

Chapter : 9. COMBINATIONS

Exercise : 9A

Question: 1 A

Evaluate:

Solution:

We know that:

$$\begin{aligned} {}^nC_r &= \frac{n!}{(n-r)! \times r!} \\ \Rightarrow {}^{20}C_4 &= \frac{20!}{(20-4)! \times 4!} \\ \Rightarrow {}^{20}C_4 &= \frac{20!}{16! \times 4!} \\ \Rightarrow {}^{20}C_4 &= \frac{20 \times 19 \times 18 \times 17 \times 16!}{16! \times 4!} \\ \Rightarrow {}^{20}C_4 &= \frac{20 \times 19 \times 18 \times 17}{4!} \\ \Rightarrow {}^{20}C_4 &= \frac{20 \times 19 \times 18 \times 17}{4 \times 3 \times 2 \times 1} \\ \Rightarrow {}^{20}C_4 &= \frac{116280}{24} \\ \Rightarrow {}^{20}C_4 &= 4845 \end{aligned}$$

Ans: ${}^{20}C_4 = 4845$

Question: 1 B

Evaluate:

Solution:

We know that:

$$\begin{aligned} {}^nC_r &= \frac{n!}{(n-r)! \times r!} \\ \Rightarrow {}^{16}C_{13} &= \frac{16!}{(16-13)! \times 13!} \\ \Rightarrow {}^{16}C_{13} &= \frac{16!}{3! \times 13!} \\ \Rightarrow {}^{16}C_{13} &= \frac{16 \times 15 \times 14 \times 13!}{3! \times 13!} \\ \Rightarrow {}^{16}C_{13} &= \frac{16 \times 15 \times 14}{3!} \\ \Rightarrow {}^{16}C_{13} &= \frac{16 \times 15 \times 14}{3 \times 2 \times 1} \\ \Rightarrow {}^{16}C_{13} &= \frac{3360}{6} \\ \Rightarrow {}^{16}C_{13} &= 560 \end{aligned}$$

Ans: ${}^{16}C_{13} = 560$

Question: 1 C

Evaluate:

Solution:

We know that:

$$\begin{aligned} {}^nC_r &= \frac{n!}{(n-r)! \times r!} \\ \Rightarrow {}^{90}C_{88} &= \frac{90!}{(90-88)! \times 88!} \\ \Rightarrow {}^{90}C_{88} &= \frac{90!}{2! \times 88!} \\ \Rightarrow {}^{90}C_{88} &= \frac{90 \times 89 \times 88!}{2! \times 88!} \\ \Rightarrow {}^{90}C_{88} &= \frac{90 \times 89}{2!} \\ \Rightarrow {}^{90}C_{88} &= \frac{90 \times 89}{2 \times 1} \\ \Rightarrow {}^{90}C_{88} &= \frac{8010}{2} \\ \Rightarrow {}^{90}C_{88} &= 4005 \end{aligned}$$

$$\text{Ans: } {}^{90}C_{88} = 4005$$

Question: 1 D

We know that:

$$\begin{aligned} {}^nC_r &= \frac{n!}{(n-r)! \times r!} \\ \Rightarrow {}^{71}C_{71} &= \frac{71!}{(71-71)! \times 71!} \\ \Rightarrow {}^{71}C_{71} &= \frac{1}{0!} \\ \Rightarrow {}^{71}C_{71} &= \frac{1}{1} \dots (0! = 1) \\ \Rightarrow {}^{71}C_{71} &= 1 \end{aligned}$$

$$\text{Ans: } {}^{71}C_{71} = 1$$

Question: 1 E

Evaluate:

Solution:

We know that:

$$\begin{aligned} {}^nC_r &= \frac{n!}{(n-r)! \times r!} \\ \Rightarrow {}^{n+1}C_n &= \frac{(n+1)!}{(n+1-n)! \times n!} \\ \Rightarrow {}^{n+1}C_n &= \frac{(n+1)!}{1! \times n!} \\ \Rightarrow {}^{n+1}C_n &= \frac{(n+1)!}{1 \times n!} \dots (1! = 1) \\ \Rightarrow {}^{n+1}C_n &= \frac{(n+1) \times n!}{1 \times n!} \\ \Rightarrow {}^{n+1}C_n &= \frac{(n+1)}{1} \\ \Rightarrow {}^{n+1}C_n &= n+1 \end{aligned}$$

$$\text{Ans: } {}^{n+1}C_n = n+1$$

Question: 1 F

Evaluate:

Solution:

We know that:

$$\sum_{r=1}^n \binom{n}{r} = 2^n - \binom{n}{0}$$

$$\Rightarrow \sum_{r=1}^6 \binom{6}{r} = 2^6 - \binom{6}{0} \Rightarrow \sum_{r=1}^6 \binom{6}{r} = 64 - 1$$

$$\Rightarrow \sum_{r=1}^6 \binom{6}{r} = 63$$

$$\text{Ans: } \sum_{r=1}^6 \binom{6}{r} = 63$$

Question: 2

Verify that:

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Solution:

$$(i) \text{ Given: } {}^{15}C_8 + {}^{15}C_9 - {}^{15}C_6 - {}^{15}C_7$$

$$\text{To prove: } {}^{15}C_8 + {}^{15}C_9 - {}^{15}C_6 - {}^{15}C_7 = 0$$

We know that:

$${}^nC_r = {}^nC_{n-r}$$

$$\Rightarrow {}^{15}C_8 = {}^{15}C_7 \text{ \& } {}^{15}C_9 = {}^{15}C_6$$

$$\Rightarrow {}^{15}C_8 + {}^{15}C_9 - {}^{15}C_6 - {}^{15}C_7 = {}^{15}C_8 + {}^{15}C_9 - {}^{15}C_9 - {}^{15}C_8 = 0$$

$$\text{Hence, proved that } {}^{15}C_8 + {}^{15}C_9 - {}^{15}C_6 - {}^{15}C_7 = 0$$

$$(ii) \text{ We know that: } {}^nC_r + {}^nC_{r-1} = {}^{n+1}C_r$$

Therefore, $n = 10$ and $r = 4$

$$\text{L.H.S} = {}^{10}C_4 + {}^{10}C_3 = {}^{11}C_4$$

Hence, proved.

