

PRINCIPLE OF MATHEMATICAL INDUCTION

SELECT THE CORRECT ALTERNATIVE (ONLY ONE CORRECT ANSWER)

- The sum of n terms of $1^2 + (1^2 + 2^2) + (1^2 + 2^2 + 3^2) + \dots$ is-
 (1) $\frac{n(n+1)(2n+1)}{6}$ (2) $\frac{n(n+1)(2n-1)}{6}$
 (3) $\frac{1}{12}n(n+1)^2(n+2)$ (4) $\frac{1}{12}n^2(n+1)^2$
- The greatest positive integer, which divides $(n+16)(n+17)(n+18)(n+19)$, for all $n \in \mathbb{N}$, is-
 (1) 2 (2) 4 (3) 24 (4) 120
- Let $P(n) : n^2 + n$ is an odd integer. It is seen that truth of $P(n) \Rightarrow$ the truth of $P(n+1)$. Therefore, $P(n)$ is true for all-
 (1) $n > 1$ (2) n
 (3) $n > 2$ (4) None of these
- For every natural number n -
 (1) $n > 2^n$ (2) $n < 2^n$ (3) $n \geq 2^n$ (4) $n \leq 2^n$
- If $n \in \mathbb{N}$, then $x^{2n-1} + y^{2n-1}$ is divisible by-
 (1) $x + y$ (2) $x - y$ (3) $x^2 + y^2$ (4) $x^2 + xy$
- The inequality $n! > 2^{n-1}$ is true-
 (1) for all $n > 1$ (2) for all $n > 2$
 (3) for all $n \in \mathbb{N}$ (4) None of these
- $1.2^2 + 2.3^2 + 3.4^2 + \dots$ upto n terms, is equal to-
 (1) $\frac{1}{12}n(n+1)(n+2)(n+3)$
 (2) $\frac{1}{12}n(n+1)(n+2)(n+5)$
 (3) $\frac{1}{12}n(n+1)(n+2)(3n+5)$
 (4) None of these
- The sum of the cubes of three consecutive natural numbers is divisible by-
 (1) 2 (2) 5 (3) 7 (4) 9
- If $n \in \mathbb{N}$, then $11^{n+2} + 12^{2n+1}$ is divisible by-
 (1) 113 (2) 123
 (3) 133 (4) None of these
- If $n \in \mathbb{N}$, then $3^{4n+2} + 5^{2n+1}$ is a multiple of-
 (1) 14 (2) 16 (3) 18 (4) 20
- For each $n \in \mathbb{N}$, $10^{2n+1} + 1$ is divisible by-
 (1) 11 (2) 13
 (3) 27 (4) None of these
- The difference between an +ve integer and its cube is divisible by-
 (1) 4 (2) 6
 (3) 9 (4) None of these
- If n is a natural number then $\left(\frac{n+1}{2}\right)^n \geq n!$ is true when-
 (1) $n > 1$ (2) $n \geq 1$ (3) $n > 2$ (4) Never
- For natural number n , $2^n (n-1)! < n^n$, if-
 (1) $n < 2$ (2) $n > 2$ (3) $n \geq 2$ (4) never
- For every positive integer
 n , $\frac{n^7}{7} + \frac{n^5}{5} + \frac{2n^3}{3} - \frac{n}{105}$ is-
 (1) an integer
 (2) a rational number
 (3) a negative real number
 (4) an odd integer
- For positive integer n , $3^n < n!$ when-
 (1) $n \geq 6$ (2) $n > 7$ (3) $n \geq 7$ (4) $n \leq 7$
- If $A = \begin{pmatrix} a & 1 \\ 0 & a \end{pmatrix}$, then for any $n \in \mathbb{N}$, A^n equals-
 (1) $\begin{pmatrix} na & n \\ 0 & na \end{pmatrix}$ (2) $\begin{pmatrix} a^n & na^{n-1} \\ 0 & a^n \end{pmatrix}$
 (3) $\begin{pmatrix} na & 1 \\ 0 & na \end{pmatrix}$ (4) $\begin{pmatrix} a^n & n \\ 0 & a^n \end{pmatrix}$
- The sum of n terms of the series
 $\frac{1}{1^3} \cdot \frac{2}{2} + \frac{2}{1^3+2^3} \cdot \frac{3}{2} + \frac{3}{1^3+2^3+3^3} \cdot \frac{4}{2} + \dots$ is-
 (1) $\frac{1}{n(n+1)}$ (2) $\frac{n}{n+1}$ (3) $\frac{n+1}{n}$ (4) $\frac{n+1}{n+2}$
- For all $n \in \mathbb{N}$, $7^{2n} - 48n - 1$ is divisible by-
 (1) 25 (2) 26 (3) 1234 (4) 2304
- The n^{th} term of the series
 $4 + 14 + 30 + 52 + 80 + 114 + \dots$ is-
 (1) $5n - 1$ (2) $2n^2 + 2n$ (3) $3n^2 + n$ (4) $2n^2 + 2$
- If $10^n + 3.4^{n+2} + \lambda$ is exactly divisible by 9 for all $n \in \mathbb{N}$, then the least positive integral value of λ is-
 (1) 5 (2) 3 (3) 7 (4) 1
- The sum of n terms of the series
 $1 + (1+a) + (1+a+a^2) + (1+a+a^2+a^3) + \dots$, is-
 (1) $\frac{n}{1-a} - \frac{a(1-a^n)}{(1-a)^2}$ (2) $\frac{n}{1-a} + \frac{a(1-a^n)}{(1-a)^2}$
 (3) $\frac{n}{1-a} + \frac{a(1+a^n)}{(1-a)^2}$ (4) $-\frac{n}{1-a} + \frac{a(1-a^n)}{(1-a)^2}$

