



Assignment

Continuity

Basic Level

1. If the function $f(x) = \begin{cases} 5x - 4 & , \text{ if } 0 < x \leq 1 \\ 4x^2 + 3bx & , \text{ if } 1 < x < 2 \end{cases}$ is continuous at every point of its domain, then the value of b is [Rajasthan PET 2000]
- (a) -1 (b) 0 (c) 1 (d) None of these
2. If $f(x) = \begin{cases} \frac{\log(1+2ax) - \log(1-bx)}{x} & , x \neq 0 \\ k & , x = 0 \end{cases}$ is continuous at $x=0$, then k equals [Rajasthan PET 1998]
- (a) $2a+b$ (b) $2a-b$ (c) $b-2a$ (d) $b+a$
3. If $f(x) = \begin{cases} x & , \text{ when } 0 \leq x < 1 \\ k-2x & , \text{ when } 1 \leq x \leq 2 \end{cases}$ is continuous at $x=1$, then value of k is [Rajasthan PET 1993]
- (a) 1 (b) -1 (c) 3 (d) 2
4. If $f(x) = \begin{cases} x & , x < 0 \\ 1 & , x = 0 \\ x^2 & , x > 0 \end{cases}$, then true statement is [Rajasthan PET 1992; DCE 2001]
- (a) $\lim_{x \rightarrow 0} f(x) = 1$ (b) $\lim_{x \rightarrow 0} f(x) = 0$ (c) $f(x)$ is continuous at $x=0$ (d) $\lim_{x \rightarrow 0} f(x)$ does not exist
5. If $f(x) = \frac{x-a}{\sqrt{x}-\sqrt{a}}$ is continuous at $x=a$, then $f(a)$ equals
- (a) \sqrt{a} (b) $2\sqrt{a}$ (c) a (d) $2a$
6. If $f(x) = |x-b|$, then function [Roorkee 1984]
- (a) Is continuous $\forall x$ (b) Is continuous at $x=\infty$ (c) Is discontinuous at $x=b$ (d) None of these
7. If $f(x) = \begin{cases} \frac{x^4-16}{x-2} & , \text{ when } x \neq 2 \\ 16 & , \text{ when } x = 2 \end{cases}$ then
- (a) $f(x)$ is continuous at $x=2$ (b) $f(x)$ is discontinuous at $x=2$ (c) $\lim_{x \rightarrow 2} f(x) = 16$ (d) None of these
8. In the following discontinuous function is [Rajasthan PET 1984]
- (a) $\sin x$ (b) x^2 (c) $\frac{1}{1-2x}$ (d) $\frac{1}{1+x^2}$
9. If $f(x) = \begin{cases} x^2 & , \text{ when } x \leq 1 \\ x+5 & , \text{ when } x > 1 \end{cases}$ then [MP PET 1996]