Question: 3

(i) If n

Solution:

$$(i) \text{ Given: } {}^nC_7 = {}^nC_5$$

To find: $n = ?$

We know that:

$${}^nC_r = {}^nC_{n-r}$$

$$\Rightarrow {}^nC_7 = {}^nC_{n-7}$$

$$\Rightarrow {}^nC_{n-7} = {}^nC_5$$

$$\Rightarrow n-7=5$$

$$\Rightarrow n=7+5=12$$

$$\text{Ans: } n=12$$

$$\text{(ii) Given: } {}^nC_{14} = {}^nC_{16}$$

$$\text{To find: } {}^nC_{28}=?$$

We know that:

$${}^nC_r = {}^nC_{n-r}$$

$$\Rightarrow {}^nC_{14} = {}^nC_{n-14}$$

$$\Rightarrow {}^nC_{n-14} = {}^nC_{16}$$

$$\Rightarrow n-14=16$$

$$\Rightarrow n=16+14=30$$

$$\Rightarrow n=30$$

So,

$${}^nC_{28} = {}^{30}C_{28}$$

$$\Rightarrow {}^{30}C_{28} = \frac{30!}{(30-28)! \times 28!}$$

$$\Rightarrow {}^{30}C_{28} = \frac{30!}{2! \times 28!}$$

$$\Rightarrow {}^{30}C_{28} = \frac{30 \times 29 \times 28!}{2! \times 28!}$$

$$\Rightarrow {}^{30}C_{28} = \frac{30 \times 29}{2!}$$

$$\Rightarrow {}^{30}C_{28} = \frac{30 \times 29}{2 \times 1}$$

$$\Rightarrow {}^{30}C_{28} = 435$$

$$\text{Ans: } {}^{30}C_{28} = 435$$

$$\text{(iii) Given: } {}^nC_{16} = {}^nC_{14}$$

$$\text{To find: } {}^nC_{27}=?$$

We know that:

$${}^nC_r = {}^nC_{n-r}$$

$$\Rightarrow {}^nC_{14} = {}^nC_{n-14}$$

$$\Rightarrow {}^nC_{n-14} = {}^nC_{16}$$

$$\Rightarrow n-14=16$$

$$\Rightarrow n=16+14=30$$

$$\Rightarrow n=30$$

So,

$${}^nC_{27} = {}^{30}C_{27}$$

$$\Rightarrow {}^{30}C_{27} = \frac{30!}{(30-27)! \times 27!}$$

$$\Rightarrow {}^{30}C_{27} = \frac{30!}{3! \times 27!}$$

$$\Rightarrow {}^{30}C_{27} = \frac{30 \times 29 \times 28 \times 27!}{3! \times 27!}$$

$$\Rightarrow {}^{30}C_{27} = \frac{30 \times 29 \times 28}{3!}$$

$$\Rightarrow {}^{30}C_{27} = \frac{30 \times 29 \times 28}{3 \times 2 \times 1}$$

$$\Rightarrow {}^{30}C_{27} = 4060$$

$$\text{Ans: } {}^{30}C_{27} = 4060$$

Question: 4

(i) If ${}^{20}C_r = {}^{20}C_{r+6}$

Solution:

$$\text{Given: } {}^{20}C_r = {}^{20}C_{r+6}$$

To find: $r = ?$

We know that:

$${}^nC_r = {}^nC_{n-r}$$

$$\Rightarrow {}^{20}C_{r+6} = {}^{20}C_{20-(r+6)}$$

$$\Rightarrow {}^{20}C_{r+6} = {}^{20}C_{20-r-6} = {}^{20}C_{14-r}$$

$$\Rightarrow {}^{20}C_{14-r} = {}^{20}C_r$$

$$\Rightarrow 14-r = r$$

$$\Rightarrow 2r = 14$$

$$\Rightarrow r = \frac{14}{2} = 7$$

$$\text{Ans: } r = 7$$

$$\text{ii) Given: } {}^{18}C_r = {}^{18}C_{r+2}$$

To find: $rC_5 = ?$

We know that:

$${}^nC_r = {}^nC_{n-r}$$

$$\Rightarrow {}^{18}C_{r+2} = {}^{18}C_{18-(r+2)}$$

$$\Rightarrow {}^{18}C_{r+2} = {}^{18}C_{18-r-2} = {}^{18}C_{16-r}$$

$$\Rightarrow {}^{18}C_{16-r} = {}^{18}C_r$$

$$\Rightarrow 16-r = r$$

$$\Rightarrow 2r = 16$$

$$\Rightarrow r = \frac{16}{2} = 8$$

So,

$$rC_5 = {}^8C_5$$

$$\Rightarrow {}^8C_5 = \frac{8!}{(8-5)! \times 5!}$$

$$\Rightarrow {}^8C_5 = \frac{8!}{3! \times 5!}$$

$$\Rightarrow {}^8C_5 = \frac{8 \times 7 \times 6 \times 5!}{3! \times 5!}$$

$$\Rightarrow {}^8C_5 = \frac{8 \times 7 \times 6}{3!}$$

$$\Rightarrow {}^8C_5 = \frac{8 \times 7 \times 6}{3 \times 2 \times 1}$$

$$\Rightarrow {}^8C_5 = 56$$

$$\text{Ans: } {}^8C_5 = 56$$

Question: 5

If ${}^nC_r <$

Solution:

$$\text{Given: } {}^nC_{r-1} = {}^nC_{3r}$$

To find: $r = ?$

We know that:

$${}^nC_r = {}^nC_{n-r}$$

$$\Rightarrow {}^nC_{r-1} = {}^nC_{n-(r-1)}$$

$$\Rightarrow {}^nC_{r-1} = {}^nC_{n-r+1}$$

$$\Rightarrow {}^nC_{n-r+1} = {}^nC_{3r}$$

$$\Rightarrow n-r+1 = 3r$$

$$\Rightarrow 4r = n+1$$

$$\Rightarrow r = \frac{n+1}{4}$$

$$\text{Ans: } r = \frac{n+1}{4}$$

Question: 6

If $2^n C$

Solution:

$$\text{Given: } {}^{2n}C_3 : {}^nC_3 = 12 : 1$$

To find: $n = ?$

$${}^{2n}C_3 : {}^nC_3 = 12 : 1$$

$$\Rightarrow \frac{{}^{(2n)}C_3}{{}^nC_3} = \frac{12}{1}$$

$$\Rightarrow \frac{\frac{(2n)!}{(2n-3)!3!}}{\frac{n!}{(n-3)!3!}} = \frac{12}{1}$$

$$\Rightarrow \frac{(2n)!(n-3)!3!}{(2n-3)!3!n!} = \frac{12}{1}$$

$$\Rightarrow \frac{(2n) \times (2n-1) \times (2n-2) \times (2n-3)! (n-3)!}{(2n-3)! n \times (n-1) \times (n-2) \times (n-3)!} = \frac{12}{1}$$

$$\Rightarrow \frac{(2n) \times (2n-1) \times (2n-2)}{n \times (n-1) \times (n-2)} = \frac{12}{1}$$

$$\Rightarrow \frac{n \times (2n-1) \times (n-1)}{n \times (n-1) \times (n-2)} = \frac{12}{4}$$

$$\Rightarrow \frac{(2n-1)}{(n-2)} = 3$$

$$\Rightarrow 2n-1=3(n-2)$$

$$\Rightarrow 2n-1=3n-6$$

$$\Rightarrow n=6-1=5$$

Ans:n=5

Question: 7

If ${}^{15}C$

Solution:

Given: ${}^{15}C_r : {}^{15}C_{r-1} = 11 : 5$

To find: r=?

$${}^{15}C_r : {}^{15}C_{r-1} = 11 : 5$$

$$\Rightarrow \frac{{}^{15}C_r}{{}^{15}C_{r-1}} = \frac{11}{5}$$

$$\Rightarrow \frac{\frac{15!}{(15-r)!r!}}{\frac{15!}{(16-r)!(r-1)!}} = \frac{11}{5}$$

$$\Rightarrow \frac{15!(16-r)!(r-1)!}{(15-r)!r!15!} = \frac{11}{5}$$

$$\Rightarrow \frac{(16-r) \times (15-r)! \times (r-1)!}{(15-r)! \times r \times (r-1)!} = \frac{11}{5}$$

$$\Rightarrow \frac{16-r}{r} = \frac{11}{5}$$

$$\Rightarrow 5 \times (16-r) = 11r$$

$$\Rightarrow 80 - 5r = 11r$$

$$\Rightarrow 16r = 80$$

$$\Rightarrow r = \frac{80}{16}$$

$$\Rightarrow r = 5$$

Ans:r=5

Question: 8

If ${}^nP <$

Solution:

Given: ${}^nP_r = 840$ and ${}^nC_r = 35$

To find: r=?

We know that:

$${}^nC_r = \frac{n!}{(n-r)!r!}$$

and

$${}^nP_r = \frac{n!}{(n-r)!}$$

$$\Rightarrow {}^nP_r = {}^nC_r \times r!$$

$$\Rightarrow 840 = 35 \times r!$$

$$\Rightarrow r! = \frac{840}{35} = 24$$

$$\Rightarrow r! = 4!$$

$$\Rightarrow r = 4$$

$$\text{Ans: } r = 4$$

Question: 9

If ${}^nC <$

Solution:

Given, ${}^nC_{r-1} = 36$, ${}^nC_r = 84$ and ${}^nC_{r+1} = 126$

To find: $r = ?$

$$\Rightarrow \frac{\binom{n}{r}}{\binom{n}{r-1}} = \frac{84}{36} = \frac{7}{3}$$

$$\Rightarrow \frac{\frac{n!}{(n-r)! \times r!}}{\frac{n!}{(n-r+1)! \times (r-1)!}} = \frac{7}{3}$$

$$\Rightarrow \frac{(n-r+1)}{r} = \frac{7}{3}$$

$$\Rightarrow 3(n-r+1) = 7r$$

$$\Rightarrow 3n - 10r = -3 \dots (1)$$

$$\Rightarrow \frac{\binom{n}{r+1}}{\binom{n}{r}} = \frac{126}{84} = \frac{3}{2}$$

$$\Rightarrow \frac{\frac{n!}{(n-r-1)! \times (r+1)!}}{\frac{n!}{(n-r)! \times r!}} = \frac{3}{2}$$

$$\Rightarrow \frac{(n-r)}{(r+1)} = \frac{3}{2}$$

$$\Rightarrow 2(n-r) = 3(r+1)$$

$$\Rightarrow 2n - 5r = 3 \dots (2)$$

From equations 1 & 2 we get

$$n = 9 \text{ \& } r = 3$$

$$\text{Ans: } r = 3$$

Question: 10

If $n+1$

Solution:

Given: ${}^{n+1}C_{r+1} : {}^nC_r = 11 : 6$ and ${}^nC_r : {}^{n-1}C_{r-1} = 6 : 3$

To Find: n & r

We use this property in this question:

$$\binom{n}{r} = \frac{n}{r} \times \binom{n-1}{r-1}$$

$${}^{n+1}C_{r+1} : {}^nC_r = 11 : 6$$

$$\Rightarrow \frac{\binom{n+1}{r+1}}{\binom{n}{r}} = \frac{11}{6}$$

$$\Rightarrow \frac{\binom{n+1}{r+1} \times \binom{n}{r}}{\binom{n}{r}} = \frac{11}{6}$$

$$\Rightarrow \frac{(n+1)}{(r+1)} = \frac{11}{6}$$

$$\Rightarrow 6(n+1) = 11(r+1)$$

$$\Rightarrow 6n+6 = 11r+11$$

$$\Rightarrow 6n-11r = 5 \dots (1)$$

$${}^nC_r : {}^{n-1}C_{r-1} = 6 : 3$$

$$\Rightarrow \frac{\binom{n}{r}}{\binom{n-1}{r-1}} = \frac{6}{3} = 2$$

$$\Rightarrow \frac{\frac{n}{r} \times \binom{n-1}{r-1}}{\binom{n-1}{r-1}} = 2$$

$$\Rightarrow \frac{n}{r} = 2$$

$$\Rightarrow n = 2r \dots (2)$$

Using equations 1 & 2 we get

$$\Rightarrow 6(2r) - 11r = 5$$

$$\Rightarrow 12r - 11r = 5$$

$$\Rightarrow r = 5$$

$$\Rightarrow n = 2 \times 5$$

$$\Rightarrow n = 10$$

$$\text{Ans: } n = 10 \text{ \& } r = 5$$

Question: 11

How many differen

Solution:

Condition: Each student has an equal chance of getting selected.

Imagine selecting the teammates one at a time. There are 15 ways of selecting the first teammate, 14 ways of selecting the second, 13 ways of selecting the third teammate, and so on down to 5 ways of selecting the eleventh teammate.

This is a problem of combination

$$\Rightarrow n = 15 \text{ \& } r = 11$$

$$\Rightarrow {}^nC_r = {}^{15}C_{11}$$

$$\Rightarrow {}^{15}C_{11} = \frac{15!}{(15-11)! \times 11!}$$

$$\Rightarrow {}^{15}C_{11} = \frac{15!}{4! \times 11!}$$

$$\Rightarrow {}^{15}C_{11} = \frac{15 \times 14 \times 13 \times 12 \times 11!}{4! \times 11!}$$

$$\Rightarrow {}^{15}C_{11} = \frac{15 \times 14 \times 13 \times 12}{4 \times 3 \times 2 \times 1}$$

$$\Rightarrow {}^{15}C_{11} = 1365$$

Ans: There can be 1365 different ways of choosing 11 players from a squad of 15.

