of them produce the [10 Jan. 2019 I] same potential is:

(a)
$$\frac{R}{\sqrt{2} + 1}$$
 (b) $\frac{\sqrt{2} R}{\sqrt{2} + 1}$
(c) $\frac{R}{\sqrt{2} - 1}$ (d) $\frac{\sqrt{2} R}{\sqrt{2} - 1}$

12. Consider two charged metallic spheres S_1 and S_2 of radii R_1 and R_2 , respectively. The electric fields E_1 (on S_1) and E_2 (on S_2) on their surfaces are such that $E_1/E_2 = R_1/R_2$. Then the ratio $V_1(\text{on } S_1)/V_2(\text{on } S_2)$ of the electrostatic [8 Jan. 2019 II] potentials on each sphere is: (b) $(R_1/R_2)^2$ (a) R_1/R_2

(c)
$$(R_2/R_1)$$
 (d) $\left(\frac{R}{R}\right)$

13. Three concentric metal shells A, B and C of respective radii a, b and c (a < b < c) have surface charge densities $+\sigma$, $-\sigma$ and $+\sigma$ respectively. The potential of shell B is: [2018]

(a)
$$\frac{\sigma}{\epsilon_0} \left[\frac{a^2 - b^2}{a} + c \right]$$
 (b) $\frac{\sigma}{\epsilon_0} \left[\frac{a^2 - b^2}{b} + c \right]$
(c) $\frac{\sigma}{\epsilon_0} \left[\frac{b^2 - c^2}{b} + a \right]$ (d) $\frac{\sigma}{\epsilon_0} \left[\frac{b^2 - c^2}{c} + a \right]$

- There is a uniform electrostatic field in a region. The 14. potential at various points on a small sphere centred at P, in the region, is found to vary between in the limits 589.0 V to 589.8 V. What is the potential at a point on the sphere whose radius vector makes an angle of 60° with the direction of the field ? [Online April 8, 2017] (a) 589.5 V (b) 589.2 V (c) 589.4 V (d) 589.6 V
- **15.** Within a spherical charge distribution of charge density $\rho(\mathbf{r})$, N equipotential surfaces of potential V₀, V₀ + Δ V, V₀ + $2\Delta V$, V_0 + $N\Delta V$ ($\Delta V > 0$), are drawn and have increasing radii r₀, r₁, r₂,..... r_N, respectively. If the difference in the radii of the surfaces is constant for all values of V_0 and ΔV then : [Online April 10, 2016]

(a)
$$\rho(r) = \text{constant}$$
 (b) $\rho(r) \propto \frac{1}{r^2}$

(c)
$$\rho(r) \propto \frac{l}{r}$$
 (d) $\rho(r) \propto r$

16. The potential (in volts) of a charge distribution is given by $V(z) = 30 - 5z^2$ for $|z| \le 1m$

$$V(z) = 35 - 10 |z|$$
 for $|z| \ge 1 m$.

V(z) does not depend on x and y. If this potential is generated by a constant charge per unit volume ρ_0 (in units of ε_0) which is spread over a certain region, then choose the correct statement. [Online April 9, 2016]

- (a) $\rho_0 = 20 \epsilon_0$ in the entire region
- (b) $\rho_0 = 10 \varepsilon_0$ for $|z| \le 1$ m and $p_0 = 0$ elsewhere
- (c) $\rho_0 = 20 \epsilon_0$ for $|z| \le 1$ m and $p_0 = 0$ elsewhere
- (d) $\rho_0 = 40 \varepsilon_0$ in the entire region A uniformly charged solid sphere of radius R has potential V_0 (measured with respect to ∞) on its surface. For this sphere the equipotential surfaces with potentials 17. $3V_0 5V_0 3V_0 V_0$

$$respectively.$$
 Then
(a) $R_1 = 0$ and $R_2 < (R_4 - R_3)$
(b) $2R = R_4$
(2015)

(c) $\mathbf{R} = 0$ and $\mathbf{R} > (\mathbf{R} - \mathbf{R})$

(d)
$$R_1 \neq 0$$
 and $R_2 > (R_4 - R_3)$
(d) $R_1 \neq 0$ and $(R_2 - R_1) > (R_4 - R_3)$

18. An electric field $\vec{E} = (25\hat{i} + 30\hat{j})NC^{-1}$ exists in a region of space. If the potential at the origin is taken to be zero

then the potential at x = 2 m, y = 2 m is :

[Online April 11, 2015]

(a) -110 J (b) -140 J (c) -120 J (d) -130 J19. Assume that an electric field $\vec{E} = 30x^2\hat{i}$ exists in space. Then the potential difference $V_A - V_O$, where V_O is the potential at the origin and V_A the potential at x = 2 m is: (b) -120 J/C (a) 120 J/C [2014] (c) -80 J/C(d) 80 J/C

- **20.** Consider a finite insulated, uncharged conductor placed near a finite positively charged conductor. The uncharged body must have a potential : [Online April 23, 2013] (a) less than the charged conductor and more than at infinity.
 - (b) more than the charged conductor and less than at infinity.
 - (c) more than the charged conductor and more than at infinity.
 - (d) less than the charged conductor and less than at infinity.
- **21.** Two small equal point charges of magnitude q are suspended from a common point on the ceiling by insulating mass less strings of equal lengths. They come to equilibrium with each string making angle θ from the vertical. If the mass of each charge is m, then the electrostatic potential at the centre of line joining them will

be
$$\left(\frac{1}{4\pi \in_0} = k\right)$$
. [Online April 22, 2013]
(a) $2\sqrt{k mg \tan \theta}$ (b) $\sqrt{k mg \tan \theta}$

a)
$$2\sqrt{k}mg\tan\theta$$
 (b) $\sqrt{k}mg\tan\theta$

- (c) $4\sqrt{k mg}/\tan\theta$ (d) $\sqrt{k mg / \tan \theta}$
- 22. A point charge of magnitude + 1 μ C is fixed at (0, 0, 0). An isolated uncharged spherical conductor, is fixed with its center at (4, 0, 0). The potential and the induced electric field at the centre of the sphere is : [Online April 22, 2013]
 - (a) 1.8×10^5 V and -5.625×10^6 V/m
 - (b) 0 V and 0 V/m
 - (c) 2.25×10^5 V and -5.625×10^6 V/m
 - (d) 2.25×10^5 V and 0 V/m
- 23. A charge of total amount Q is distributed over two concentric hollow spheres of radii r and R(R > r) such that the surface charge densities on the two spheres are equal. The electric potential at the common centre is

[Online May 19, 2012]

(a)
$$\frac{1}{4\pi\varepsilon_0} \frac{(R-r)Q}{(R^2+r^2)}$$
 (b)
$$\frac{1}{4\pi\varepsilon_0} \frac{(R+r)Q}{2(R^2+r^2)}$$

(c)
$$\frac{1}{4\pi\varepsilon_0} \frac{(R+r)Q}{(R^2+r^2)}$$
 (d)
$$\frac{1}{4\pi\varepsilon_0} \frac{(R-r)Q}{2(R^2+r^2)}$$

24. The electric potential V(x) in a region around the origin is given by $V(x) = 4x^2$ volts. The electric charge enclosed in a cube of 1 m side with its centre at the origin is (in coulomb) [Online May 7, 2012]

(c) 0 (d)
$$-8\varepsilon_0$$

(a) $8\varepsilon_0$ (b) $-4\epsilon_0$ (c) 0 25. The electrostatic potential inside a charged spherical ball is given by $\phi = ar^2 + b$ where r is the distance from the centre and a, b are constants. Then the charge density inside the ball is: [2011]

(a)
$$-6a\epsilon_0 r$$
 (b) $-24\pi a\epsilon_0$

(c)
$$-6a\varepsilon_0$$
 (d) $-24\pi a\varepsilon_0 r$

- **26.** An electric charge $10^{-3} \mu$ C is placed at the origin (0, 0) of X - Y co-ordinate system. Two points A and B are situated at $(\sqrt{2}, \sqrt{2})$ and (2, 0) respectively. The potential difference between the points A and B will be [2007] (a) 4.5 volts (b) 9 volts (c) Zero (d) 2 volt
- Charges are placed on the vertices of a square as shown. 27.
 - Let \vec{E} be the electric field and V the potential at the centre. If the charges on A and B are interchanged with those on D and C respectively, then [2007]



- (a) \vec{E} changes, V remains unchanged
- (b) \vec{E} remains unchanged, V changes
- (c) both \vec{E} and V change
- (d) \vec{E} and V remain unchanged
- The potential at a point x (measured in μ m) due to some 28. charges situated on the x-axis is given by $V(x) = 20/(x^2 - 4)$ volt. The electric field E at $x = 4 \mu$ m is given by [2007]
 - (a) (10/9) volt/ μ m and in the +ve x direction
 - (b) (5/3) volt/ μ m and in the –ve x direction
 - (c) (5/3) volt/ μ m and in the +ve x direction
 - (d) (10/9) volt/ μ m and in the –ve x direction
- **29.** Two thin wire rings each having a radius *R* are placed at a distance d apart with their axes coinciding. The charges on the two rings are +q and -q. The potential difference between the centres of the two rings is [2005]

(a)
$$\frac{q}{2\pi \epsilon_0} \left[\frac{1}{R} - \frac{1}{\sqrt{R^2 + d^2}} \right]$$
 (b)
$$\frac{qR}{4\pi \epsilon_0 d^2}$$

(c)
$$\frac{q}{4\pi \epsilon_0} \left[\frac{1}{R} - \frac{1}{\sqrt{R^2 + d^2}} \right]$$
 (d) zero

30. A thin spherical conducting shell of radius *R* has a charge q. Another charge Q is placed at the centre of the shell.

The electrostatic potential at a point P , a distance $\frac{R}{2}$ from the centre of the shell is [2003]

(a)
$$\frac{2Q}{4\pi\varepsilon_o R}$$
 (b) $\frac{2Q}{4\pi\varepsilon_o R} - \frac{2q}{4\pi\varepsilon_o R}$

(c)
$$\frac{2Q}{4\pi\varepsilon_o R} + \frac{q}{4\pi\varepsilon_o R}$$
 (d) $\frac{(q+Q)2}{4\pi\varepsilon_o R}$

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31. A solid sphere of radius *R* carries a charge Q + q distributed uniformaly over its volume. A very small point like piece of it of mass *m* gets detached from the bottom of the sphere and falls down vertically under gravity. This piece carries charge *q*. If it acquires a speed *v* when it has fallen through a vertical height *y* (see figure), then : (assume the remaining portion to be spherical).

