

# MATHEMATICAL REASONING

13

## MCQs with One Correct Answer

- For the statement “17 is a real number or a positive integer”, the “or” is
  - Inclusive
  - Exclusive
  - Only (a)
  - None of these
- Let  $p$  and  $q$  be any two logical statements and  $r : p \rightarrow (\sim p \vee q)$ . If  $r$  has a truth value  $F$ , then the truth values of  $p$  and  $q$  are respectively :
  - F, F
  - T, T
  - T, F
  - F, T
- If  $p$  : Ashok works hard  
 $q$  : Ashok gets good grade  
 The verbal form for  $(\sim p \rightarrow q)$  is
  - If Ashok works hard then gets good grade
  - If Ashok does not work hard then he gets good grade
  - If Ashok does not work hard then he does not get good grade
  - Ashok works hard if and only if he gets grade
- If  $p$  is false and  $q$  is true, then
  - $p \wedge q$  is true
  - $p \vee \sim q$  is true
  - $q \wedge p$  is true
  - $p \Rightarrow q$  is true
- $\sim p \wedge q$  is logically equivalent to
  - $p \rightarrow q$
  - $q \rightarrow p$
  - $\sim(p \rightarrow q)$
  - $\sim(q \rightarrow p)$
- Which of the following is a contradiction?
  - $(p \wedge q) \wedge \sim(p \vee q)$
  - $p \vee (\sim p \wedge q)$
  - $(p \Rightarrow q) \Rightarrow p$
  - None of these
- $(p \wedge \sim q) \wedge (\sim p \wedge q)$  is
  - A tautology
  - A contradiction
  - Both a tautology and a contradiction
  - Neither a tautology nor a contradiction
- The false statement in the following is
  - $p \wedge (\sim p)$  is contradiction
  - $(p \Rightarrow q) \Leftrightarrow (\sim q \Rightarrow \sim p)$  is a contradiction
  - $\sim(\sim p) \Leftrightarrow p$  is a tautology
  - $p \vee (\sim p) \Leftrightarrow p$  is a tautology
- The conditional  $(p \wedge q) \Rightarrow p$  is
  - A tautology
  - A fallacy *i.e.*, contradiction
  - Neither tautology nor fallacy
  - None of these
- If  $p$  and  $q$  are two statements, then  $(p \Rightarrow q) \Leftrightarrow (\sim q \Rightarrow \sim p)$  is a
  - contradiction
  - tautology
  - neither (a) nor (b)
  - None of these
- Which of the following is false?
  - $p \vee \sim p$  is a tautology
  - $\sim(\sim p) \Leftrightarrow p$  is a tautology
  - $p \wedge \sim p$  is a contradiction
  - $((p \wedge q) \rightarrow q) \rightarrow p$  is a tautology
- In the truth table for the statement  $(p \rightarrow q) \Leftrightarrow (\sim p \vee q)$ , the last column has the truth value in the following order is
  - TTFF
  - TTTT
  - FFFF
  - FTFT