- (a) $f(x)$ is continuous at $x = 1$ (b) $f(x)$ is discontinuous at $x = 1$
 (c) $\lim_{x \rightarrow 1} f(x) = 1$ (d) None of these
10. If $f(x) = \begin{cases} 1+x, & \text{when } x \leq 2 \\ 5-x, & \text{when } x > 2 \end{cases}$ then
 (a) $f(x)$ is continuous at $x=2$ (b) $f(x)$ is discontinuous at $x=2$ (c) $f(x)$ is discontinuous at $x = 0$ (d) None of these
11. The point of discontinuity of the function $f(x) = \frac{1 + \cos 5x}{1 - \cos 4x}$ is
 (a) $x = 0$ (b) $x = \pi$ (c) $x = \pi/2$ (d) All of these
12. Function $f(x) = |x|$ is [Rajasthan PET 1992]
 (a) Discontinuous at $x=0$ (b) Discontinuous at $x = 1$ (c) Continuous at all points (d) Discontinuous at all points
13. If $f(x) = \begin{cases} x^2, & \text{when } x \neq 1 \\ 2, & \text{when } x = 1 \end{cases}$ then
 (a) $\lim_{x \rightarrow 1} f(x) = 2$ (b) $f(x)$ is continuous at $x = 1$ (c) $f(x)$ is discontinuous at $x = 1$ (d) None of these
14. Let $f(x) = \begin{cases} \frac{\sin \pi x}{5x}, & x \neq 0 \\ k, & x = 0 \end{cases}$. If $f(x)$ is continuous at $x = 0$, then $k =$
 (a) $\frac{\pi}{5}$ (b) $\frac{5}{\pi}$ (c) 1 (d) 0
15. Function $f(x) = x - |x|$ is
 (a) Discontinuous at $x = 0$ (b) Discontinuous at $x = 1$ (c) Continuous at all points (d) Discontinuous at all points
16. Function $f(x) = x + |x|$ is
 (a) Continuous at all points (b) Discontinuous at $x = 0$ (c) Discontinuous at $x = 1$ (d) Discontinuous at all points
17. If $f(x)$ is continuous function and $g(x)$ is discontinuous function, then correct statement is
 (a) $f(x) + g(x)$ is continuous function (b) $f(x) - g(x)$ is continuous function
 (c) $f(x) \cdot g(x)$ is discontinuous function (d) $f(x)/g(x)$ is discontinuous function
18. Function $f(x) = \begin{cases} -1, & \text{when } x < -1 \\ -x, & \text{when } -1 \leq x \leq 1 \\ 1, & \text{when } x > 1 \end{cases}$ is continuous [Rajasthan PET 1986]
 (a) Only at $x = 1$ (b) Only at $x = -1$ (c) At both $x = 1$ and $x = -1$ (d) Neither at $x = 1$ nor at $x = -1$

Advance Level

19. Let $f(x) = \frac{\sqrt{1 + \sin x} - \sqrt{1 - \sin x}}{x}$ the value which should be assigned to f at $x = 0$ so that it is continuous everywhere is [MP PET 1992]
 (a) $\frac{1}{2}$ (b) -2 (c) 2 (d) 1
20. The value of $f(0)$ so that the function $f(x) = \frac{\sqrt{1+x} - (1+x)^{1/3}}{x}$ becomes continuous is equal to

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(a) $\frac{1}{6}$

(b) $\frac{1}{4}$

(c) 2

(d) $\frac{1}{3}$

21. If $f(x) = \begin{cases} |x-a| & \text{when } x \neq a \\ 1 & \text{when } x = a \end{cases}$ then [AI CBSE 1983]

- (a) $f(x)$ is continuous at $x=a$ (b) $f(x)$ is discontinuous at $x=a$ (c) $\lim_{x \rightarrow a} f(x) = 1$ (d) None of these

22. If $f(x) = \begin{cases} \frac{x}{e^{1/x} + 1}, & \text{when } x \neq 0 \\ 0 & \text{when } x = 0 \end{cases}$ then [BIT Rnchi 1999]

- (a) $\lim_{x \rightarrow 0^+} f(x) = 1$ (b) $\lim_{x \rightarrow 0^-} f(x) = 1$ (c) $f(x)$ is continuous at $x = 0$ (d) None of these

23. If the function $f(x) = \begin{cases} \frac{k \cos x}{\pi - 2x}, & \text{when } x \neq \frac{\pi}{2} \\ 3 & \text{when } x = \frac{\pi}{2} \end{cases}$ be continuous at $x = \frac{\pi}{2}$, then $k =$

- (a) 3 (b) 6 (c) 12 (d) None of these

24. A function $f(x)$ is defined in $[0,1]$ as follows $f(x) = \begin{cases} x, & \text{if } x \text{ is rational} \\ 1-x, & \text{if } x \text{ is irrational} \end{cases}$, then correct statement is

- (a) $f(x)$ is continuous at $x = 0$ (b) $f(x)$ is continuous at $x = 1$
 (c) $f(x)$ is continuous at $x = \frac{1}{2}$ (d) $f(x)$ is everywhere discontinuous