This means there can be 1365 eleven-member teams formed with 15 players.

Question: 12

If there are 12 p

Solution:

With 12 people , we need to choose a subset of two different people where order does not matter. Also, we need to choose all such subsets because each person is shaking hands with everyone else exactly once. The number of ways is: nC_r

Where: $n=12$ & $r=2$

$${}^nC_r = {}^{12}C_2$$

$$\Rightarrow {}^{12}C_2 = \frac{12!}{(12-2)! \times 2!}$$

$$\Rightarrow {}^{15}C_{11} = \frac{12!}{10! \times 2!}$$

$$\Rightarrow {}^{15}C_{11} = \frac{12 \times 11 \times 10!}{10! \times 2!}$$

$$\Rightarrow {}^{15}C_{11} = \frac{12 \times 11}{2 \times 1}$$

$$\Rightarrow {}^{15}C_{11} = 66$$

Ans: In total 66 handshakes are possible, if there are 12 persons in a party and if each two of them shake hands with each other

Question: 13

How many chords c

Solution:

Number of points = 21

$$\Rightarrow n = 21$$

A chord connects circle at two points.

$$\Rightarrow r = 2$$

\Rightarrow Number of chords from 21 points = nC_r

$$\Rightarrow {}^nC_r = {}^{21}C_2$$

$$\Rightarrow {}^{21}C_2 = \frac{21!}{(21-2)! \times 2!}$$

$$\Rightarrow {}^{21}C_2 = \frac{21!}{19! \times 2!}$$

$$\Rightarrow {}^{21}C_2 = \frac{21 \times 20 \times 19!}{19! \times 2!}$$

$$\Rightarrow {}^{21}C_2 = \frac{21 \times 20}{2 \times 1}$$

$$\Rightarrow {}^{21}C_2 = 210 \text{ chords.}$$

Ans: 210 chords can be drawn through 21 points on a circle.

Question: 14

From a class of 2

Solution:

This is a case of combination:

Here,

$$n = 25$$

$$r=4$$

$$\Rightarrow {}^nC_r = {}^{25}C_4$$

$$\Rightarrow {}^{25}C_4 = \frac{25!}{(25-4)! \times 4!}$$

$$\Rightarrow {}^{25}C_4 = \frac{25!}{21! \times 4!}$$

$$\Rightarrow {}^{25}C_4 = \frac{25 \times 24 \times 23 \times 22 \times 21!}{21! \times 4!}$$

$$\Rightarrow {}^{25}C_4 = \frac{25 \times 24 \times 23 \times 22}{4 \times 3 \times 2 \times 1}$$

$$\Rightarrow {}^{25}C_4 = 12650 \text{ possible ways.}$$

Ans: In 12650 ways, from a class of 25 students, 4 can be chosen for a competition.

Exercise : 9B

Question: 1

In how many ways

Solution:

As there are 10 sportsmen out of which 5 are to be selected.

5 sportsmen can be selected out of 10 in ${}^{10}C_5$ ways.

$$\text{Applying } {}^nC_r = \frac{n!}{r!(n-r)!}$$

We get,

$$\Rightarrow {}^{10}C_5 = \frac{10!}{5!(10-5)!}$$

$$\Rightarrow 252 \text{ ways}$$

Hence, there are 252 ways of selecting 5 sportsmen from 10 sportsmen.

Question: 2

A bag contains 5

Solution:

There are 5 black and 6 red balls. So,

The number of ways of selecting 2 black balls from 5 black balls is 5C_2 , and number of ways of selecting 3 red balls from 6 red balls is 6C_3 .

Thus using the multiplication principle, the total number of ways will be

$$\Rightarrow {}^5C_2 \times {}^6C_3 \text{ ways.}$$

$$\text{Applying } {}^nC_r = \frac{n!}{r!(n-r)!}$$

$$\Rightarrow 200 \text{ ways}$$

Thus, the total number of ways in which 2 black and 3 red balls can be selected is 200.

Question: 3

Find the number of

Solution:

Total number of red balls = 6

Total number of white balls = 5

Total number of blue balls = 4

No. of ways of selecting 3 balls which is red = 6C_3

No. of ways of selecting 3 balls which is white = 5C_3

No. of ways of selecting 3 balls which is blue = 4C_3

Thus, by Multiplication principle, the total number of ways would be,

$$\Rightarrow {}^6C_3 \times {}^5C_3 \times {}^4C_3$$

Applying formula, ${}^nC_r = \frac{n!}{r!(n-r)!}$, we get

$$\Rightarrow 800 \text{ ways}$$

Thus, the number of ways of selecting 9 balls from 6 red balls, 5 white balls and 4 blue balls if each selection consists of 3 balls of each colour would be 800.

Question: 4

How many differen

Solution:

Number of ways of choosing 5 boys out of 20 boys = ${}^{20}C_5$

$$= \frac{20!}{5! \times (20-5)!}$$

$$= \frac{20!}{5! \times 15!}$$

$$= 19 \times 17 \times 16 \times 3 = 15,504$$

Number of ways of choosing 3 girls out of 10 girls = ${}^{10}C_3$

$$= \frac{10!}{3! \times (10-3)!}$$

$$= \frac{10!}{3! \times 7!}$$

$$= 15 \times 8 = 120$$

$$\text{Total number of ways} = 120 \times 15,504 = 1,860,480$$

OR

$$\text{Total number of ways} = {}^{20}C_5 \times {}^{10}C_3$$

Question: 5

In How many ways

Solution:

Since every student needs to choose 5 courses out of which 2 are compulsory. So, the student needs to choose 3 subjects out of 7.

No. of ways for choosing 3 subjects out of 7 is 7C_3

Applying formula, ${}^nC_r = \frac{n!}{r!(n-r)!}$, we get

$$= 35 \text{ ways.}$$

Question: 6

A sports team of

Solution:

There are 20 students in each classes and there is need of at least 5 students in each class to form a team of team of 11.