[Sep. 05, 2020 (I)]



32. A two point charges 4q and -q are fixed on the x-axis at $x = -\frac{d}{2}$ and $x = \frac{d}{2}$, respectively. If a third point charge

'q' is taken from the origin to x = d along the semicircle as shown in the figure, the energy of the charge will :

[Sep. 04, 2020 (I)]



33. Hydrogen ion and singly ionized helium atom are accelerated, from rest, through the same potential difference. The ratio of final speeds of hydrogen and helium ions is close to : [Sep. 03, 2020 (II)]
(a) 1:2
(b) 10:7

34. In free space, a particle A of charge 1 μ C is held fixed at a point P. Another particle B of the same charge and mass 4 μ g is kept at a distance of 1 mm from P. If B is released, then its velocity at a distance of 9 mm from P is :

$$\begin{bmatrix} Take \frac{1}{4\pi\epsilon_0} = 9 \times 10^9 Nm^2 C^{-2} \end{bmatrix}$$
 [10 April 2019 II]
(a) 1.0m/s (b) 3.0×10^4 m/s
(c) 2.0×10^3 m/s (d) 1.5×10^2 m/s

35. A system of three charges are placed as shown in the figure:



If D >> d, the potential energy of the system is best given by [9 April 2019 I]

(a)
$$\frac{1}{4\pi \epsilon_0} \left[\frac{-q^2}{d} \frac{-qQd}{2D^2} \right]$$
 (b) $\frac{1}{4\pi \epsilon_0} \left[\frac{-q^2}{d} + \frac{2qQd}{D^2} \right]$
(c) $\frac{1}{4\pi \epsilon_0} \left[+ \frac{q^2}{d} + \frac{qQd}{D^2} \right]$ (d) $\frac{1}{4\pi \epsilon_0} \left[-\frac{q^2}{d} - \frac{qQd}{D^2} \right]$

36. A positive point charge is released from rest at a distance r_0 from a positive line charge with uniform density. The speed (v) of the point charge, as a function of instantaneous distance r from line charge, is proportional to : [8 April 2019 II]

(a)
$$v \propto e^{+r/r_0}$$
 (b) $v \propto \sqrt{ln\left(\frac{r}{r_0}\right)}$
(c) $v \propto ln\left(\frac{r}{r_0}\right)$ (d) $v \propto \left(\frac{r}{r_0}\right)$

37. There is a uniform spherically symmetric surface charge density at a distance R_o from the origin. The charge distribution is initially at rest and starts expanding because of mutual repulsion. The figure that represents best the speed V (R(t)) of the distribution as a function of its instantaneous radius R(t) is: [12 Jan. 2019 I]

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38. Three charges Q, +q and +q are placed at the vertices of a right-angle isosceles triangle as shown below. The net electrostatic energy of the configuration is zero, if the value of Q is : [11 Jan. 2019 I]



39. Four equal point charges Q each are placed in the xy plane at (0, 2), (4, 2), (4, -2) and (0, -2). The work required to put a fifth charge Q at the origin of the coordinate system will be: [10 Jan. 2019 II]

(a)
$$\frac{Q^2}{4\pi\varepsilon_0} \left(1 + \frac{1}{\sqrt{3}} \right)$$
 (b)
$$\frac{Q^2}{4\pi\varepsilon_0} \left(1 + \frac{1}{\sqrt{5}} \right)$$

(c)
$$\frac{Q^2}{2\sqrt{2}\pi\varepsilon_0}$$
 (d)
$$\frac{Q^2}{4\pi\varepsilon_0}$$

40. Statement 1 : No work is required to be done to move a test charge between any two points on an equipotential surface.

Statement 2 : Electric lines of force at the equipotential surfaces are mutually perpendicular to each other.

[Online April 25, 2013]

- (a) Statement 1 is true, Statement 2 is true, Statement 2 is the correct explanation of Statement 1.
- (b) Statement 1 is true, Statement 2 is true, Statement 2 is not the correct explanation of Statement 1.
- (c) Statement 1 is true, Statement 2 is false.
- (d) Statement 1 is false, Statement 2 is true.

41. An insulating solid sphere of radius *R* has a uniformly positive charge density ρ. As a result of this uniform charge distribution there is a finite value of electric potential at the centre of the sphere, at the surface of the sphere and also at a point outside the sphere. The electric potential at infinite is zero. [2012]
Statement -1 When a charge *q* is taken from the centre to the surface of the sphere its potential energy changes

by
$$\frac{qp}{3\epsilon_0}$$

Statement -2 The electric field at a distance r(r < R) from

the centre of the sphere is $\frac{\rho r}{3\varepsilon_0}$.

- (a) Statement 1 is true, Statement 2 is true; Statement 2 is not the correct explanation of statement 1.
- (b) Statement 1 is true Statement 2 is false.
- (c) Statement 1 is false Statement 2 is true.

(d) Statement 1 is true, Statement 2 is true, Statement 2 is the correct explanation of Statement 1

42. Two positive charges of magnitude 'q' are placed, at the ends of a side (side 1) of a square of side '2a'. Two negative charges of the same magnitude are kept at the other corners. Starting from rest, if a charge Q moves from the middle of side 1 to the centre of square, its kinetic energy at the centre of square is [2011 RS]

(a) zero (b)
$$\frac{1}{4\pi\varepsilon_0} \frac{2qQ}{a} \left(1 + \frac{1}{\sqrt{5}}\right)$$

(c)
$$\frac{1}{4\pi\varepsilon_0} \frac{2qQ}{a} \left(1 - \frac{2}{\sqrt{5}}\right)$$
 (d) $\frac{1}{4\pi\varepsilon_0} \frac{2qQ}{a} \left(1 - \frac{1}{\sqrt{5}}\right)$

- 43. Two points P and Q are maintained at the potentials of 10 V and -4 V, respectively. The work done in moving 100 electrons from P to Q is: [2009] (a) 9.60×10^{-17} J (b) -2.24×10^{-16} J (c) 2.24×10^{-16} J (d) -9.60×10^{-17} J
- 44. Two insulating plates are both uniformly charged in such a way that the potential difference between them is $V_2 V_1 = 20$ V. (i.e., plate 2 is at a higher potential). The plates are separated by d = 0.1 m and can be treated as infinitely large. An electron is released from rest on the inner surface of plate 1. What is its speed when it hits plate 2? ($e = 1.6 \times 10^{-19}$ C, $m_e = 9.11 \times 10^{-31}$ kg) [2006]



Electrostatic Potential and Capacitance

- **45.** A charged particle 'q' is shot towards another charged particle 'Q' which is fixed, with a speed 'v'. It approaches 'Q' upto a closest distance r and then returns. If q were given a speed of '2v' the closest distances of approach would be [2004] (a) r/2 (b) 2r (c) r (d) r/4
- 46. On moving a charge of 20 coulomb by 2 cm, 2 J of work is done, then the potential difference between the points is [2002]
 (a) 0.1 V
 (b) 8 V
 (c) 2 V
 (d) 0.5 V

(a) 0.1 V (b) 8 V (c) 2 V (d) 0.5 V Capacitors, Grouping of

TOPIC 3 Capacitors and Energy Stored in a Capacitor
47. Two capacitors of capacitances C and 2C are charged to

47. Two capacitors of capacitances C and 2C are charged to potential differences V and 2V, respectively. These are then connected in parallel in such a manner that the positive terminal of one is connected to the negative terminal of the other. The final energy of this configuration is :

[Sep. 05, 2020 (I)]

(a)
$$\frac{25}{6}$$
CV² (b) $\frac{3}{2}$ CV²
(c) zero (d) $\frac{9}{2}$ CV²

48. In the circuit shown, charge on the 5 μ F capacitor is :



49. A capacitor *C* is fully charged with voltage V_0 . After disconnecting the voltage source, it is connected in parallel with another uncharged capacitor of capacitance $\frac{C}{2}$. The energy loss in the process after the charge is distributed

between the two capacitors is : [Sep. 04, 2020 (II)]

- (a) $\frac{1}{2}CV_0^2$ (b) $\frac{1}{3}CV_0^2$ (c) $\frac{1}{4}CV_0^2$ (d) $\frac{1}{6}CV_0^2$
- **50.** In the circuit shown in the figure, the total charge is $750 \,\mu\text{C}$ and the voltage across capacitor C_2 is 20 V. Then the charge on capacitor C_2 is : [Sep. 03, 2020 (I)]



(a) $450 \,\mu C$ (b) $590 \,\mu C$

(c) $160 \,\mu\text{C}$ (d) $650 \,\mu\text{C}$

51. A 5 μ F capacitor is charged fully by a 220 V supply. It is then disconnected from the supply and is connected in series to another uncharged 2.5 μ F capacitor. If the energy

change during the charge redistribution is $\frac{X}{100}$ J then value

of X to the nearest integer is _

[NA Sep. 02, 2020 (I)]

- 52. A 10 μ F capacitor is fully charged to a potential difference of 50 V. After removing the source voltage it is connected to an uncharged capacitor in parallel. Now the potential difference across them becomes 20 V. The capacitance of the second capacitor is : [Sep. 02, 2020 (II)] (a) 15 μ F (b) 30 μ F
 - (c) $20 \,\mu\text{F}$ (d) $10 \,\mu\text{F}$
- 53. Effective capacitance of parallel combination of two capacitors C_1 and C_2 is 10 µF. When these capacitors are individually connected to a voltage source of 1 V, the energy stored in the capacitor C_2 is 4 times that of C_1 . If these capacitors are connected in series, their effective capacitance will be: [8 Jan. 2020 I]
- (a) 4.2 μF (b) 3.2 μF (c) 1.6 μF (d) 8.4 μF
 54. A capacitor is made of two square plates each of side 'a' making a very small angle a between them, as shown in figure. The capacitance will be close to: [8 Jan. 2020 II]



55. A parallel plate capacitor has plates of area A separated by distance '*d*' between them. It is filled with a dielectric which has a dielectric constant that varies as $k(x) = K(1 + \alpha x)$ where 'x' is the distance measured from one of the plates. If $(\alpha d) << 1$, the total capacitance of the system is best given by the expression: [7 Jan. 2020 I]

(a)
$$\frac{AK \in_{0}}{d} \left(1 + \frac{\alpha d}{2}\right)$$

(b)
$$\frac{A \in_{0} K}{d} \left(1 + \left(\frac{\alpha d}{2}\right)^{2}\right)$$

(c)
$$\frac{A \in_{0} K}{d} \left(1 + \frac{\alpha^{2} d}{2}\right)$$

(d)
$$\frac{AK \in_{0}}{d} (1 + \alpha d)$$

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- 56. A 60 pF capacitor is fully charged by a 20 V supply. It is then disconnected from the supply and is connected to another uncharged 60 pF capacitor in parallel. The electrostatic energy that is lost in this process by the time the charge is redistributed between them is (in nJ) [NA 7 Jan. 2020 II]
- 57. The parallel combination of two air filled parallel plate capacitors of capacitance C and nC is connected to a battery of voltage, V. When the capacitors are fully charged, the battery is removed and after that a dielectric material of dielectric constant K is placed between the two plates of the first capacitor. The new potential difference of the combined system is: [9 April 2020 II]

(a)
$$\frac{nV}{K+n}$$
 (b) V
(c) $\frac{V}{K+n}$ (d) $\frac{(n+1)V}{(K+n)}$

58. Two identical parallel plate capacitors, of capacitance C each, have plates of area A, separated by a distance d. The space between the plates of the two capacitors, is filled with three dielectrics, of equal thickness and dielectric constants K1, K2 and K3. The first capacitors is filled as shown in Fig. I, and the second one is filled as shown in Fig. II.

If these two modified capacitors are charged by the same potential V, the ratio of the energy stored in the two, would be (E_1 refers to capacitors (I) and E_2 to capacitors (II) :



59. In the given circuit, the charge on $4 \,\mu\text{F}$ capacitor will be : [12 April 2019 II]



- Physics
- 60. Figure shows charge (q) versus voltage (V) graph for series and parallel combination of two given capacitors. The capacitances are : [10 April 2019 I]



(a) $40 \mu\text{F}$ and $10 \mu\text{F}$	(b) $60 \mu\text{F}$ and $40 \mu\text{F}$
(c) $50 \mu\text{F}$ and $30 \mu\text{F}$	(d) $20 \ \mu F$ and $30 \ \mu F$

61. A capacitor with capacitance 5μ F is charged to 5μ C. If the plates are pulled apart to reduce the capacitance to 2 ¹/₄F, how much work is done? [9 April 2019 I]

(a)
$$6.25 \times 10^{-6} \text{ J}$$
 (b) $3.75 \times 10^{-6} \text{ J}$

(c)
$$2.16 \times 10^{-6}$$
 J (d) 2.55×10^{-6} J

- Voltage rating of a parallel plate capacitor is 500 V. Its 62. dielectric can withstand a maximum electric field of 10^6 V/ m. The plate area is 10^{-4} m². What is the dielectric constant if the capacitance is 15 pF? [8 April 2019 I] (given " $_0 = 8.86 \times 10^{-12} \text{ C}^2/\text{Nm}^2$) (a) 3.8 (b) 8.5 (c) 4.5 (d) 6.2
- 63. A parallel plate capacitor has 1µF capacitance. One of its two plates is given $+ 2\mu C$ charge and the other plate, $+4\mu$ C charge. The potential difference developed across the capacitor is : [8 April 2019 II]
- (a) 3V (b) 1V (c) 5V (d) 2V 64. In the figure shown, after the switch 'S' is turned from position 'A' to position 'B', the energy dissipated in the circuit in terms of capacitance 'C' and total charge 'Q' is:

[12 Jan. 2019 I]



65. A parallel plate capacitor with plates of area 1 m^2 each, are at a separation of 0.1 m. If the electric field between the plates is 100 N/C, the magnitude of charge on each plate is :

 $(\text{Take} \in_0 = 8.85 \times 10^{-12} \frac{\text{C}^2}{\text{N} - \text{M}^2})$ [12 Jan. 2019 II] (a) 7.85×10^{-10} C (b) 6.85×10^{-10} C (c) 8.85×10^{-10} C (d) 9.85×10^{-10} C

Electrostatic Potential and Capacitance

66. In the circuit shown, find C if the effective capacitance of the whole circuit is to be 0.5 μF. All values in the circuit are in μF. [12 Jan. 2019 II]



67. In the figure shown below, the charge on the left plate of the $10 \ \mu\text{F}$ capacitor is $-30 \ \mu\text{C}$. The charge on the right plate of the $6 \ \mu\text{F}$ capacitor is : [11 Jan. 2019 I]



68. Seven capacitors, each of capacitance 2 μ F, are to be connected in a configuration to obtain an effective capacitance of $\left(\frac{6}{13}\right)$ μ F. Which of the combinations, shown in figures below, will achieve the desired value?

