

Motion in a Straight Line

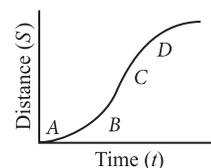
3.3 Average Velocity and Average Speed

- A particle covers half of its total distance with speed v_1 and the rest half distance with speed v_2 . Its average speed during the complete journey is
 - $\frac{v_1 + v_2}{2}$
 - $\frac{v_1 v_2}{v_1 + v_2}$
 - $\frac{2v_1 v_2}{v_1 + v_2}$
 - $\frac{v_1^2 v_2^2}{v_1^2 + v_2^2}$ (Mains 2011)
- A car moves from X to Y with a uniform speed v_u and returns to X with a uniform speed v_d . The average speed for this round trip is
 - $\sqrt{v_u v_d}$
 - $\frac{v_d v_u}{v_d + v_u}$
 - $\frac{v_u + v_d}{2}$
 - $\frac{2v_d v_u}{v_d + v_u}$ (2007)
- A car runs at a constant speed on a circular track of radius 100 m, taking 62.8 seconds for every circular lap. The average velocity and average speed for each circular lap respectively is
 - 10 m/s, 0
 - 0, 0
 - 0, 10 m/s
 - 10 m/s, 10 m/s. (2006)
- A car moves a distance of 200 m. It covers the first half of the distance at speed 40 km/h and the second half of distance at speed v . The average speed is 48 km/h. The value of v is
 - 56 km/h
 - 60 km/h
 - 50 km/h
 - 48 km/h. (1991)
- A bus travelling the first one-third distance at a speed of 10 km/h, the next one-third at 20 km/h and at last one-third at 60 km/h. The average speed of the bus is
 - 9 km/h
 - 16 km/h
 - 18 km/h
 - 48 km/h. (1991)
- A car covers the first half of the distance between two places at 40 km/h and another half at 60 km/h. The average speed of the car is

- 40 km/h
- 48 km/h
- 50 km/h
- 60 km/h. (1990)

3.4 Instantaneous Velocity and Speed

- Two cars P and Q start from a point at the same time in a straight line and their positions are represented by $x_P(t) = (at + bt^2)$ and $x_Q(t) = (ft - t^2)$. At what time do the cars have the same velocity?
 - $\frac{a-f}{1+b}$
 - $\frac{a+f}{2(b-1)}$
 - $\frac{a+f}{2(1+b)}$
 - $\frac{f-a}{2(1+b)}$ (NEET-II 2016)
- If the velocity of a particle is $v = At + Bt^2$, where A and B are constants, then the distance travelled by it between 1 s and 2 s is
 - $\frac{3}{2}A + \frac{7}{3}B$
 - $\frac{A}{2} + \frac{B}{3}$
 - $\frac{3}{2}A + 4B$
 - $3A + 7B$ (NEET-I 2016)
- The displacement 'x' (in meter) of a particle of mass 'm' (in kg) moving in one dimension under the action of a force, is related to time 't' (in sec) by $t = \sqrt{x} + 3$. The displacement of the particle when its velocity is zero, will be
 - 4 m
 - 0 m (zero)
 - 6 m
 - 2 m (Karnataka NEET 2013)
- A particle shows distance-time curve as given in this figure. The maximum instantaneous velocity of the particle is around the point
 - D
 - A
 - B
 - C (2008)



11. The position x of a particle with respect to time t along x -axis is given by $x = 9t^2 - t^3$ where x is in metres and t in seconds. What will be the position of this particle when it achieves maximum speed along the $+x$ direction?

(a) 54 m (b) 81 m (c) 24 m (d) 32 m. (2007)

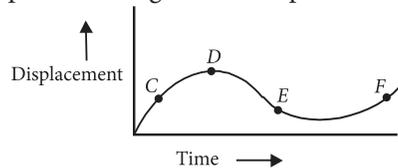
12. A particle moves along a straight line OX . At a time t (in seconds) the distance x (in metres) of the particle from O is given by $x = 40 + 12t - t^3$. How long would the particle travel before coming to rest?

(a) 16 m (b) 24 m (c) 40 m (d) 56 m (2006)

13. The displacement x of a particle varies with time t as $x = ae^{-\alpha t} + be^{\beta t}$, where a, b, α and β are positive constants. The velocity of the particle will

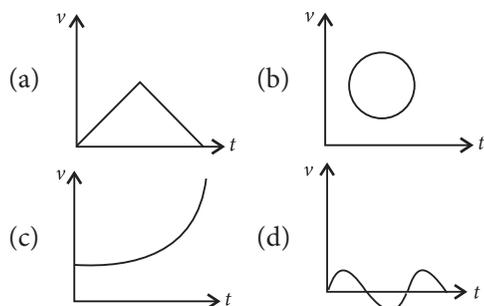
(a) be independent of β
 (b) drop to zero when $\alpha = \beta$
 (c) go on decreasing with time
 (d) go on increasing with time. (2005)

14. The displacement-time graph of a moving particle is shown below. The instantaneous velocity of the particle is negative at the point



(a) E (b) F (c) C (d) D (1994)

15. Which of the following curve does not represent motion in one dimension?



(1992)

3.5 Acceleration

16. A particle of unit mass undergoes one-dimensional motion such that its velocity varies according to $v(x) = \beta x^{-2n}$, where β and n are constants and x is the position of the particle. The acceleration of the particle as a function of x , is given by

