



JEE (MAIN + ADVANCED) 2023 NURTURE COURSE

RACE # 08 MATHEMATICS

TIME: 30 Min. M.M.: 24

# **READ THE FOLLOWING THEOREMS:**

## **MENSURATION**

• For a goemetrical figure, plane or solid:

**Perimeter** is the length of its boundary and its unit is the same as that of length. **Area** is the measure of the surface enclosed by its boundary. Its unit is square units.

Volume of a solid is the measure of the part of space occupied by it. Its unit is cubic units.

- (i) Triangles:
- Considering the base as 'b'

Corresponding altitude as 'h'

Area = 
$$\frac{1}{2} \times b \times h$$

Longest Altitude = 
$$\frac{2 \times \text{Area}}{\text{Shortest Base}}$$
 Shortest Altitude =  $\frac{2 \times \text{Area}}{\text{Longest Base}}$ 

• Heron's Formula :

If a, b, c are the sides of a triangle

Area = 
$$\sqrt{S(S-a)(S-b)(S-c)}$$
 where  $S = \frac{a+b+c}{2}$ 

• If 'a' is a side of an equilateral triangle,

Area = 
$$\frac{\sqrt{3}a^2}{4}$$
 Altitude =  $\frac{\sqrt{3}a}{2}$ 

• If 'a' is the measure of the equal sides and 'b' the third side of an isosceles triangle,

Area = 
$$\frac{1}{4}b\sqrt{4a^2 - b^2}$$
 Altitude =  $\frac{\sqrt{4a^2 - b^2}}{2}$ 

Perimeter in all cases is the sum of the three sides

(ii) Quadrilaterals:

## **Rectangle:**

If ' $\ell$ ', 'b', 'd' are the length, breadth and diagonal, then

Area = 
$$\ell \times b$$
 Perimeter =  $2(\ell + b)$   $d = \sqrt{\ell^2 + b^2}$ 

• Square:

If each side is 'a'

Area = 
$$a^2$$
 Perimeter =  $4a$  Diagonal (d) =  $\sqrt{2}a$  Area =  $\frac{d^2}{2}$ 

• General Quadrilateral:

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In any general quadrilateral ABCD if diagonal AC = d perpendiculars from B and D to AC are  $h_1$  and  $h_2$ , then

Area = 
$$\frac{1}{2}$$
d  $(h_1 + h_2)$ 

## • Rhombus:

If the diagonals are d<sub>1</sub>, d<sub>2</sub> and each side 'a', then

Area = 
$$\frac{1}{2} d_1 \times d_2$$
  $a^2 = \left(\frac{d_1}{2}\right)^2 + \left(\frac{d_2}{2}\right)^2$ 

## • Note:

For any quadrilateral whose diagonals d<sub>1</sub> and d<sub>2</sub> are perpendicular to each other,

Area = 
$$\frac{1}{2}$$
d<sub>1</sub> × d<sub>2</sub>

## • Parallelogram:

If 'b' any side and 'h' the corresponding altitude

Area = 
$$b \times h$$

# • Trapezium:

If the parallel sides are a and b and the distance between them h,

Area = 
$$\frac{1}{2}$$
(a + b)h

# 10 CIRCLE, SECTOR AND SEGMENT:

# (i) Let in a circle of centre O

radius = r AB a chord

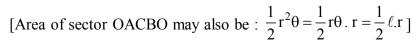
 $\angle AOB = \theta$  (the angle subtended by arc ACB at the centre)

OACBO the minor sector,

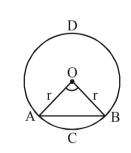
ACB the minor segment,

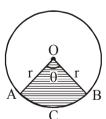
BDAB the major segment.

- Circumference of the circle =  $2\pi r$
- Area of the circle =  $\pi r^2$
- Perimeter of semi-circle =  $\pi r + 2r$
- Length of arc  $ACB(\widehat{ABC}) = \ell = r\theta$ where  $\theta$  is in radian
- Area of sector OACBO =  $\frac{1}{2}$ r<sup>2</sup> $\theta$



• Perimeter of sector OACBO = OA = OB + Arc ACB =  $r + r + r\theta = 2r + r\theta$ 



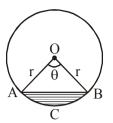






Area of the minor segment ACBA = Area of sector OACBO – Area of  $\triangle$ OAB

$$= \left[ \frac{1}{2} r^2 \theta - \frac{1}{2} r^2 \sin \theta \right]$$

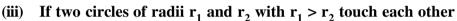


Area of the major segment ABDA = Area of the circle – Area of minor segment ACBA.

#### (ii) Ring:

Part of the plane between two concentric circles of different radii  $(r_1 \text{ and } r_2 \text{ where } r_1 > r_2),$ 

Area of Ring = 
$$\pi r_1^2 - \pi r_2^2 = \pi (r_1 + r_2)(r_1 - r_2)$$



- Externally, the distance between their centres =  $(r_1 + r_2)$
- Internally, the distance betweeen their centres =  $(r_1 r_2)$

In the case of rotating wheels (iv)

Distance moved by a wheel is one rotation is the circumference of the wheel,

• Number of rotation = 
$$\frac{\text{Distance Travelled}}{\text{Circumference of the wheel}}$$

Rotation of the hands of a clock: **(v)** 

- Angle described by the minute hand of a clock in 1 hour (60 minute) i.e. one rotation = 360°.
- Angle described by the hour hand of a clock in 12 hours (i.e. one rotation) =  $360^{\circ}$ .

**ANSWER THE FOLLOWING QUESTIONS:** 

1. The area of a rhombus is 2016 sq cm and its side is 65 cm. The lengths of the diagonals (in cm) are

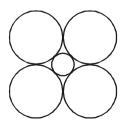
2. A square and an equilateral triangle have the same perimeter. If the diagonal of the square is  $12\sqrt{2}$  cm, then the area of the triangle is

(A) 
$$24\sqrt{3}$$
 cm<sup>2</sup>

(B) 
$$24\sqrt{2}$$
 cm<sup>2</sup>

(C) 
$$64\sqrt{3}$$
 cm<sup>2</sup>(D)  $32\sqrt{3}$  cm<sup>2</sup>

In the figure, when the outer circles all have radii 'r', then the radius of the inner circle will be 3.



$$(A) \sqrt{2} r$$

(A) 
$$\sqrt{2} r$$
 (B)  $(\sqrt{2} - 1)r$ 

(C) 
$$\frac{1}{\sqrt{2}r}$$

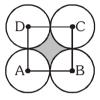
(D) 
$$\frac{2}{(\sqrt{2}+1)r}$$

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- 4. A wire is in the form of a circle of radius 35 cm. If it is bent into the shape of a rhombus, what is the side of the rhombus?
  - (A) 32 cm
- (B) 70 cm
- (C) 55 cm
- (D) 17 cm
- 5. There are two concentric circles whose areas are in the ratio of 9: 16 and the difference between their diameters is 4 cm. What is the area of the outer circle?
  - (A)  $32\pi \text{ cm}^2$
- (B)  $64\pi \text{ cm}^2$
- (C)  $36\pi \text{ cm}^2$
- (D)  $48\pi \text{ cm}^2$
- **6.** ABCD is a square, four equal circles are just touching each other whose centres are the vertices A, B, C, D of the square. What is the ratio of the shaded to the unshaded area within square?



- (A)  $\frac{8}{11}$
- (B)  $\frac{3}{11}$
- (C)  $\frac{5}{11}$
- (D)  $\frac{6}{11}$

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SECTION-I	Q.	1	2	3	4	5	6
	A.	С	В	В	В	В	Α

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