[11 Jan. 2019 II]



- A parallel plate capacitor having capacitance 12 pF is charged by a battery to a potential difference of 10 V between its plates. The charging battery is now disconnected and a porcelain slab of dielectric constant 6.5 is slipped between the plates. The work done by the
- capacitor on the slab is: [10 Jan. 2019 II] (a) 692 pJ (b) 508 pJ
- (c) 560 pJ (d) 600 pJ

69.

70. A parallel plate capacitor is of area 6 cm² and a separation 3 mm. The gap is filled with three dielectric materials of equal thickness (see figure) with dielectric constants $K_1 = 10$, $K_2 = 12$ and $K_3 = 1(4)$ The dielectric constant of a material which when fully inserted in above capacitor, gives same capacitance would be:





(a) 4 (b) 14 (c) 12 (d) 36
71. A parallel plate capacitor is made of two square plates of side 'a', separated by a distance d (d<<a). The lower triangular portion is filled with a dielectric of dielectric constant K, as shown in the figure. Capacitance of this capacitor is: [9 Jan. 2019 I]



72. A parallel plate capacitor with square plates is filled with four dielectrics of dielectric constants K₁, K₂, K₃, K₄ arranged as shown in the figure. The effective dielectric constant K will be: [9 Jan. 2019 II]

(a)
$$K = \frac{\begin{pmatrix} K_1 + K_2 \end{pmatrix} \begin{pmatrix} K_2 \\ K_3 \end{pmatrix} \begin{pmatrix} K_4 \\ L/2 \end{pmatrix}}{\begin{pmatrix} K_4 \\ L/2 \end{pmatrix}}$$

(a)
$$K = \frac{\begin{pmatrix} K_1 + K_3 \end{pmatrix} \begin{pmatrix} K_2 + K_4 \end{pmatrix}}{K_1 + K_2 + K_3 + K_4}$$

(b)
$$K = \frac{\begin{pmatrix} K_1 + K_2 \end{pmatrix} \begin{pmatrix} K_3 + K_4 \end{pmatrix}}{2(K_1 + K_2 + K_3 + K_4)}$$

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(c)
$$K = \frac{(K_1 + K_2) (K_3 + K_4)}{K_1 + K_2 + K_3 + K_4}$$

(d) $K = \frac{(K_1 + K_4) (K_2 + K_3)}{2(K_1 - K_2) (K_2 - K_3)}$

constant $k = \frac{5}{3}$ is inserted between the plates, the magnitude of the induced charge will be: [2018] (a) 1.2 n C (b) 0.3 n C (c) 2.4 n C (d) 0.9 n C

т7

74. In the following circuit, the switch S is closed at t = 0. The charge on the capacitor C_1 as a function of time will be

given by
$$\left(C_{eq} = \frac{C_1C_2}{C_1 + C_2}\right)$$
. [Online April 16, 2018]
(a) $C_{eq}E[1 - exp(-t/RC_{eq})]$
(b) $C_1E[1 - exp(-tR/C_1)]$
(c) $C_2E[1 - exp(-t/RC_2)]$
(d) $C_{eq}E exp(-t/RC_{eq})$

75. The equivalent capacitance between A and B in the circuit given below is:



[Online April 15, 2018]

(a)
$$4.9\,\mu\text{F}$$
 (b) $3.6\,\mu\text{F}$ (c) $5.4\,\mu\text{F}$ (d) $2.4\,\mu\text{F}$

76. A parallel plate capacitor with area 200 cm^2 and separation between the plates 1.5cm, is connected across a battery of emfV. If the force of attraction between the plates is 25×10^{-10} ⁶N, the value of V is approximately: [Online April 15, 2018]

$$\left(\varepsilon_0 = 8.85 \times 10^{-12} \, \frac{\mathrm{C}^2}{\mathrm{N.m}^2}\right)$$

(a) 150V (b) 100V (c) 250V (d) 300V

77. A capacitor C_1 is charged up to a voltage V = 60V by connecting it to battery B through switch (1), Now C_1 is disconnected from battery and connected to a circuit consisting of two uncharged capacitors $C_2 = 3.0 \mu F$ and $C_3 =$ 6.0μ F through a switch (2) as shown in the figure. The sum of final charges on C₂ and C₃ is: [Online April 15, 2018]



- **78.** A capacitance of $2\mu F$ is required in an electrical circuit across a potential difference of 1.0 kV. A large number of 1μ F capacitors are available which can withstand a potential difference of not more than 300 V. The minimum number of capacitors required to achieve this is [2017] (a) 24 (b) 32 (c) 2 (d) 16
- A combination of parallel plate capacitors is maintained at 79 a certain potential difference.



When a 3 mm thick slab is introduced between all the plates, in order to maintain the same potential difference, the distance between the plates is increased by 2.4 mm. Find the dielectric constant of the slab.

[Online April 9, 2017]

(c) 5 (d) 6 (a) 3 (b) 4 80. The energy stored in the electric field produced by a metal sphere is 4.5 J. If the sphere contains 4 μ C charge, its

radius will be : [Take : $\frac{1}{4\pi\epsilon_0} = 9 \times 10^9 \text{ N} - \text{m}^2 / \text{C}^2$]

[Online April 8, 2017]

- (a) 20mm (b) 32mm (c) 28mm (d) 16mm
- 81. A combination of capacitors is set up as shown in the figure. The magnitude of the electric field, due to a point charge Q (having a charge equal to the sum of the charges on the 4 μ F and 9 μ F capacitors), at a point distance 30 m from it, would equal: [2016]





82. Figure shows a network of capacitors where the numbers indicates capacitances in micro Farad. The value of capacitance C if the equivalent capacitance between point A and B is to be 1 µF is : [Online April 10, 2016]



(a)
$$\frac{32}{23}\mu F$$
 (b) $\frac{31}{23}\mu F$ (c) $\frac{33}{23}\mu F$ (d) $\frac{34}{23}\mu F$

- 83. Three capacitors each of 4 μF are to be connected in such a way that the effective capacitance is 6μF. This can be done by connecting them : [Online April 9, 2016]
 (a) all in series
 - (b) all in parallel
 - (c) two in parallel and one in series
 - (d) two in series and one in parallel
- 84. In the given circuit, charge Q_2 on the 2μ F capacitor changes as C is varied from 1μ F to 3μ F. Q_2 as a function of 'C' is given properly by: (*figures are drawn schematically and are not to scale*) [2015]



85. In figure a system of four capacitors connected across a 10 V battery is shown. Charge that will flow from switch S when it is closed is : [Online April 11, 2015]



(a)	5 μ C from b to a	(b) 20 μ C from a to b
(c)	zero	(d) 5 μ C from a to b

86. A parallel plate capacitor is made of two circular plates separated by a distance 5 mm and with a dielectric of dialectric constant 2.2 between them. When the electric field in the dielectric is 3×10^4 V/m the charge density of the positive plate will be close to: [2014]

(a)
$$6 \times 10^{-7} \text{ C/m}^2$$
 (b) $3 \times 10^{-7} \text{ C/m}^2$
(c) $3 \times 10^4 \text{ C/m}^2$ (d) $6 \times 10^4 \text{ C/m}^2$

87. The gap between the plates of a parallel plate capacitor of area A and distance between plates d, is filled with a dielectric whose permittivity varies linearly from ∈₁ at one

plate to \in_2 at the other. The capacitance of capacitor is:

[Online April 19, 2014]

(a)
$$\in_0 (\in_1 + \in_2) A / d$$

(b) $\in_0 (\in_2 + \in_1) A / 2d$

- (b) $\epsilon_0 (\epsilon_2 + \epsilon_1) A / 2d$ (c) $\epsilon_0 A / [d ln(\epsilon_2 / \epsilon_1)]$
- (d) $\epsilon_0 (\epsilon_2 \epsilon_1) \mathbf{A} / [d \ln(\epsilon_2 / \epsilon_1)]$
- **88.** The space between the plates of a parallel plate capacitor is filled with a 'dielectric' whose 'dielectric constant' varies with distance as per the relation:

 $K(x) = K_0 + \lambda x (\lambda = a \text{ constant})$

The capacitance C, of the capacitor, would be related to its vacuum capacitance C_0 for the relation :

[Online April 12, 2014]

(a)
$$C = \frac{\lambda d}{ln(1 + K_o\lambda d)}C_o$$
 (b) $C = \frac{\lambda}{d.ln(1 + K_o\lambda d)}C_o$

(c)
$$C = \frac{\lambda d}{ln(1 + \lambda d / K_o)} C_o$$
 (d) $C = \frac{\lambda}{d ln(1 + K_o / \lambda d)} C_o$

89. A parallel plate capacitor is made of two plates of length l, width w and separated by distance d. A dielectric slab (dielectric constant K) that fits exactly between the plates is held near the edge of the plates. It is pulled into the

capacitor by a force $F = -\frac{\partial U}{\partial x}$ where U is the energy of

the capacitor when dielectric is inside the capacitor up to distance x (See figure). If the charge on the capacitor is Q then the force on the dielectric when it is near the edge is: [Online April 11, 2014]



90. Three capacitors, each of 3μ F, are provided. These cannot be combined to provide the resultant capacitance of:

[Online April 9, 2014]

(a) 1 μF
(b) 2 μF
(c) 4.5 μF
(d) 6 μF
91. A parallel plate capacitor having a separation between the plates d, plate area A and material with dielectric constant K has capacitance C₀. Now one-third of the material is replaced by another material with dielectric constant 2K, so that effectively there are two capacitors one with area

 $\frac{1}{3}$ A, dielectric constant 2K and another with area $\frac{2}{3}$ A and dielectric constant K. If the capacitance of this new capacitor is C then $\frac{C}{C_0}$ is **[Online April 25, 2013]** (a) 1 (b) $\frac{4}{3}$ (c) $\frac{2}{3}$ (d) $\frac{1}{3}$

- 92. To establish an instantaneous current of 2 A through a 1 μ F capacitor ; the potential difference across the capacitor plates should be changed at the rate of :
 - $\begin{array}{ccc} [Online April 22, 2013] \\ (a) & 2 \times 10^4 \, \text{V/s} \\ (b) & 4 \times 10^6 \, \text{V/s} \\ (c) & 2 \times 10^6 \, \text{V/s} \\ (d) & 4 \times 10^4 \, \text{V/s} \end{array}$
- 93. A uniform electric field \vec{E} exists between the plates of a charged condenser. A charged particle enters the space

between the plates and perpendicular to \vec{E} . The path of the particle between the plates is a :

(a) straight line

(c) parabola

(a) 1.001

- ne (b) hyperbola (d) circle
- 94. The figure shows an experimental plot discharging of a capacitor in an RC circuit. The time constant τ of this circuit lies between : [2012]







95. The capacitor of an oscillatory circuit is enclosed in a container. When the container is evacuated, the resonance frequency of the circuit is 10 kHz. When the container is filled with a gas, the resonance frequency changes by 50 Hz. The dielectric constant of the gas is

[Online April 9, 2013]

(b) 2.001 (c) 1.01 (d) 3.01

- **96.** Statement 1: It is not possible to make a sphere of capacity 1 farad using a conducting material.
 - **Statement 2:** It is possible for earth as its radius is 6.4×10^6 m. [Online May 26, 2012]
 - (a) Statement 1 is true, Statement 2 is true, Statement 2 is the correct explanation of Statement 1.
 - (b) Statement 1 is false, Statement 2 is true.
 - (c) Statement 1 is true, Statement 2 is true, Statement 2 is not the correct explanation of Statement 1.
 - (d) Statement 1 is true, Statement 2 is false.