(a) $-2\beta^2 x^{-2n+1}$ (b) $-2n\beta^2 e^{-4n+1}$
 (c) $-2n\beta^2 x^{-2n-1}$ (d) $-2n\beta^2 x^{-4n-1}$

(2015 Cancelled)

17. The motion of a particle along a straight line is described by equation $x = 8 + 12t - t^3$ where x is in metre and t in second. The retardation of the particle

when its velocity becomes zero is

(a) 24 m s⁻² (b) zero
 (c) 6 m s⁻² (d) 12 m s⁻² (2012)

18. A particle moves a distance x in time t according to equation $x = (t + 5)^{-1}$. The acceleration of particle is proportional to

(a) (velocity)^{3/2} (b) (distance)²
 (c) (distance)⁻² (d) (velocity)^{2/3} (2010)

19. A particle moving along x -axis has acceleration f , at time t , given by $f = f_0 \left(1 - \frac{t}{T}\right)$, where f_0 and T are constants. The particle at $t = 0$ has zero velocity. In the time interval between $t = 0$ and the instant when $f = 0$, the particle's velocity (v_x) is

(a) $\frac{1}{2} f_0 T^2$ (b) $f_0 T^2$
 (c) $\frac{1}{2} f_0 T$ (d) $f_0 T$ (2007)

20. Motion of a particle is given by equation $s = (3t^3 + 7t^2 + 14t + 8)$ m. The value of acceleration of the particle at $t = 1$ sec is

(a) 10 m/s² (b) 32 m/s²
 (c) 23 m/s² (d) 16 m/s². (2000)

21. The position x of a particle varies with time, (t) as $x = at^2 - bt^3$. The acceleration will be zero at time t is equal to

(a) $\frac{a}{3b}$ (b) zero (c) $\frac{2a}{3b}$ (d) $\frac{a}{b}$ (1997)

22. The acceleration of a particle is increasing linearly with time t as bt . The particle starts from origin with an initial velocity v_0 . The distance travelled by the particle in time t will be

(a) $v_0 t + \frac{1}{3} bt^2$ (b) $v_0 t + \frac{1}{2} bt^2$
 (c) $v_0 t + \frac{1}{6} bt^3$ (d) $v_0 t + \frac{1}{3} bt^3$ (1995)

23. A particle moves along a straight line such that its displacement at any time t is given by $s = (t^3 - 6t^2 + 3t + 4)$ metres. The velocity when the acceleration is zero is

(a) 3 m/s (b) 42 m/s
 (c) -9 m/s (d) -15 m/s (1994)

3.6 Kinematic Equations for Uniformly Accelerated Motion

24. A ball is thrown vertically downward with a velocity of 20 m/s from the top of a tower. It hits the ground after some time with a velocity of 80 m/s. The height of the tower is ($g = 10$ m/s²)

(a) 360 m (b) 340 m
 (c) 320 m (d) 300 m (NEET 2020)