Now,

There are two ways in which the selection can be possible

1. Selecting 5 from XI and 6 from XII
2. Selecting 6 from XI and 5 from XII

Now, considering first case ,

No. of ways in selection of 5 students from 20 in class XI = ${}^{20}C_5$

No. of ways in selection of 6 students from 20 in class XII = ${}^{20}C_6$

By multiplication principle total no. of ways in first case is

$$= {}^{20}C_5 \times {}^{20}C_6$$

Now, considering second case,

No. of ways in selection of 6 students from 20 in class XI = ${}^{20}C_6$

No. of ways in selection of 5 students from 20 in class XII = ${}^{20}C_5$

By multiplication principle total no. of ways in second case is

$$= {}^{20}C_6 \times {}^{20}C_5$$

Now the total no. of ways will be the addition of both the cases

$$= {}^{20}C_5 \times {}^{20}C_6 + {}^{20}C_6 \times {}^{20}C_5$$

$$= 2 \times {}^{20}C_6 \times {}^{20}C_5$$

Thus these are the ways by which A sports team of 11 students is to be constituted

Question: 7

From 4 officers a

Solution:

The team of 6 has to be chosen from 4 officers and 8 clerks. There are some restrictions which are

1. To include exactly one officer

In this case ,

One officer will be chosen from 4 in 4C_1 ways

Therefore, 5 will be chosen form 8 clerks in 8C_5 ways.

Thus by multiplication principle , we get

Total no. of ways in 1 case is ${}^4C_1 \times {}^8C_5$.

2. To include at least one officer

In this case, there will be subcases for selection which is as follows.

- (i) One officer and 5 clerks
- (ii) Two officers and 4 clerks
- (iii) Three officers and 3 clerks
- (iv) Four officers and 2 clerks

Or

The required case of at least one officer would be

= Total cases - cases having only clerks

Now,

The total case would be choosing 6 out of 12 in $^{12}C_6$ ways.

And cases that would have only clerks would be i.e. selecting 6 from 8 clerks in 8C_6 ways.

$\Rightarrow ^{12}C_6 - ^8C_6$ ways.

Applying ${}^nC_r = \frac{n!}{r!(n-r)!}$

$\Rightarrow 924 - 28$ ways

= 896 ways

Question: 8

A cricket team of

Solution:

There is a cricket team of 11 players is to be selected from 16 players, which must include 3 bowlers and a wicketkeeper.

\Rightarrow there will be a team of 7 batsmen, 1 wicketkeeper and 3 bowlers.

\Rightarrow there are 5 bowlers from which 3 is to be selected in 5C_3 ways

\Rightarrow there are two wicketkeepers out of which 1 is to be selected in 2C_1

\Rightarrow hence, from 9 players left 7 is to be selected from that in $^{11}C_7$ ways.

\Rightarrow by Multiplication principle, we get

= $^5C_3 \times ^2C_1 \times ^9C_7$

Applying ${}^nC_r = \frac{n!}{r!(n-r)!}$

= 720 ways

Question: 9

In how many ways

Solution:

A team of 11 players is to be made from 25 players.

\Rightarrow selecting 5 batsmen from 10 in $^{10}C_5$ ways.

\Rightarrow selecting 3 all-rounders from 5 in 5C_3 ways.

\Rightarrow selecting 2 bowlers from 8 in 8C_2 ways.

\Rightarrow selecting 1 wicketkeeper from 2 in 2C_1 ways.

Thus, by the multiplication principle, we get

= $^{10}C_5 \times ^8C_2 \times ^5C_3 \times ^2C_1$ ways

Applying ${}^nC_r = \frac{n!}{r!(n-r)!}$

= 141120 ways

Question: 10

A question paper

Solution:

The question paper has two sets each containing 10 questions . so the student has to choose 8 from part A and 5 from part B.

⇒choosing 8 questions from 10 of part A in $^{10}C_8$

⇒ choosing 5 questions from 10 of part B in $^{10}C_5$

⇒by Multiplication principle, we get

⇒total no. of ways in which he can attempt the paper is $^{10}C_8 \times ^{10}C_5$

Applying $^nC_r = \frac{n!}{r!(n-r)!}$

= 11340 ways

Question: 11

In an examination

Solution:

A student has to answer 4 questions out of 5 in which he is compelled to do the 1 and 2 questions compulsory. So he has to attempt 2 questions from 3 of his choice.

Choosing 2 questions from 3 will be in 3C_2 ways.

Applying $^nC_r = \frac{n!}{r!(n-r)!}$

= 3 ways.

Question: 12

In an examination

Solution:

There are total 13 questions out of which 10 is to be answered .The student can answer in the following ways:

⇒ 6 questions from part A and 4 from part B

⇒ 5 questions from part A and 5 from part B

⇒ 4 questions from part A and 6 from part B

⇒total ways in the 1st case are $^6C_6 \times ^7C_4$

⇒ total ways in the 2nd case are $^6C_5 \times ^7C_5$

⇒ total ways in the 3rd case are $^6C_4 \times ^7C_6$

thus the total of the all the cases would be total ways in the 1st case is $= ^6C_6 \times ^7C_4 + ^6C_5 \times ^7C_5 + ^6C_4 \times ^7C_6$

Applying $^nC_r = \frac{n!}{r!(n-r)!}$

= 266 ways.

Question: 13

In an examination

Solution:

There are total 13 questions out of which 10 is to be answered .The student can answer in the following ways:

⇒ 3 questions from part A and 4 from part B

⇒ 4 questions from part A and 3 from part B

⇒ 5 questions from part A and 2 from part B

⇒ 2 questions from part A and 5 from part B

⇒ total ways in the 1st case are ${}^6C_3 \times {}^6C_4$

⇒ total ways in the 2nd case are ${}^6C_4 \times {}^6C_3$

⇒ total ways in the 3rd case are ${}^6C_5 \times {}^6C_2$

⇒ total ways in the 4th case are ${}^6C_2 \times {}^6C_5$

thus the total of all the cases would be $= {}^6C_4 \times {}^6C_3 + {}^6C_3 \times {}^6C_4 + {}^6C_5 \times {}^6C_2 + {}^6C_2 \times {}^6C_5$

Applying ${}^nC_r = \frac{n!}{r!(n-r)!}$

= 780 ways.

Question: 14

Out of 6 teachers

Solution:

Since the committee of 11 is to be formed from 6 teachers and 8 students.

(i) Forming a committee with exactly 4 teachers

Choosing 4 teachers out of 6 in 6C_4 ways.

Remaining 7 from 8 students in 8C_7 ways.

Thus, total ways in (i) are ${}^6C_4 \times {}^8C_7$ ways.

(ii) The number of ways in this case is

1. 4 teachers and 7 students

2. 5 teachers and 6 students

3. 6 teachers and 5 students

$= {}^6C_4 \times {}^8C_7 + {}^6C_5 \times {}^8C_6 + {}^6C_6 \times {}^8C_5$

Applying ${}^nC_r = \frac{n!}{r!(n-r)!}$

= 344 ways

Question: 15

A committee of 7

Solution:

A committee of 7 has to be formed from 9 boys and 4 girls.