97. A series combination of n_1 capacitors, each of capacity C_1 is charged by source of potential difference 4 V. When another parallel combination of n_2 capacitors each of capacity C_2 is charged by a source of potential difference V, it has the same total energy stored in it as the first combination has. The value of C_2 in terms of C_1 is then

[Online May 12, 2012]

(a)
$$16\frac{n_2}{n_1}C_1$$
 (b) $\frac{2C_1}{n_1n_2}$
(c) $2\frac{n_2}{n_1}C_1$ (d) $\frac{16C_1}{n_1n_2}$

98. Two circuits (a) and (b) have charged capacitors of capacitance C, 2C and 3C with open switches. Charges on each of the capacitor are as shown in the figures. On closing the switches [Online May 7, 2012]



(a) No charge flows in (a) but charge flows from R to L in (b)

(b) Charges flow from *L* to *R* in both (a) and (b)

(c) Charges flow from R to L in (a) and from L to R in (b)

(d) No charge flows in (a) but charge flows from L to R in (b)

99. Let C be the capacitance of a capacitor discharging through a resistor R. Suppose t_1 is the time taken for the energy stored in the capacitor to reduce to half its initial value and t_2 is the time taken for the charge to reduce to one-fourth its initial value. Then the ratio t_1/t_2 will be [2010]

(a) 1 (b)
$$\frac{1}{2}$$
 (c) $\frac{1}{4}$ (d) 2

100. A parallel plate capacitor with air between the plates has capacitance of 9 pF. The separation between its plates is 'd'. The space between the plates is now filled with two dielectrics. One of the dielectrics has dielectric constant

 $k_1 = 3$ and thickness $\frac{d}{3}$ while the other one has dielectric

constant $k_2 = 6$ and thickness $\frac{2d}{3}$. Capacitance of the capacitor is now [2008]

(a)
$$1.8\,pF$$
 (b) $45\,pF$ (c) $40.5\,pF$ (d) $20.25\,pF$

101. A parallel plate condenser with a dielectric of dielectric constant K between the plates has a capacity C and is charged to a potential V volt. The dielectric slab is slowly removed from between the plates and then reinserted. The net work done by the system in this process is **[2007]**

(a) zero (b) $\frac{1}{2}(K-1) CV^2$ (c) $CV^2(K-1)$ (d) $(K-1) CV^2$

(c)
$$\frac{CV^2(K-1)}{K}$$
 (d) $(K-1) CV$

102. A parallel plate capacitor is made by stacking *n* equally spaced plates connected alternatively. If the capacitance between any two adjacent plates is 'C' then the resultant capacitance is (2005)

(a) $(n+1)C$	(b) $(n-1)C$
--------------	--------------

- (c) nC (d) C
- **103.** A fully charged capacitor has a capacitance 'C'. It is discharged through a small coil of resistance wire embedded in a thermally insulated block of specific heat capacity 's' and mass 'm'. If the temperature of the block is raised by ' ΔT ', the potential difference 'V' across the capacitance is [2005]

(a)
$$\frac{mC\Delta T}{s}$$
 (b) $\sqrt{\frac{2mC\Delta T}{s}}$

(c)
$$\sqrt{\frac{2ms\Delta T}{C}}$$
 (d) $\frac{ms\Delta T}{C}$

- 104. A sheet of aluminium foil of negligible thickness is introduced between the plates of a capacitor. The capacitance of the capacitor [2003]
 - (a) decreases (b) remains unchanged
 - (c) becomes infinite (d) increases
- **105.** The work done in placing a charge of 8×10^{-18} coulomb on a condenser of capacity 100 micro-farad is [2003]
 - (a) 16×10^{-32} joule (b) 3.1×10^{-26} joule
 - (c) 4×10^{-10} joule (d) 32×10^{-32} joule
- **106.** If there are *n* capacitors in parallel connected to *V* volt source, then the energy stored is equal to [2002]

(a)
$$CV$$
 (b) $\frac{1}{2}nCV^2$ (c) CV^2 (d) $\frac{1}{2n}CV^2$

- **107.** Capacitance (in F) of a spherical conductor with radius 1 m is [2002]
 - (a) 1.1×10^{-10} (b) 10^{-6}

(c)
$$9 \times 10^{-9}$$
 (d) 10^{-3}



Hints & Solutions

1. (c) Potential at the centre,
$$V_C = \frac{KQ_{\text{net}}}{R}$$

$$\therefore Q_{\text{net}} = 0$$

 $\therefore V_C = 0$

Let *E* be electric field produced by each charge at the centre, then resultant electric field will be $E_C = 0$, since equal electric field vectors are acting at equal angle so their resultant is equal to zero.



2. (d) Total charge $Q_1 + Q_2 = Q'_1 + Q'_2$ = $12\mu C - 3\mu C = 9\mu C$

Two isolated conducting sphres S_1 and S_2 are now connected by a conducting wire.

$$\therefore V_1 = V_2 = \frac{KQ'_1}{\frac{2}{3}R} = \frac{KQ'_2}{\frac{R}{3}} = 12 - 3 = 9 \,\mu\text{C}$$
$$Q'_1 = 2Q'_2 \Longrightarrow 2Q'_2 + Q'_2 = 9 \,\mu\text{C}$$
$$\therefore Q'_1 = 6 \,\mu\text{C and } Q'_2 = 3 \,\mu\text{C}$$

3. (a) We have given two metallic hollow spheres of radii R and 4R having charges Q₁ and Q₂ respectively.
Potential on the surface of inner sphere (at A)

$$V_A = \frac{kQ_1}{R} + \frac{kQ_2}{4R}$$

Potential on the surface of outer sphere (at *B*)



Potential difference,

$$\Delta V = V_A - V_B = \frac{3}{4} \cdot \frac{kQ_1}{R} = \frac{3}{16\pi \epsilon_0} \cdot \frac{Q_1}{R}$$

4. (d) Let σ be the surface charge density of the shells.



Charge on the inner shell, $Q_1 = \sigma 4\pi r^2$ Charge on the outer shell, $Q_2 = \sigma 4\pi R^2$ \therefore Total charge, $Q = \sigma 4\pi (r^2 + R^2)$

$$\Rightarrow \sigma = \frac{Q}{4\pi(r^2 + R^2)}$$

Potential at the common centre,

$$V_C = \frac{KQ_1}{r} + \frac{KQ_2}{R} \qquad \left(\text{ where } K = \frac{1}{4\pi\varepsilon_0} \right)$$
$$= \frac{K\sigma 4\pi r^2}{r} + \frac{K\sigma 4\pi R^2}{R}$$
$$= K\sigma 4\pi (r+R)$$
$$= \frac{KQ4\pi (r+R)}{4\pi (r^2+R^2)}$$
$$= \frac{1}{4\pi\varepsilon_0} \frac{(r+R)Q}{(r^2+R^2)}$$

5. (b) The electric potential at the bisector is zero and electric field is antiparallel to the dipole moment.

$$\therefore V = 0 \text{ and } \vec{E} = \frac{1}{4\pi\varepsilon_0} \left(\frac{-\vec{P}}{d^3} \right)$$

6. (c) Potential at any point of the charged ring

$$V_{p} = \frac{Kq}{\sqrt{R^{2} + Z^{2}}}$$

$$+q,$$

$$Q_{R} = \frac{\sqrt{R^{2} + Z^{2}}}{C}$$

$$R = 3a$$

$$Z = 4a$$



$$\ell = \sqrt{R^2 + Z^2} = 5a$$

The minimum velocity (v_0) should just sufficient to reach the point charge at the center, therefore

$$\frac{1}{2}mv_0^2 = q \left[V_C - V_P\right]$$
$$= q \left[\frac{Kq}{3a} - \frac{Kq}{5a}\right]$$
$$v_0^2 = \frac{4Kq^2}{15ma} = \frac{4}{15}\frac{1}{4\pi\epsilon_0}\frac{q^2}{ma}$$
$$\Rightarrow v_0 = \sqrt{\frac{2}{m}} \left(\frac{2q^2}{15 \times 4\pi\epsilon_0 a}\right)^{\frac{1}{2}}$$

7. (d) When charge Q is on inner solid conducting sphere



Electric field between spherical surface

$$\vec{E} = \frac{KQ}{r^2}$$
 So $\int \vec{E} \cdot d\vec{r} = V$ given

Now when a charge -4Q is given to hollow shell



Electric field between surface remain unchanged.

$$\vec{E} = \frac{KQ}{r^2}$$

as, field inside the hollow spherical shell = 0

... Potential difference between them remain unchanged

i.e.
$$\int \vec{E} d\vec{r} = V$$

8.

(c) Given,
$$\overrightarrow{E} = (Ax + B)\hat{i}$$

or $E = 20x + 10$
Using $V = \int Edx$, we have
 $V_2 - V_1 = \int_{-5}^{1} (20x + 10)dx = -180 \text{ V}$
or $V_1 - V_2 = 180 \text{ V}$

9. (b) Electric potential is constant inside a charged spherical shell.

10. (d)

Potential at point P, $V = \frac{kQ_a}{a} + \frac{kQ_b}{b} + \frac{kQ_c}{c}$ Since surface charge densities are equal to one another i.e., $\sigma_a = \sigma_b = \sigma_c$

$$\therefore Q_a : Q_b : Q_c :: a^2 : b^2 : c^2$$
$$\therefore Q_a = \left[\frac{a^2}{a^2 + b^2 + c^2}\right]Q$$
$$Q_b = \left[\frac{b^2}{a^2 + b^2 + c^2}\right]Q$$
$$Q_c = \left[\frac{c^2}{a^2 + b^2 + c^2}\right]Q$$
$$\therefore V = \frac{Q}{4\pi \in_0} \left[\frac{(a+b+c)}{a^2 + b^2 + c^2}\right]$$

11. (d) Let at a distance 'x' from point B, both the dipoles produce same potential

$$\Rightarrow R \leftarrow 2qa$$

$$\therefore \frac{4qa}{(R+x)} = \frac{2qa}{(x^2)}$$

$$\Rightarrow \sqrt{2x} = R + x \Rightarrow x = \frac{R}{\sqrt{2} - 1}$$

Therefore distance from A at which both of them produce the same potential

$$=\frac{R}{\sqrt{2}-1}+R=\frac{\sqrt{2}R}{\sqrt{2}-1}$$

12. (b) Electric field at a point outside the sphere is given by

$$E = \frac{1Q}{4\pi \in_0 r^2} \text{ But } \rho = \frac{Q}{\frac{4}{3}\pi R^3}$$

$$\therefore E = \frac{\rho R^3}{3 \in_0 r^2}$$

At surface $r = R$
$$\therefore E = \frac{\rho R^3}{3 \in_0}$$

Let e_i and e_i are the chores do

Let ρ_1 and ρ_2 are the charge densities of two sphere.

$$E_1 = \frac{\rho R_1}{3\varepsilon_0}$$
 and $E_2 = \frac{\rho_2 R_2}{3\varepsilon_0}$

$$\therefore \frac{E_1}{E_2} = \frac{\rho_1 R_1}{\rho_2 R_2} = \frac{R_1}{R_2}$$

This gives $\rho_1 = \rho_2 = \rho$
Potential at a point outside the sphere
$$V = \frac{1}{4\pi\varepsilon_0} \frac{Q}{r} = \frac{\rho R^3}{3\varepsilon_0 r} \left(\because \rho = \frac{Q}{\frac{4}{3}\pi R^3} \right)$$

At surface, $r = R$
$$V = \frac{\rho R^2}{3\varepsilon_0} \text{ so, } V_1 = \frac{\rho R_1^2}{3\varepsilon_0} \text{ and } V_2 = \frac{\rho R_2^2}{3\varepsilon_0}$$

$$\therefore \frac{V_1}{V_2} = \left(\frac{R_1}{R_2}\right)^2$$

13. (b) Potential outside the shell, $V_{outside} = \frac{KQ}{r}$ where r is distance of point from the centre of shell Potential inside the shell, $V_{inside} = \frac{KQ}{R}$

where 'R" is radius of the shell



- 14. (c) Potential gradient is given by, $\Delta V = E.d$ 0.8 = Ed (max) $\Delta V = Ed \cos \theta = 0.8 \times \cos 60 = 0.4$ Hence, maximum potential at a point on the sphere
- = 589.4 V **15.** (c) As we know electric field, $E = \frac{-dv}{dr}$

E = constant \therefore dv and dr same

$$E = \frac{K\phi}{r^2} = c$$

$$\Rightarrow \phi \propto r^2$$

$$\therefore \phi = \int_0^r \rho 4\pi r^2 dr$$

$$\Rightarrow \rho \propto \frac{1}{r}$$

- **16.** (b) $\Sigma_1 = \frac{-dv}{dr} = 10 |z|$ $\Sigma_2 = \frac{-dv}{dr} = 10$ (constant : E) : The source is an infinity large non conducting thick plate of thickness 2 m. $\therefore 10Z \cdot 10A = \frac{\rho \cdot A \propto Z}{\varepsilon_0}$ $r_0 = 10e_0$ for $|z| \le 1$ m. 17. (a) We know, $V_0 = \frac{Kq}{R} = V$ surface Now, $V_i = \frac{Kq}{2R^3}(3R^2 - r^2)$ [For r < R] At the centre of sphare r = 0. Here $V = \frac{3}{2}V_0$ Now, $\frac{5}{4}\frac{Kq}{R} = \frac{Kq}{2R^3}(3R^2 - r^2)$ $\Rightarrow R_2 = \frac{R}{\sqrt{2}}$ $\frac{3}{4}\frac{Kq}{R} = \frac{Kq}{R^3}$ $\frac{1}{4}\frac{Kq}{R} = \frac{Kq}{R_4}$ $R_{A} = 4R$ Also, $R_1 = 0$ and $R_2 < (R_4 - R_3)$
- 18. (a) As we know, $E = -\frac{dv}{dx}$ Potential at the point x = 2m, y = 2m is given by :

$$\int_{0}^{V} dV = -\int_{0}^{2,2} (25dx + 30dy)$$

on solving we get, V = -110 volt.