25. A stone falls freely under gravity. It covers distances h_1, h_2 and h_3 in the first 5 seconds, the next 5 seconds and the next 5 seconds respectively. The relation between h_1, h_2 and h_3 is
 (a) $h_2 = 3h_1$ and $h_3 = 3h_2$
 (b) $h_1 = h_2 = h_3$
 (c) $h_1 = 2h_2 = 3h_3$ (d) $h_1 = \frac{h_2}{3} = \frac{h_3}{5}$ (NEET 2013)
26. A boy standing at the top of a tower of 20 m height drops a stone. Assuming $g = 10 \text{ m s}^{-2}$, the velocity with which it hits the ground is
 (a) 10.0 m/s (b) 20.0 m/s
 (c) 40.0 m/s (d) 5.0 m/s (2011)
27. A ball is dropped from a high rise platform at $t = 0$ starting from rest. After 6 seconds another ball is thrown downwards from the same platform with a speed v . The two balls meet at $t = 18 \text{ s}$. What is the value of v ? (Take $g = 10 \text{ m/s}^2$)
 (a) 75 m/s (b) 55 m/s (c) 40 m/s (d) 60 m/s (2010)
28. A particle starts its motion from rest under the action of a constant force. If the distance covered in first 10 seconds is S_1 and that covered in the first 20 seconds is S_2 , then
 (a) $S_2 = 3S_1$ (b) $S_2 = 4S_1$
 (c) $S_2 = S_1$ (d) $S_2 = 2S_1$ (2009)
29. A particle moves in a straight line with a constant acceleration. It changes its velocity from 10 m s^{-1} to 20 m s^{-1} while passing through a distance 135 m in t second. The value of t is
 (a) 12 (b) 9 (c) 10 (d) 1.8 (2008)
30. The distance travelled by a particle starting from rest and moving with an acceleration $\frac{4}{3} \text{ m s}^{-2}$, in the third second is
 (a) $\frac{10}{3} \text{ m}$ (b) $\frac{19}{3} \text{ m}$ (c) 6 m (d) 4 m (2008)
31. Two bodies A (of mass 1 kg) and B (of mass 3 kg) are dropped from heights of 16 m and 25 m, respectively. The ratio of the time taken by them to reach the ground is
 (a) 4/5 (b) 5/4 (c) 12/5 (d) 5/12 (2006)
32. A ball is thrown vertically upward. It has a speed of 10 m/sec when it has reached one half of its maximum height. How high does the ball rise? (Take $g = 10 \text{ m/s}^2$)
 (a) 10 m (b) 5 m (c) 15 m (d) 20 m (2005)
33. A man throws balls with the same speed vertically upwards one after the other at an interval of 2 seconds. What should be the speed of the throw so that more than two balls are in the sky at any time? (Given $g = 9.8 \text{ m/s}^2$)
 (a) more than 19.6 m/s
 (b) at least 9.8 m/s
 (c) any speed less than 19.6 m/s
 (d) only with speed 19.6 m/s (2003)
34. If a ball is thrown vertically upwards with speed u , the distance covered during the last t seconds of its ascent is
 (a) ut (b) $\frac{1}{2}gt^2$
 (c) $ut - \frac{1}{2}gt^2$ (d) $(u + gt)t$ (2003)
35. A particle is thrown vertically upward. Its velocity at half of the height is 10 m/s, then the maximum height attained by it ($g = 10 \text{ m/s}^2$)
 (a) 8 m (b) 20 m (c) 10 m (d) 16 m. (2001)
36. A car moving with a speed of 40 km/h can be stopped by applying brakes after atleast 2 m. If the same car is moving with a speed of 80 km/h, what is the minimum stopping distance?
 (a) 4 m (b) 6 m (c) 8 m (d) 2 m (1998)
37. If a car at rest accelerates uniformly to a speed of 144 km/h in 20 s, it covers a distance of
 (a) 1440 cm (b) 2980 cm
 (c) 20 m (d) 400 m (1997)
38. A body dropped from a height h with initial velocity zero, strikes the ground with a velocity 3 m/s. Another body of same mass dropped from the same height h with an initial velocity of 4 m/s. The final velocity of second mass, with which it strikes the ground is
 (a) 5 m/s (b) 12 m/s
 (c) 3 m/s (d) 4 m/s. (1996)
39. The water drop falls at regular intervals from a tap 5 m above the ground. The third drop is leaving the tap at instant the first drop touches the ground. How far above the ground is the second drop at that instant?
 (a) 3.75 m (b) 4.00 m (c) 1.25 m (d) 2.50 m. (1995)
40. A car accelerates from rest at a constant rate α for some time after which it decelerates at a constant rate β and comes to rest. If total time elapsed is t , then maximum velocity acquired by car will be
 (a) $\frac{(\alpha^2 - \beta^2)t}{\alpha\beta}$ (b) $\frac{(\alpha^2 + \beta^2)t}{\alpha\beta}$
 (c) $\frac{(\alpha + \beta)t}{\alpha\beta}$ (d) $\frac{\alpha\beta t}{\alpha + \beta}$ (1994)
41. The velocity of train increases uniformly from 20 km/h to 60 km/h in 4 hours. The distance travelled by the train during this period is
 (a) 160 km (b) 180 km
 (c) 100 km (d) 120 km (1994)

42. A body starts from rest, what is the ratio of the distance travelled by the body during the 4th and 3rd second ?

- (a) $\frac{7}{5}$ (b) $\frac{5}{7}$
 (c) $\frac{7}{3}$ (d) $\frac{3}{7}$ (1993)

43. A body dropped from top of a tower fall through 40 m during the last two seconds of its fall. The height of tower is ($g = 10 \text{ m/s}^2$)

- (a) 60 m (b) 45 m
 (c) 80 m (d) 50 m (1992)

44. What will be the ratio of the distance moved by a freely falling body from rest in 4th and 5th seconds of journey ?

- (a) 4 : 5 (b) 7 : 9
 (c) 16 : 25 (d) 1 : 1. (1989)

45. A car is moving along a straight road with a uniform acceleration. It passes through two points P and Q separated by a distance with velocity 30 km/h and 40 km/h respectively. The velocity of the car midway between P and Q is

- (a) 33.3 km/h (b) $20\sqrt{2}$ km/h
 (c) $25\sqrt{2}$ km/h (d) 35 km/h. (1988)

3.7 Relative Velocity

46. Preeti reached the metro station and found that the escalator was not working. She walked up the stationary escalator in time t_1 . On other days, if she remains stationary on the moving escalator, then the escalator takes her up in time t_2 . The time taken by her to walk up on the moving escalator will be

- (a) $\frac{t_1 t_2}{t_2 - t_1}$ (b) $\frac{t_1 t_2}{t_2 + t_1}$
 (c) $t_1 - t_2$ (d) $\frac{t_1 + t_2}{2}$ (NEET 2017)

47. A bus is moving with a speed of 10 m s^{-1} on a straight road. A scooterist wishes to overtake the bus in 100 s. If the bus is at a distance of 1 km from the scooterist, with what speed should the scooterist chase the bus?

- (a) 40 m s^{-1} (b) 25 m s^{-1}
 (c) 10 m s^{-1} (d) 20 m s^{-1} (2009)

48. A train of 150 metre length is going towards north direction at a speed of 10 m/s . A parrot flies at the speed of 5 m/s towards south direction parallel to the railways track. The time taken by the parrot to cross the train is

- (a) 12 s (b) 8 s (c) 15 s (d) 10 s (1988)

ANSWER KEY

1. (c) 2. (d) 3. (c) 4. (b) 5. (c) 6. (b) 7. (d) 8. (a) 9. (b) 10. (d)
 11. (a) 12. (a) 13. (d) 14. (a) 15. (b) 16. (b) 17. (d) 18. (a) 19. (c) 20. (b)
 21. (a) 22. (c) 23. (c) 24. (d) 25. (d) 26. (b) 27. (a) 28. (b) 29. (b) 30. (a)
 31. (a) 32. (a) 33. (a) 34. (b) 35. (c) 36. (c) 37. (d) 38. (a) 39. (a) 40. (d)
 41. (a) 42. (a) 43. (b) 44. (b) 45. (c) 46. (b) 47. (d) 48. (d)

Hints & Explanations

1. (c) : Let S be the total distance travelled by the particle.