13. If  $p \Rightarrow (\sim p \vee q)$  is false, then truth values of  $p$  and  $q$  are respectively  
 (a) F, T (b) F, F  
 (c) T, T (d) T, F
14. Negation of " $2 + 3 = 5$  and  $8 < 10$ " is  
 (a)  $2 + 3 \neq 5$  and  $< 10$  (b)  $2 + 3 = 5$  and  $8 \not< 10$   
 (c)  $2 + 3 \neq 5$  or  $8 \not< 10$  (d) None of these
15. If the compound statement  $p \rightarrow (\sim p \vee q)$  is false then the truth value of  $p$  and  $q$  are respectively  
 (a) T, T (b) T, F (c) F, T (d) F, F
16. The contrapositive of  $p \rightarrow (\sim q \rightarrow \sim r)$  is  
 (a)  $(\sim q \wedge r) \rightarrow \sim p$  (b)  $(q \rightarrow r) \rightarrow \sim p$   
 (c)  $(q \vee \sim r) \rightarrow \sim p$  (d) None of these
17. The negation of the compound proposition  $p \vee (\sim p \vee q)$  is  
 (a)  $(p \wedge \sim q) \wedge \sim p$  (b)  $(p \wedge \sim q) \vee \sim p$   
 (c)  $(p \vee \sim q) \vee \sim p$  (d) None of these
18. The inverse of the statement  $(p \wedge \sim q) \rightarrow r$  is  
 (a)  $\sim(p \vee \sim q) \rightarrow \sim r$  (b)  $(\sim p \wedge q) \rightarrow \sim r$   
 (c)  $(\sim p \vee q) \rightarrow \sim r$  (d) None of these
19.  $\sim((\sim p) \wedge q)$  is equal to  
 (a)  $p \vee (\sim q)$  (b)  $p \vee q$   
 (c)  $p \wedge (\sim q)$  (d)  $\sim p \wedge \sim q$
20. Which of the following is true?  
 (a)  $p \Rightarrow q \equiv \sim p \Rightarrow \sim q$   
 (b)  $\sim(p \Rightarrow \sim q) \equiv p \wedge q$   
 (c)  $\sim(\sim p \Rightarrow \sim q) \equiv \sim p \wedge q$   
 (d)  $\sim(\sim p \Leftrightarrow q) \equiv [\sim(p \Rightarrow q) \wedge \sim(q \Rightarrow p)]$
21. The negation of  $(p \vee q) \wedge (p \vee \sim r)$  is  
 (a)  $(\sim p \wedge \sim q) \vee (q \wedge \sim r)$   
 (b)  $(\sim p \wedge \sim q) \vee (\sim q \wedge r)$   
 (c)  $(\sim p \wedge \sim q) \vee (\sim q \wedge r)$   
 (d)  $(p \wedge q) \vee (\sim q \wedge \sim r)$
22. Let  $p$ ,  $q$  and  $r$  be any three logical statements. Which of the following is true?  
 (a)  $\sim[p \wedge (\sim q)] \equiv (\sim p) \wedge q$   
 (b)  $\sim[(p \vee q) \wedge (\sim r)] \equiv (\sim p) \vee (\sim q) \vee (\sim r)$   
 (c)  $\sim[p \vee (\sim q)] \equiv (\sim p) \wedge q$   
 (d)  $\sim[p \vee (\sim q)] \equiv (\sim p) \wedge \sim q$
23. Identify the false statements  
 (a)  $\sim[p \vee (\sim q)] \equiv (\sim p) \vee q$   
 (b)  $[p \vee q] \vee (\sim p)$  is a tautology  
 (c)  $[p \wedge q] \wedge (\sim p)$  is a contradiction  
 (d)  $\sim[p \vee q] \equiv (\sim p) \vee (\sim q)$
24. Negation of the statement  $(p \wedge r) \rightarrow (r \vee q)$  is  
 (a)  $\sim(p \wedge r) \rightarrow \sim(r \vee q)$   
 (b)  $(\sim p \vee \sim r) \vee (r \vee q)$   
 (c)  $(p \wedge r) \wedge (r \wedge q)$   
 (d)  $(p \wedge r) \wedge (\sim r \wedge \sim q)$
25. Let  $A$ ,  $B$ ,  $C$  and  $D$  be four non-empty sets. The contrapositive statement of "If  $A \subseteq B$  and  $B \subseteq D$ , then  $A \subseteq C$ " is:  
 (a) If  $A \not\subseteq C$ , then  $A \subseteq B$  and  $B \subseteq D$   
 (b) If  $A \subseteq C$ , then  $B \subset A$  or  $D \subset B$   
 (c) If  $A \not\subseteq C$ , then  $A \not\subseteq B$  and  $B \subseteq D$   
 (d) If  $A \not\subseteq C$ , then  $A \not\subseteq B$  or  $B \not\subseteq D$

## ANSWER KEY

|   |     |   |     |   |     |    |     |    |     |    |     |    |     |    |     |    |     |
|---|-----|---|-----|---|-----|----|-----|----|-----|----|-----|----|-----|----|-----|----|-----|
| 1 | (a) | 4 | (d) | 7 | (b) | 10 | (b) | 13 | (d) | 16 | (a) | 19 | (a) | 22 | (c) | 25 | (d) |
| 2 | (c) | 5 | (d) | 8 | (b) | 11 | (b) | 14 | (c) | 17 | (a) | 20 | (c) | 23 | (d) |    |     |
| 3 | (b) | 6 | (a) | 9 | (a) | 12 | (c) | 15 | (b) | 18 | (c) | 21 | (c) | 24 | (d) |    |     |