19. (c) Potential difference between any two points in an electric field is given by,

$$dV = -\vec{E} \cdot \vec{dx}$$
$$\int_{V_O}^{V_A} dV = -\int_0^2 30x^2 dx$$

 $V_A - V_O = -[10x^3]_0^2 = -80 \,\text{J/C}$

20. (a) The potential of uncharged body is less than that of the charged conductor and more than at infinity.

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In equilibrium,
$$F_e = T \sin \theta$$

mg = T cos θ

$$\tan \theta = \frac{F_e}{mg} = \frac{q^2}{4\pi \in_0 x^2 \times mg}$$

$$\therefore x = \sqrt{\frac{q^2}{4\pi \in_0 \tan \theta \, \mathrm{mg}}}$$

Electric potential at the centre of the line

$$V = \frac{kq}{x/2} + \frac{kq}{x/2} = 4\sqrt{kmg/\tan\theta}$$

22. (c) $q = 1\mu C = 1 \times 10^{-6}C$ r = 4 cm = 4 × 10⁻² m

Potential
$$V = \frac{kq}{r} = \frac{9 \times 10^9 \times 10^{-6}}{4 \times 10^{-2}} = 2.25 \times 10^5 V$$

Induced electric field $E = -\frac{kq}{r^2}$

$$=\frac{9\times10^9\times1\times10^{-6}}{16\times10^{-4}}=-5.625\times10^6\,\mathrm{V/m}$$

23. (c) Let q₁ and q₂ be charge on two spheres of radius 'r' and 'R' respectively As, q₁ + q₂ = Q

and $\sigma_1 = \sigma_2$ [Surface charge density are equal]

$$\therefore \frac{q_1}{r\pi r^2} = \frac{q_2}{4\pi R^2}$$

So, $q_1 = \frac{Qr^2}{R^2 + r^2}$ and $q_2 = \frac{QR^2}{R^2 + r^2}$
Now, potential, $V = \frac{1}{4\pi\varepsilon_0} \left[\frac{q_1}{r} + \frac{q_2}{R} \right]$
$$= \frac{1}{4\pi\varepsilon_0} \left[\frac{Qr}{R^2 + r^2} + \frac{QR}{R^2 + r^2} \right]$$
$$= \frac{Q(R+r)}{R^2 + r^2} \frac{1}{4\pi\varepsilon_0}$$

- 24. (c) Charges reside only on the outer surface of a conductor with cavity.
- 25. (c) Electric field

$$E = -\frac{d\phi}{dr} = -2ar \quad \dots(i)$$

By Gauss's theorem

The distance of point $A(\sqrt{2}, \sqrt{2})$ from the origin,

$$r_A = \sqrt{(\sqrt{2})^2 + (\sqrt{2})^2} = \sqrt{4} = 2$$
 units.

The distance of point
$$B(2, 0)$$
 from the origin

$$r_B = \sqrt{(2)^2 + (0)^2} = 2$$
 units.

Now, potential at A, due to charge $\theta = 10^{-3} \mu C$

$$V_A = \frac{1}{4\pi\epsilon_0} \cdot \frac{Q}{(r_A)}$$

Potential at B, due to charge $Q = 10^{-3} QC V_B = \frac{1}{4\pi\epsilon_0} \cdot \frac{Q}{(r_B)}$

 \therefore Potential difference between the points A and B is given by

$$V_A - V_B = \frac{1}{4\pi\epsilon_0} \cdot \frac{10^{-3}}{r_A} - \frac{1}{4\pi\epsilon_0} \cdot \frac{10^{-3}}{r_B}$$
$$= \frac{10^{-3}}{4\pi\epsilon_0} \left(\frac{1}{r_A} - \frac{1}{r_B}\right) = \frac{10^{-3}}{4\pi\epsilon_0} \left(\frac{1}{2} - \frac{1}{2}\right)$$
$$= \frac{Q}{4\pi\epsilon_0} \times 0 = 0.$$

27. (a) As shown in the figure, the resultant electric fields before and after interchanging the charges will have the same magnitude, but opposite directions. As potential is a scalar quantity, So the potential will be same in both cases.





Positive sign indicates that \vec{E} is in +ve x-direction.



Potential at the center of ring of charge +q = potential due to iteself + potential due to other ring of charge -q.

$$\Rightarrow V_1 = \frac{1}{4\pi\varepsilon_0} \left[\frac{q}{R} - \frac{q}{\sqrt{R^2 + d^2}} \right]$$

Potential at the centre of ring of charge -q = potential due to itself + potential due to other ring of charge +q.

$$\Rightarrow V_2 = \frac{1}{4\pi\varepsilon_0} \left[\frac{-q}{R} + \frac{q}{\sqrt{R^2 + d^2}} \right]$$
$$\Delta V = V_1 - V_2$$
$$= \frac{1}{4\pi\varepsilon_0} \left[\frac{q}{R} + \frac{q}{R} - \frac{q}{\sqrt{R^2 + d^2}} - \frac{q}{\sqrt{R^2 + d^2}} \right]$$
$$= \frac{1}{2\pi\varepsilon_0} \left[\frac{q}{R} - \frac{q}{\sqrt{R^2 + d^2}} \right]$$

30. (c) Electric potential due to charge Q at point P is



Electric potential due to charge q inside the shell is

$$V_2 = \frac{1}{4\pi\varepsilon_o} \frac{q}{R}$$

 \therefore The net electric potential at point *P* is

$$V = V_1 + V_2 = \frac{1}{4\pi\varepsilon_o} \frac{2Q}{R} + \frac{1}{4\pi\varepsilon_o} \frac{q}{R}$$

31. (d) By using energy conservation,

$$\Delta KE + (\Delta PE)_{\text{Electro}} + (\Delta PE)_{\text{gravitational}} = 0$$



32. (d) Change in potential energy, $\Delta u = q(V_f - V_i)$

Potential of -q is same as initial and final point of the path.



-ve sign shows the energy of the charge is decreasing.

33. (c) According to work energy theorem, gain in kinetic energy is equal to work done in displacement of charge.

$$\therefore \quad \frac{1}{2}mv^2 = q\Delta V$$

Here, $\Delta V =$ potential difference between two positions of charge q.

For same q and ΔV .

$$v \propto \frac{1}{\sqrt{m}}$$

Mass of hydrogen ion $m_{H} = 1$ Mass of helium ion $m_{He} = 4$

$$\therefore \quad \frac{v_{\rm H}}{v_{\rm He}} = \sqrt{\frac{4}{1}} = 2:1.$$

34. (c) Using conservation of energy

$$U_{i} = U_{F} + \frac{1}{2}mv^{2}$$

$$\frac{kq_{1}q_{2}}{r_{1}} = \frac{kq_{1}q_{2}}{r_{2}} + \frac{1}{2}mv^{2}$$

$$\Rightarrow \frac{1}{2}mv^{2} = kq_{1}q_{2}\left[\frac{1}{r_{1}} - \frac{1}{r_{2}}\right]$$

$$v^{2} = \frac{2kq_{1}q_{2}}{m}\left[\frac{1}{r_{1}} - \frac{1}{r_{2}}\right]$$

$$= \frac{2 \times 9 \times 10^{9} \times 10^{-12}}{4 \times 10^{-6} \times 10^{-3}}\left[1 - \frac{1}{9}\right] = 4 \times 10^{+6}$$

$$v = 2 \times 10^{3} \text{ m/s}$$

35. (d)
$$U = \frac{1}{4\pi \epsilon_0} \left[\frac{q(-q)}{d} + \frac{qQ}{\left(D + \frac{d}{2}\right)} + \frac{(-q)Q}{\left(D - \frac{d}{2}\right)} \right]$$
$$= \frac{1}{4\pi \epsilon_0} \left[-\frac{q^2}{d} - \frac{qQd}{D^2} \right], \text{ Ignoring } \frac{d^2}{4}$$

-

- 36. (b) Using, $[K+U]_i = [K+U]_f$ or $0+Vq = mv^2 + v'q$ or $mv^2 = (V-V')q$ $= -q \int_{r_0}^r Edr = q \int_{r_0}^r \frac{\lambda}{2\pi \epsilon_0} r dr = \frac{\lambda q}{2\pi \epsilon_0} \left(\frac{\ln^3}{r_0}\right)$ $\Rightarrow v \propto \sqrt{\ln \frac{r}{r_0}}$
- **37.** (c) Total energy of charge distribution is constant at any instant t.

$$U_{f} + K_{f} = U_{i} + K_{i}$$

i.e., $\frac{1}{2}mV^{2} + \frac{KQ^{2}}{2R} = 0 + \frac{KQ^{2}}{2R_{0}}$
 $\therefore \frac{1}{2}mV^{2} = \frac{KQ^{2}}{2R_{0}} - \frac{KQ^{2}}{2R}$
 $\therefore V = \sqrt{\frac{2}{m}\frac{KQ^{2}}{2}\left(\frac{1}{R_{0}} - \frac{1}{R}\right)}$
 $\therefore V = \sqrt{\frac{KQ^{2}}{m}\left(\frac{1}{R_{0}} - \frac{1}{R}\right)} = C\sqrt{\frac{1}{R_{0}} - \frac{1}{R}}$

Also the slope of V – R curve will go on decreasing.