Let t_1 be the time taken by the particle to cover first half of the distance. Then $t_1 = \frac{S/2}{v_1} = \frac{S}{2v_1}$

Let t_2 be the time taken by the particle to cover remaining half of the distance. Then

$$t_2 = \frac{S/2}{v_2} = \frac{S}{2v_2}$$

Average speed,

$$v_{av} = \frac{\text{Total distance travelled}}{\text{Total time taken}} \\ = \frac{S}{t_1 + t_2} = \frac{S}{\frac{S}{2v_1} + \frac{S}{2v_2}} = \frac{2v_1 v_2}{v_1 + v_2}$$

2. (d) : Average speed = $\frac{\text{total distance travelled}}{\text{total time taken}}$

$$= \frac{s+s}{t_1+t_2} = \frac{2s}{\frac{s}{v_u} + \frac{s}{v_d}} = \frac{2v_u v_d}{v_d + v_u}$$

3. (c) : Distance travelled in one rotation (lap) = $2\pi r$

$$\therefore \text{Average speed} = \frac{\text{distance}}{\text{time}} = \frac{2\pi r}{t} \\ = \frac{2 \times 3.14 \times 100}{62.8} = 10 \text{ m s}^{-1}$$

Net displacement in one lap = 0

$$\text{Average velocity} = \frac{\text{net displacement}}{\text{time}} = \frac{0}{t} = 0.$$

4. (b) : Total distance travelled = 200 m

$$\text{Total time taken} = \frac{100}{40} + \frac{100}{v}$$

$$\text{Average speed} = \frac{\text{total distance travelled}}{\text{total time taken}}$$

$$48 = \frac{200}{\left(\frac{100}{40} + \frac{100}{v}\right)} \text{ or } 48 = \frac{2}{\left(\frac{1}{40} + \frac{1}{v}\right)}$$

$$\text{or } \frac{1}{40} + \frac{1}{v} = \frac{1}{24} \text{ or } \frac{1}{v} = \frac{1}{24} - \frac{1}{40} = \frac{5-3}{120} = \frac{1}{60}$$

$$\text{or } v = 60 \text{ km/h}$$

5. (c) : Total distance travelled = s

$$\begin{aligned} \text{Total time taken} &= \frac{s/3}{10} + \frac{s/3}{20} + \frac{s/3}{60} \\ &= \frac{s}{30} + \frac{s}{60} + \frac{s}{180} = \frac{10s}{180} = \frac{s}{18} \end{aligned}$$

$$\begin{aligned} \text{Average speed} &= \frac{\text{total distance travelled}}{\text{total time taken}} \\ &= \frac{s}{s/18} = 18 \text{ km/h} \end{aligned}$$

6. (b) : Total distance covered = s

$$\text{Total time taken} = \frac{s/2}{40} + \frac{s/2}{60} = \frac{5s}{240} = \frac{s}{48}$$

$$\begin{aligned} \therefore \text{Average speed} &= \frac{\text{total distance covered}}{\text{total time taken}} \\ &= \frac{s}{\left(\frac{s}{48}\right)} = 48 \text{ km/h} \end{aligned}$$

7. (d) : Position of the car P at any time t , is

$$x_P(t) = at + bt^2; \quad v_P(t) = \frac{dx_P(t)}{dt} = a + 2bt \quad \dots(i)$$

Similarly, for car Q ,

$$x_Q(t) = ft - t^2; \quad v_Q(t) = \frac{dx_Q(t)}{dt} = f - 2t \quad \dots(ii)$$

$$\therefore v_P(t) = v_Q(t) \quad (\text{Given})$$

$$\therefore a + 2bt = f - 2t \text{ or } 2t(b + 1) = f - a$$

$$\therefore t = \frac{f - a}{2(1 + b)}$$

8. (a) : Velocity of the particle is $v = At + Bt^2$

$$\frac{ds}{dt} = At + Bt^2; \quad \int ds = \int (At + Bt^2) dt$$

$$\therefore s = \frac{At^2}{2} + B \frac{t^3}{3} + C$$

$$s(t = 1 \text{ s}) = \frac{A}{2} + \frac{B}{3} + C; \quad s(t = 2 \text{ s}) = 2A + \frac{8}{3}B + C$$

$$\text{Required distance} = s(t = 2 \text{ s}) - s(t = 1 \text{ s})$$

$$= \left(2A + \frac{8}{3}B + C\right) - \left(\frac{A}{2} + \frac{B}{3} + C\right) = \frac{3}{2}A + \frac{7}{3}B$$