I. Exactly 3 girls: If there are exactly 3 girls in the committee, then there must be 4 boys, and the ways in which they can be chosen is

$= {}^4C_3 \times {}^9C_4$

= 504 ways

II. At least 3 girls: Here the possibilities are

(i) 3 girls and 4 boys and

(ii) 4 girls and 3 boys.

the number of ways they can be selected

$$= {}^4C_3 \times {}^9C_4 + {}^4C_4 \times {}^9C_3$$

$$= 588$$

III. At most 3 girls:

(i) 7 boys but no girls

(ii) 6 boys and 1 girl

(iii) 5 boys and 2 girls &

(iv) 4 boys and 3 girls.

And the number of their selection is

$$= {}^4C_3 \times {}^9C_4 + {}^4C_2 \times {}^9C_5 + {}^4C_1 \times {}^9C_6 + {}^4C_0 \times {}^9C_7$$

$$= 1584 \text{ ways.}$$

Question: 16

A committee of th

Solution:

Total number of persons = 2 + 3 = 5

Now, committee consist of 3 persons.

$$\text{Therefore, total number of ways} = {}^5C_3 = \frac{5!}{3! \times (5-3)!} = 5 \times 2 = 10$$

Now,

When 1 man is selected, total ways = 2C_1

When 2 women are selected, total ways = 3C_2

Total number of ways when 1 man and 2 women are selected = ${}^2C_1 \times {}^3C_2 = 2 \times 3 = 6$

Question: 17

A committee of 5

Solution:

Since the committee of 5 is to be formed from 6 gents and 4 ladies.

(i) Forming a committee with at least 2 ladies

Here the possibilities are

(i) 2 ladies and 3 gents

(ii) 3 ladies and 2 gents

(iii) 4 ladies and 1 gent

the number of ways they can be selected

$$= {}^4C_2 \times {}^6C_3 + {}^4C_3 \times {}^6C_2 + {}^4C_4 \times {}^6C_1$$

$$\text{Applying } {}^nC_r = \frac{n!}{r!(n-r)!}$$

$$= 186 \text{ ways}$$

(ii) The number of ways in this case is

1. 0 ladies and 5 gents
2. 1 lady and 4 gents
3. 2 ladies and 3 gents.

The total ways are

$$= {}^4C_0 \times {}^6C_5 + {}^4C_1 \times {}^6C_4 + {}^4C_2 \times {}^6C_3$$

$$\text{Applying } {}^nC_r = \frac{n!}{r!(n-r)!}$$

$$= 186 \text{ ways.}$$

Question: 18

From a class of 1

Solution:

2 girls who won the prize last year are surely to be taken. So, we have to make a selection of 8 students out of 14 boys and 8 girls, choosing at least 4 boys and at least 2 girls.

Thus, we may choose:

(4 boys, 4 girls) or (5 boys, 3 girls) or (6 boys, 2 girls)

$$\text{Therefore, the required number of ways} = ({}^{14}C_4 \times {}^8C_4) + ({}^{14}C_5 \times {}^8C_3) + ({}^{14}C_6 \times {}^8C_2)$$

Question: 19

Find the number o

Solution:

Since there are 52 cards in a deck out of which 4 are king and others are non-kings.

So, the no. of ways are as follows:

1. 1 king and 4 non-king
2. 2 king and 3 non-king
3. 3 king and 2 non-king
4. 4 king and 1 non-king

So , total no. of ways are

$$= {}^4C_1 \times {}^{48}C_4 + {}^4C_2 \times {}^{48}C_3 + {}^4C_3 \times {}^{48}C_2 + {}^4C_4 \times {}^{48}C_1$$

$$\text{Applying } {}^nC_r = \frac{n!}{r!(n-r)!}$$

$$= 778320 + 103776 + 4512 + 48$$

$$= 886656 \text{ ways.}$$

Question: 20

Find the number o

Solution:

For a diagonal to be formed, 2 vertices are required. Thus in a polygon, there are 10 sides. And no. of lines can be formed are nC_2 , but in nC_2 the sides are also included. N of them is sides.

Thus the no. of diagonals are ${}^nC_2 - n$

(i) hexagon

$$n=6$$

$$\text{so no of diagonal is } {}^6C_2 - 6 = 9$$

(ii) decagon

$$n = 10$$

so no of diagonal is ${}^{10}C_2 - 10$

$$= 35$$

(iii) $N = 18$

so no of diagonal is ${}^{18}C_2 - 18$

$$= 135$$

Question: 21

How many triangle

Solution:

Total number of points on plane = 12

Triangles can be formed from these points = ${}^{12}C_3$

$$= 220$$

But 4 points are colinear, the number of triangles can be formed from these points

$$= {}^4C_3$$

$$= 4$$

We need to subtract 4 from 220 because in the formation of triangles from 4 colinear points are added there.

So no of triangle formed is = $220 - 4$

$$= 216$$

Question: 22

How many triangle

Solution:

Total number of sides in a decagon = 10

We know that number of vertices in triangle = 3

So, out of 10 vertices we have to choose 3 vertices.

Therefore,

$$\text{Total number of triangles in a decagon} = {}^{10}C_3 = \frac{10!}{3! \times (10-3)!} = \frac{10 \times 9 \times 8}{3 \times 2}$$

Total number of triangles = 120

Question: 23

How many differen

Solution:

Since there are 10 different books out of which 4 is to be selected .

(i) When there is no restriction

No. of ways in which 4 books be selected = ${}^{10}C_4$

$$= 210 \text{ ways}$$

(ii) two particular books are always selected

since two particular books are always selected, so ways of selecting 2 books from 8 are = 8C_2

ways

$$= 28 \text{ ways}$$

(iii) two particular books are never selected

since two particular books are never selected so , ways of selecting 4 books from 8 are $= {}^8C_4$ ways

$$= 70 \text{ ways}$$

Question: 24

How many differen

Solution:

The given no. is 3,5,7,11.

The no. of different products when two or more is taking= the no. of ways of taking the product of two no.+ the no. of ways of taking the product of three no. + the no. of ways of taking the product of four no.

$$= {}^4C_2 + {}^4C_3 + {}^4C_4$$

$$\text{Applying } {}^nC_r = \frac{n!}{r!(n-r)!}$$

$$= 6+4+1$$

$$= 11$$

Question: 25

Find the number o

Solution:

Since a committee is to be formed of 2 teachers and 3 students

(i) When a particular teacher is included

$$\text{No. of ways in which committee can be formed} = {}^9C_1 \times {}^{20}C_3$$

$$= 9720 \text{ ways}$$

(ii) a particular student is included

since a particular student is always selected so ways of selecting 2 teachers and 2 students from 10 and 19 respect. is $= {}^{10}C_2 \times {}^{19}C_2$ ways

$$= 7695 \text{ ways}$$

(iii) a particular student is excluded

since 1 particular student is excluded so , ways of selecting 2 teachers and 3 students from 10 and 19 respt. is $= {}^{10}C_2 \times {}^{19}C_3$ ways

$$= 43605 \text{ ways}$$

Question: 26

There are 18 poin

Solution:

A line is formed by joining two points.

$$\text{If the total number of points is 18, the total number of lines would be} = {}^{18}C_2$$

But 5 points are collinear, so the lines made by these points are the same and would be only 1.