38. (b) Net electrostatic energy for the system

Potential at origin

$$v = \frac{KQ}{2} + \frac{KQ}{2} + \frac{KQ}{\sqrt{20}} + \frac{KQ}{\sqrt{20}}$$

and potential at $\infty = 0 = KQ \left(1 + \frac{1}{\sqrt{5}}\right)$

 \therefore Work required to put a fifth charge Q at origin W =

$$VQ = \frac{Q^2}{4\pi\varepsilon_0} \left(1 + \frac{1}{\sqrt{5}} \right)$$

- 40. (c) The work done in moving a charge along an equipotential surface is always zero.The direction of electric field is perpendicular to the equipotential surface or lines.
- 41. (c) The potential energy at the centre of the sphere

$$U_c = \frac{3}{2} \frac{KQq}{R}$$

The potential energy at the surface of the sphere

$$U_{s} = \frac{K qQ}{R}$$

Now change in the energy
$$\Delta U = U_{c} - U_{s}$$

$$= \frac{K Qq}{R} \left[\frac{3}{2} - 1\right] = \frac{K Qq}{2R}$$

Where $Q = \rho . V = \rho . \frac{4}{3} \pi R^{3}$
$$\Delta U = \frac{2K}{3} \frac{\pi R^{3} \rho q}{R}$$

$$\Delta U = \frac{2}{3} \times \frac{1}{4\pi \epsilon_{0}} \frac{\pi R^{3} \rho q}{R}$$

$$\Delta U = \frac{R^{2} \rho q}{6 \epsilon_{0}}$$

Using Gauss's law

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$$\int \vec{E} \cdot \vec{dA} = \frac{q_{en}}{E_0} = \frac{\beta \times \frac{4}{3} \pi R^3}{E_0}$$
$$\Rightarrow \int E dA(\cos \theta) = \frac{\beta \times 4\pi R^3}{3E_0}$$
$$\Rightarrow E(4\pi R^2) = \beta \times \frac{4}{3} \pi R^3 \times \frac{1}{E_0}$$
$$\Rightarrow E = \frac{\beta r}{3E_0} (r < R)$$

42. (d) Initial potential of the charge,

$$V_A = \frac{2kq}{a} - \frac{2kq}{a\sqrt{5}}$$
$$\Rightarrow V_A = \frac{1}{4\pi E} \frac{2q}{a} \left(1 - \frac{1}{\sqrt{5}}\right)$$

(Here potential due to each $q = \frac{kq}{a}$ and potential due



Final potential of the charge

$$V_B = 0$$

(∴ Point *B* is equidistant from all the four charges) ∴ Using work energy theorem, $(W_{AB})_{\text{electric}} = Q(V_A - V_B)$ $= \frac{2qQ}{4\pi E_0 a} \left[1 - \frac{1}{\sqrt{5}}\right]$

$$= \left(\frac{1}{4\pi\varepsilon_0}\right) \frac{2Qq}{a} \left[1 - \frac{1}{\sqrt{5}}\right]$$

43. (c) Work done, $W_{PQ} = q(V_Q - V_P)$ = $(-100 \times 1.6 \times 10^{-19})(-4 - 10)$ = $+2.24 \times 10^{-16}$ J

44. (a) Gain in kinetic energy = work done by potential difference

$$eV = \frac{1}{2}mv^{2} \implies v = \sqrt{\frac{2eV}{m}}$$
$$= \sqrt{\frac{2 \times 1.6 \times 10^{-19} \times 20}{9.1 \times 10^{-31}}} = 2.65 \times 10^{6} \,\mathrm{m/s}$$

45. (d)
$$\frac{1}{2}mv^2 = \frac{kQq}{r}$$

$$\Rightarrow \frac{1}{2}m(2v)^2 = \frac{kqQ}{r'} \Rightarrow r' = \frac{r}{4}$$
46. (a) By using
 $W = q(V_B - V_A)$
 $\therefore V_B - V_A = \frac{2J}{20C} = 0.1 \text{ J/C} = 0.1 \text{ V}$

47. (b) When capacitors *C* and 2*C* capacitance are charged to V and 2V respectively.

 $Q_1 = CV \quad Q_2 = 2C \times 2V = 4CV$



By conservation of charge

$$4CV - CV = (C + 2C)V_{\text{common}}$$

$$V_{\text{common}} = \frac{3CV}{3C} = J$$

Therefore final energy of this configuration,

$$U_f = \left(\frac{1}{2}CV^2 + \frac{1}{2} \times 2CV^2\right) = \frac{3}{2}CV^2$$



Let q_1 and q_2 be the charge on the capacitors of 2μ F and 4μ F. Then charge on capacitor of 5μ F

$$Q = q_1 + q_2$$

$$\Rightarrow 5V_0 = 2(6 - V_0) + 4(6 - V_0)$$

$$\Rightarrow 5V_0 = 12 - 2V_0 + 24 - 4V_0$$

$$\Rightarrow 11V_0 = 36 \Rightarrow V_0 = \frac{36}{11}V$$

$$\Rightarrow Q = 5V_0 = \frac{180}{11}\mu C$$

49. (d) When two capacitors with capacitance C_1 and C_2 at potential V_1 and V_2 connected to each other by wire, charge begins to flow from higher to lower potential till they acquire common potential. Here, some loss of energy takes place which is given by.

Heat loss,
$$H = \frac{C_1 C_2}{2(C_1 + C_2)} (V_1 - V_2)^2$$

In the equation, put $V_2 = 0$, $V_1 = V_0$
 $C_1 = C$, $C_2 = \frac{C}{2}$
Loss of heat $= \frac{C \times \frac{C}{2}}{2\left(C + \frac{C}{2}\right)} (V_0 - 0)^2 = \frac{C}{6} V_0^2$
 $H = \frac{1}{6} C V_0^2$

50. (b) According to question,

Q

$$= 750\mu C = q_2 + q_3$$

$$C_1 = 15 \ \mu F$$

$$C_3 = 8 \ \mu F$$

$$Q$$

$$C_3 = 0$$

$$C_3 = 0$$

Capacitors C_2 and C_3 are in parallel hence, Voltage across C_2 = voltage across C_3 = 20 V Change on capacitor C_3 ,

$$q_3 = C_3 \times V_3 = 8 \times 20 = 160 \mu C$$

$$\therefore q_2 = 750 \mu C - 160 \mu C = 590 \mu C$$

51. (4)

Given,
$$C_1 = 5 \,\mu\text{F}$$
 and $V_1 = 220 \,\text{Volt}$

When capacitor C_1 fully charged it is disconnected from the supply and connected to uncharged capacitor C_2 . $C_2 = 2.5 \,\mu\text{F}, V_2 = 0$

Energy change during the charge redistribution,

$$\Delta U = U_i - U_f = \frac{1}{2} \frac{C_1 C_2}{C_1 + C_2} (V_1 - V_2)^2$$

= $\frac{1}{2} \times \frac{5 \times 2.5}{(5 + 2.5)} (220 - 0)^2 \,\mu J$
= $\frac{5}{2 \times 3} \times 22 \times 22 \times 100 \times 10^{-6} \,J$
= $\frac{5 \times 11 \times 22}{3} \times 10^{-4} \,J = \frac{55 \times 22}{3} \times 10^{-4} \,J$
= $\frac{1210}{3} \times 10^{-4} \,J = \frac{1210}{3} \times 10^{-3} \,J \approx 4 \times 10^{-2} \,J$
According to questions $\frac{x}{2} = 4 \times 10^{-2}$

According to questions, $\frac{1}{100} = 4 \times 1$

 $\therefore x = 4$

52. (a) Given,

Capacitance of capacitor, $C_1 = 10 \,\mu\text{F}$

Potential difference before removing the source voltage, $V_1 = 50 \text{ V}$

If C_2 be the capacitance of uncharged capacitor, then common potential is

$$V = \frac{C_1 V_1 + C_2 V_2}{C_1 + C_2}$$
$$\Rightarrow 20 = \frac{10 \times 50 + 0}{20 + C} \Rightarrow C = 15 \,\mu F$$

53. (c) In parallel combination, $C_{eq} = C_1 + C_2 = 10 \,\mu F$ When connected across 1 V battery, then

$$\frac{U_1}{U_2} = \frac{\left(\frac{1}{2}C_1V^2\right)}{\left(\frac{1}{2}C_2V^2\right)} = \frac{1}{4} \Rightarrow \frac{C_1}{C_2} = \frac{1}{4}$$

$$C_2 = 8 \,\mu F$$
 and $C_1 = 2 \,\mu F$
Now C_1 and C_2 are connected in series combination,

$$\therefore C_{\text{equivalent}} = \frac{C_1 C_2}{C_1 + C_2} = \frac{2 \times 8}{2 + 8} = \frac{16}{10} = 1.6 \mu F$$



Consider an infinitesimal strip of capacitor of thickness dx at a distance x as shown.

Capacitance of parallel plate capacitor of area A is given

by
$$C = \frac{\varepsilon_0 A}{t}$$

.

[Here *t* = seperation between plates] So, capacitance of thickness dx will be

$$\therefore dC = \frac{\varepsilon_0 a dx}{d + x \tan \alpha}$$

Total capacitance of system can be obtained by integrating with limits x = 0 to x = a

$$C_{eq} = \int dC = a\varepsilon_0 \int_{x=0}^{x=a} \frac{dx}{x \tan \alpha + d}$$

[By Binomial expansion]

$$\Rightarrow C_{eq} = \frac{a\varepsilon_0}{d} \int_0^a \left(1 - \frac{x\tan\alpha}{d}\right) dx = \frac{a\varepsilon_0}{d} \left(x - \frac{x^2\tan\alpha}{2d}\right)_0^a$$
$$\Rightarrow C_{eq} = \frac{a^2\varepsilon_0}{d} = \left(1 - \frac{a\tan\alpha}{2d}\right) = \frac{\varepsilon_0 a^2}{d} \left(1 - \frac{\alpha a}{2d}\right)$$

55. (a) Given, $K(x) = K(1 + \alpha x)$

Capacitance of element, $C_{el} = \frac{K\varepsilon_0 A}{dx}$

$$\Rightarrow C_{el} = \frac{\varepsilon_0 K(1 + \alpha x)A}{dx}$$
$$\therefore \int d\left(\frac{1}{C}\right) = \frac{1}{C_{el}} = \int_0^d \left(\frac{dx}{\varepsilon_0 KA(1 + \alpha x)}\right)$$
$$\Rightarrow \frac{1}{C} = \frac{1}{\varepsilon_0 KA\alpha} [ln(1 + \alpha x)]_0^d$$
$$\Rightarrow \frac{1}{C} = \frac{1}{\varepsilon_0 KA\alpha} \left[\alpha d - \frac{\alpha^2 d^2}{2}\right]$$
$$= \frac{1}{\varepsilon_0 KA\alpha} \left[\alpha d - \frac{\alpha^2 d^2}{2}\right]$$
$$= \frac{1}{\varepsilon_0 KA} \left[1 - \frac{\alpha d}{2}\right]$$
$$\Rightarrow C = \frac{\varepsilon_0 KA}{d\left(1 - \frac{\alpha d}{2}\right)} \Rightarrow C = \frac{\varepsilon_0 KA}{d} \left(1 + \frac{\alpha d}{2}\right)$$

56. (6) In the first condition, electrostatic energy is $U_i = \frac{1}{2}CV_0^2 = \frac{1}{2} \times 60 \times 10^{-12} \times 400 = 12 \times 10^{-9} J$

$$L_{1}^{(1)} = \frac{1}{2} C W^{2}$$

In the second condition $U_F = \frac{1}{2}C'V'^2$

$$U_{f} = \frac{1}{2} 2C \left(\frac{V_{0}}{2}\right)^{2} \qquad \left(\because C' = 2C, V' = \frac{V_{0}}{2}\right)^{2}$$
$$= \frac{1}{4} \times 60 \times 10^{-12} \times (20)^{2} = 6 \times 10^{-9} J$$
Energy lost = $U_{i} - U_{f} = 12 \times 10^{-9} J - 6 \times 10^{-9} J = 6 nJ$

57. (d)
$$V \phi = \frac{CV + (nC)V}{kC + nC}$$

$$\frac{(n+1)V}{k+n}$$

58. (c)
$$\frac{1}{C_{1}} = \frac{d/3}{k_{1}\epsilon_{0}A} + \frac{d/3}{k_{2}\epsilon_{0}A} + \frac{d/3}{k_{3}\epsilon_{0}A}$$
or
$$C_{1} = \frac{3k_{1}k_{2}k_{3}\epsilon_{0}A}{d(k_{1}k_{2} + k_{2}k_{3} + k_{3}k_{1})}$$

$$C_{2}$$

$$= \frac{k_{1}\epsilon_{0}(A/3)}{d} + \frac{k_{2}\epsilon_{0}(A/3)}{d} + \frac{k_{3}\epsilon_{0}(A/3)}{d}$$

$$= \frac{(k_{1} + k_{2} + k_{3})\epsilon_{0}A}{3d}$$

$$\frac{U_{1}}{U_{2}} = \frac{\frac{1}{2}C_{1}V^{2}}{\frac{1}{2}C_{2}V^{2}}$$

$$= \frac{E_1}{E_2} = \frac{9k_1k_2k_3}{(k_1 + k_2 + k_3)(k_1k_2 + k_2k_3 + k_3k_1)}$$
59. (d) $V_1 + V_2 = 10$

$$4\mu F \quad 6\mu F$$

$$10V \quad 9$$
and $4V_1 = 6V_2$
On solving above equations, we get
 $V_1 = 6V$

Charge on 4
$$\mu f$$
,
 $q = CV_1 = 4 \times 6 = 24 \,\mu\text{C}$.