9. (b) : Given $t = \sqrt{x} + 3$ or $\sqrt{x} = t - 3$

Squaring both sides, we get

$$x = (t - 3)^2$$

$$\text{Velocity, } v = \frac{dx}{dt} = \frac{d}{dt}(t - 3)^2 = 2(t - 3)$$

Velocity of the particle becomes zero, when

$$2(t - 3) = 0 \text{ or } t = 3 \text{ s}$$

$$\text{At } t = 3 \text{ s, } x = (3 - 3)^2 = 0 \text{ m}$$

10. (d) : Because the slope is highest at C ,

$$v = \frac{ds}{dt} \text{ is maximum}$$

11. (a) : Given : $x = 9t^2 - t^3$

$$\text{Speed } v = \frac{dx}{dt} = \frac{d}{dt}(9t^2 - t^3) = 18t - 3t^2.$$

$$\text{For maximum speed, } \frac{dv}{dt} = 0 \Rightarrow 18 - 6t = 0$$

$$\therefore t = 3 \text{ s}$$

$$\therefore x_{\text{max}} = 81 \text{ m} - 27 \text{ m} = 54 \text{ m}$$

12. (a) : $x = 40 + 12t - t^3$

$$\therefore \text{Velocity, } v = \frac{dx}{dt} = 12 - 3t^2$$

$$\text{When particle come to rest, } \frac{dx}{dt} = v = 0$$

$$\therefore 12 - 3t^2 = 0 \Rightarrow 3t^2 = 12 \Rightarrow t = 2 \text{ sec.}$$

Distance travelled by the particle before coming to rest

$$\int_0^s ds = \int_0^2 v dt \text{ or } s = \int_0^2 (12 - 3t^2) dt = 12t - \frac{3t^3}{3} \Big|_0^2$$

$$s = 12 \times 2 - 8 = 24 - 8 = 16 \text{ m.}$$

$$13. (d) : x = ae^{-\alpha t} + be^{\beta t}; \quad \frac{dx}{dt} = -a\alpha e^{-\alpha t} + b\beta e^{\beta t}$$

$$v = -a\alpha e^{-\alpha t} + b\beta e^{\beta t}$$

Velocity will increase with time

$$14. (a) : \text{The velocity } (v) = \frac{ds}{dt}$$

Therefore, instantaneous velocity at point E is negative.

15. (b) : In one dimensional motion, the body can have one value of velocity at a time but not two values of velocities at a time.

16. (d) : According to question, velocity of unit mass varies as

$$v(x) = \beta x^{-2n} \quad \dots(i)$$

$$\frac{dv}{dx} = -2n\beta x^{-2n-1} \quad \dots(ii)$$

Acceleration of the particle is given by

$$a = \frac{dv}{dt} = \frac{dv}{dx} \times \frac{dx}{dt} = \frac{dv}{dx} \times v$$

Using equation (i) and (ii), we get

$$a = (-2n\beta x^{-2n-1}) \times (\beta x^{-2n}) = -2n\beta^2 x^{-4n-1}$$

17. (d) : Given : $x = 8 + 12t - t^3$

$$\text{Velocity, } v = \frac{dx}{dt} = 12 - 3t^2$$

$$\text{When } v = 0, 12 - 3t^2 = 0 \text{ or } t = 2 \text{ s}$$

$$a = \frac{dv}{dt} = -6t$$

$$a|_{t=2 \text{ s}} = -12 \text{ m s}^{-2}$$

Retardation = 12 m s^{-2} **18. (a) :** Distance, $x = (t + 5)^{-1}$... (i)Velocity, $v = \frac{dx}{dt} = \frac{d}{dt}(t + 5)^{-1} = -(t + 5)^{-2}$... (ii)Acceleration, $a = \frac{dv}{dt} = \frac{d}{dt}[-(t + 5)^{-2}] = 2(t + 5)^{-3}$... (iii)From equation (ii), we get $v^{3/2} = -(t + 5)^{-3}$... (iv)

Substituting this in equation (iii), we get

Acceleration, $a = -2v^{3/2}$ or $a \propto (\text{velocity})^{3/2}$

From equation (i), we get

$$x^3 = (t + 5)^{-3}$$

Substituting this in equation (iii), we get

Acceleration, $a = 2x^3$ or $a \propto (\text{distance})^3$

Hence option (a) is correct.

19. (c) : Given : At time $t = 0$, velocity, $v = 0$.Acceleration $f = f_0 \left(1 - \frac{t}{T}\right)$ At $f = 0$, $0 = f_0 \left(1 - \frac{t}{T}\right)$ Since f_0 is a constant,

$$\therefore 1 - \frac{t}{T} = 0 \quad \text{or} \quad t = T.$$

Also, acceleration $f = \frac{dv}{dt}$

$$\therefore \int_0^{v_x} dv = \int_{t=0}^{t=T} f dt = \int_0^T f_0 \left(1 - \frac{t}{T}\right) dt$$

$$\therefore v_x = \left[f_0 t - \frac{f_0 t^2}{2T} \right]_0^T = f_0 T - \frac{f_0 T^2}{2T} = \frac{1}{2} f_0 T.$$

