

1. Set of value of  $r$  for which,  ${}^{18}C_{r-2} + 2 \cdot {}^{18}C_{r-1} + {}^{18}C_r \geq {}^{20}C_{13}$  contains  
(A) 4 element (B) 5 elements (C) 7 elements (D) 10 elements
2. The number of values of ' $r$ ' satisfying the equation,  ${}^{39}C_{3r-1} - {}^{39}C_{r^2} = {}^{39}C_{r^2-1} - {}^{39}C_{3r}$  is  
(A) 1 (B) 2 (C) 3 (D) 4
3. In the expansion of  $\left(\frac{x+1}{x^{2/3} - x^{1/3} + 1} - \frac{x-1}{x-x^{1/2}}\right)^{10}$ , the term which does not contain  $x$  is  
(A)  ${}^{10}C_0$  (B)  ${}^{10}C_7$  (C)  ${}^{10}C_4$  (D) none
4. If the second, third and fourth terms in the expansion of  $(a+b)^n$  are 135, 30 and  $10/3$  respectively, then  
(A)  $a = 3$  (B)  $b = 1/3$  (C)  $n = 5$  (D) all are correct
5. The coefficient of the term independent of  $x$  in the expansion of  $(1+x+2x^3)\left(\frac{3}{2}x^2 - \frac{1}{3x}\right)^9$ , is  
(A)  $\frac{1}{3}$  (B)  $\frac{19}{54}$  (C)  $\frac{17}{54}$  (D)  $\frac{1}{4}$
6. The number of irrational terms in the expansion of  $(5^{1/6} + 2^{1/8})^{100}$  is  
(A) 96 (B) 97 (C) 98 (D) 99
7. The sum of the rational terms of  $(2^{1/5} + \sqrt{3})^{20}$  is  
(A) 71 (B) 85 (C) 97 (D) None of these
8. The sum of the binomial coefficients of  $\left[2x + \frac{1}{x}\right]^n$  is equal to 256. The constant term in the expansion is  
(A) 1120 (B) 2110 (C) 1210 (D) none
9. In the expansion of  $\left(3^{-\frac{x}{4}} + 3^{\frac{5x}{4}}\right)^n$  the sum of the binomial coefficients is 64 and the term with the greatest binomial coefficient exceeds the third term by  $(n-1)$ , then the value of  $x$  must be  
(A) 1 (B) 2 (C) 0 (D) -1
10. Number of rational terms in the expansion of  $(\sqrt{2} + \sqrt[4]{3})^{100}$  is  
(A) 25 (B) 26 (C) 27 (D) 28
11. The term independent of ' $x$ ' in the expansion of  $\left(9x - \frac{1}{3\sqrt{x}}\right)^{18}$ ,  $x > 0$ , is  $\alpha$  times the corresponding binomial coefficient. Then ' $\alpha$ ' is  
(A) 3 (B)  $\frac{1}{3}$  (C)  $-\frac{1}{3}$  (D) 1

12. The coefficient of  $x^5$  in the expansion of  $(1 + x^2)^5 (1 + x)^4$  is  
 (A) 30 (B) 60 (C) 40 (D) None of these
13. The middle term in the expansion of  $(x^2 - 2x)^{10}$  is  
 (A)  $^{10}C_4 x^{17} \cdot 2^4$  (B)  $^{-10}C_5 2^5 x^{15}$  (C)  $^{-10}C_4 2^4 \cdot x^{17}$  (D) None of these
14. The middle term in the expansion of  $(1 - 3x + 3x^2 - x^3)^6$  is  
 (A)  $^{18}C_{10} x^{10}$  (B)  $^{18}C_9 (-x)^9$  (C)  $^{18}C_9 x^9$  (D) None of these
15. The middle terms of the expansion  $\left(2a - \frac{a^2}{4}\right)^9$  is/ are  
 (A)  $\frac{63}{4} a^{13}, -\frac{63}{32} a^{14}$  (B)  $\frac{63}{4} a^{14}, -\frac{63}{32} a^{13}$  (C)  $-\frac{63}{4} a^{13}, \frac{63}{32} a^{14}$  (D) None of these
16. If  $6^{83} + 8^{83}$  is divided by 49, then the remainder is  
 (A) 35 (B) 5 (C) 1 (D) 0
17. The remainder, when  $(15^{23} + 23^{23})$  is divided by 19, is  
 (A) 4 (B) 15 (C) 0 (D) 18
18. Last three digits of the number  $N = 7^{100} - 3^{100}$  are  
 (A) 100 (B) 300 (C) 500 (D) 000
19. If  $(1 + x - 3x^2)^{2145} = a_0 + a_1 x + a_2 x^2 + \dots$  then  $a_0 - a_1 + a_2 - a_3 + \dots$  ends with  
 (A) 1 (B) 3 (C) 7 (D) 9
20. The coefficient of  $x^{49}$  in the expansion of  $(x - 1)\left(x - \frac{1}{2}\right)\left(x - \frac{1}{2^2}\right) \dots \left(x - \frac{1}{2^{49}}\right)$  is equal to  
 (A)  $-2\left(1 - \frac{1}{2^{50}}\right)$  (B)  $2\left(1 - \frac{1}{2^{49}}\right)$   
 (C)  $2\left(1 - \frac{1}{2^{50}}\right)$  (D)  $-2\left(1 - \frac{1}{2^{49}}\right)$

## Answers

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1. (C) 2. (B) 3. (C) 4. (D) 5. (C) 6. (B) 7. (D) 8. (A) 9. (C) 10. (B)  
 11. (D) 12. (B) 13. (B) 14. (B) 15. (A) 16. (A) 17. (C) 18. (D) 19. (B) 20. (A)