Hence there is 1 common line joining the 5 collinear points.

As these 5 points are also included in 18 points so these must be subtracted from the total case ,

i.e. 5C_2 must be subtracted from ${}^{18}C_2$.

Finally, the number of straight line = ${}^{18}C_2 - {}^5C_2 + 1$

= 144 lines

Exercise : 9C

Question: 1

Out of 12 consona

Solution:

3 consonants out of 12 consonants can be chosen in ${}^{12}C_3$ ways. 2 vowels out of 5 vowels can be chosen in 5C_2 ways. And also 5 letters can be written in 5! Ways. Therefore, the number of words can be formed is $({}^{12}C_3 \times {}^5C_2 \times 5!) = 264000$.

Question: 2

How many words, e

Solution:

In the word 'INVOLUTE' there are 4 vowels, 'I', 'O', 'U' and 'E' and there are 4 consonants, 'N', 'V', 'L' and 'T'. 3 vowels out of 4 vowels can be chosen in 4C_3 ways. 2 consonants out of 4 consonants can be chosen in 4C_2 ways. Length of the formed words will be $(3 + 2) = 5$. So, the 5 letters can be written in 5! Ways. Therefore, the total number of words can be formed is $= ({}^4C_3 \times {}^4C_2 \times 5!) = 2880$.

Question: 3

The English alpha

Solution:

2 consonants out of 21 consonants can be chosen in ${}^{21}C_2$ ways. 3 vowels out of 5 vowels can be chosen in 5C_3 ways. Length of the word is $= (2 + 3) = 5$ And also 5 letters can be written in 5! Ways. Therefore, the number of words can be formed is $= ({}^{21}C_2 \times {}^5C_3 \times 5!) = 252000$.

Question: 4

In how many ways

Solution:

The seating arrangement would be like this: B G B G B G B G So, 4 girls can seat among the four places. Number of ways they can seat is $= {}^4P_4 = 24$ Boys have to seat among the 'B' areas. So, there are 5 seats available for 3 boys. The number of ways the 3 boys can seat among the 5 places is $= {}^5P_3 = 60$ Therefore, the total number of ways they can seat in this manner is $= (24 \times 60) = 1440$.

Question: 5

How many words, w

Solution:

There are 6 letters in the word 'MONDAY', and there is no letter repeating. (i) 4 letters are used at first. 4 letters can sit in different ways. So, here permutation is to be used. So, the number of words that can be formed $= {}^6P_4 = 360$. [Answer(i)] (ii) Now all the letters are used. Therefore, the number of words can be formed is $= 6! = 720$ [Answer(ii)] (iii) Now the first letter is a vowel. There are 2 vowels in the word 'MONDAY', 'O' and 'A'. Let's take 'O' as the first letter. Then we can place the 5 letters among the 5 places. So, taking 'O' as the first letter, a number of words can be formed is $= 5! = 120$. Similarly, taking 'A' as the first letter, a number of words can be formed $= 5! = 120$. So, the total number of words can be formed taking first letter a vowel is $= (120 + 120) = 240$. [Answer(iii)]

Exercise : 9D

Question: 1

If ${}^{20}C$

Solution:

Given: ${}^{20}C_r = {}^{20}C_{r-10}$ Need to find: Value of ${}^{17}C_r$ We know, one of the property of combination is: If ${}^nC_r = {}^nC_t$, then, (i) $r = t$ OR (ii) $r + t = n$ We can't apply the property (i) here. So we are going to use property (ii) ${}^{20}C_r = {}^{20}C_{r-10}$ By the property (ii), $\Rightarrow r + r - 10 = 20 \Rightarrow 2r = 30 \Rightarrow r = 15$ Therefore, ${}^{17}C_{15} = 136$.

Question: 2

If ${}^{20}C$

Solution:

Given: ${}^{20}C_{r+1} = {}^{20}C_{r-10}$ Need to find: Value of ${}^{10}C_r$ We know, one of the property of combination is: If ${}^nC_r = {}^nC_t$, then, (i) $r = t$ OR (ii) $r + t = n$ We can't apply the property (i) here. So we are going to use property (ii) ${}^{20}C_{r+1} = {}^{20}C_{r-10}$ By the property (ii), $\Rightarrow r + 1 + r - 10 = 20 \Rightarrow 2r = 29 \Rightarrow r = 14.5$ We need to find out the value of ${}^{10}C_r$. But here r can't be a rational number. Therefore the value of ${}^{10}C_r$ can't be find out.

Question: 3

If ${}^nC <$

Solution:

Given: ${}^nC_{r+1} = {}^nC_8$ Need to find: Value of ${}^{22}C_n$ We know, one of the property of combination is: If ${}^nC_r = {}^nC_t$, then, (i) $r = t$ OR (ii) $r + t = n$ We are going to use property (i) ${}^nC_{r+1} = {}^nC_8$ By the property (i), $\Rightarrow r + 1 = 8 \Rightarrow r = 7$ Now we are going to use property (ii) $\Rightarrow n = 8 + 7 + 1 = 16$ Therefore, ${}^{22}C_n = {}^{22}C_{16} = 74613$.

Question: 4

If ${}^{35}C$

Solution:

Given: ${}^{35}C_{n+7} = {}^{35}C_{4n-2}$ Need to find: Value of n We know, one of the property of combination is: If ${}^nC_r = {}^nC_t$, then, (i) $r = t$ OR (ii) $r + t = n$ Applying property (i) we get, $\Rightarrow n + 7 = 4n - 2 \Rightarrow 3n = 9 \Rightarrow n = 3$ Applying property (ii) we get, $\Rightarrow n + 7 + 4n - 2 = 35 \Rightarrow 5n = 30 \Rightarrow n = 6$ Therefore, the value of n is either 3 or 6.