20. (b) : $\frac{ds}{dt} = 9t^2 + 14t + 14$

$$\Rightarrow \frac{d^2s}{dt^2} = 18t + 14 = a$$

$$a_{t=1s} = 18 \times 1 + 14 = 32 \text{ m/s}^2$$

21. (a) : Distance $(x) = at^2 - bt^3$ Therefore velocity $(v) = \frac{dx}{dt} = \frac{d}{dt}(at^2 - bt^3) = 2at - 3bt^2$ Acceleration = $\frac{dv}{dt} = \frac{d}{dt}(2at - 3bt^2) = 2a - 6bt = 0$

$$\text{or } t = \frac{2a}{6b} = \frac{a}{3b}$$

22. (c) : Acceleration $\propto bt$. i.e., $\frac{d^2x}{dt^2} = a \propto bt$ Integrating, $\frac{dx}{dt} = \frac{bt^2}{2} + C$ Initially, $t = 0$, $dx/dt = v_0$

$$\text{Therefore, } \frac{dx}{dt} = \frac{bt^2}{2} + v_0$$

Integrating again, $x = \frac{bt^3}{6} + v_0 t + C$ When $t = 0$, $x = 0 \Rightarrow C = 0$.i.e., distance travelled by the particle in time $t = v_0 t + \frac{bt^3}{6}$.**23. (c) :** Displacement $(s) = t^3 - 6t^2 + 3t + 4 \text{ m}$.Velocity $(v) = \frac{ds}{dt} = 3t^2 - 12t + 3$ Acceleration $(a) = \frac{dv}{dt} = 6t - 12$.When $a = 0$, we get $t = 2$ seconds.

Therefore velocity when the acceleration is zero is

$$v = 3 \times (2)^2 - (12 \times 2) + 3 = -9 \text{ m/s}$$

24. (d) : Here, $u = 20 \text{ m/s}$, $v = 80 \text{ m/s}$, $g = 10 \text{ m/s}^2$, $h = ?$

$$v^2 = u^2 + 2gh$$

$$\Rightarrow 80^2 = 20^2 + 2 \times 10 \times h$$

Hence, $h = 300 \text{ m}$ **25. (d) :** Distance covered by the stone in first 5 seconds(i.e. $t = 5 \text{ s}$) is

$$h_1 = \frac{1}{2} g(5)^2 = \frac{25}{2} g \quad \dots(i)$$

Distance travelled by the stone in next 5 seconds

(i.e. $t = 10 \text{ s}$) is

$$h_1 + h_2 = \frac{1}{2} g(10)^2 = \frac{100}{2} g$$

Distance travelled by the stone in next 5 seconds

(i.e. $t = 15 \text{ s}$) is

$$h_1 + h_2 + h_3 = \frac{1}{2} g(15)^2 = \frac{225}{2} g \quad \dots(iii)$$

Subtract (i) from (ii), we get

$$(h_1 + h_2) - h_1 = \frac{100}{2} g - \frac{25}{2} g = \frac{75}{2} g$$

$$h_2 = \frac{75}{2} g = 3h_1 \quad \dots(iv)$$

Subtract (ii) from (iii), we get

$$(h_1 + h_2 + h_3) - (h_2 + h_1) = \frac{225}{2} g - \frac{100}{2} g$$

$$h_3 = \frac{125}{2} g = 5h_1 \quad \dots(v)$$

From (i), (iv) and (v), we get

$$h_1 = \frac{h_2}{3} = \frac{h_3}{5}$$

26. (b) : Here, $u = 0$, $g = 10 \text{ m s}^{-2}$, $h = 20 \text{ m}$ Let v be the velocity with which the stone hits the ground.

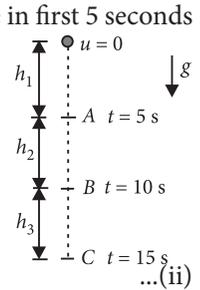
$$\therefore v^2 = u^2 + 2gh$$

$$\text{or } v = \sqrt{2gh} = \sqrt{2 \times 10 \times 20} = 20 \text{ m/s} \quad [\because u = 0]$$

27. (a) : Let the two balls meet after $t \text{ s}$ at distance x from the platform.For the first ball, $u = 0$, $t = 18 \text{ s}$, $g = 10 \text{ m/s}^2$

$$\text{Using } h = ut + \frac{1}{2} gt^2$$

$$\therefore x = \frac{1}{2} \times 10 \times 18^2 \quad \dots(i)$$

For the second ball, $u = v$, $t = 12 \text{ s}$, $g = 10 \text{ m/s}^2$ 

Using $h = ut + \frac{1}{2}gt^2$

$\therefore x = v \times 12 + \frac{1}{2} \times 10 \times 12^2$... (ii)

From equations (i) and (ii), we get

$$\frac{1}{2} \times 10 \times 18^2 = 12v + \frac{1}{2} \times 10 \times (12)^2$$

or $12v = \frac{1}{2} \times 10 \times [(18)^2 - (12)^2]$

$$12v = \frac{1}{2} \times 10 \times 30 \times 6 \quad \text{or} \quad v = \frac{1 \times 10 \times 30 \times 6}{2 \times 12} = 75 \text{ m/s}$$

28. (b) : Given $u = 0$.

Distance travelled in 10 s, $S_1 = \frac{1}{2}a \cdot 10^2 = 50a$

Distance travelled in 20 s, $S_2 = \frac{1}{2}a \cdot 20^2 = 200a$

$\therefore S_2 = 4S_1$

29. (b) : $v^2 - u^2 = 2as$

Given $v = 20 \text{ m s}^{-1}$, $u = 10 \text{ m s}^{-1}$, $s = 135 \text{ m}$

$$\therefore a = \frac{400 - 100}{2 \times 135} = \frac{300}{270} = \frac{10}{9} \text{ m/s}^2$$

$$v = u + at \Rightarrow t = \frac{v - u}{a} = \frac{10 \text{ m/s}}{\frac{10}{9} \text{ m/s}^2} = 9 \text{ s}$$

30. (a) : Distance travelled in the 3rd second = Distance travelled in 3 s - distance travelled in 2 s.