q - Cν₁ - 4×6 - 24 μC.
60. (a) Equivalent capacitance in series combination (C') is given by

$$\frac{1}{C'} = \frac{1}{C_1} + \frac{1}{C_2} \Longrightarrow C' = \frac{C_1 C_2}{C_1 + C_2}$$

For parallel combination equivalent capacitance
$$C^{2} = C_1 + C_2$$

For parallel combination

$$q = 10(C_1 + C_2)$$

 $q_1 = 500 \ \mu\text{C}$
 $500 = 10(C_1 + C_2)$
 $C_1 + C_2 = 50 \ \mu\text{F}$ (i)
For Series Combination-

$$q_{2} = 10 \frac{C_{1}C_{2}}{(C_{1} + C_{2})}$$

$$80 = 10 \frac{C_{1}C_{2}}{50}$$
 From equation(ii)

$$C_{1}C_{2} = 400$$
(iii)
From equation (i) and (ii)

$$C_{1} = 10\mu F$$

$$C_{2} = 40\mu F$$

61. **(b)**
$$\omega = \omega_f - v_i = \frac{q}{2} \left(\frac{1}{C_f} - \frac{1}{C_i} \right)$$

= $\frac{(5 \times 10)^2}{2} \left(\frac{1}{2} - \frac{1}{5} \right) \times 10^6$
= 3.75×10^{-6} J

62. (b) Capacitance of a capacitor with a dielectric of dielectric constant k is given by

$$C = \frac{k \epsilon_0 A}{d}$$

$$\therefore E = \frac{V}{d} \qquad \therefore C = \frac{k \epsilon_0 A E}{V}$$

$$15 \times 10^{-12} = \frac{k \times 8.86 \times 10^{-12} \times 10^{-4} \times 10^6}{500}$$

$$k = 8.5$$

63. (b)
$$V = \frac{Q}{C}$$

 $= \left(\frac{Q_1 - Q_2}{2C}\right)$
 $= \left(\frac{4 - 2}{2 \times 1}\right) = 1 V$
 Q_1
 Q_2
 Q_1
 Q_2
 Q_1
 Q_2
 Q_2
 Q_1
 Q_2
 Q_2
 Q_1
 Q_2
 Q_2

64. (b) Energy stored in the system initially

For series combination

Ā

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$$\frac{1}{C_{eq}} = \frac{1}{C_1} + \frac{1}{C_2}$$

$$\Rightarrow \frac{\frac{7C}{3}}{\frac{7}{3} + C} = \frac{1}{2}$$

$$\Rightarrow 14 C = 7 + 3 C$$

$$\Rightarrow C = \frac{7}{11} \mu F$$

$$\cdot (\mathbf{d}) \underbrace{30\mu C}_{-\mu} \underbrace{-\mu}_{+\mu} \underbrace{-\mu}_{-\mu} \underbrace{+\mu}_{-\mu} \underbrace{-\mu}_{+\mu}_{+\mu} \underbrace{-\mu}_{+\mu} \underbrace{+\mu}_{-\mu} \underbrace{-\mu}_{+\mu}_{+\mu} \underbrace{-\mu}_{+\mu} \underbrace{+\mu}_{-\mu} \underbrace{-\mu}_{+\mu}_{+\mu} \underbrace{-\mu}_{+\mu} \underbrace{-\mu} \underbrace{-\mu}_{+\mu} \underbrace{-\mu}_{+\mu} \underbrace{-\mu}_{+\mu} \underbrace{-\mu}_{+\mu} \underbrace{-\mu} \underbrace{-\mu}_$$

As given in the figure, $6\mu F$ and $4\mu F$ are in parallel. Now using charge conservation

4μF

B

Charge on 6μ F capacitor $=\frac{6}{6+4} \times 30 = 18\mu$ C Since charge is asked on right plate therefore is $+18\mu$ C

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- 68. (b) As required equivalent capacitance should be

$$C_{eq} = \frac{6}{13} \mu F$$

Therefore three capacitors must be in parallel and 4 must be in series with it.

$$\frac{1}{C_{eq}} = \left[\frac{1}{3C}\right] + \left[\frac{1}{C} + \frac{1}{C} + \frac{1}{C} + \frac{1}{C}\right]$$
$$C_{eq} = \frac{3C}{13} = \frac{6}{13}\mu F \quad [as C = 2\mu F]$$

So, desired combination will be as below:



69. (b)
$$W = -\Delta u$$

= $(-1) \left| \frac{(c\epsilon)^2}{2kc} - \frac{(c\epsilon)^2}{2c} \right|$
= $\frac{\epsilon^2 c}{2} \frac{k-1}{k}$
= 508 J

70. (c) Let dielectric constant of material used be K.

$$= \frac{\varepsilon_{0}a^{2}}{\left(\frac{1}{k}-1\right)d} \left[\ell n \left(d+y\left(\frac{1}{k}-1\right)\right) \right]_{0}^{d}$$

$$= \frac{k \varepsilon_{0} a^{2}}{(1-k)d} \ell n \left(\frac{d}{k}\right) = \frac{k \varepsilon_{0} a^{2} \ell n k}{(k-1)d}$$

$$= \frac{k \varepsilon_{0} a^{2}}{(1-k)d} \ell n \left(\frac{1}{k}\right) = \frac{k \varepsilon_{0} a^{2} \ell n k}{(k-1)d}$$
72. (Bonus) $\frac{k_{1}}{k_{3}} \frac{k_{2}}{k_{4}} \frac{L/2}{L/2} \Rightarrow \begin{bmatrix} k_{1} & k_{2} & k_{3} \\ k_{4} & k_{2} \\ k_{3} & k_{4} \end{bmatrix} = \frac{k_{1} \varepsilon_{0} \frac{1}{2} \times L}{C_{3}} \frac{k_{2} \left[\varepsilon_{0} \frac{1}{2} \times L\right]}{C_{3}}$

$$C_{12} = \frac{C_{1}C_{2}}{C_{1}+C_{2}} = \frac{k_{1} \varepsilon_{0} \frac{1}{2} \times L}{(k_{1}+k_{2})\left[\frac{\varepsilon_{0} \frac{1}{2} \times L}{d/2}\right]}$$

$$C_{12} = \frac{k_{1}k_{2}}{k_{1}+k_{2}} \frac{\varepsilon_{0} L^{2}}{d}$$
in the same way we get,
$$C_{34} = \frac{k_{3}k_{4}}{k_{3}+k_{4}} \frac{\varepsilon_{0} L^{2}}{d}$$

$$\therefore C_{eq} = C_{12} + C_{34} = \left[\frac{k_{1}k_{2}}{k_{1}+k_{2}} + \frac{k_{3}k_{4}}{k_{3}+k_{4}}\right] \frac{\varepsilon_{0} L^{2}}{d} \dots (i)$$
Now if $k_{eq} = K$, $C_{eq} = \frac{k \varepsilon_{0} L^{2}}{d} \dots (i)$
Now if $k_{eq} = K$, $C_{eq} = \frac{k \varepsilon_{0} L^{2}}{d} \dots (i)$
This does not match with any of the options so this must be a bonus.

73. (a) Charge on Capacitor, $Q_i = CV$ After inserting dielectric of dielectric constant $= K Q_f = (kC) V$ Induced charges on dielectric $Q_{\text{ind}} = Q_f - Q_i = \text{KCV} - \text{CV}$

.. (i)

$$(K-1)CV = \left(\frac{5}{3} - 1\right) \times 90 \text{ pF} \times 2\text{V} = 1.2\text{nc}$$

74. (a) During charging charge on the capacitor increases with time. Charge on the capacitor C1 as a function of time, $Q = Q_0(1 - e^{-t/\bar{R}C})$



Both capacitor will have charge as they are connected in series

75. (d) The simplified circuit of the circuit given in question as follows:



The equivalent capacitance between C & D capacitors of 2μ F, 5μ F and 5μ F are in parallel.

 $\therefore C_{CD} = 2 + 5 + 5 = 12 \ \mu F \ (\because \text{ In parallel grouping} \\ C_{eq} = C_1 + C_2 + ... + C_n)$ Similarly equivalent capacitance between E & B C_{EB}

 $=4+2=6\mu F$

Now equivalent capacitance between A & B

$$\frac{1}{C_{eq}} = \frac{1}{6} + \frac{1}{12} + \frac{1}{6} = \frac{5}{12}$$

$$\Rightarrow C_{eq} = \frac{12}{5} = 2.4 \,\mu\text{F} \qquad (\because \text{ In series grouping}, \frac{1}{C_{eq}} = \frac{1}{C_1} + \frac{1}{C_2} + \dots + \frac{1}{C_n})$$

76. (c) Given area of Parallel plate capacitor, $A = 200 \text{ cm}^2$ Separation between the plates, d = 1.5 cm Force of attraction between the plates, $F = 25 \times 10^{-6}$ N F = QE

$$F = \frac{Q^2}{2A \epsilon_0} \quad (\text{E due to parallel plate} = \frac{\sigma}{2\epsilon_0} = \frac{Q}{A2\epsilon_0})$$

But $Q = CV = \frac{\epsilon_0 A(V)}{d}$

$$\therefore F = \frac{(\epsilon_0 AV)^2}{d^2 \times 2A \epsilon_0} + V^2$$
$$= \frac{(\epsilon_0 A)^2 \times V^2}{d^2 \times 2 \times (A \epsilon_0)} = \frac{(\epsilon_0 A) \times V^2}{d^2 \times 2}$$

or,
$$25 \times 10^{-6} = \frac{(8.85 \times 10^{-12}) \times (200 \times 10^{-4}) \times V^2}{2.25 \times 10^{-4} \times 2}$$

$$\Rightarrow V = \sqrt{\frac{25 \times 10^{-6} \times 2.25 \times 10^{-4} \times 2}{8.85 \times 10^{-12} \times 200 \times 10^{-4}}} \approx 250 \text{ V}$$

- 77. (a) The sum of final charges on C_2 and C_3 is 36 μ C.
- 78. (b) To get a capacitance of $2\mu F$ arrangement of capacitors of capacitance 1µF as shown in figure 8 capacitors of 1µF in parallel with four such branches in series i.e., 32 such capacitors are required.



79. (c) Before introducing a slab capacitance of plates

$$C_1 = \frac{\varepsilon_0 A}{3}$$

If a slab of dielectric constant K is introduced between plates then

$$C = \frac{K\varepsilon_0 A}{d} \text{ then } C'_1 = \frac{\varepsilon_0 A}{2.4}$$

$$C_1 \text{ and } C'_1 \text{ are in series hence,}$$

$$\frac{\varepsilon_0 A}{3} = \frac{k \frac{\varepsilon_0 A}{3} \cdot \frac{\varepsilon_0 A}{2.4}}{k \frac{\varepsilon_0 A}{3} + \frac{\varepsilon_0 A}{2.4}}$$

$$3k = 2.4 k + 3$$

$$Slab$$

$$0.6 \,\mathrm{k} = 3$$

Hence, the dielectric constant of slap is given by, 30

$$k = \frac{1}{6} = 5$$

80. (d) Energy of sphere
$$= \frac{Q^2}{2C}$$

 $4.5 = \frac{16 \times 10^{-12}}{2C}$
 $C = \frac{16 \times 10^{-12}}{10} = 4\pi\epsilon_0 R$

$$=\frac{16\times10}{9}=4\pi\varepsilon_0R$$

(capacity of spherical conductor)

$$R = \frac{16 \times 10^{-12}}{9} \times \frac{1}{4\pi\epsilon_0} \qquad \because \quad \frac{1}{4\pi\epsilon_0} = 9 \times 10^9$$
$$= 9 \times 10^9 \times \frac{16}{9} \times 10^{-12} = 16 \text{ mm}$$
$$(a) \quad {}^{4\mu}F_{\mu} \qquad {}^{-1}\frac{3^{\mu}F_{\mu}}{2} \qquad C_1 = 4\mu F_{\mu} \quad 12\mu F = C_p$$



Charge on C₁ is q₁ =
$$\left[\left(\frac{12}{4+12}\right) \times 8\right] \times 4 = 24\mu C$$

The voltage across C_p is $V_p = \frac{4}{4+12} \times 8 = 2V$

- :. Voltage across 9µF is also 2V
- \therefore Charge on 9µF capacitor = 9 × 2 = 18µC
- \therefore Total charge on 4 μ F and 9 μ F = 42 μ C

$$\therefore E = \frac{KQ}{r^2} = 9 \times 10^9 \times \frac{42 \times 10^{-6}}{30 \times 30} = 420 \text{ NC}^{-1}$$

82. (a) Capacitors 2μ F and 2μ F are parallel, their equivalent $=4 \mu F$

 6μ F and 12 μ F are in series, their equivalent = 4μ F

Now $4\mu F (2 \text{ and } 2 \mu F)$ and $8\mu F$ in series = $\frac{3}{8}\mu F$ And $4\mu F (12 \& 6 \mu F)$ and $4\mu F$ in parallel = $4 + 4 = 8\mu F$ 8μ F in series with 1μ F = $\frac{1}{8} + 1 \Rightarrow \frac{8}{9}\mu$ F

Now
$$C_{eq} = \frac{8}{9} + \frac{8}{3} = \frac{32}{9}$$

 C_{eq} of circuit = $\frac{32}{9}$

With C -
$$\frac{1}{C_{eq}} = \frac{1}{C} + \frac{9}{32} = 1 \implies C = \frac{32}{23}$$

(d) To get effective capacitance of $6 \,\mu\text{F}$ two capacitors of 83. 4 μ F each connected in sereies and one of 4 μ F capacitor in parallel with them.