Question: 5

Find the values o

Solution:

$$(i) {}^{200}C_{198} = \frac{200!}{198!(200-198)!} = \frac{200!}{198!2!} = \frac{200 \times 199}{2!} = 100 \times 199 = 19900 \quad (ii) {}^{76}C_0 = \frac{76!}{0!76!} = 1 \quad [\text{As } 0! = 1] \quad (iii)$$

$${}^{15}C_{15} = \frac{15!}{15!0!} = 1$$

Question: 6

If ${}^mC <$

Solution:

$$\text{Given: } {}^mC_1 = {}^nC_2 \text{ Need to prove: } m = \frac{1}{2}n(n-1) \quad {}^mC_1 = {}^nC_2 \Rightarrow \frac{m!}{1!(m-1)!} = \frac{n!}{2!(n-2)!} \Rightarrow$$

$$\frac{m(m-1)!}{(m-1)!} = \frac{1}{2} \frac{n(n-1)(n-2)!}{(n-2)!} \Rightarrow m = \frac{1}{2}n(n-1) \quad [\text{Proved}]$$

Question: 7

Write the value o

Solution:

$$\Rightarrow {}^5C_1 + {}^5C_2 + {}^5C_3 + {}^5C_4 + {}^5C_5 = {}^6C_2 + {}^6C_4 + 1 \text{ [As } {}^5C_5 = 1] = 15 + 15 + 1 = 31$$

Question: 8

If $n+1$

Solution:

$$\text{Given: } {}^{n+1}C_3 = 2({}^nC_2) \text{ Need to find: Value of } n \Rightarrow {}^{n+1}C_3 = 2({}^nC_2) = \frac{(n+1)!}{3!(n+1-3)!} = 2 \frac{n!}{2!(n-2)!} \Rightarrow$$

$$\frac{(n+1)n(n-1)}{6} = n(n-1) \Rightarrow \frac{n+1}{6} = 1 \text{ [As } n \neq 0] \Rightarrow n = 5$$

Question: 9

If ${}^nP <$

Solution:

Given: ${}^nP_r = 720$ & ${}^nC_r = 120$ Need to find: Value of r We know that, ${}^nP_r = r! \times {}^nC_r$ Putting the values, $\Rightarrow 720 = r! \times 120 \Rightarrow r! = 6 = 3! \Rightarrow r = 3$.

Question: 10

If (n^2-n)

Solution:

Given: $(n^2-n)C_2 = (n^2-n)C_4 = 120$ Need to find: Value of n $(n^2-n)C_2 = (n^2-n)C_4 = 120$ We know, one of the property of combination is: If ${}^nC_r = {}^nC_t$, then, (i) $r = t$ OR (ii) $r + t = n$ Applying property (ii) we get, $n^2 - n = 2 + 4 = 6$ $n^2 - n - 6 = 0$ $n^2 - 3n + 2n - 6 = 0$ $n(n-3) + 2(n-3) = 0$ $(n-3)(n+2) = 0$ So, the value of n is either 3 or -2.

Question: 11

How many words ar

Solution:

3 consonants out of 5 consonants can be chosen in 5C_3 ways. 2 vowels out of 4 vowels can be chosen in 4C_2 ways. And also 5 letters can be written in $5!$ Ways. Therefore, the number of words can be formed is $({}^5C_3 \times {}^4C_2 \times 5!) = 7200$.

Question: 12

Find the number o

Solution:

n -sided polygon has n numbers of vertices. Diagonals are formed by joining the opposite vertices from one vertex, except the two adjacent vertices. So, from one vertex $(n-3)$ diagonals can be drawn. Similarly, for n numbers of vertices, $n(n-3)$ diagonals can be drawn. But, the diagonal joins 2 points at a time, here two vertices. Therefore, the actual number of diagonals is $= \frac{n(n-3)}{2}$.

Question: 13

Three persons ent

Solution:

Three persons enter a compartment where 5 seats are vacant. The number of ways they can be seated is $= {}^5P_3 = 60$.

Question: 14

There are 12 poin

Solution:

To get a straight line we just need to join two points. There are 12 numbers of points. Therefore, there is $^{12}C_2 = 66$ number of straight lines. Among the 12 points, there are 3 points which are collinear. That means joining those 3 lines give a single straight line. That means the real number of straight lines present in the table is $= (66 - ^3C_2 + 1) = (66 - 3 + 1) = 64$.

Question: 15

In how many ways

Solution:

We need to include at least 2 women. If we include 2 women in the committee, then a number of men is 3. The number of ways, 2 women can be selected out of 4 is $= ^4C_2 = 6$ The number of ways, 3 men can be selected out of 6 is $= ^6C_3 = 20$ So, the committee can be formed including 2 women in $(20 \times 6) = 120$ ways. If we include 3 women in the committee, then a number of men is 2. The number of ways, 3 women can be selected out of 4 is $= ^4C_3 = 4$ The number of ways, 2 men can be selected out of 6 is $= ^6C_2 = 15$ So, the committee can be formed including 3 women in $(15 \times 4) = 60$ ways. Therefore, the total number of ways the committee can be formed is $= (120 + 60) = 180$ ways.

Question: 16

There are 13 cric

Solution:

There are 4 bowlers in 13 player team. So, maximum we can add 4 bowlers. And we need to include at least 3 bowlers. If we include 3 bowlers then from the remaining 9 [13 - 4 bowlers] players, we need to include 8. The number of ways, 8 players can be selected among 9 is $= ^9C_8 = 9$ The number of ways, 3 players can be selected among 4 is $= ^4C_3 = 4$ So, taking 3 bowlers the team can be represented in $(9 \times 4) = 36$ ways. If we include 4 bowlers then from the remaining 9 [13 - 4 bowlers] players, we need to include 7. The number of ways, 7 players can be selected among 9 is $= ^9C_7 = 36$ The number of ways, 4 players can be selected among 4 is $= ^4C_4 = 1$ So, taking 4 bowlers the team can be represented in $(36 \times 1) = 36$ ways. Therefore, the total possible ways are $= (36 + 36) = 72$.

Question: 17

How many differen

Solution:

Each committee consists of 3 men and 2 women. So, we need to select 3 men out of 6 and 2 women out of 4. The number of ways, 3 men can be selected out of 6, is $= ^6C_3 = 20$ The number of ways, 2 women can be selected out of 4, is $= ^4C_2 = 6$ So, the totally $(20 + 6) = 26$ numbers of different committees can be formed.

Question: 18

How many parallel

Solution:

To form a parallelogram we need 2 sets of 2 parallel lines intersecting the other 2 lines from the other set. So, first of all, we need to get 2 lines from the sets. From the first parallel set, 2 out of 4 lines can be selected in $^4C_2 = 6$ ways. From the second parallel set, 2 out of 3 lines can be selected in $^3C_2 = 3$ ways. So, the total number of parallelograms can be formed is $= (6 \times 3) = 18$.