23. For all $n \in \mathbb{N}$, n^4 is less than-
 (1) 10^n (2) 4^n
 (3) 10^{10} (4) None of these
24. For all $n \in \mathbb{N}$, Σn
 (1) $< \frac{(2n+1)^2}{8}$ (2) $> \frac{(2n+1)^2}{8}$
 (3) $= \frac{(2n+1)^2}{8}$ (4) None of these
25. For all $n \in \mathbb{N}$, $\cos \theta \cos 2\theta \cos 4\theta \dots \cos 2^{n-1}\theta$ equals to-
 (1) $\frac{\sin 2^n \theta}{2^n \sin \theta}$ (2) $\frac{\sin 2^n \theta}{\sin \theta}$
 (3) $\frac{\cos 2^n \theta}{2^n \cos 2\theta}$ (4) $\frac{\cos 2^n \theta}{2^n \sin \theta}$
26. For all positive integral values of n , $3^{2n} - 2n + 1$ is divisible by-
 (1) 2 (2) 4 (3) 8 (4) 12
27. $\frac{1^2}{1} + \frac{1^2+2^2}{1+2} + \frac{1^2+2^2+3^2}{1+2+3} + \dots$ upto n terms is-
 (1) $\frac{1}{3}(2n+1)$ (2) $\frac{1}{3}n^2$
 (3) $\frac{1}{3}(n+2)$ (4) $\frac{1}{3}n(n+2)$
28. The smallest positive integer for which the statement $3^{n+1} < 4^n$ holds is-
 (1) 1 (2) 2 (3) 3 (4) 4
29. Sum of n terms of the series $\frac{1}{1} + \frac{1}{1+2} + \frac{1}{1+2+3} + \dots$ is-
 (1) $\frac{n}{n+1}$ (2) $\frac{2}{n(n+1)}$ (3) $\frac{2n}{n+1}$ (4) $\frac{2(n+1)}{n+2}$
30. For every natural number n , $n(n+3)$ is always-
 (1) multiple of 4 (2) multiple of 5
 (3) even (4) odd

31. $\frac{1}{1.3} + \frac{1}{3.5} + \frac{1}{5.7} + \dots$ upto n terms is-
 (1) $\frac{1}{2n+1}$ (2) $\frac{n}{2n+1}$ (3) $\frac{1}{2n-1}$ (4) $\frac{2n}{3(n+1)}$
32. For positive integer n , $10^{n-2} > 81n$ when-
 (1) $n < 5$ (2) $n > 5$ (3) $n \geq 5$ (4) $n > 6$
33. If P is a prime number then $n^p - n$ is divisible by p when n is a
 (1) natural number greater than 1
 (2) odd number
 (3) even number
 (4) None of these
34. $1 + 3 + 6 + 10 + \dots$ upto n terms is equal to-
 (1) $\frac{1}{3}n(n+1)(n+2)$ (2) $\frac{1}{6}n(n+1)(n+2)$
 (3) $\frac{1}{12}n(n+2)(n+3)$ (4) $\frac{1}{12}n(n+1)(n+2)$
35. A student was asked to prove a statement by induction. He proved
 (i) $P(5)$ is true and
 (ii) Truth of $P(n) \Rightarrow$ truth of $p(n+1)$, $n \in \mathbb{N}$
 On the basis of this, he could conclude that $P(n)$ is true for
 (1) no $n \in \mathbb{N}$ (2) all $n \in \mathbb{N}$
 (3) all $n \geq 5$ (4) None of these
36. The sum of the series $\frac{3}{1^2} + \frac{5}{1^2+2^2} + \frac{7}{1^2+2^2+3^2} + \dots$ upto n terms
 (1) $\frac{2n}{n+1}$ (2) $\frac{3n}{n+1}$ (3) $\frac{3n}{2(n+1)}$ (4) $\frac{6n}{n+1}$
37. $\frac{1}{2} + \frac{3}{4} + \frac{7}{8} + \frac{15}{16} + \dots$ upto n terms equal to-
 (1) $n + \frac{1}{2^n}$ (2) $2n + \frac{1}{2^n}$
 (3) $n - 1 + \frac{1}{2^n}$ (4) $n + 1 + \frac{1}{2^n}$

ANSWER KEY

Que.	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15
Ans.	3	3	4	2	1	2	3	4	3	1	1	2	2	2	1
Que.	16	17	18	19	20	21	22	23	24	25	26	27	28	29	30
Ans.	3	2	2	4	3	1	1	1	1	1	1	4	4	3	3
Que.	31	32	33	34	35	36	37								
Ans.	2	3	1	2	3	4	3								

PRINCIPLE OF MATHEMATICAL INDUCTION

- (1) Statement-1 is false, statement-2 is true.
- (2) Statement-1 is true, statement-2 is true;
Statement-2 is correct explanation for
statement-1.
- (3) Statement-1 is true, statement-2 is true;
Statement-2 is not a correct explanation for
statement-1.
- (4) Statement-1 is true, statement-2 is false.

[illegible]