25. If $f(x) = \begin{cases} \frac{e^{1/x} - 1}{e^{1/x} + 1}, & x \neq 0 \\ 1 & x = 0 \end{cases}$, then at $x = 0, f(x)$ is [BITS (Mesra) 1998]

- (a) Continuous (b) Left continuous (c) Right continuous (d) None of these

26. The function $f(x) = \begin{cases} x+2, & 1 \leq x \leq 2 \\ 4, & x = 2 \\ 3x-2, & x > 2 \end{cases}$ is continuous [DCE 1999]

- (a) $x = 2$ only (b) $x \leq 2$ (c) $1 \leq x$ (d) None of these

27. If $f(x) = \begin{cases} 1, & \text{when } 0 < x \leq \frac{3\pi}{4} \\ 2 \sin \frac{2x}{9}, & \text{when } \frac{3\pi}{4} < x < \pi \end{cases}$ then [IIT 1991]

- (a) $f(x)$ is continuous at $x = 0$ (b) $f(x)$ is continuous at $x = \pi$
 (c) $f(x)$ is continuous at $x = \frac{3\pi}{4}$ (d) $f(x)$ is discontinuous at $x = \frac{3\pi}{4}$

28. If $f(x) = \begin{cases} 1/2 - x, & 0 < x < 1/2 \\ 0, & x = 0 \\ 1/2, & x = 1/2 \\ 3/2 - x, & 1/2 < x < 1 \\ 1, & x = 1 \end{cases}$, then false statement is [Rajasthan PET 1984 (Similar to MP PET 1996)]

- (a) $f(x)$ is discontinuous at $x = 0$ (b) $f(x)$ is continuous at $x = \frac{1}{2}$
 (c) $f(x)$ is discontinuous at $x = 1$ (d) $f(x)$ is continuous at $x = \frac{1}{4}$

29. $f(x) = \frac{\sqrt{1+px} - \sqrt{1-px}}{x}, -1 \leq x < 0 = \frac{2x+1}{x-2}, 0 \leq x \leq 1$ is continuous in the interval $[-1, 1]$ then p equals
 (a) -1 (b) $-\frac{1}{2}$ (c) $\frac{1}{2}$ (d) 1
30. The function $f(x) = \begin{cases} x^2/a & , 0 \leq x < 1 \\ a & , 1 \leq x < \sqrt{2} \\ (2b^2 - 4b)/x^2, & \sqrt{2} \leq x < \infty \end{cases}$ is continuous for $0 \leq x < \infty$, then the most suitable values of a and b are
 [BIT Ranchi 1984]
 (a) $a=1, b=-1$ (b) $a=-1, b=1+\sqrt{2}$ (c) $a=-1, b=1$ (d) None of these
31. Let $f(x) = \begin{cases} \frac{x^3 + x^2 - 16x + 20}{(x-2)^2}, & \text{if } x \neq 2 \\ k & , \text{if } x = 2 \end{cases}$ if $f(x)$ be continuous for all x , then $k =$ [IIT 1981]
 (a) 7 (b) -7 (c) ± 7 (d) None of these
32. If $f(x) = \begin{cases} \frac{x^2 + 3x - 10}{x^2 + 2x - 15}, & \text{when } x \neq -5 \\ a & , \text{when } x = -5 \end{cases}$ is continuous at $x = -5$, then the value of 'a' will be
 (a) $\frac{3}{2}$ (b) $\frac{7}{8}$ (c) $\frac{8}{7}$ (d) $\frac{2}{3}$
33. The function $f(x) = [x]^2 - [x^2]$ (where $[y]$ is the greatest integer less than or equal to y), is discontinuous at [IIT 1990]
 (a) All integers (b) All integers except 0 and 1 (c) All integers except 0
 (d) All integers except 1
34. If $f(x) = \frac{1}{2}x - 1$, then on the interval $[0, \pi]$
 (a) $\tan[f(x)]$ and $\frac{1}{f(x)}$ are both continuous (b) $\tan[f(x)]$ and $\frac{1}{f(x)}$ are both discontinuous
 (c) $\tan[f(x)]$ and $f^{-1}(x)$ are both continuous (d) $\tan[f(x)]$ is continuous but $\frac{1}{f(x)}$ is not continuous
35. Let $f(x) = [x] + \sqrt{x - [x]}$, where $[x]$ denotes the greatest integer function. Then,
 (a) $f(x)$ is continuous on R^+ (b) $f(x)$ is continuous on R
 (c) $f(x)$ is continuous on $R - Z$ (d) None of these
36. Let $f(x) = [2x^3 - 5]$, $[.]$ denotes the greatest integer function. Then number of points in $(1, 2)$ where the function is discontinuous, is
 (a) 0 (b) 13 (c) 10 (d) 3
37. The number of points at which the function $f(x) = \frac{1}{x - [x]}$ ($[.]$ denotes, the greatest integer function) is not continuous is
 (a) 1 (b) 2 (c) 3 (d) None of these
38. If $f(x) = \begin{cases} \frac{\sin x}{x} + \cos x, & \text{when } x \neq 0 \\ \frac{1}{2} & , \text{when } x = 0 \end{cases}$, then
 (a) $\lim_{x \rightarrow 0^+} f(x) \neq 2$ (b) $\lim_{x \rightarrow 0^-} f(x) = 0$ (c) $f(x)$ is continuous at $x = 0$ (d) None of these
39. The number of points at which the function $f(x) = \frac{1}{\log|x|}$ is discontinuous is
 (a) 1 (b) 2 (c) 3 (d) 4
40. The function $f(x) = p[x+1] + q[x-1]$, where $[x]$ is the greatest integer function is continuous at $x = 1$ if
 (a) $p - q = 0$ (b) $p + q = 0$ (c) $p = 0$ (d) $q = 0$