As, $u = 0$,

$$S_{(3\text{rd s})} = \frac{1}{2}a \cdot 3^2 - \frac{1}{2}a \cdot 2^2 = \frac{1}{2} \cdot a \cdot 5$$

Given $a = \frac{4}{3} \text{ m s}^{-2}$; $\therefore S_{(3\text{rd s})} = \frac{1}{2} \times \frac{4}{3} \times 5 = \frac{10}{3} \text{ m}$

31. (a) : Time taken by a body fall from a height h to reach the ground is $t = \sqrt{\frac{2h}{g}}$

$$\therefore \frac{t_A}{t_B} = \frac{\sqrt{\frac{2h_A}{g}}}{\sqrt{\frac{2h_B}{g}}} = \sqrt{\frac{h_A}{h_B}} = \sqrt{\frac{16}{25}} = \frac{4}{5}$$

32. (a) : As, $v^2 = u^2 - 2gh$

After reaching maximum height velocity becomes zero.

$$0 = (10)^2 - 2 \times 10 \times \frac{h}{2} \quad \therefore h = \frac{200}{20} = 10 \text{ m}$$

33. (a) : Interval of ball thrown = 2 s

If we want that minimum three (more than two) balls remain in air then time of flight of first ball must be greater than 4 s.

$$T > 4 \text{ sec} \quad \text{or} \quad \frac{2u}{g} > 4 \text{ sec} \Rightarrow u > 19.6 \text{ m/s.}$$

34. (b) : Let total height = H

Time of ascent = T

So, $H = uT - \frac{1}{2}gT^2$

Distance covered by ball in time $(T - t)$ sec.

$$y = u(T - t) - \frac{1}{2}g(T - t)^2$$

So distance covered by ball in last t sec.,

$$h = H - y = \left[uT - \frac{1}{2}gT^2 \right] - \left[u(T - t) - \frac{1}{2}g(T - t)^2 \right]$$

By solving and putting $T = \frac{u}{g}$ we will get

$$h = \frac{1}{2}gt^2.$$

35. (c) : For half height,

$$10^2 = u^2 - 2g \frac{h}{2} \quad \dots(i)$$

For total height,

$$0 = u^2 - 2gh \quad \dots(ii)$$

From (i) and (ii)

$$\Rightarrow 10^2 = \frac{2gh}{2} \Rightarrow h = 10 \text{ m}$$

36. (c) : 1st case $v^2 - u^2 = 2as$

$$0 - \left(\frac{100}{9}\right)^2 = 2 \times a \times 2 \quad [\because 40 \text{ km/h} = 100/9 \text{ m/s}]$$

$$a = -\frac{10^4}{81 \times 4} \text{ m/s}^2$$

$$2^{\text{nd}} \text{ case : } 0 - \left(\frac{200}{9}\right)^2 = 2 \times \left(-\frac{10^4}{81 \times 4}\right) \times s$$

[$\because 80 \text{ km/h} = 200/9 \text{ m/s}$]

or $s = 8 \text{ m.}$

37. (d) : Initial velocity $u = 0$,

Final velocity = 144 km/h = 40 m/s and time = 20 s

Using $v = u + at \Rightarrow a = v/t = 2 \text{ m/s}^2$

Again, $s = ut + \frac{1}{2}at^2 = \frac{1}{2} \times 2 \times (20)^2 = 400 \text{ m.}$

38. (a) : Initial velocity of first body (u_1) = 0;

Final velocity (v_1) = 3 m/s and initial velocity of second body (u_2) = 4 m/s.

$$\text{Height } (h) = \frac{v_1^2}{2g} = \frac{(3)^2}{2 \times 9.8} = 0.46 \text{ m}$$

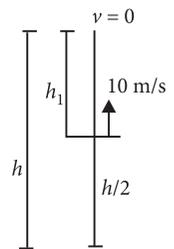
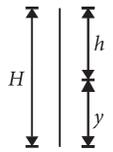
Therefore required velocity of the second body,

$$v_2 = \sqrt{u_2^2 + 2gh} = \sqrt{(4)^2 + 2 \times 9.8 \times 0.46} = 5 \text{ m/s}$$

39. (a) : Height of tap = 5 m. For the first drop,

$$5 = ut + \frac{1}{2}gt^2 = \frac{1}{2} \times 10t^2 = 5t^2 \quad \text{or} \quad t = 1 \text{ s}$$

It means that the third drop leaves after one second of the first drop, or each drop leaves after every 0.5 s. Distance covered by the second drop in 0.5 s



$$= \frac{1}{2}gt^2 = \frac{1}{2} \times 10 \times (0.5)^2 = 1.25 \text{ m}$$

Therefore distance of the second drop above the ground = $5 - 1.25 = 3.75 \text{ m}$

40. (d) : Initial velocity (u) = 0; acceleration in the first phase = α ; deceleration in the second phase = β and total time = t .