Two capacitances in series

$$\therefore \frac{1}{C} = \frac{1}{C_1} + \frac{1}{C_2} = \frac{1}{4} + \frac{1}{4} = \frac{1}{2}$$

1 capacitor in parallel

$$\therefore C_{eq} = C_3 + C = 4 + 2 = 6 \,\mu I$$



From figure, $Q_2 = \frac{2}{2+1}Q = \frac{2}{3}Q$

$$Q = E\left(\frac{C \times 3}{C+3}\right)$$
$$\therefore Q_2 = \frac{2}{3}\left(\frac{3CE}{C+3}\right) = \frac{2CE}{C+3}$$

Therefore graph d correctly dipicts.







When switch is open





86. (a) Electric field in presence of dielectric between the two plates of a parallel plate capaciator is given by,

$$E = \frac{\sigma}{K\varepsilon_0}$$

Then, charge density

$$\sigma = K\varepsilon_0 E$$

= 2.2 × 8.85 × 10⁻¹² × 3 × 10⁴
≈ 6 × 10⁻⁷ C/m²

87. (d)

88. (c) The value of dielectric constant is given as, $K = K_0 + \lambda x$

And,
$$V = \int_{0}^{d} E dr \Rightarrow V = \int_{0}^{d} \frac{\sigma}{K} dx$$

= $\sigma \int_{0}^{d} \frac{1}{(K_{0} + \lambda x)} dx = \frac{\sigma}{\lambda} \Big[\ln(K_{0} + \lambda d) - \ln K_{0} \Big]$

$$= \frac{\sigma}{\lambda} \ln\left(1 + \frac{\lambda d}{K_0}\right)$$

Now it is given that capacitance of vacuum = C₀.
Thus, $C = \frac{Q}{V}$
$$= \frac{\sigma.s}{v} \text{ (Let surface area of plates = s)}$$

$$= \frac{\sigma.s}{\frac{\sigma}{\lambda} \ln\left(1 + \frac{\lambda d}{K_0}\right)}$$

$$= s\lambda \cdot \frac{d}{d} \frac{1}{\ln\left(1 + \frac{\lambda d}{K_0}\right)} (\because \text{ in vacuum } \varepsilon_0 = 1)$$

$$c = \frac{\lambda d}{\ln\left(1 + \frac{\lambda d}{K_0}\right)} \cdot C_0 \quad \left(\text{here, } C_0 = \frac{s}{d}\right)$$

89. (c)
90. (d) Possible combination of capacitors
(b) Three capacitors in series combination

(i) Three capacitors in series combination 3uF 3uF 3uF

$$\frac{1}{C_{eq}} = \frac{1}{3} + \frac{1}{3} + \frac{1}{3}$$

$$\therefore \frac{1}{C_{eq}} = 1\mu F$$

(ii) Three capacitors in parallel combination











A

$$C = \frac{k \in_0 2}{3d} + \frac{2k \in_0 A}{3d} = \frac{4}{3} \frac{k \in_0}{d}$$
$$\therefore \frac{C}{C_0} = \frac{\frac{4}{3} \frac{k \in_0 A}{d}}{\frac{k \in_0 A}{d}} = \frac{4}{3}$$

92. (c) As, $C = \frac{Q}{V} = \frac{It}{V}$
$$\Rightarrow \frac{V}{t} = \frac{I}{C} = \frac{2}{1 \times 10^{-6}}$$
$$= 2 \times 10^6 \text{ V/s}$$

93. (c) When charged particle enters perpendicularly in an electric field, it describes a parabolic path

$$y = \frac{1}{2} \left(\frac{QE}{m} \right) \left(\frac{x}{4} \right)^2$$

This is the equation of parabola.



94. (d) The discharging of a capacitor is given as $q = q_0 exp[-t/RC]$ RC = time constant = τ $q = q_0 e^{-t/\tau}$ If e is the capacitance of the capacitor

$$q = CV$$
 and $q = CV_0$

Thus,
$$CV = CV_0 e^{t/\tau}$$

 $V = V_0 e^{-t/\tau}$...(i)

From the graph (given in the problem when t = 0.5, V = 25 i.e., $V_0 = 25$ volt. and when t = 200, V = 5 volt

Thus equation (i) becomes
$$5 - 25e^{-200/\tau}$$

$$\Rightarrow 1/5 = e^{-200/\tau}$$

Taking loge on both sides

$$\log_{e} \frac{1}{5} = -200 / \tau \implies -\frac{200}{\tau} = \log e^{5}$$

$$\tau = \frac{200}{\log_{e} 5}$$

or
$$\tau = \frac{200}{\log_{e} \left(\frac{10}{2}\right)} = \frac{200}{\log_{e} 10 - \log_{e} 2}$$

$$\tau = \frac{200}{2.302 - 0.693} = \frac{200}{1.609} = 124.300$$

Which lies between 100 s and 150 s

- **95.** (c) The dielectric constant of the gas is 1.01
- **96.** (d) Capacitance of sphere is given by :

$$C = 4\pi \in_0 r$$

If, $C = 1F$ then radius of sphere needed:

$$r = \frac{C}{4\pi \epsilon_0} = \frac{1}{4\pi \times 8.85 \times 10^{-12}}$$

or, $r = \frac{10^{12}}{4\pi \times 8.85} = 9 \times 10^9 \text{ m}$

 9×10^9 m is very large, it is not possible to obtain such a large sphere. Infact earth has radius 6.4×10^6 m only and capacitance of earth is 711μ F.

97. (d) Equivalent capacitance of n_2 number of capacitors each of capacitance C_2 in parallel = n_2C_2

Equivalent capacitance of n_1 number of capacitors each of capacitances C_1 in series.

Capacitance of each is
$$C_1 = \frac{C_1}{n_1}$$

According to question, total energy stored in both the combinations are same

i.e.,
$$\frac{1}{2} \left(\frac{C_1}{n_1} \right) (4V)^2 = \frac{1}{2} (n_2 C_2) V^2$$

 $\therefore C_2 = \frac{16C_1}{n_1 n_2}$

98. (c) Charge (or current) always flows from higher potential to lower potential.

 $Potential = \frac{Charge}{Capacitance}$

99. (c) Initial energy of capacitor, $E_1 = \frac{q_1^2}{2C}$ Final energy of capacitor,

$$E_2 = \frac{1}{2}E_1 = \frac{q_1^2}{4C} = \left(\frac{\frac{q_1}{\sqrt{2}}}{\frac{\sqrt{2}}{2C}}\right)$$

 $\therefore t_1 = \text{time for the charge to reduce to } \frac{1}{\sqrt{2}}$ of its initial value

and t_2 = time for the charge to reduce to $\frac{1}{4}$ of its initial value

We have,
$$q_2 = q_1 e^{-t/CR} \implies \ln\left(\frac{q_2}{q_1}\right) = -\frac{t}{CR}$$

 $\therefore \ln\left(\frac{1}{\sqrt{2}}\right) = \frac{-t_1}{CR} \dots (1)$
and $\ln\left(\frac{1}{4}\right) = \frac{-t_2}{CR} \dots (2)$
By (1) and (2), $\frac{t_1}{t_2} = \frac{\ln\left(\frac{1}{\sqrt{2}}\right)}{\ln\left(\frac{1}{4}\right)} = \frac{1}{2} \frac{\ln\left(\frac{1}{2}\right)}{2\ln\left(\frac{1}{2}\right)} = \frac{1}{4}$



The capacitance with air between the plates

$$C = \frac{\varepsilon_0 A}{d} = 9 \text{pF}$$

On introducing two dielectric between the plates, the given capacitance is equal to two capacitances connected in series where

$$C_1 = \frac{k_1 \in A}{d/3} = \frac{3 \in A}{d/3}$$
$$= \frac{3 \times 3 \in A}{d}$$
$$= \frac{9 \in A}{d}$$
and

$$C_2 = \frac{k_2 \in A}{2d/3} = \frac{3k_2 \in A}{2d}$$
$$= \frac{3 \times 6 \in A}{2d} = \frac{9 \in A}{d}$$

The equivalent capacitance C_{eq} is

$$\frac{1}{C_{eq}} = \frac{1}{C_1} + \frac{1}{C_2}$$
$$= \frac{d}{9 \in A} + \frac{d}{9 \in A} = \frac{2d}{9 \in A}$$
$$\therefore C_{eq} = \frac{9}{2} \frac{\in A}{d} = \frac{9}{2} \times 9 \ pF = 40.5 pF$$

101. (a) The potential energy of a charged capacitor is given

by
$$U = \frac{Q^2}{2C}$$
.

When a dielectric slab is introduced between the plates

the energy is given by $\frac{Q^2}{2KC}$, where *K* is the dielectric

constant.

Again, when the dielectric slab is removed slowly its energy increases to initial potential energy. Thus, work done is zero.

- **102.** (b) As *n* plates are joined alternately positive plate of all (n-1) capacitor are connected to one point and negative plate of all (n-1) capacitors are connected to other point. It means (n-1) capacitors joined in parallel.
 - \therefore Resultant capacitance = (n-1)C

Electric potential energy of capacitor = heat absorbed

$$\frac{1}{2}CV^2 = m.s\,\Delta t; \ \mathbf{V} = \sqrt{\frac{2m.s.\Delta}{C}}$$

104. (b) The capacitance without aluminium foil is

$$C = \frac{\varepsilon_0 A}{d}$$

Here, d is distance between the plates of a capacitor A = Area of plates of capacitor

When an aluminium foil of thickness t is introduced between the plates.

Capacitance,
$$C' = \frac{\varepsilon_0 A}{d - \epsilon}$$

If thickness of foil is negligible $50 d - t \sim d$. Hence, C = C'.

105. (d) The work done is stored in the form of potential energy which is given by

$$U = \frac{1}{2} \frac{Q^2}{C}$$

: $U = \frac{1}{2} \times \frac{\left(8 \times 10^{-18}\right)^2}{100 \times 10^{-6}} = 32 \times 10^{-32} \,\mathrm{J}$

106. (b) In parallel, equivalent capacitance of *n* capacitor of capacitance *C*

$$C' = nC$$

Energy stored in this capacitor

$$E = \frac{1}{2}C^{1}V^{2}$$

$$\Rightarrow E = \frac{1}{2}(nC)V^{2} = \frac{1}{2}nCV^{2}$$

$$\square U$$

Alternatively

Each capacitor has a potential difference of *V* between the plates.

So, energy stored in each capacitor

$$= \frac{1}{2} CV^2.$$

∴ Energy stored in n capacitor

$$= \left[\frac{1}{2} CV^2\right] \times n$$

107. (a) Capacitance of spherical conductor = $4\pi E_0 R$ Here, *R* is radius of conductor

:.
$$C = 4\pi \in_0 R = \frac{1}{9 \times 10^9} \times 1 = 1.1 \times 10^{-10} F$$