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41. Function $f(x) = \left(1 + \frac{x}{a}\right)^{1/x}$ is continuous at $x = 0$, if $f(0)$ equals
- (a) e^a (b) e^{-a} (c) 0 (d) $e^{1/a}$
42. Let $[.]$ denote the greatest integer function and $f(x) = [\tan^2 x]$. Then [IIT 1993]
- (a) $\lim_{x \rightarrow 0} f(x)$ does not exist (b) $f(x)$ is continuous at $x = 0$
- (c) $f(x)$ is not differentiable at $x = 0$ (d) $f'(0) = 1$
43. The function $f(x) = \begin{cases} x + a\sqrt{2} \sin x & 0 \leq x < \pi/4 \\ 2x \cot x + b & \pi/4 \leq x \leq \pi/2 \\ a \cos 2x - b \sin x & \pi/2 < x \leq \pi \end{cases}$ is continuous for $0 \leq x \leq \pi$ then a, b are
- (a) $\frac{\pi}{6}, \frac{\pi}{12}$ (b) $\frac{\pi}{3}, \frac{\pi}{6}$ (c) $\frac{\pi}{6}, -\frac{\pi}{12}$ (d) None of these
44. Let $f: R \rightarrow R$ be any function. Define $g: R \rightarrow R$ by $g(x) = |f(x)|$ for all x , Then g is [IIT 2000]
- (a) Onto if f is onto (b) One-one if f is one-one
- (c) Continuous if f is continuous (d) Differentiable if f is differentiable

Answer Sheet

Assignment (Basic & Advance Level)

1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20
a	a	c	b	b	a,b	b	c	b	a	d	c	c	a	c	a	c	d	d	a
21	22	23	24	25	26	27	28	29	30	31	32	33	34	35	36	37	38	39	40
b	c	b	c	c	c	c	b	b	c	a	b	d	b	b	b	d	c	c	b
41	42	43	44																
d	b	c	c																