When car is accelerating then

$$\text{final velocity } (v) = u + \alpha t = 0 + \alpha t_1$$

or $t_1 = \frac{v}{\alpha}$ and when car is decelerating,

then final velocity $0 = v - \beta t$ or $t_2 = \frac{v}{\beta}$

Therefore total time (t) = $t_1 + t_2 = \frac{v}{\alpha} + \frac{v}{\beta}$

$$t = v \left(\frac{1}{\alpha} + \frac{1}{\beta} \right) = v \left(\frac{\beta + \alpha}{\alpha\beta} \right) \text{ or } v = \frac{\alpha\beta t}{\alpha + \beta}$$

41. (a) : Initial velocity (u) = 20 km/h;
Final velocity (v) = 60 km/h and time (t) = 4 hours.
velocity (v) = 60 = $u + at = 20 + (a \times 4)$

$$\text{or, } a = \frac{60 - 20}{4} = 10 \text{ km/h}^2.$$

Therefore distance travelled in 4 hours is

$$s = ut + \frac{1}{2}at^2 = (20 \times 4) + \frac{1}{2} \times 10 \times (4)^2 = 160 \text{ km}$$

42. (a) : Distance covered in n^{th} second is given by

$$s_n = u + \frac{a}{2}(2n - 1)$$

$$\text{Here, } u = 0. \therefore s_4 = 0 + \frac{a}{2}(2 \times 4 - 1) = \frac{7a}{2}$$

$$s_3 = 0 + \frac{a}{2}(2 \times 3 - 1) = \frac{5a}{2} \therefore \frac{s_4}{s_3} = \frac{7}{5}$$

43. (b) : Let h be height of the tower and t is the time taken by the body to reach the ground.

Here, $u = 0, a = g$

$$\therefore h = ut + \frac{1}{2}gt^2 \text{ or } h = 0 \times t + \frac{1}{2}gt^2$$

$$\text{or } h = \frac{1}{2}gt^2 \quad \dots(i)$$

Distance covered in last two seconds is

$$40 = \frac{1}{2}gt^2 - \frac{1}{2}g(t-2)^2 \text{ or } 40 = \frac{1}{2}gt^2 - \frac{1}{2}g(t^2 + 4 - 4t)$$

$$\text{or } 40 = (2t - 2)g \text{ or } t = 3 \text{ s}$$

From eqn (i), we get

$$h = \frac{1}{2} \times 10 \times (3)^2 \text{ or } h = 45 \text{ m}$$

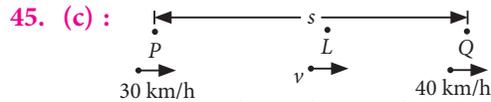
44. (b) : Distance covered in n^{th} second is given by

$$s_n = u + \frac{a}{2}(2n - 1)$$

Given : $u = 0, a = g$

$$\therefore s_4 = \frac{g}{2}(2 \times 4 - 1) = \frac{7g}{2}$$

$$s_5 = \frac{g}{2}(2 \times 5 - 1) = \frac{9g}{2} \therefore \frac{s_4}{s_5} = \frac{7}{9}$$



Let $PQ = s$ and L is the midpoint of PQ and v be velocity of the car at point L .

Using third equation of motion, we get $(40)^2 - (30)^2 = 2as$

$$\text{or } a = \frac{(40)^2 - (30)^2}{2s} = \frac{350}{s} \quad \dots(i)$$

$$\text{Also, } v^2 - (30)^2 = 2a \frac{s}{2}$$

$$\text{or } v^2 - (30)^2 = 2 \times \frac{350}{s} \times \frac{s}{2} \quad [\text{Using (i)}]$$

$$\text{or } v = 25\sqrt{2} \text{ km/h}$$

46. (b) : Let v_1 is the velocity of Preeti on stationary escalator and d is the distance travelled by her

$$\therefore v_1 = \frac{d}{t_1}$$

Again, let v_2 is the velocity of escalator

$$\therefore v_2 = \frac{d}{t_2}$$

\therefore Net velocity of Preeti on moving escalator with respect to the ground

$$v = v_1 + v_2 = \frac{d}{t_1} + \frac{d}{t_2} = d \left(\frac{t_1 + t_2}{t_1 t_2} \right)$$

The time taken by her to walk up on the moving escalator will be

$$t = \frac{d}{v} = \frac{d}{d \left(\frac{t_1 + t_2}{t_1 t_2} \right)} = \frac{t_1 t_2}{t_1 + t_2}$$

47. (d) : Let v_s be the velocity of the scooter, the distance between the scooter and the bus = 1000 m,

The velocity of the bus = 10 m s^{-1}

Time taken to overtake = 100 s

Relative velocity of the scooter with respect to the bus = $(v_s - 10)$

$$\therefore \frac{1000}{(v_s - 10)} = 100 \text{ s} \Rightarrow v_s = 20 \text{ m s}^{-1}.$$

48. (d) : Choose the positive direction of x -axis to be from south to north. Then

velocity of train $v_T = +10 \text{ m s}^{-1}$

velocity of parrot $v_P = -5 \text{ m s}^{-1}$

Relative velocity of parrot with respect to train

$$= v_P - v_T = (-5 \text{ m s}^{-1}) - (+10 \text{ m s}^{-1})$$

$$= -15 \text{ m s}^{-1}$$

i.e. parrot appears to move with a speed of 15 m s^{-1} from north to south

\therefore Time taken by parrot to cross the train

$$= \frac{150 \text{ m}}{15 \text{ m s}^{-1}} = 10 \text{ s}$$

